Results for instances from collection Dispersion-QKP with strategy geo

$File\ dispersion-qkp-geo_0100_005.txt$

| Property of graph | Value |
|--------------------|-------|
| Nodes (n) | 100 |
| Density (Δ) | 5.0~% |
| Edges (m) | 268 |

| - | | Rı | ınnin | o tin | ne (s) | | | | | | | | |
|----------|--------------|-------|-------|-------|--------|--------|--------|-------|-----|-----|-----|--------|--------|
| | | - | | | | OFV (% | | | | | | . , | |
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 726.7 | 3.15 | 17.83 | 4.85 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.0 | 0.0 |
| 5.0 | 1,204.0 | 0.48 | 10.55 | 0.48 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.2 | 0.1 | 1.0 |
| 10.0 | $2,\!151.5$ | 2.71 | 5.72 | 1.57 | 0.02 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.3 | 0.3 | 1.0 |
| 25.0 | 4,935.1 | 0.80 | 2.10 | 0.48 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.4 | 0.3 | 0.5 | 2.0 |
| 50.0 | 9,420.0 | 0.00 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.5 | 0.3 | 0.0 | 0.0 |
| 75.0 | 13,091.5 | 0.24 | 0.16 | 0.25 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.0 | 0.0 |
| 90.0 | 14,681.0 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.1 | 0.0 |
| 95.0 | $15,\!072.2$ | 0.02 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.4 | 0.6 | 0.1 | 0.0 | 1.0 |
| Avg | | 0.92 | 4.55 | 0.95 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 0.1 | 0.6 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.0 | 0.0 |
| Max | | 3.15 | 17.83 | 4.85 | 0.02 | 0.00 | 0.00 | 0.00 | 0.4 | 0.6 | 0.3 | 0.5 | 2.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 25 |
| Running time in seconds for writing input file (t^{write}) | 0.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0100_010.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 100 |
| Density (Δ) | 10.0 % |
| Edges (m) | 500 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|-------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 991.6 | 0.00 | 0.00 | 1.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.1 | 1.0 |
| 5.0 | 1,752.6 | 0.45 | 0.31 | 3.74 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.3 | 1.0 |
| 10.0 | 3,262.1 | 2.63 | 0.28 | 1.18 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.7 | 0.8 | 2.0 |
| 25.0 | $8,\!176.4$ | 0.21 | 0.21 | 0.51 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.3 | 0.2 | 2.0 |
| 50.0 | $15,\!319.4$ | 0.00 | 0.00 | 0.47 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.5 | 0.5 | 0.1 | 1.0 |
| 75.0 | $21,\!865.8$ | 0.04 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.1 | 1.0 |
| 90.0 | 24,611.9 | 0.07 | 0.07 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.1 | 2.0 |
| 95.0 | 25,440.3 | 0.54 | 0.54 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.1 | 0.1 | 0.0 |
| Avg | | 0.49 | 0.18 | 0.87 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.3 | 0.2 | 1.3 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.1 | 0.0 |
| Max | | 2.63 | 0.54 | 3.74 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.7 | 0.8 | 2.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 22 |
| Running time in seconds for writing input file (t^{write}) | 0.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0100_025.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 100 |
| Density (Δ) | 25.0~% |
| Edges (m) | 1,258 |

| | Running time (s) | | | | | | | | | | | | |
|----------|--|------|------|------|------|------|------|------|-----|-----|-----|--------|--------|
| γ | γ Best OFV $\overline{\text{QKBP}^*}$ GR DP QK Gurobi Hexaly $\overline{\text{QKBP}^*}$ | | | | | | | | | DP | QK | Gurobi | Hexaly |
| 2.5 | 2,751.2 | 0.00 | 0.00 | 5.59 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.2 | 1.0 |
| 5.0 | 4,973.8 | 1.12 | 0.51 | 0.65 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.7 | 1.0 |
| 10.0 | 9,447.0 | 3.02 | 0.97 | 1.10 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.2 | 2.0 |
| 25.0 | 20,903.8 | 0.09 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.3 | 0.2 | 0.4 | 3.0 |
| 50.0 | 38,347.6 | 1.10 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.5 | 0.3 | 0.2 | 1.0 |
| 75.0 | 55,561.1 | 0.20 | 0.20 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.5 | 0.2 | 0.4 | 2.0 |
| 90.0 | $64,\!506.6$ | 0.12 | 0.12 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 2.4 | 14.0 |
| 95.0 | 67,498.8 | 0.30 | 0.29 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.1 | 1.0 |
| Avg | | 0.74 | 0.26 | 0.92 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 0.6 | 3.1 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.1 | 1.0 |
| Max | | 3.02 | 0.97 | 5.59 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.3 | 2.4 | 14.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 18 |
| Running time in seconds for writing input file (t^{write}) | 0.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0100_050.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 100 |
| Density (Δ) | 50.0 % |
| Edges (m) | 2,533 |

| | Running time (s) | | | | | | | | | | | | |
|----------|---|------|------|------|------|------|------|------|-----|-----|-----|--------|--------|
| γ | γ Best OFV $\overline{	ext{QKBP}^*}$ GR DP QK Gurobi Hexaly $\overline{	ext{Q}}$ | | | | | | | | | DP | QK | Gurobi | Hexaly |
| 2.5 | 4,394.1 | 3.67 | 0.53 | 0.33 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.2 | 0.7 | 3.0 |
| 5.0 | 8,235.2 | 1.92 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.9 | 4.0 |
| 10.0 | 16,060.5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.3 | 3.0 |
| 25.0 | 38,792.0 | 0.05 | 0.00 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.3 | 0.2 | 0.9 | 11.0 |
| 50.0 | $71,\!544.1$ | 0.04 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.5 | 0.6 | 0.8 | 4.0 |
| 75.0 | 104,945.1 | 0.49 | 0.00 | 0.12 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.3 | 2.1 | 6.0 |
| 90.0 | $124,\!597.9$ | 0.59 | 0.43 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.4 | 0.6 | 0.2 | 7.0 | 21.0 |
| 95.0 | 131,028.1 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.4 | 0.6 | 0.2 | 0.4 | 4.0 |
| Avg | | 0.84 | 0.12 | 0.06 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 1.6 | 7.0 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.2 | 0.3 | 3.0 |
| Max | | 3.67 | 0.53 | 0.33 | 0.00 | 0.00 | 0.00 | 0.00 | 0.4 | 0.6 | 0.6 | 7.0 | 21.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|------------------------|
| Number of breakpoints | 17 |
| Running time in seconds for writing input file (t^{write}) | 0.3 |
| Running time in seconds for executing parametric cut procedure | (t^{cut}) 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0100_075.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 100 |
| Density (Δ) | 75.0 % |
| Edges (m) | 3,739 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|-------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV \mid | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 6,271.2 | 0.55 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.8 | 3.0 |
| 5.0 | $12,\!232.5$ | 1.95 | 1.57 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 1.1 | 9.0 |
| 10.0 | 23,008.0 | 1.84 | 0.33 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.3 | 0.2 | 2.2 | 27.0 |
| 25.0 | 54,684.6 | 0.55 | 0.40 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 2.2 | 14.0 |
| 50.0 | 100,495.1 | 1.95 | 0.41 | 0.18 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.5 | 0.2 | 5.1 | 32.0 |
| 75.0 | 145,700.8 | 0.92 | 0.06 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.4 | 0.6 | 0.2 | 3.8 | 67.0 |
| 90.0 | 169,987.9 | 0.58 | 0.56 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.7 | 0.2 | 28.4 | 120.0 |
| 95.0 | 178,436.8 | 0.13 | 0.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 4.3 | 16.0 |
| Avg | | 1.06 | 0.43 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 6.0 | 36.0 |
| Min | | 0.13 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.8 | 3.0 |
| Max | | 1.95 | 1.57 | 0.18 | 0.00 | 0.00 | 0.00 | 0.00 | 0.4 | 0.7 | 0.2 | 28.4 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|--------------------------|
| Number of breakpoints | 15 |
| Running time in seconds for writing input file (t^{write}) | 0.3 |
| Running time in seconds for executing parametric cut procedure (| (t^{cut}) 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0100_100.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 100 |
| Density (Δ) | 100.0~% |
| Edges (m) | 4,950 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|-------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 9,133.4 | 0.72 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.2 | 1.2 | 7.0 |
| 5.0 | $16,\!107.5$ | 1.58 | 0.81 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.1 | 3.7 | 49.0 |
| 10.0 | 29,976.4 | 0.33 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.3 | 0.2 | 1.4 | 14.0 |
| 25.0 | $73,\!100.3$ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 0.7 | 13.0 |
| 50.0 | $138,\!473.7$ | 0.69 | 0.30 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.5 | 0.2 | 8.9 | 88.0 |
| 75.0 | 204,405.3 | 1.19 | 0.82 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 7.2 | 37.0 |
| 90.0 | $240,\!460.1$ | 0.25 | 0.09 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 60.6 | 120.0 |
| 95.0 | 252,685.3 | 0.15 | 0.15 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.7 | 0.2 | 6.1 | 27.0 |
| Avg | | 0.61 | 0.27 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 11.2 | 44.4 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.7 | 7.0 |
| Max | | 1.58 | 0.82 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.7 | 0.2 | 60.6 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|------------------------|
| Number of breakpoints | 12 |
| Running time in seconds for writing input file (t^{write}) | 0.3 |
| Running time in seconds for executing parametric cut procedure | (t^{cut}) 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0200_005.txt$

| Property of graph | Value |
|--------------------|-------|
| Nodes (n) | 200 |
| Density (Δ) | 5.0 % |
| Edges (m) | 1,029 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|-------|------|------|------|--------|--------|------------------------------|-----|-----|------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | $\overline{\mathrm{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 2,082.2 | 0.12 | 0.00 | 6.31 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.2 | 0.7 | 0.3 | 2.0 |
| 5.0 | 3,796.5 | 0.61 | 0.26 | 4.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.5 | 1.1 | 0.2 | 2.0 |
| 10.0 | 7,007.1 | 2.94 | 0.35 | 3.22 | 0.00 | 0.00 | 0.00 | 0.00 | 0.4 | 2.2 | 34.6 | 0.2 | 4.0 |
| 25.0 | $16,\!842.2$ | 0.00 | 0.93 | 0.32 | 0.00 | 0.00 | 0.00 | 0.00 | 0.7 | 3.2 | 5.7 | 0.4 | 5.0 |
| 50.0 | $32,\!209.6$ | 0.01 | 0.09 | 0.04 | 0.00 | 0.00 | 0.00 | 0.00 | 1.1 | 4.1 | 5.1 | 0.2 | 9.0 |
| 75.0 | 46,087.0 | 0.06 | 0.06 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.3 | 4.7 | 1.6 | 0.2 | 10.0 |
| 90.0 | $53,\!001.5$ | 0.23 | 0.16 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.5 | 4.4 | 0.7 | 0.3 | 10.0 |
| 95.0 | 54,942.0 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.5 | 5.5 | 0.5 | 0.0 | 1.0 |
| Avg | | 0.50 | 0.23 | 1.74 | 0.00 | 0.00 | 0.00 | 0.00 | 0.9 | 3.4 | 6.2 | 0.2 | 5.4 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.2 | 0.5 | 0.0 | 1.0 |
| Max | | 2.94 | 0.93 | 6.31 | 0.00 | 0.00 | 0.00 | 0.00 | 1.5 | 5.5 | 34.6 | 0.4 | 10.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 23 |
| Running time in seconds for writing input file (t^{write}) | 0.6 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0200_010.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 200 |
| Density (Δ) | 10.0 % |
| Edges (m) | 2,008 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|-------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV \mid | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 3,986.3 | 1.31 | 1.08 | 1.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.5 | 0.2 | 1.0 |
| 5.0 | 7,634.2 | 0.51 | 0.17 | 0.35 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.7 | 0.6 | 0.2 | 3.0 |
| 10.0 | 14,125.3 | 0.52 | 0.00 | 0.49 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 2.4 | 1.1 | 0.3 | 2.0 |
| 25.0 | 31,729.8 | 0.40 | 0.34 | 0.16 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 3.2 | 2.5 | 1.0 | 9.0 |
| 50.0 | 58,996.3 | 0.08 | 0.05 | 0.05 | 0.00 | 0.01 | 0.00 | 0.00 | 1.1 | 4.2 | 1.4 | 0.6 | 8.0 |
| 75.0 | 83,317.8 | 0.16 | 0.20 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 1.3 | 4.3 | 2.1 | 0.6 | 12.0 |
| 90.0 | 97,029.4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.5 | 5.0 | 0.7 | 0.3 | 8.0 |
| 95.0 | $100,\!692.7$ | 0.21 | 0.16 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.5 | 4.5 | 0.5 | 0.3 | 5.0 |
| Avg | | 0.40 | 0.25 | 0.27 | 0.00 | 0.00 | 0.00 | 0.00 | 0.9 | 3.3 | 1.2 | 0.4 | 6.0 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.5 | 0.2 | 1.0 |
| Max | | 1.31 | 1.08 | 1.08 | 0.00 | 0.01 | 0.00 | 0.00 | 1.5 | 5.0 | 2.5 | 1.0 | 12.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|--------|
| Number of breakpoints | 25 |
| Running time in seconds for writing input file (t^{write}) | 0.7 |
| Running time in seconds for executing parametric cut procedure (t^{cu} | t) 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0200_025.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 200 |
| Density (Δ) | 25.0 % |
| Edges (m) | 4,983 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|-------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 8,478.6 | 1.15 | 0.27 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.4 | 0.6 | 1.2 | 8.0 |
| 5.0 | 16,093.4 | 0.79 | 0.00 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.7 | 0.7 | 0.9 | 15.0 |
| 10.0 | $30,\!173.6$ | 0.34 | 0.08 | 0.19 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 2.5 | 1.2 | 2.5 | 21.0 |
| 25.0 | 71,916.0 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 3.2 | 2.2 | 0.9 | 10.0 |
| 50.0 | 137,772.4 | 0.11 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.1 | 4.2 | 2.6 | 6.4 | 59.0 |
| 75.0 | $201,\!548.7$ | 0.11 | 0.00 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 1.3 | 4.3 | 1.3 | 0.9 | 11.0 |
| 90.0 | 237,390.2 | 0.03 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 5.0 | 0.7 | 0.9 | 15.0 |
| 95.0 | $247,\!059.5$ | 0.14 | 0.13 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.5 | 4.5 | 0.6 | 19.3 | 120.0 |
| Avg | | 0.33 | 0.07 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 0.9 | 3.3 | 1.2 | 4.1 | 32.4 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.4 | 0.6 | 0.9 | 8.0 |
| Max | | 1.15 | 0.27 | 0.19 | 0.00 | 0.00 | 0.00 | 0.00 | 1.5 | 5.0 | 2.6 | 19.3 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 15 |
| Running time in seconds for writing input file (t^{write}) | 0.7 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0200_050.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 200 |
| Density (Δ) | 50.0 % |
| Edges (m) | 9,983 |

| Deviation from best OFV (%) | | | | | | | | | Running time (s) | | | | | |
|-----------------------------|---------------|----------------------------|------|------|------|--------|--------|-------|------------------|-----|-----|--------|--------|--|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly | |
| 2.5 | 14,831.6 | 1.45 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.7 | 4.9 | 38.0 | |
| 5.0 | $29,\!563.4$ | 0.83 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.8 | 1.0 | 6.4 | 28.0 | |
| 10.0 | 59,097.1 | 0.30 | 0.13 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 2.3 | 0.8 | 6.7 | 73.0 | |
| 25.0 | 142,035.3 | 1.05 | 0.21 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.7 | 3.2 | 2.6 | 32.7 | 120.0 | |
| 50.0 | 278,928.4 | 0.72 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.0 | 3.9 | 1.0 | 16.9 | 120.0 | |
| 75.0 | $409,\!407.0$ | 0.62 | 0.13 | 0.00 | 0.00 | 0.00 | 0.06 | 0.00 | 1.3 | 4.6 | 1.0 | 26.9 | 120.0 | |
| 90.0 | $484,\!250.3$ | 0.58 | 0.47 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.4 | 0.7 | 50.3 | 120.0 | |
| 95.0 | 505,920.0 | 0.32 | 0.32 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.7 | 5.5 | 0.6 | 120.5 | 120.0 | |
| Avg | | 0.73 | 0.16 | 0.01 | 0.00 | 0.00 | 0.01 | 0.00 | 0.9 | 3.4 | 1.1 | 33.2 | 92.4 | |
| Min | | 0.30 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.6 | 4.9 | 28.0 | |
| Max | | 1.45 | 0.47 | 0.05 | 0.00 | 0.00 | 0.06 | 0.00 | 1.7 | 5.5 | 2.6 | 120.5 | 120.0 | |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 17 |
| Running time in seconds for writing input file (t^{write}) | 0.7 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0200_075.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 200 |
| Density (Δ) | 75.0 % |
| Edges (m) | 14,888 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|-------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 20,531.5 | 1.42 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.6 | 9.2 | 37.0 |
| 5.0 | $41,\!584.5$ | 1.98 | 0.39 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.7 | 0.6 | 18.7 | 120.0 |
| 10.0 | 82,148.9 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 2.3 | 0.7 | 11.5 | 77.0 |
| 25.0 | 206,025.8 | 1.20 | 0.75 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 3.2 | 2.2 | 20.4 | 120.0 |
| 50.0 | 408,854.9 | 0.29 | 0.18 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.1 | 3.9 | 0.9 | 47.1 | 120.0 |
| 75.0 | 602,384.4 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.3 | 4.3 | 0.8 | 34.2 | 110.0 |
| 90.0 | 707,475.9 | 0.29 | 0.29 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.3 | 0.7 | 120.1 | 120.0 |
| 95.0 | 737,401.5 | 0.14 | 0.14 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 5.7 | 0.7 | 120.1 | 120.0 |
| Avg | | 0.67 | 0.22 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.9 | 3.4 | 0.9 | 47.7 | 103.0 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.6 | 9.2 | 37.0 |
| Max | | 1.98 | 0.75 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 5.7 | 2.2 | 120.1 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|--|----------|
| Number of breakpoints | 12 |
| Running time in seconds for writing input file (t^{write}) | 0.7 |
| Running time in seconds for executing parametric cut procedure (t | cut) 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0200_100.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 200 |
| Density (Δ) | 100.0 % |
| Edges (m) | 19,900 |

| Deviation from best OFV (%) | | | | | | | | | Rı | ınnin | g tin | ne (s) | |
|--|---------------|------|------|------|------|------|------|------|-----|-------|-------|--------|--------|
| γ Best OFV QKBP* GR DP QK Gurobi Hexaly 0 | | | | | | | | | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 27,139.3 | 1.63 | 1.34 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.2 | 1.3 | 0.6 | 7.3 | 91.0 |
| 5.0 | 52,913.8 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.9 | 0.6 | 19.9 | 120.0 |
| 10.0 | 106,663.0 | 2.33 | 0.65 | 0.00 | 0.00 | 0.00 | 0.47 | 0.00 | 0.5 | 2.3 | 0.6 | 36.7 | 120.0 |
| 25.0 | 268,035.6 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.8 | 3.4 | 0.7 | 35.1 | 120.0 |
| 50.0 | 541,679.7 | 0.21 | 0.09 | 0.00 | 0.00 | 0.00 | 0.11 | 0.00 | 1.1 | 3.9 | 0.7 | 39.3 | 120.0 |
| 75.0 | 800,376.6 | 0.42 | 0.35 | 0.00 | 0.00 | 0.00 | 0.38 | 0.00 | 1.3 | 4.9 | 0.7 | 120.4 | 120.0 |
| 90.0 | $947,\!386.9$ | 0.20 | 0.11 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.4 | 0.7 | 120.2 | 120.0 |
| 95.0 | $988,\!179.2$ | 0.08 | 0.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.5 | 5.7 | 0.7 | 120.1 | 120.0 |
| Avg | | 0.61 | 0.33 | 0.00 | 0.00 | 0.00 | 0.12 | 0.00 | 0.9 | 3.5 | 0.7 | 62.4 | 116.4 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.6 | 7.3 | 91.0 |
| Max | | 2.33 | 1.34 | 0.00 | 0.00 | 0.00 | 0.47 | 0.01 | 1.5 | 5.7 | 0.7 | 120.4 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|---------------------------|
| Number of breakpoints | 11 |
| Running time in seconds for writing input file (t^{write}) | 0.8 |
| Running time in seconds for executing parametric cut procedur | $e(t^{\text{cut}}) = 0.2$ |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0300_005.txt$

| Property of graph | Value |
|--------------------|-------|
| Nodes (n) | 300 |
| Density (Δ) | 5.0 % |
| Edges (m) | 2,351 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|-------|------|------|--------|--------|--------|-------|-----|------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 4,382.6 | 1.57 | 1.13 | 3.21 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 5.9 | 3.0 | 1.1 | 10.0 |
| 5.0 | 8,160.5 | 0.58 | 0.32 | 1.96 | 0.00 | 0.00 | 0.00 | 0.00 | 0.7 | 7.8 | 4.0 | 0.4 | 5.0 |
| 10.0 | $15,\!421.0$ | 0.82 | 0.60 | 0.52 | 0.00 | 0.00 | 0.00 | 0.00 | 1.2 | 11.0 | 6.2 | 0.5 | 14.0 |
| 25.0 | 35,680.6 | 0.41 | 0.46 | 0.35 | 0.00 | 0.00 | 0.00 | 0.01 | 1.8 | 14.0 | 18.1 | 0.7 | 10.0 |
| 50.0 | $67,\!858.7$ | 0.32 | 0.17 | 0.20 | \inf | 0.00 | 0.00 | 0.01 | 2.6 | 19.1 | 120.0 | 2.3 | 38.0 |
| 75.0 | 99,014.8 | 0.09 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.2 | 16.4 | 14.1 | 0.2 | 6.0 |
| 90.0 | $115,\!356.1$ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.5 | 18.9 | 2.5 | 0.2 | 7.0 |
| 95.0 | 119,938.5 | 0.01 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.6 | 15.5 | 1.4 | 0.2 | 21.0 |
| Avg | | 0.47 | 0.34 | 0.78 | inf | 0.00 | 0.00 | 0.00 | 2.2 | 13.6 | 21.2 | 0.7 | 13.9 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 5.9 | 1.4 | 0.2 | 5.0 |
| Max | | 1.57 | 1.13 | 3.21 | \inf | 0.00 | 0.00 | 0.01 | 3.6 | 19.1 | 120.0 | 2.3 | 38.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 31 |
| Running time in seconds for writing input file (t^{write}) | 1.0 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0300_010.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 300 |
| Density (Δ) | 10.0 % |
| Edges (m) | 4,388 |

| Deviation from best OFV (%) | | | | | | | | | Running time (s) | | | | | |
|-----------------------------|---------------|-------|------|------|--------|--------|--------|-------|------------------|------|-------|--------|--------|--|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly | |
| 2.5 | 8,829.2 | 0.31 | 0.31 | 0.09 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.0 | 1.2 | 0.4 | 9.0 | |
| 5.0 | 15,161.4 | 0.87 | 0.66 | 0.30 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 8.1 | 14.4 | 1.9 | 30.0 | |
| 10.0 | $27,\!152.5$ | 0.11 | 0.11 | 0.46 | \inf | 0.00 | 0.00 | 0.00 | 1.1 | 10.5 | 120.0 | 4.1 | 54.0 | |
| 25.0 | 65,001.9 | 0.00 | 0.00 | 0.24 | \inf | 0.00 | 0.00 | 0.01 | 1.8 | 14.0 | 120.0 | 1.7 | 25.0 | |
| 50.0 | $126,\!886.4$ | 0.19 | 0.02 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 | 2.5 | 18.0 | 19.2 | 2.3 | 62.0 | |
| 75.0 | 184,706.0 | 0.13 | 0.12 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.0 | 15.9 | 2.3 | 0.9 | 25.0 | |
| 90.0 | $214,\!263.5$ | 0.11 | 0.10 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.2 | 17.8 | 2.0 | 1.6 | 120.0 | |
| 95.0 | $222,\!899.5$ | 0.26 | 0.25 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.4 | 15.3 | 1.4 | 0.5 | 53.0 | |
| Avg | | 0.25 | 0.20 | 0.14 | \inf | 0.00 | 0.00 | 0.00 | 2.0 | 13.2 | 35.1 | 1.7 | 47.2 | |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.0 | 1.2 | 0.4 | 9.0 | |
| Max | | 0.87 | 0.66 | 0.46 | \inf | 0.00 | 0.00 | 0.01 | 3.4 | 18.0 | 120.0 | 4.1 | 120.0 | |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 22 |
| Running time in seconds for writing input file (t^{write}) | 0.9 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0300_025.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 300 |
| Density (Δ) | 25.0 % |
| Edges (m) | 11,110 |

| | | Running time (s) | | | | | | | | | | | |
|----------|--------------|------------------|------|------|------|--------|--------|-------|-----|------|-----|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 18,008.6 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.2 | 1.7 | 0.8 | 7.0 |
| 5.0 | 33,657.9 | 0.00 | 0.14 | 0.53 | 0.00 | 0.00 | 0.00 | 0.00 | 0.9 | 8.6 | 3.8 | 12.9 | 60.0 |
| 10.0 | $66,\!196.1$ | 0.38 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.2 | 10.5 | 4.5 | 18.1 | 120.0 |
| 25.0 | 160,146.9 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 2.0 | 15.0 | 6.9 | 10.6 | 120.0 |
| 50.0 | 311,752.1 | 0.10 | 0.09 | 0.00 | 0.00 | 0.00 | 0.04 | 0.00 | 2.8 | 15.9 | 3.4 | 14.2 | 120.0 |
| 75.0 | 457,767.4 | 0.24 | 0.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.3 | 18.2 | 3.1 | 3.6 | 120.0 |
| 90.0 | 537,090.0 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.6 | 16.0 | 1.9 | 1.1 | 8.0 |
| 95.0 | 560,685.1 | 0.11 | 0.11 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.7 | 17.5 | 1.5 | 3.6 | 120.0 |
| Avg | | 0.10 | 0.05 | 0.07 | 0.00 | 0.00 | 0.01 | 0.00 | 2.2 | 13.5 | 3.4 | 8.1 | 84.4 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.2 | 1.5 | 0.8 | 7.0 |
| Max | | 0.38 | 0.14 | 0.53 | 0.00 | 0.00 | 0.04 | 0.01 | 3.7 | 18.2 | 6.9 | 18.1 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 22 |
| Running time in seconds for writing input file (t^{write}) | 1.1 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0300_050.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 300 |
| Density (Δ) | 50.0 % |
| Edges (m) | 22,346 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|----------------------------|------|------|------|--------|--------|-------|-----|------|-----|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 35,472.5 | 0.27 | 0.07 | 0.15 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.7 | 1.7 | 8.8 | 60.0 |
| 5.0 | $67,\!862.5$ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.9 | 8.3 | 1.5 | 17.5 | 120.0 |
| 10.0 | 129,880.8 | 1.05 | 0.00 | 0.01 | 0.00 | 0.00 | 0.21 | 0.00 | 1.3 | 11.2 | 9.6 | 99.4 | 120.0 |
| 25.0 | $323,\!564.4$ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.13 | 0.00 | 2.0 | 14.0 | 2.4 | 15.2 | 120.0 |
| 50.0 | $626,\!497.3$ | 0.43 | 0.05 | 0.01 | 0.01 | 0.00 | 0.28 | 0.01 | 2.8 | 18.6 | 5.1 | 72.1 | 120.0 |
| 75.0 | $923,\!919.0$ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.16 | 0.00 | 3.4 | 15.9 | 2.4 | 95.9 | 120.0 |
| 90.0 | 1,089,340.3 | 0.09 | 0.07 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.6 | 18.5 | 1.9 | 8.7 | 120.0 |
| 95.0 | 1,140,262.5 | 0.10 | 0.07 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 4.2 | 15.3 | 1.6 | 15.9 | 120.0 |
| Avg | | 0.24 | 0.03 | 0.02 | 0.00 | 0.00 | 0.10 | 0.00 | 2.4 | 13.6 | 3.3 | 41.7 | 112.5 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.7 | 1.5 | 8.7 | 60.0 |
| Max | | 1.05 | 0.07 | 0.15 | 0.01 | 0.00 | 0.28 | 0.01 | 4.2 | 18.6 | 9.6 | 99.4 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 14 |
| Running time in seconds for writing input file (t^{write}) | 1.2 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0300_075.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 300 |
| Density (Δ) | 75.0 % |
| Edges (m) | 33,590 |

| | | Running time (s) | | | | | | | | | | | |
|----------|---------------|----------------------------|------|------|------|--------|--------|-------|-----|------|-----|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 54,838.8 | 0.93 | 0.18 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.6 | 6.3 | 1.5 | 13.0 | 81.0 |
| 5.0 | 105,730.5 | 0.64 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 8.3 | 1.4 | 42.2 | 120.0 |
| 10.0 | 199,845.1 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.56 | 0.01 | 1.2 | 10.7 | 1.7 | 40.4 | 120.0 |
| 25.0 | 480,039.5 | 0.16 | 0.04 | 0.00 | 0.00 | 0.01 | 0.23 | 0.01 | 1.9 | 14.0 | 4.6 | 120.6 | 120.0 |
| 50.0 | $951,\!522.6$ | 0.41 | 0.00 | 0.01 | 0.00 | 0.00 | 0.26 | 0.00 | 2.6 | 17.6 | 2.7 | 120.9 | 120.0 |
| 75.0 | 1,401,988.9 | 0.13 | 0.06 | 0.00 | 0.00 | 0.00 | 0.21 | 0.00 | 3.1 | 15.9 | 2.2 | 37.0 | 120.0 |
| 90.0 | 1,652,923.5 | 0.14 | 0.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.4 | 17.6 | 1.9 | 24.7 | 120.0 |
| 95.0 | 1,731,654.8 | 0.04 | 0.04 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.4 | 16.6 | 1.7 | 38.4 | 120.0 |
| Avg | | 0.31 | 0.05 | 0.00 | 0.00 | 0.00 | 0.28 | 0.00 | 2.1 | 13.4 | 2.2 | 54.6 | 115.1 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.3 | 1.4 | 13.0 | 81.0 |
| Max | | 0.93 | 0.18 | 0.01 | 0.00 | 0.01 | 1.56 | 0.01 | 3.4 | 17.6 | 4.6 | 120.9 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 13 |
| Running time in seconds for writing input file (t^{write}) | 1.2 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0300_100.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 300 |
| Density (Δ) | 100.0~% |
| Edges (m) | 44,850 |

| | | Rı | ınnin | g tim | ne (s) | | | | | | | | |
|----------|---------------|-------|-------|-------|--------|--------|--------|-------|-----|------|-----|-------|-------|
| γ | Best OFV | QKBP* | | | | Gurobi | Hevaly | | | | | | |
| | <u> </u> | QKBP* | GR | DP | | Guiobi | | &IIDI | OI. | | Ø11 | | |
| 2.5 | $72,\!119.8$ | 2.98 | 0.00 | 0.00 | 0.00 | 0.00 | 0.83 | 0.01 | 0.6 | 6.4 | 1.4 | 17.2 | 120.0 |
| 5.0 | $140,\!460.0$ | 0.11 | 0.06 | 0.00 | 0.00 | 0.00 | 1.04 | 0.00 | 0.9 | 8.8 | 1.4 | 32.2 | 120.0 |
| 10.0 | 269,956.6 | 0.10 | 0.04 | 0.00 | 0.00 | 0.00 | 1.27 | 0.00 | 1.2 | 10.6 | 1.7 | 45.1 | 120.0 |
| 25.0 | 667,497.5 | 0.37 | 0.04 | 0.00 | 0.00 | 0.03 | 0.46 | 0.00 | 2.0 | 15.0 | 1.7 | 120.3 | 120.0 |
| 50.0 | 1,256,002.6 | 0.28 | 0.00 | 0.00 | 0.00 | 0.00 | 0.27 | 0.00 | 2.7 | 15.9 | 1.9 | 120.4 | 120.0 |
| 75.0 | 1,822,703.3 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.59 | 0.00 | 3.2 | 17.8 | 1.8 | 120.4 | 120.0 |
| 90.0 | 2,149,725.8 | 0.12 | 0.02 | 0.00 | 0.00 | 0.00 | 0.34 | 0.00 | 3.5 | 15.8 | 1.7 | 37.3 | 120.0 |
| 95.0 | 2,248,957.1 | 0.11 | 0.09 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.6 | 15.3 | 1.5 | 38.2 | 120.0 |
| Avg | | 0.51 | 0.03 | 0.00 | 0.00 | 0.00 | 0.60 | 0.00 | 2.2 | 13.2 | 1.7 | 66.4 | 120.0 |
| Min | | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.4 | 1.4 | 17.2 | 120.0 |
| Max | | 2.98 | 0.09 | 0.00 | 0.00 | 0.03 | 1.27 | 0.01 | 3.6 | 17.8 | 1.9 | 120.4 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 14 |
| Running time in seconds for writing input file (t^{write}) | 1.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0500_005.txt$

| Property of graph | Value |
|--------------------|-------|
| Nodes (n) | 500 |
| Density (Δ) | 5.0 % |
| Edges (m) | 6,287 |

| Deviation from best OFV (%) | | | | | | | | | | | Running time (s) | | | | |
|-----------------------------|---------------|-------|------|------|--------|--------|--------|-------|------|-------|------------------|--------|--------|--|--|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly | | |
| 2.5 | 10,279.5 | 0.01 | 0.96 | 1.47 | inf | 0.00 | 0.00 | 0.01 | 1.6 | 42.3 | 120.0 | 0.8 | 26.0 | | |
| 5.0 | 19,006.0 | 0.80 | 0.91 | 0.91 | \inf | 0.00 | 0.00 | 0.01 | 2.4 | 55.2 | 120.0 | 2.1 | 65.0 | | |
| 10.0 | $36,\!218.0$ | 0.38 | 0.06 | 0.59 | \inf | 0.00 | 0.00 | 0.01 | 3.4 | 73.1 | 120.0 | 7.2 | 120.0 | | |
| 25.0 | 88,661.2 | 0.18 | 0.04 | 0.43 | \inf | 0.00 | 0.00 | 0.01 | 5.6 | 103.3 | 120.0 | 5.8 | 94.0 | | |
| 50.0 | $175,\!132.8$ | 0.07 | 0.05 | 0.05 | \inf | 0.00 | 0.02 | 0.01 | 8.1 | 106.5 | 120.0 | 2.1 | 120.0 | | |
| 75.0 | $255,\!337.1$ | 0.02 | 0.01 | 0.03 | \inf | 0.00 | 0.00 | 0.00 | 9.8 | 111.1 | 120.0 | 0.8 | 54.0 | | |
| 90.0 | 297,237.9 | 0.00 | 0.00 | 0.00 | \inf | 0.00 | 0.01 | 0.00 | 10.6 | 99.0 | 120.0 | 0.8 | 82.0 | | |
| 95.0 | $309,\!846.2$ | 0.07 | 0.04 | 0.00 | \inf | 0.01 | 0.00 | 0.00 | 10.9 | 89.1 | 120.0 | 1.5 | 120.0 | | |
| Avg | | 0.19 | 0.26 | 0.43 | inf | 0.00 | 0.00 | 0.01 | 6.5 | 85.0 | 120.0 | 2.6 | 85.1 | | |
| Min | | 0.00 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 1.6 | 42.3 | 120.0 | 0.8 | 26.0 | | |
| Max | | 0.80 | 0.96 | 1.47 | \inf | 0.01 | 0.02 | 0.01 | 10.9 | 111.1 | 120.0 | 7.2 | 120.0 | | |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 28 |
| Running time in seconds for writing input file (t^{write}) | 1.5 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0500_010.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 500 |
| Density (Δ) | 10.0~% |
| Edges (m) | 12,436 |

| | | | T | Runnin | g time | (e) | | | | | | | |
|----------|---------------|--------|------|--------|--------|--------|--------|-------|------|-------|-------|--------|--------|
| | | n from | | 1 | tumm | g time | (8) | | | | | | |
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 16,851.5 | 0.13 | 0.14 | 0.49 | inf | 0.00 | 0.00 | 0.01 | 1.6 | 40.5 | 120.0 | 28.3 | 104.0 |
| 5.0 | 33,465.0 | 0.13 | 0.02 | 0.34 | \inf | 0.00 | 0.10 | 0.01 | 2.4 | 56.0 | 120.0 | 24.2 | 120.0 |
| 10.0 | $66,\!376.0$ | 0.35 | 0.39 | 0.53 | \inf | 0.00 | 0.23 | 0.01 | 3.5 | 73.7 | 120.0 | 30.8 | 120.0 |
| 25.0 | $168,\!126.2$ | 0.25 | 0.07 | 0.08 | \inf | 0.00 | 0.08 | 0.01 | 5.8 | 103.3 | 120.0 | 23.3 | 120.0 |
| 50.0 | 338,629.6 | 0.03 | 0.03 | 0.04 | \inf | 0.00 | 0.10 | 0.01 | 8.2 | 109.7 | 120.0 | 26.9 | 120.0 |
| 75.0 | 506,632.2 | 0.04 | 0.01 | 0.01 | \inf | 0.00 | 0.00 | 0.01 | 9.8 | 107.1 | 120.0 | 4.5 | 120.0 |
| 90.0 | 599,934.3 | 0.05 | 0.05 | 0.00 | \inf | 0.00 | 0.03 | 0.00 | 10.8 | 96.9 | 120.0 | 2.7 | 120.0 |
| 95.0 | $627,\!844.9$ | 0.02 | 0.02 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 10.9 | 91.1 | 120.0 | 3.1 | 120.0 |
| Avg | | 0.12 | 0.09 | 0.19 | inf | 0.00 | 0.07 | 0.01 | 6.6 | 84.8 | 120.0 | 17.9 | 118.0 |
| Min | | 0.02 | 0.01 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 1.6 | 40.5 | 120.0 | 2.7 | 104.0 |
| Max | | 0.35 | 0.39 | 0.53 | \inf | 0.00 | 0.23 | 0.01 | 10.9 | 109.7 | 120.0 | 30.8 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 12 |
| Running time in seconds for writing input file (t^{write}) | 1.6 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0500_025.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 500 |
| Density (Δ) | 25.0 % |
| Edges (m) | 30,983 |

| | | Running time (s) | | | | | | | | | | | |
|----------|-------------|----------------------------|------|------|--------|--------|--------|----------------------------|------|-------|-------|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 39,971.0 | 0.00 | 0.20 | 0.20 | inf | 0.00 | 0.00 | 0.01 | 1.8 | 45.1 | 120.0 | 59.5 | 120.0 |
| 5.0 | 81,928.3 | 0.18 | 0.00 | 0.04 | \inf | 0.00 | 0.00 | 0.01 | 2.6 | 57.4 | 120.0 | 125.6 | 120.0 |
| 10.0 | 162,304.2 | 0.14 | 0.06 | 0.00 | \inf | 4.48 | 0.23 | 0.01 | 3.8 | 78.5 | 120.0 | 121.0 | 120.0 |
| 25.0 | 417,083.5 | 0.11 | 0.00 | 0.00 | \inf | 3.63 | 0.12 | 0.01 | 6.1 | 106.0 | 120.0 | 120.5 | 120.0 |
| 50.0 | 845,997.6 | 0.21 | 0.03 | 0.00 | \inf | 0.66 | 0.10 | 0.01 | 8.6 | 105.4 | 120.0 | 120.1 | 120.0 |
| 75.0 | 1,266,974.9 | 0.00 | 0.01 | 0.01 | \inf | 0.00 | 0.41 | 0.01 | 10.4 | 105.1 | 120.0 | 10.9 | 120.0 |
| 90.0 | 1,504,077.4 | 0.12 | 0.09 | 0.00 | \inf | 0.02 | 0.18 | 0.00 | 11.3 | 97.7 | 120.0 | 120.1 | 120.0 |
| 95.0 | 1,575,775.3 | 0.00 | 0.00 | 0.00 | \inf | 0.00 | 0.17 | 0.00 | 11.5 | 87.7 | 120.0 | 4.0 | 120.0 |
| Avg | | 0.10 | 0.05 | 0.03 | inf | 1.10 | 0.15 | 0.01 | 7.0 | 85.4 | 120.0 | 85.2 | 120.0 |
| Min | | 0.00 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 1.8 | 45.1 | 120.0 | 4.0 | 120.0 |
| Max | | 0.21 | 0.20 | 0.20 | \inf | 4.48 | 0.41 | 0.01 | 11.5 | 106.0 | 120.0 | 125.6 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 10 |
| Running time in seconds for writing input file (t^{write}) | 1.9 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.3 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0500_050.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 500 |
| Density (Δ) | 50.0~% |
| Edges (m) | 62,868 |

| | | Running time (s) | | | | | | | | | | | |
|----------|---------------|----------------------------|------|------|--------|--------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 80,394.6 | 0.09 | 0.09 | 0.00 | inf | 5.57 | 0.20 | 0.01 | 1.7 | 43.2 | 120.0 | 120.1 | 120.0 |
| 5.0 | $164,\!824.7$ | 0.23 | 0.12 | 0.00 | \inf | 4.66 | 0.42 | 0.01 | 2.4 | 61.3 | 120.0 | 120.2 | 120.0 |
| 10.0 | $330,\!688.7$ | 0.03 | 0.00 | 0.00 | \inf | 3.00 | 0.32 | 0.01 | 3.5 | 75.2 | 120.0 | 120.1 | 120.0 |
| 25.0 | 825,678.4 | 0.16 | 0.00 | 0.01 | \inf | 3.73 | 0.26 | 0.01 | 5.6 | 103.9 | 120.0 | 120.1 | 120.0 |
| 50.0 | 1,674,269.7 | 0.38 | 0.00 | 0.00 | \inf | 2.47 | 0.27 | 0.01 | 8.1 | 114.0 | 120.0 | 120.1 | 120.0 |
| 75.0 | 2,517,928.6 | 0.21 | 0.00 | 0.00 | \inf | 0.00 | 0.43 | 0.01 | 10.1 | 114.2 | 120.0 | 101.2 | 120.0 |
| 90.0 | 3,002,648.0 | 0.01 | 0.00 | 0.00 | \inf | 0.00 | 0.28 | 0.00 | 10.7 | 102.0 | 120.0 | 27.8 | 120.0 |
| 95.0 | 3,147,311.4 | 0.18 | 0.18 | 0.00 | inf | 0.00 | 0.04 | 0.00 | 11.0 | 93.3 | 120.0 | 120.1 | 120.0 |
| Avg | | 0.16 | 0.05 | 0.00 | inf | 2.43 | 0.28 | 0.01 | 6.6 | 88.4 | 120.0 | 106.2 | 120.0 |
| Min | | 0.01 | 0.00 | 0.00 | \inf | 0.00 | 0.04 | 0.00 | 1.7 | 43.2 | 120.0 | 27.8 | 120.0 |
| Max | | 0.38 | 0.18 | 0.01 | \inf | 5.57 | 0.43 | 0.01 | 11.0 | 114.2 | 120.0 | 120.2 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 7 |
| Running time in seconds for writing input file (t^{write}) | 2.0 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.3 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0500_075.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 500 |
| Density (Δ) | 75.0 % |
| Edges (m) | 93,584 |

| Deviation from best OFV (%) | | | | | | | | | Running time (s) | | | | | |
|-----------------------------|-------------|-------|------|------|--------|--------------|--------|-------|------------------|-------|-------|--------|--------|--|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly | |
| 2.5 | 125,730.7 | 0.12 | 0.12 | 0.00 | inf | 1,154.23 | 0.20 | 0.01 | 1.9 | 46.1 | 120.0 | 120.1 | 120.0 | |
| 5.0 | 252,651.6 | 1.33 | 0.53 | 0.00 | \inf | 1,072.69 | 0.58 | 0.01 | 2.7 | 57.7 | 120.0 | 120.1 | 120.0 | |
| 10.0 | 491,984.0 | 0.49 | 0.10 | 0.00 | \inf | 633.08 | 1.53 | 0.01 | 3.9 | 79.6 | 120.0 | 120.2 | 120.0 | |
| 25.0 | 1,249,318.7 | 0.01 | 0.00 | 0.00 | \inf | 1.83 | 0.97 | 0.01 | 6.3 | 104.5 | 120.0 | 120.1 | 120.0 | |
| 50.0 | 2,508,630.9 | 0.09 | 0.01 | 0.00 | \inf | 17.17 | 0.62 | 0.01 | 8.9 | 105.1 | 120.0 | 120.0 | 120.0 | |
| 75.0 | 3,735,354.4 | 0.11 | 0.00 | 0.00 | \inf | 11.52 | 0.78 | 0.01 | 10.8 | 108.5 | 120.0 | 120.1 | 120.0 | |
| 90.0 | 4,437,010.7 | 0.01 | 0.01 | 0.00 | \inf | 0.00 | 0.48 | 0.00 | 11.7 | 98.0 | 120.0 | 32.1 | 120.0 | |
| 95.0 | 4,656,801.2 | 0.13 | 0.09 | 0.00 | \inf | 0.07 | 0.00 | 0.00 | 12.0 | 88.2 | 120.0 | 120.1 | 120.0 | |
| Avg | | 0.29 | 0.11 | 0.00 | inf | 361.32 | 0.65 | 0.01 | 7.3 | 86.0 | 120.0 | 109.1 | 120.0 | |
| Min | | 0.01 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 1.9 | 46.1 | 120.0 | 32.1 | 120.0 | |
| Max | | 1.33 | 0.53 | 0.00 | \inf | $1,\!154.23$ | 1.53 | 0.01 | 12.0 | 108.5 | 120.0 | 120.2 | 120.0 | |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 7 |
| Running time in seconds for writing input file (t^{write}) | 2.4 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.3 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_0500_100.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 500 |
| Density (Δ) | 100.0 % |
| Edges (m) | 124,750 |

| Deviation from best OFV (%) | | | | | | | | | Running time (s) | | | | | |
|-----------------------------|-------------------|-------|------|------|--------|----------|--------|-------|------------------|-------|-------|--------|--------|--|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly | |
| 2.5 | 148,301.2 | 0.36 | 0.20 | 0.00 | \inf | 2,784.87 | 0.63 | 0.01 | 1.8 | 43.1 | 120.0 | 120.1 | 120.0 | |
| 5.0 | 301,338.9 | 0.35 | 0.07 | 0.00 | \inf | 1,333.34 | 0.35 | 0.01 | 2.6 | 61.1 | 120.0 | 120.1 | 120.0 | |
| 10.0 | 609,934.3 | 0.47 | 0.10 | 0.00 | \inf | 631.34 | 0.25 | 0.01 | 4.2 | 79.5 | 120.0 | 120.1 | 120.0 | |
| 25.0 | 1,604,214.3 | 0.60 | 0.00 | 0.00 | \inf | 266.56 | 0.36 | 0.01 | 6.6 | 104.5 | 120.0 | 120.1 | 120.0 | |
| 50.0 | 3,300,381.5 | 0.31 | 0.02 | 0.00 | \inf | 101.92 | 0.55 | 0.01 | 9.1 | 105.6 | 120.0 | 120.1 | 120.0 | |
| 75.0 | 4,964,219.9 | 0.09 | 0.02 | 0.00 | \inf | 29.14 | 0.43 | 0.00 | 10.7 | 105.7 | 120.0 | 120.1 | 120.0 | |
| 90.0 | 5,900,911.9 | 0.12 | 0.12 | 0.00 | \inf | 0.09 | 0.21 | 0.00 | 11.8 | 102.1 | 120.0 | 120.1 | 120.0 | |
| 95.0 | $6,\!180,\!619.2$ | 0.01 | 0.01 | 0.00 | \inf | 0.01 | 0.18 | 0.00 | 11.8 | 94.1 | 120.0 | 85.3 | 120.0 | |
| Avg | | 0.29 | 0.07 | 0.00 | inf | 643.41 | 0.37 | 0.01 | 7.3 | 87.0 | 120.0 | 115.7 | 120.0 | |
| Min | | 0.01 | 0.00 | 0.00 | \inf | 0.01 | 0.18 | 0.00 | 1.8 | 43.1 | 120.0 | 85.3 | 120.0 | |
| Max | | 0.60 | 0.20 | 0.00 | \inf | 2,784.87 | 0.63 | 0.01 | 11.8 | 105.7 | 120.0 | 120.1 | 120.0 | |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 8 |
| Running time in seconds for writing input file (t^{write}) | 2.6 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.4 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_1000_005.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 1,000 |
| Density (Δ) | 5.0~% |
| Edges (m) | 25,194 |

| | | Dev | viation | Running time (s) | | | | | | | | | |
|----------|---------------|----------------------------|---------|------------------|--------|--------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 34,115.6 | 0.22 | 0.52 | \inf | \inf | 0.00 | 0.00 | 0.02 | 9.8 | 120.0 | 120.0 | 59.6 | 120.0 |
| 5.0 | 67,342.3 | 0.33 | 0.26 | \inf | \inf | 0.00 | 0.15 | 0.01 | 14.5 | 120.0 | 120.0 | 120.8 | 120.0 |
| 10.0 | $136,\!118.6$ | 0.10 | 0.07 | \inf | \inf | 0.00 | 0.07 | 0.02 | 22.0 | 120.0 | 120.0 | 122.6 | 120.0 |
| 25.0 | $345,\!626.7$ | 0.04 | 0.04 | \inf | \inf | 0.00 | 0.10 | 0.03 | 36.2 | 120.0 | 120.0 | 48.9 | 120.0 |
| 50.0 | $688,\!278.2$ | 0.03 | 0.02 | \inf | \inf | 0.00 | 0.13 | 0.02 | 50.6 | 120.0 | 120.0 | 19.4 | 120.0 |
| 75.0 | 1,017,018.2 | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.24 | 0.01 | 58.9 | 120.0 | 120.0 | 5.2 | 120.0 |
| 90.0 | 1,197,808.3 | 0.01 | 0.00 | \inf | \inf | 0.00 | 0.16 | 0.01 | 63.3 | 120.0 | 120.0 | 5.3 | 120.0 |
| 95.0 | 1,251,125.7 | 0.02 | 0.00 | \inf | \inf | 0.00 | 0.00 | 0.01 | 65.2 | 120.0 | 120.0 | 3.7 | 88.0 |
| Avg | | 0.09 | 0.11 | \inf | \inf | 0.00 | 0.11 | 0.02 | 40.1 | 120.0 | 120.0 | 48.2 | 116.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.00 | 0.01 | 9.8 | 120.0 | 120.0 | 3.7 | 88.0 |
| Max | | 0.33 | 0.52 | \inf | \inf | 0.00 | 0.24 | 0.03 | 65.2 | 120.0 | 120.0 | 122.6 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 16 |
| Running time in seconds for writing input file (t^{write}) | 3.2 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.4 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_1000_010.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 1,000 |
| Density (Δ) | 10.0 % |
| Edges (m) | 50,127 |

| | | Dev | viation | Running time (s) | | | | | | | | | |
|----------|-------------------|----------------------------|---------|------------------|--------|--------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 67,443.8 | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.55 | 0.03 | 10.0 | 120.0 | 120.0 | 120.1 | 120.0 |
| 5.0 | $137,\!244.2$ | 0.00 | 0.06 | \inf | \inf | 0.00 | 0.06 | 0.01 | 14.9 | 120.0 | 120.0 | 82.1 | 120.0 |
| 10.0 | $273,\!351.6$ | 0.09 | 0.00 | \inf | \inf | 0.01 | 0.25 | 0.02 | 21.7 | 120.0 | 120.0 | 120.8 | 120.0 |
| 25.0 | 688,048.8 | 0.04 | 0.00 | \inf | \inf | 0.00 | 0.17 | 0.02 | 35.5 | 120.0 | 120.0 | 120.2 | 120.0 |
| 50.0 | 1,363,588.6 | 0.01 | 0.00 | \inf | \inf | 0.00 | 0.13 | 0.03 | 50.1 | 120.0 | 120.0 | 120.9 | 120.0 |
| 75.0 | 2,032,806.1 | 0.06 | 0.02 | \inf | \inf | 0.00 | 0.32 | 0.02 | 59.4 | 120.0 | 120.0 | 13.6 | 120.0 |
| 90.0 | 2,411,527.8 | 0.07 | 0.07 | \inf | \inf | 0.00 | 0.19 | 0.01 | 62.7 | 120.0 | 120.0 | 34.8 | 120.0 |
| 95.0 | $2,\!529,\!974.3$ | 0.02 | 0.01 | \inf | \inf | 0.00 | 0.05 | 0.01 | 64.4 | 120.0 | 120.0 | 11.5 | 120.0 |
| Avg | | 0.04 | 0.02 | \inf | \inf | 0.00 | 0.22 | 0.02 | 39.8 | 120.0 | 120.0 | 78.0 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.05 | 0.01 | 10.0 | 120.0 | 120.0 | 11.5 | 120.0 |
| Max | | 0.09 | 0.07 | \inf | \inf | 0.01 | 0.55 | 0.03 | 64.4 | 120.0 | 120.0 | 120.9 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 9 |
| Running time in seconds for writing input file (t^{write}) | 3.4 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.5 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_1000_025.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 1,000 |
| Density (Δ) | 25.0 % |
| Edges (m) | 124,947 |

| | | Running time (s) | | | | | | | | | | | |
|----------|---------------|----------------------------|------|--------|--------|--------------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 157,343.2 | 0.16 | 0.00 | \inf | inf | 2,176.80 | 0.49 | 0.03 | 10.8 | 120.0 | 120.0 | 120.3 | 120.0 |
| 5.0 | $327,\!489.1$ | 0.17 | 0.00 | \inf | \inf | $1,\!478.36$ | 0.30 | 0.01 | 16.1 | 120.0 | 120.0 | 120.3 | 120.0 |
| 10.0 | $665,\!399.5$ | 0.13 | 0.00 | \inf | \inf | 3.33 | 0.21 | 0.02 | 23.8 | 120.0 | 120.0 | 120.2 | 120.0 |
| 25.0 | 1,680,443.2 | 0.01 | 0.00 | \inf | \inf | 36.72 | 0.19 | 0.03 | 38.5 | 120.0 | 120.0 | 120.2 | 120.0 |
| 50.0 | 3,360,809.1 | 0.02 | 0.00 | \inf | \inf | 31.22 | 0.30 | 0.03 | 52.4 | 120.0 | 120.0 | 120.3 | 120.0 |
| 75.0 | 5,041,732.8 | 0.02 | 0.00 | \inf | \inf | 0.00 | 0.34 | 0.02 | 63.4 | 120.0 | 120.0 | 22.0 | 120.0 |
| 90.0 | 5,994,850.1 | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.29 | 0.01 | 68.6 | 120.0 | 120.0 | 41.7 | 120.0 |
| 95.0 | 6,285,518.1 | 0.08 | 0.07 | \inf | \inf | 0.00 | 0.17 | 0.01 | 69.5 | 120.0 | 120.0 | 97.7 | 120.0 |
| Avg | | 0.07 | 0.01 | inf | inf | 465.80 | 0.29 | 0.02 | 42.9 | 120.0 | 120.0 | 95.3 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.17 | 0.01 | 10.8 | 120.0 | 120.0 | 22.0 | 120.0 |
| Max | | 0.17 | 0.07 | \inf | \inf | $2,\!176.80$ | 0.49 | 0.03 | 69.5 | 120.0 | 120.0 | 120.3 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 8 |
| Running time in seconds for writing input file (t^{write}) | 4.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.6 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_1000_050.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 1,000 |
| Density (Δ) | 50.0 % |
| Edges (m) | 249,988 |

| - | | Running time (s) | | | | | | | | | | | |
|----------|--------------------|------------------|------|--------|--------|--------------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 314,939.5 | 0.66 | 0.00 | \inf | \inf | 2,223.13 | 0.37 | 0.03 | 10.8 | 120.0 | 120.0 | 120.4 | 120.0 |
| 5.0 | $647,\!545.7$ | 0.11 | 0.00 | \inf | \inf | 1,586.98 | 1.05 | 0.01 | 15.5 | 120.0 | 120.0 | 120.4 | 120.0 |
| 10.0 | 1,300,651.4 | 0.02 | 0.00 | \inf | \inf | 784.02 | 0.86 | 0.02 | 23.2 | 120.0 | 120.0 | 120.5 | 120.0 |
| 25.0 | 3,272,599.4 | 0.03 | 0.00 | \inf | \inf | 292.42 | 0.72 | 0.03 | 37.7 | 120.0 | 120.0 | 120.3 | 120.0 |
| 50.0 | 6,623,406.3 | 0.01 | 0.00 | \inf | \inf | 105.90 | 0.69 | 0.03 | 52.0 | 120.0 | 120.0 | 120.4 | 120.0 |
| 75.0 | 9,992,797.1 | 0.00 | 0.00 | \inf | \inf | 37.83 | 0.63 | 0.02 | 62.7 | 120.0 | 120.0 | 120.4 | 120.0 |
| 90.0 | $11,\!873,\!410.7$ | 0.04 | 0.00 | \inf | \inf | 10.04 | 0.19 | 0.01 | 68.4 | 120.0 | 120.0 | 120.3 | 120.0 |
| 95.0 | $12,\!447,\!967.5$ | 0.02 | 0.00 | \inf | \inf | 4.71 | 0.04 | 0.01 | 73.0 | 120.0 | 120.0 | 120.5 | 120.0 |
| Avg | | 0.11 | 0.00 | \inf | inf | 630.63 | 0.57 | 0.02 | 42.9 | 120.0 | 120.0 | 120.4 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 4.71 | 0.04 | 0.01 | 10.8 | 120.0 | 120.0 | 120.3 | 120.0 |
| Max | | 0.66 | 0.00 | \inf | \inf | $2,\!223.13$ | 1.05 | 0.03 | 73.0 | 120.0 | 120.0 | 120.5 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 8 |
| Running time in seconds for writing input file (t^{write}) | 5.2 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.7 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_1000_075.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 1,000 |
| Density (Δ) | 75.0 % |
| Edges (m) | 374,545 |

| | | Running time (s) | | | | | | | | | | | |
|----------|--------------------|------------------|------|--------|--------|--------------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 460,812.3 | 0.08 | 0.00 | \inf | \inf | 3,372.15 | 1.16 | 0.03 | 11.5 | 120.0 | 120.0 | 120.5 | 120.0 |
| 5.0 | $940,\!602.0$ | 0.22 | 0.00 | \inf | \inf | 1,756.63 | 0.75 | 0.01 | 17.0 | 120.0 | 120.0 | 120.5 | 120.0 |
| 10.0 | 1,912,031.0 | 0.05 | 0.00 | \inf | \inf | 821.15 | 0.61 | 0.02 | 27.1 | 120.0 | 120.0 | 120.4 | 120.0 |
| 25.0 | 4,927,131.5 | 0.25 | 0.00 | \inf | \inf | 287.81 | 1.06 | 0.03 | 43.1 | 120.0 | 120.0 | 120.4 | 120.0 |
| 50.0 | 9,930,130.4 | 0.17 | 0.00 | \inf | \inf | 104.72 | 1.06 | 0.03 | 57.5 | 120.0 | 120.0 | 120.5 | 120.0 |
| 75.0 | 14,868,341.5 | 0.00 | 0.00 | \inf | \inf | 33.90 | 0.85 | 0.01 | 71.0 | 120.0 | 120.0 | 120.4 | 120.0 |
| 90.0 | 17,641,539.2 | 0.03 | 0.00 | \inf | \inf | 12.70 | 0.33 | 0.01 | 76.7 | 120.0 | 120.0 | 120.3 | 120.0 |
| 95.0 | $18,\!503,\!122.9$ | 0.01 | 0.00 | \inf | \inf | 6.19 | 0.16 | 0.01 | 78.7 | 120.0 | 120.0 | 120.4 | 120.0 |
| Avg | | 0.10 | 0.00 | inf | inf | 799.41 | 0.75 | 0.02 | 47.8 | 120.0 | 120.0 | 120.4 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 6.19 | 0.16 | 0.01 | 11.5 | 120.0 | 120.0 | 120.3 | 120.0 |
| Max | | 0.25 | 0.00 | \inf | \inf | $3,\!372.15$ | 1.16 | 0.03 | 78.7 | 120.0 | 120.0 | 120.5 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 10 |
| Running time in seconds for writing input file (t^{write}) | 7.4 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.8 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_1000_100.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 1,000 |
| Density (Δ) | 100.0 % |
| Edges (m) | 499,500 |

| - | | Running time (s) | | | | | | | | | | | |
|----------|--------------------|------------------|------|--------|--------|----------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 626,009.1 | 0.32 | 0.00 | \inf | \inf | 1,889.30 | 1.56 | 0.03 | 11.4 | 120.0 | 120.0 | 120.4 | 121.0 |
| 5.0 | 1,288,133.1 | 0.32 | 0.00 | \inf | \inf | 1,314.91 | 1.07 | 0.01 | 16.5 | 120.0 | 120.0 | 120.6 | 121.0 |
| 10.0 | 2,617,034.9 | 0.12 | 0.00 | \inf | \inf | 817.94 | 1.70 | 0.02 | 24.5 | 120.0 | 120.0 | 120.6 | 121.0 |
| 25.0 | 6,573,200.3 | 0.30 | 0.00 | \inf | \inf | 302.93 | 2.38 | 0.03 | 39.1 | 120.0 | 120.0 | 120.4 | 121.0 |
| 50.0 | $13,\!180,\!965.3$ | 0.02 | 0.00 | \inf | \inf | 104.08 | 1.86 | 0.03 | 53.9 | 120.0 | 120.0 | 120.5 | 121.0 |
| 75.0 | 19,855,996.0 | 0.06 | 0.00 | \inf | \inf | 39.31 | 0.87 | 0.01 | 63.2 | 120.0 | 120.0 | 120.5 | 120.0 |
| 90.0 | $23,\!618,\!998.4$ | 0.01 | 0.00 | \inf | \inf | 14.84 | 0.44 | 0.01 | 68.2 | 120.0 | 120.0 | 120.6 | 121.0 |
| 95.0 | $24,\!783,\!815.3$ | 0.02 | 0.00 | \inf | \inf | 7.06 | 0.13 | 0.01 | 70.6 | 120.0 | 120.0 | 120.5 | 121.0 |
| Avg | | 0.15 | 0.00 | \inf | inf | 561.30 | 1.25 | 0.02 | 43.4 | 120.0 | 120.0 | 120.5 | 120.9 |
| Min | | 0.01 | 0.00 | \inf | \inf | 7.06 | 0.13 | 0.01 | 11.4 | 120.0 | 120.0 | 120.4 | 120.0 |
| Max | | 0.32 | 0.00 | \inf | \inf | 1,889.30 | 2.38 | 0.03 | 70.6 | 120.0 | 120.0 | 120.6 | 121.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 8 |
| Running time in seconds for writing input file (t^{write}) | 7.4 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.9 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_2000_005.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 2,000 |
| Density (Δ) | 5.0 % |
| Edges (m) | 100,341 |

| | | | | | | st OFV (9 | | | | | | | |
|----------------|---------------|------------------|------|--------|--------|-----------|--------|-------|-------|-------|-------|--------|--------|
| | | Running time (s) | | | | | | | | | | | |
| $\underline{}$ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 136,660.3 | 0.13 | 0.00 | \inf | \inf | 1,694.33 | 0.12 | 0.13 | 69.6 | 120.0 | 120.0 | 120.1 | 120.0 |
| 5.0 | $276,\!555.0$ | 0.06 | 0.00 | \inf | \inf | 0.08 | 0.17 | 0.03 | 106.3 | 120.0 | 120.0 | 120.4 | 120.0 |
| 10.0 | 549,513.7 | 0.02 | 0.00 | \inf | \inf | 42.29 | 0.21 | 0.07 | 120.0 | 120.0 | 120.0 | 120.0 | 120.0 |
| 25.0 | 1,352,294.5 | 0.03 | 0.00 | \inf | \inf | 66.72 | 0.20 | 0.11 | 120.1 | 120.0 | 120.0 | 120.2 | 120.0 |
| 50.0 | 2,711,346.8 | 0.02 | 0.00 | \inf | \inf | 2.05 | 0.31 | 0.12 | 120.0 | 120.0 | 120.0 | 121.7 | 120.0 |
| 75.0 | 4,059,730.8 | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.37 | 0.09 | 120.0 | 120.0 | 120.0 | 52.3 | 120.0 |
| 90.0 | 4,831,701.6 | 0.03 | 0.02 | \inf | \inf | 0.00 | 0.23 | 0.07 | 120.0 | 120.0 | 120.0 | 45.1 | 120.0 |
| 95.0 | 5,066,863.6 | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.07 | 0.07 | 120.1 | 120.0 | 120.0 | 21.9 | 120.0 |
| Avg | | 0.04 | 0.00 | inf | inf | 225.68 | 0.21 | 0.09 | 112.0 | 120.0 | 120.0 | 90.2 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.07 | 0.03 | 69.6 | 120.0 | 120.0 | 21.9 | 120.0 |
| Max | | 0.13 | 0.02 | \inf | \inf | 1,694.33 | 0.37 | 0.13 | 120.1 | 120.0 | 120.0 | 121.7 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 12 |
| Running time in seconds for writing input file (t^{write}) | 7.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.9 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_2000_010.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 2,000 |
| Density (Δ) | 10.0 % |
| Edges (m) | 200,031 |

| | | Running time (s) | | | | | | | | | | | |
|----------|--------------------|------------------|------|--------|--------|--------------|--------|-------|-------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 267,431.9 | 0.00 | 0.00 | \inf | \inf | 2,422.60 | 0.34 | 0.13 | 70.9 | 120.0 | 120.0 | 121.0 | 120.0 |
| 5.0 | $541,\!331.9$ | 0.12 | 0.00 | \inf | \inf | 1,539.85 | 0.51 | 0.03 | 101.9 | 120.0 | 120.0 | 120.7 | 120.0 |
| 10.0 | $1,\!095,\!925.4$ | 0.03 | 0.00 | \inf | \inf | 853.00 | 0.38 | 0.06 | 120.1 | 120.0 | 120.0 | 120.8 | 120.0 |
| 25.0 | 2,712,968.6 | 0.00 | 0.00 | \inf | \inf | 301.76 | 0.62 | 0.10 | 120.1 | 120.0 | 120.0 | 120.7 | 120.0 |
| 50.0 | $5,\!406,\!517.5$ | 0.00 | 0.00 | \inf | \inf | 96.53 | 0.67 | 0.09 | 120.1 | 120.0 | 120.0 | 120.9 | 120.0 |
| 75.0 | 8,047,887.6 | 0.00 | 0.00 | \inf | \inf | 34.44 | 0.44 | 0.09 | 120.1 | 120.0 | 120.0 | 120.6 | 120.0 |
| 90.0 | $9,\!557,\!256.5$ | 0.02 | 0.00 | \inf | \inf | 11.04 | 0.24 | 0.08 | 120.1 | 120.0 | 120.0 | 120.6 | 120.0 |
| 95.0 | $10,\!027,\!586.5$ | 0.01 | 0.00 | \inf | \inf | 4.96 | 0.11 | 0.07 | 120.0 | 120.0 | 120.0 | 120.7 | 120.0 |
| Avg | | 0.02 | 0.00 | inf | inf | 658.02 | 0.41 | 0.08 | 111.7 | 120.0 | 120.0 | 120.7 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 4.96 | 0.11 | 0.03 | 70.9 | 120.0 | 120.0 | 120.6 | 120.0 |
| Max | | 0.12 | 0.00 | \inf | \inf | $2,\!422.60$ | 0.67 | 0.13 | 120.1 | 120.0 | 120.0 | 121.0 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 9 |
| Running time in seconds for writing input file (t^{write}) | 8.0 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 1.0 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_2000_025.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 2,000 |
| Density (Δ) | 25.0 % |
| Edges (m) | 500,156 |

| | | De | viatio | Running time (s) | | | | | | | | | |
|----------|--------------------|-------|--------|------------------|--------|--------------|--------|-------|-------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 632,319.1 | 0.00 | 0.00 | \inf | \inf | 3,408.45 | 1.13 | 0.13 | 71.5 | 120.0 | 120.0 | 120.8 | 121.0 |
| 5.0 | 1,291,370.9 | 0.10 | 0.00 | \inf | \inf | 1,993.28 | 1.40 | 0.03 | 104.0 | 120.0 | 120.0 | 120.8 | 120.0 |
| 10.0 | 2,609,725.4 | 0.04 | 0.00 | \inf | \inf | 905.08 | 1.70 | 0.06 | 120.1 | 120.0 | 120.0 | 123.4 | 121.0 |
| 25.0 | 6,576,563.4 | 0.00 | 0.00 | \inf | \inf | 312.79 | 1.54 | 0.10 | 120.0 | 120.0 | 120.0 | 125.0 | 121.0 |
| 50.0 | 13,266,581.8 | 0.07 | 0.00 | \inf | \inf | 100.88 | 1.70 | 0.12 | 120.1 | 120.0 | 120.0 | 120.6 | 121.0 |
| 75.0 | 19,925,356.7 | 0.02 | 0.00 | \inf | \inf | 32.77 | 0.77 | 0.09 | 120.2 | 120.0 | 120.0 | 120.4 | 121.0 |
| 90.0 | 23,697,405.0 | 0.01 | 0.00 | \inf | \inf | 13.00 | 0.26 | 0.07 | 120.2 | 120.0 | 120.0 | 120.4 | 121.0 |
| 95.0 | $24,\!844,\!743.8$ | 0.00 | 0.00 | \inf | \inf | 6.64 | 0.09 | 0.07 | 120.0 | 120.0 | 120.0 | 120.5 | 120.0 |
| Avg | | 0.03 | 0.00 | inf | inf | 846.61 | 1.07 | 0.08 | 112.0 | 120.0 | 120.0 | 121.5 | 120.8 |
| Min | | 0.00 | 0.00 | \inf | \inf | 6.64 | 0.09 | 0.03 | 71.5 | 120.0 | 120.0 | 120.4 | 120.0 |
| Max | | 0.10 | 0.00 | \inf | \inf | $3,\!408.45$ | 1.70 | 0.13 | 120.2 | 120.0 | 120.0 | 125.0 | 121.0 |

^{*}The contribution in this paper

| QKBP-specific information | Val | lue |
|---------------------------------------|--|-----|
| Number of breakpoints | | 9 |
| Running time in seconds for writing | input file (t^{write}) 10 | 0.3 |
| Running time in seconds for executing | ng parametric cut procedure (t^{cut}) | 1.3 |
| Running time in seconds for reading | result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_2000_050.txt$

| Property of graph | Value |
|--------------------|-----------|
| Nodes (n) | 2,000 |
| Density (Δ) | 50.0 % |
| Edges (m) | 1,000,241 |

| | | De | viatio | ı froi | n bes | Running time (s) | | | | | | | |
|----------|--------------|-------|--------|--------|--------|------------------|--------|----------------------------|-------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 1,277,868.8 | 0.19 | 0.00 | \inf | \inf | 4,177.33 | 2.93 | 0.14 | 75.7 | 120.0 | 120.0 | 120.7 | 122.0 |
| 5.0 | 2,599,290.7 | 0.00 | 0.00 | \inf | \inf | 1,889.56 | 3.43 | 0.03 | 112.0 | 120.0 | 120.0 | 120.6 | 122.0 |
| 10.0 | 5,292,988.5 | 0.14 | 0.00 | \inf | \inf | 860.41 | 3.22 | 0.06 | 120.0 | 120.0 | 120.0 | 121.8 | 122.0 |
| 25.0 | 13,331,731.0 | 0.01 | 0.00 | \inf | \inf | 290.98 | 3.30 | 0.10 | 120.0 | 120.0 | 120.0 | 120.6 | 122.0 |
| 50.0 | 26,731,177.1 | 0.06 | 0.00 | \inf | \inf | 99.04 | 3.19 | 0.10 | 120.1 | 120.0 | 120.0 | 120.8 | 122.0 |
| 75.0 | 39,883,405.7 | 0.00 | 0.00 | \inf | \inf | 30.89 | 1.31 | 0.10 | 120.2 | 120.0 | 120.0 | 120.6 | 122.0 |
| 90.0 | 47,559,360.5 | 0.00 | 0.00 | \inf | \inf | 10.96 | 0.47 | 0.08 | 120.2 | 120.0 | 120.0 | 121.3 | 122.0 |
| 95.0 | 49,920,793.9 | 0.00 | 0.00 | \inf | \inf | 5.53 | 0.16 | 0.08 | 120.0 | 120.0 | 120.0 | 120.6 | 122.0 |
| Avg | | 0.05 | 0.00 | \inf | \inf | 920.59 | 2.25 | 0.08 | 113.5 | 120.0 | 120.0 | 120.9 | 122.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 5.53 | 0.16 | 0.03 | 75.7 | 120.0 | 120.0 | 120.6 | 122.0 |
| Max | | 0.19 | 0.00 | inf | inf | 4,177.33 | 3.43 | 0.14 | 120.2 | 120.0 | 120.0 | 121.8 | 122.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 8 |
| Running time in seconds for writing input file (t^{write}) | 15.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 2.0 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_2000_075.txt$

| Property of graph | Value |
|--------------------|-----------|
| Nodes (n) | 2,000 |
| Density (Δ) | 75.0 % |
| Edges (m) | 1,500,364 |

| - | | Running time (s) | | | | | | | | | | | |
|----------|--------------|------------------|------|--------|--------|--------------|--------|-------|-------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 1,906,596.5 | 0.20 | 0.00 | \inf | \inf | 2,981.14 | 3.71 | 0.13 | 73.6 | 120.0 | 120.0 | 121.2 | 120.0 |
| 5.0 | 3,891,354.5 | 0.04 | 0.00 | \inf | \inf | 1,493.71 | 5.37 | 0.03 | 107.5 | 120.0 | 120.0 | 120.8 | 120.0 |
| 10.0 | 7,880,918.6 | 0.00 | 0.00 | \inf | \inf | 809.50 | 4.68 | 0.06 | 120.0 | 120.0 | 120.0 | 121.8 | 120.0 |
| 25.0 | 19,785,366.9 | 0.04 | 0.00 | \inf | \inf | 284.39 | 4.64 | 0.10 | 120.1 | 120.0 | 120.0 | 120.9 | 120.0 |
| 50.0 | 40,022,117.0 | 0.03 | 0.00 | \inf | \inf | 103.18 | 3.67 | 0.12 | 120.2 | 120.0 | 120.0 | 122.0 | 120.0 |
| 75.0 | 60,033,170.7 | 0.00 | 0.00 | \inf | \inf | 36.13 | 1.74 | 0.09 | 120.2 | 120.0 | 120.0 | 121.8 | 120.0 |
| 90.0 | 71,642,587.6 | 0.01 | 0.00 | \inf | \inf | 12.87 | 0.51 | 0.07 | 120.1 | 120.0 | 120.0 | 121.0 | 120.0 |
| 95.0 | 75,214,166.8 | 0.00 | 0.00 | \inf | \inf | 7.01 | 0.31 | 0.07 | 120.2 | 120.0 | 120.0 | 121.9 | 120.0 |
| Avg | | 0.04 | 0.00 | inf | inf | 715.99 | 3.08 | 0.08 | 112.7 | 120.0 | 120.0 | 121.4 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 7.01 | 0.31 | 0.03 | 73.6 | 120.0 | 120.0 | 120.8 | 120.0 |
| Max | | 0.20 | 0.00 | \inf | \inf | $2,\!981.14$ | 5.37 | 0.13 | 120.2 | 120.0 | 120.0 | 122.0 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 7 |
| Running time in seconds for writing input file (t^{write}) | 18.6 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 2.5 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-geo_2000_100.txt$

| Property of graph | Value |
|--------------------|-----------|
| Nodes (n) | 2,000 |
| Density (Δ) | 100.0 % |
| Edges (m) | 1,999,000 |

| | | Running time (s) | | | | | | | | | | | |
|----------|--------------------|------------------------------|------|--------|--------|--------------|--------|-------|-------|-------|-------|--------|--------|
| γ | Best OFV | $ \overline{\text{QKBP}^*} $ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 2,580,579.7 | 0.43 | 0.00 | \inf | inf | 3,073.28 | 6.59 | 0.14 | 77.0 | 120.0 | 120.0 | 122.1 | 120.0 |
| 5.0 | 5,201,991.9 | 0.19 | 0.00 | \inf | \inf | 1,957.72 | 6.78 | 0.03 | 111.8 | 120.0 | 120.0 | 121.5 | 120.0 |
| 10.0 | $10,\!471,\!412.4$ | 0.04 | 0.00 | \inf | \inf | 919.85 | 5.54 | 0.06 | 120.0 | 120.0 | 120.0 | 121.7 | 120.0 |
| 25.0 | 26,453,990.6 | 0.13 | 0.00 | \inf | \inf | 313.89 | 5.58 | 0.11 | 120.1 | 120.0 | 120.0 | 121.2 | 120.0 |
| 50.0 | $53,\!197,\!682.5$ | 0.02 | 0.00 | \inf | \inf | 102.96 | 4.73 | 0.12 | 120.0 | 120.0 | 120.0 | 121.8 | 120.0 |
| 75.0 | 79,943,158.1 | 0.00 | 0.00 | \inf | \inf | 34.88 | 2.15 | 0.07 | 120.1 | 120.0 | 120.0 | 121.9 | 120.0 |
| 90.0 | 95,323,342.7 | 0.02 | 0.00 | \inf | \inf | 11.60 | 0.67 | 0.07 | 120.2 | 120.0 | 120.0 | 122.9 | 120.0 |
| 95.0 | 100,105,415.9 | 0.08 | 0.00 | inf | \inf | 5.64 | 0.38 | 0.07 | 120.0 | 120.0 | 120.0 | 121.5 | 120.0 |
| Avg | | 0.11 | 0.00 | inf | inf | 802.48 | 4.05 | 0.08 | 113.6 | 120.0 | 120.0 | 121.8 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 5.64 | 0.38 | 0.03 | 77.0 | 120.0 | 120.0 | 121.2 | 120.0 |
| Max | | 0.43 | 0.00 | \inf | \inf | $3,\!073.28$ | 6.78 | 0.14 | 120.2 | 120.0 | 120.0 | 122.9 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 8 |
| Running time in seconds for writing input file (t^{write}) | 23.5 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 3.5 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0100_005.txt$

| Property of graph | Value |
|--------------------|-------|
| Nodes (n) | 100 |
| Density (Δ) | 5.0 % |
| Edges (m) | 251 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|-------|------|-------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 38,140.3 | 0.00 | 5.03 | 10.27 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.0 | 0.0 |
| 5.0 | $67,\!460.6$ | 2.02 | 3.08 | 2.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.1 | 0.1 | 1.0 |
| 10.0 | $119,\!872.3$ | 5.02 | 2.50 | 0.86 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.2 | 0.0 |
| 25.0 | 264,565.2 | 0.10 | 0.12 | 1.40 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.4 | 0.2 | 0.1 | 2.0 |
| 50.0 | $471,\!375.7$ | 0.47 | 0.47 | 0.35 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.5 | 0.2 | 0.0 | 0.0 |
| 75.0 | 621,400.2 | 0.00 | 0.41 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.0 | 1.0 |
| 90.0 | 687,642.2 | 0.08 | 0.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.0 | 0.0 |
| 95.0 | 701,748.5 | 0.32 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.1 | 0.0 | 0.0 |
| Avg | | 1.00 | 1.46 | 1.86 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 0.1 | 0.5 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.0 | 0.0 |
| Max | | 5.02 | 5.03 | 10.27 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.2 | 2.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 35 |
| Running time in seconds for writing input file (t^{write}) | 0.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0100_010.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 100 |
| Density (Δ) | 10.0 % |
| Edges (m) | 471 |

| | Running time (s) | | | | | | | | | | | | |
|----------|-------------------|----------------------------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 57,117.0 | 1.35 | 0.00 | 6.30 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.1 | 1.0 |
| 5.0 | $106,\!422.9$ | 0.00 | 1.53 | 2.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.2 | 0.0 |
| 10.0 | $205,\!559.9$ | 0.59 | 0.11 | 0.11 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.1 | 1.0 |
| 25.0 | 470,964.6 | 0.00 | 0.37 | 0.58 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.3 | 0.4 | 0.1 | 1.0 |
| 50.0 | 906,817.7 | 0.37 | 0.00 | 0.19 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.5 | 0.3 | 0.4 | 2.0 |
| 75.0 | 1,290,738.3 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.1 | 1.0 |
| 90.0 | 1,477,953.3 | 0.50 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.1 | 1.0 |
| 95.0 | $1,\!526,\!199.7$ | 0.26 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.0 | 0.0 |
| Avg | | 0.38 | 0.25 | 1.15 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 0.1 | 0.9 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.0 | 0.0 |
| Max | | 1.35 | 1.53 | 6.30 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.4 | 0.4 | 2.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 26 |
| Running time in seconds for writing input file (t^{write}) | 0.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0100_025.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 100 |
| Density (Δ) | 25.0~% |
| Edges (m) | 1,226 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|----------------------------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 123,713.2 | 0.89 | 0.89 | 0.89 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.2 | 0.2 | 1.0 |
| 5.0 | 245,784.7 | 1.02 | 0.76 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.4 | 2.0 |
| 10.0 | 477,217.8 | 0.00 | 0.00 | 0.32 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.7 | 1.0 |
| 25.0 | 1,146,784.5 | 0.97 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 0.9 | 9.0 |
| 50.0 | 2,164,788.7 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 0.1 | 1.0 |
| 75.0 | 3,051,221.7 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.1 | 1.0 |
| 90.0 | 3,520,123.3 | 0.23 | 0.35 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.4 | 4.0 |
| 95.0 | 3,662,096.9 | 0.00 | 0.00 | 0.04 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.7 | 0.1 | 0.1 | 0.0 |
| Avg | | 0.39 | 0.25 | 0.16 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 0.4 | 2.4 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.1 | 0.0 |
| Max | | 1.02 | 0.89 | 0.89 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.7 | 0.2 | 0.9 | 9.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 17 |
| Running time in seconds for writing input file (t^{write}) | 0.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0100_050.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 100 |
| Density (Δ) | 50.0~% |
| Edges (m) | 2,492 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|----------------------------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 255,249.4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.2 | 0.5 | 1.0 |
| 5.0 | 448,743.8 | 4.28 | 0.39 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.6 | 4.0 |
| 10.0 | 810,400.3 | 1.20 | 0.17 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 5.1 | 12.0 |
| 25.0 | 1,980,919.5 | 0.46 | 0.10 | 0.10 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.5 | 3.6 | 15.0 |
| 50.0 | 3,949,444.1 | 1.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.5 | 0.2 | 1.2 | 6.0 |
| 75.0 | 5,810,921.5 | 1.16 | 0.25 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.5 | 0.2 | 0.7 | 5.0 |
| 90.0 | 6,802,356.0 | 0.75 | 0.56 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.9 | 13.0 |
| 95.0 | 7,105,637.9 | 0.01 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.1 | 0.6 | 3.0 |
| Avg | | 1.11 | 0.18 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 1.6 | 7.4 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.0 | 0.2 | 0.1 | 0.5 | 1.0 |
| Max | | 4.28 | 0.56 | 0.10 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.5 | 5.1 | 15.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 14 |
| Running time in seconds for writing input file (t^{write}) | 0.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0100_075.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 100 |
| Density (Δ) | 75.0 % |
| Edges (m) | 3,684 |

| Deviation from best OFV (%) | | | | | | | | | Running time (s) | | | | |
|-----------------------------|--------------------|-------|------|------|------|--------|--------|-------|------------------|-----|-----|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 352,111.5 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.7 | 2.0 |
| 5.0 | 673,237.6 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.4 | 3.0 |
| 10.0 | 1,278,185.2 | 1.93 | 0.70 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 1.9 | 19.0 |
| 25.0 | 3,092,915.6 | 0.12 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 1.1 | 8.0 |
| 50.0 | 6,073,147.4 | 0.72 | 0.23 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 1.4 | 4.0 |
| 75.0 | 8,589,661.3 | 0.44 | 0.13 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.5 | 0.2 | 3.3 | 27.0 |
| 90.0 | 9,990,593.6 | 0.17 | 0.17 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 2.0 | 7.0 |
| 95.0 | $10,\!451,\!536.1$ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 0.4 | 3.0 |
| Avg | | 0.42 | 0.15 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 1.4 | 9.1 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 0.4 | 2.0 |
| Max | | 1.93 | 0.70 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 3.3 | 27.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 17 |
| Running time in seconds for writing input file (t^{write}) | 0.4 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0100_100.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 100 |
| Density (Δ) | 100.0~% |
| Edges (m) | 4,950 |

| Deviation from best OFV (%) | | | | | | | | | Running time (s) | | | | |
|-----------------------------|-------------------|-------|------|------|------|--------|--------|-------|------------------|-----|-----|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 529,986.9 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 1.3 | 3.0 |
| 5.0 | 1,040,809.6 | 2.79 | 2.66 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 1.5 | 8.0 |
| 10.0 | 1,891,834.7 | 0.45 | 0.14 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 4.3 | 88.0 |
| 25.0 | $4,\!289,\!387.5$ | 0.98 | 0.59 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 10.2 | 48.0 |
| 50.0 | 8,218,566.5 | 0.15 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.5 | 0.2 | 4.6 | 18.0 |
| 75.0 | 12,029,434.1 | 0.48 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.5 | 0.2 | 1.6 | 11.0 |
| 90.0 | 14,039,399.1 | 0.73 | 0.73 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 4.5 | 35.0 |
| 95.0 | 14,651,459.4 | 0.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 1.4 | 12.0 |
| Avg | | 0.71 | 0.52 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 0.4 | 0.2 | 3.7 | 27.9 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.1 | 0.2 | 0.2 | 1.3 | 3.0 |
| Max | | 2.79 | 2.66 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 0.6 | 0.2 | 10.2 | 88.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 15 |
| Running time in seconds for writing input file (t^{write}) | 0.4 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0200_005.txt$

| Property of graph | Value |
|--------------------|-------|
| Nodes (n) | 200 |
| Density (Δ) | 5.0~% |
| Edges (m) | 995 |

| Deviation from best OFV (%) | | | | | | | | | Running time (s) | | | | | |
|-----------------------------|-------------|-------|------|------|------|--------|--------|-------|------------------|-----|-----|--------|--------|--|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly | |
| 2.5 | 146,162.4 | 0.99 | 0.12 | 5.21 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.2 | 0.5 | 0.2 | 5.0 | |
| 5.0 | 266,776.3 | 0.59 | 0.59 | 2.31 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.7 | 0.6 | 0.2 | 2.0 | |
| 10.0 | 481,767.3 | 0.00 | 0.80 | 1.17 | 0.00 | 0.00 | 0.00 | 0.00 | 0.4 | 2.2 | 0.7 | 0.1 | 0.0 | |
| 25.0 | 1,032,383.2 | 0.31 | 0.17 | 0.40 | 0.00 | 0.00 | 0.00 | 0.00 | 0.7 | 3.2 | 2.2 | 0.4 | 13.0 | |
| 50.0 | 1,890,439.1 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.9 | 4.1 | 1.2 | 0.2 | 8.0 | |
| 75.0 | 2,561,740.8 | 0.11 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.2 | 4.5 | 1.1 | 0.1 | 4.0 | |
| 90.0 | 2,884,872.8 | 0.09 | 0.11 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.3 | 4.5 | 0.7 | 0.2 | 19.0 | |
| 95.0 | 2,982,533.4 | 0.10 | 0.06 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.7 | 0.5 | 0.2 | 4.0 | |
| Avg | | 0.27 | 0.23 | 1.14 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 3.3 | 1.0 | 0.2 | 6.9 | |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.2 | 0.5 | 0.1 | 0.0 | |
| Max | | 0.99 | 0.80 | 5.21 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.7 | 2.2 | 0.4 | 19.0 | |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 35 |
| Running time in seconds for writing input file (t^{write}) | 0.6 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0200_010.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 200 |
| Density (Δ) | 10.0~% |
| Edges (m) | 2,014 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|----------------------------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 205,919.5 | 0.57 | 2.17 | 1.82 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.7 | 0.6 | 5.0 |
| 5.0 | 387,143.6 | 0.59 | 0.17 | 0.49 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.6 | 1.3 | 1.8 | 11.0 |
| 10.0 | 756,587.5 | 1.11 | 0.04 | 0.60 | 0.00 | 0.00 | 0.00 | 0.00 | 0.4 | 2.2 | 2.1 | 1.2 | 9.0 |
| 25.0 | 1,819,489.9 | 0.63 | 0.68 | 0.41 | 0.00 | 0.00 | 0.00 | 0.00 | 0.7 | 3.3 | 1.4 | 0.2 | 3.0 |
| 50.0 | 3,395,526.8 | 0.25 | 0.04 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 1.0 | 4.0 | 1.3 | 0.8 | 17.0 |
| 75.0 | 4,751,300.8 | 0.19 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.2 | 4.4 | 1.1 | 0.5 | 9.0 |
| 90.0 | 5,448,694.2 | 0.04 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.4 | 0.7 | 0.5 | 21.0 |
| 95.0 | 5,645,401.4 | 0.02 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.7 | 0.5 | 0.4 | 9.0 |
| Avg | | 0.43 | 0.39 | 0.42 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 3.2 | 1.1 | 0.7 | 10.5 |
| Min | | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.5 | 0.2 | 3.0 |
| Max | | 1.11 | 2.17 | 1.82 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.7 | 2.1 | 1.8 | 21.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 33 |
| Running time in seconds for writing input file (t^{write}) | 0.7 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0200_025.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 200 |
| Density (Δ) | 25.0 % |
| Edges (m) | 4,912 |

| | Running time (s) | | | | | | | | | | | | |
|----------|--------------------|-------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 423,393.2 | 0.62 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.5 | 2.3 | 10.0 |
| 5.0 | $816,\!435.9$ | 0.56 | 0.60 | 0.39 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.7 | 1.1 | 1.4 | 19.0 |
| 10.0 | 1,585,981.8 | 0.73 | 0.31 | 0.22 | 0.00 | 0.00 | 0.00 | 0.00 | 0.4 | 2.3 | 3.7 | 8.5 | 40.0 |
| 25.0 | 3,971,396.9 | 0.22 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.7 | 3.2 | 1.8 | 2.6 | 22.0 |
| 50.0 | 7,732,914.9 | 0.11 | 0.11 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.0 | 3.9 | 1.7 | 1.8 | 9.0 |
| 75.0 | $11,\!273,\!958.2$ | 0.24 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.2 | 4.4 | 1.1 | 1.2 | 13.0 |
| 90.0 | 13,196,202.6 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.3 | 4.4 | 0.6 | 0.5 | 7.0 |
| 95.0 | 13,741,499.1 | 0.35 | 0.25 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.5 | 0.6 | 1.0 | 32.0 |
| Avg | | 0.35 | 0.16 | 0.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 3.2 | 1.4 | 2.4 | 19.0 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.5 | 0.5 | 7.0 |
| Max | | 0.73 | 0.60 | 0.39 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.5 | 3.7 | 8.5 | 40.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 17 |
| Running time in seconds for writing input file (t^{write}) | 0.7 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0200_050.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 200 |
| Density (Δ) | 50.0 % |
| Edges (m) | 9,910 |

| | Running time (s) | | | | | | | | | | | | |
|----------|--------------------|-------|------|------|------|--------|--------|-------|-----|-----|-----|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 776,259.1 | 3.25 | 0.00 | 0.40 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.6 | 5.2 | 22.0 |
| 5.0 | 1,542,504.5 | 1.09 | 0.32 | 0.07 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.7 | 0.6 | 6.1 | 55.0 |
| 10.0 | 3,021,738.5 | 0.06 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 2.3 | 1.1 | 10.4 | 98.0 |
| 25.0 | 7,397,481.2 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.7 | 3.2 | 1.7 | 8.9 | 60.0 |
| 50.0 | $14,\!569,\!299.9$ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.09 | 0.00 | 1.0 | 4.0 | 7.5 | 19.8 | 120.0 |
| 75.0 | 21,775,525.8 | 0.14 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.2 | 4.3 | 0.9 | 9.7 | 120.0 |
| 90.0 | 25,605,308.3 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.3 | 4.4 | 0.7 | 2.7 | 39.0 |
| 95.0 | 26,758,444.1 | 0.28 | 0.28 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.5 | 0.6 | 2.1 | 24.0 |
| Avg | | 0.60 | 0.08 | 0.06 | 0.00 | 0.00 | 0.01 | 0.00 | 0.8 | 3.2 | 1.7 | 8.1 | 67.2 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.6 | 2.1 | 22.0 |
| Max | | 3.25 | 0.32 | 0.40 | 0.00 | 0.00 | 0.09 | 0.00 | 1.4 | 4.5 | 7.5 | 19.8 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 16 |
| Running time in seconds for writing input file (t^{write}) | 0.7 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.1 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0200_075.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 200 |
| Density (Δ) | 75.0~% |
| Edges (m) | 14,844 |

| Deviation from best OFV (%) | | | | | | | | | Running time (s) | | | | | |
|-----------------------------|--------------------|-------|------|------|------|--------|--------|-------|------------------|-----|-----|--------|--------|--|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly | |
| 2.5 | 1,295,780.2 | 0.48 | 0.48 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.6 | 5.4 | 29.0 | |
| 5.0 | 2,435,088.9 | 0.84 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.7 | 0.6 | 17.6 | 75.0 | |
| 10.0 | 4,676,319.6 | 0.19 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 2.3 | 0.8 | 15.4 | 103.0 | |
| 25.0 | $11,\!535,\!176.1$ | 0.19 | 0.02 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.7 | 3.2 | 0.8 | 22.3 | 120.0 | |
| 50.0 | $22,\!470,\!347.1$ | 0.53 | 0.11 | 0.00 | 0.00 | 0.00 | 0.04 | 0.00 | 1.0 | 3.9 | 1.1 | 21.3 | 120.0 | |
| 75.0 | $32,\!810,\!498.6$ | 0.32 | 0.25 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.2 | 4.4 | 0.8 | 14.3 | 120.0 | |
| 90.0 | $38,\!301,\!995.6$ | 0.49 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.3 | 0.7 | 15.3 | 120.0 | |
| 95.0 | $39,\!956,\!717.1$ | 0.28 | 0.28 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.7 | 0.6 | 7.9 | 120.0 | |
| Avg | | 0.41 | 0.14 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 0.8 | 3.2 | 0.7 | 14.9 | 100.9 | |
| Min | | 0.19 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.6 | 5.4 | 29.0 | |
| Max | | 0.84 | 0.48 | 0.02 | 0.00 | 0.00 | 0.04 | 0.00 | 1.4 | 4.7 | 1.1 | 22.3 | 120.0 | |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 14 |
| Running time in seconds for writing input file (t^{write}) | 0.8 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0200_100.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 200 |
| Density (Δ) | 100.0~% |
| Edges (m) | 19,900 |

| Deviation from best OFV (%) | | | | | | | | | Rı | ınnin | g tin | ne (s) | |
|-----------------------------|--------------------|-------|------|------|------|--------|--------|-------|-----|-------|-------|--------|--------|
| | | | | | | | | | | | | | |
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 1,503,340.4 | 3.20 | 0.14 | 0.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.6 | 25.6 | 120.0 |
| 5.0 | 3,161,207.9 | 1.68 | 0.23 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.3 | 1.7 | 0.6 | 30.6 | 120.0 |
| 10.0 | 6,389,157.8 | 0.23 | 0.07 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 2.3 | 0.7 | 37.6 | 120.0 |
| 25.0 | 16,254,572.2 | 0.29 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.7 | 3.2 | 0.7 | 63.5 | 120.0 |
| 50.0 | $31,\!852,\!586.8$ | 0.09 | 0.09 | 0.00 | 0.00 | 0.00 | 0.03 | 0.00 | 1.0 | 3.9 | 0.7 | 30.2 | 120.0 |
| 75.0 | 46,718,823.1 | 0.39 | 0.00 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 1.2 | 4.4 | 0.7 | 30.5 | 120.0 |
| 90.0 | 54,656,763.5 | 0.36 | 0.33 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.3 | 0.6 | 40.7 | 120.0 |
| 95.0 | $57,\!126,\!753.6$ | 0.18 | 0.18 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.4 | 4.5 | 0.6 | 18.2 | 120.0 |
| Avg | | 0.80 | 0.14 | 0.01 | 0.00 | 0.00 | 0.01 | 0.00 | 0.9 | 3.2 | 0.6 | 34.6 | 120.0 |
| Min | | 0.09 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.2 | 1.3 | 0.6 | 18.2 | 120.0 |
| Max | | 3.20 | 0.33 | 0.08 | 0.00 | 0.00 | 0.03 | 0.00 | 1.4 | 4.5 | 0.7 | 63.5 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 10 |
| Running time in seconds for writing input file (t^{write}) | 0.8 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

File dispersion-qkp-wgeo_0300_005.txt

| Property of graph | Value |
|--------------------|-------|
| Nodes (n) | 300 |
| Density (Δ) | 5.0~% |
| Edges (m) | 2,311 |

| | Running time (s) | | | | | | | | | | | | |
|----------|------------------|-------|------|------|--------|--------|--------|-------|-----|------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 243,827.0 | 0.00 | 0.89 | 3.22 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 5.8 | 1.8 | 0.2 | 4.0 |
| 5.0 | 456,069.3 | 0.79 | 1.12 | 1.92 | 0.00 | 0.00 | 0.00 | 0.00 | 0.7 | 7.6 | 2.4 | 0.3 | 4.0 |
| 10.0 | 871,396.1 | 0.34 | 0.79 | 1.66 | 0.00 | 0.00 | 0.00 | 0.00 | 1.1 | 9.9 | 3.3 | 0.7 | 22.0 |
| 25.0 | 1,982,381.4 | 0.45 | 0.27 | 0.32 | \inf | 0.00 | 0.00 | 0.01 | 1.7 | 14.1 | 120.0 | 1.3 | 21.0 |
| 50.0 | 3,784,007.6 | 0.00 | 0.12 | 0.17 | \inf | 0.00 | 0.00 | 0.01 | 2.5 | 16.5 | 120.0 | 0.6 | 5.0 |
| 75.0 | 5,342,038.6 | 0.03 | 0.07 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 3.1 | 16.8 | 6.2 | 0.4 | 21.0 |
| 90.0 | 6,136,494.3 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.4 | 15.7 | 1.6 | 0.2 | 5.0 |
| 95.0 | 6,334,829.4 | 0.20 | 0.16 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.4 | 16.0 | 1.3 | 0.4 | 55.0 |
| Avg | | 0.23 | 0.43 | 0.91 | inf | 0.00 | 0.00 | 0.00 | 2.0 | 12.8 | 32.1 | 0.5 | 17.1 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 5.8 | 1.3 | 0.2 | 4.0 |
| Max | | 0.79 | 1.12 | 3.22 | \inf | 0.00 | 0.00 | 0.01 | 3.4 | 16.8 | 120.0 | 1.3 | 55.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 24 |
| Running time in seconds for writing input file (t^{write}) | 1.0 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0300_010.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 300 |
| Density (Δ) | 10.0 % |
| Edges (m) | 4,491 |

| Deviation from best OFV (%) | | | | | | | | | | Runnii | ng time | e (s) | |
|-----------------------------|--------------------|-------|------|------|--------|--------|--------|-------|-----|--------|---------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 458,676.4 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 6.0 | 1.5 | 0.3 | 4.0 |
| 5.0 | $844,\!525.4$ | 0.00 | 0.00 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 7.9 | 2.2 | 0.9 | 36.0 |
| 10.0 | $1,\!556,\!993.5$ | 0.49 | 0.44 | 0.23 | 0.00 | 0.00 | 0.00 | 0.00 | 1.1 | 10.3 | 12.9 | 4.6 | 59.0 |
| 25.0 | 3,619,800.7 | 0.36 | 0.03 | 0.05 | \inf | 0.00 | 0.00 | 0.01 | 1.7 | 14.0 | 120.0 | 4.1 | 117.0 |
| 50.0 | 7,002,766.4 | 0.18 | 0.10 | 0.07 | 0.00 | 0.00 | 0.00 | 0.00 | 2.5 | 16.4 | 32.5 | 2.0 | 48.0 |
| 75.0 | 10,160,390.8 | 0.01 | 0.01 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 3.0 | 16.1 | 5.8 | 1.1 | 115.0 |
| 90.0 | 11,857,368.3 | 0.26 | 0.26 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.3 | 16.2 | 2.5 | 1.4 | 120.0 |
| 95.0 | $12,\!374,\!781.3$ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.4 | 15.5 | 1.4 | 0.2 | 1.0 |
| Avg | | 0.16 | 0.10 | 0.05 | \inf | 0.00 | 0.00 | 0.00 | 2.0 | 12.8 | 22.4 | 1.8 | 62.5 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.5 | 6.0 | 1.4 | 0.2 | 1.0 |
| Max | | 0.49 | 0.44 | 0.23 | \inf | 0.00 | 0.00 | 0.01 | 3.4 | 16.4 | 120.0 | 4.6 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 35 |
| Running time in seconds for writing input file (t^{write}) | 1.0 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0300_025.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 300 |
| Density (Δ) | 25.0 % |
| Edges (m) | 11,240 |

| Deviation from best OFV (%) | | | | | | | | | | Running time (s) | | | | |
|-----------------------------|--------------|-------|------|------|------|--------|--------|-------|-----|------------------|------|--------|--------|--|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly | |
| 2.5 | 931,558.9 | 0.50 | 0.08 | 0.11 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.3 | 3.0 | 7.6 | 35.0 | |
| 5.0 | 1,853,334.4 | 0.08 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 8.1 | 4.1 | 7.8 | 66.0 | |
| 10.0 | 3,664,060.9 | 0.52 | 0.26 | 0.05 | 0.00 | 0.00 | 0.00 | 0.01 | 1.1 | 10.4 | 16.7 | 14.0 | 59.0 | |
| 25.0 | 9,131,039.3 | 0.17 | 0.03 | 0.03 | 0.00 | 0.00 | 0.00 | 0.01 | 1.8 | 14.2 | 17.4 | 16.6 | 120.0 | |
| 50.0 | 17,810,122.9 | 0.19 | 0.05 | 0.01 | 0.00 | 0.00 | 0.03 | 0.00 | 2.5 | 16.0 | 6.7 | 11.0 | 120.0 | |
| 75.0 | 25,817,371.7 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.06 | 0.00 | 3.1 | 16.4 | 2.8 | 4.2 | 120.0 | |
| 90.0 | 30,166,923.7 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.3 | 15.5 | 1.8 | 3.1 | 109.0 | |
| 95.0 | 31,466,609.4 | 0.02 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.4 | 15.8 | 1.4 | 5.8 | 97.0 | |
| Avg | | 0.19 | 0.05 | 0.03 | 0.00 | 0.00 | 0.01 | 0.00 | 2.1 | 12.8 | 6.7 | 8.8 | 90.8 | |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.3 | 1.4 | 3.1 | 35.0 | |
| Max | | 0.52 | 0.26 | 0.11 | 0.00 | 0.00 | 0.06 | 0.01 | 3.4 | 16.4 | 17.4 | 16.6 | 120.0 | |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 21 |
| Running time in seconds for writing input file (t^{write}) | 1.0 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0300_050.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 300 |
| Density (Δ) | 50.0 % |
| Edges (m) | 22,294 |

| | | Running time (s) | | | | | | | | | | | |
|----------|--|------------------|------|------|------|------|------|------|-----|------|------|--------|--------|
| γ | γ Best OFV QKBP* GR DP QK Gurobi Hexaly | | | | | | | | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 1,785,890.6 | 0.30 | 0.11 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.2 | 2.5 | 73.6 | 120.0 |
| 5.0 | 3,600,198.8 | 0.70 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 8.2 | 1.5 | 38.7 | 120.0 |
| 10.0 | 6,955,208.0 | 1.06 | 0.00 | 0.00 | 0.00 | 0.00 | 0.07 | 0.00 | 1.2 | 10.6 | 6.6 | 120.7 | 120.0 |
| 25.0 | 17,494,277.6 | 0.11 | 0.04 | 0.03 | 0.00 | 0.00 | 0.00 | 0.01 | 1.8 | 14.0 | 15.4 | 76.8 | 120.0 |
| 50.0 | $35,\!223,\!495.4$ | 0.45 | 0.03 | 0.00 | 0.00 | 0.00 | 0.03 | 0.00 | 2.6 | 16.4 | 3.2 | 44.3 | 120.0 |
| 75.0 | 51,060,804.8 | 0.01 | 0.01 | 0.01 | 0.00 | 0.00 | 0.00 | 0.00 | 3.1 | 16.0 | 2.2 | 24.3 | 120.0 |
| 90.0 | 59,418,082.5 | 0.31 | 0.22 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.4 | 15.7 | 1.7 | 24.5 | 120.0 |
| 95.0 | $61,\!900,\!195.6$ | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.4 | 15.8 | 1.4 | 7.8 | 120.0 |
| Avg | | 0.37 | 0.05 | 0.01 | 0.00 | 0.00 | 0.01 | 0.00 | 2.1 | 12.8 | 4.3 | 51.3 | 120.0 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.2 | 1.4 | 7.8 | 120.0 |
| Max | | 1.06 | 0.22 | 0.03 | 0.00 | 0.00 | 0.07 | 0.01 | 3.4 | 16.4 | 15.4 | 120.7 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 17 |
| Running time in seconds for writing input file (t^{write}) | 1.1 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0300_075.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 300 |
| Density (Δ) | 75.0 % |
| Edges (m) | 33,661 |

| | | Running time (s) | | | | | | | | | | | |
|----------|--|------------------|------|------|------|------|------|------|-----|------|-----|--------|--------|
| γ | γ Best OFV QKBP* GR DP QK Gurobi Hexaly | | | | | | | | | DP | QK | Gurobi | Hexaly |
| 2.5 | 2,999,792.3 | 0.36 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.3 | 1.4 | 25.6 | 120.0 |
| 5.0 | 5,522,693.0 | 0.72 | 0.36 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.8 | 8.2 | 1.6 | 44.2 | 120.0 |
| 10.0 | $10,\!622,\!771.9$ | 0.05 | 0.04 | 0.00 | 0.00 | 0.00 | 0.02 | 0.01 | 1.1 | 10.5 | 2.5 | 113.7 | 120.0 |
| 25.0 | $26,\!124,\!846.2$ | 0.14 | 0.00 | 0.00 | 0.00 | 0.00 | 0.02 | 0.01 | 1.8 | 14.0 | 3.0 | 120.7 | 120.0 |
| 50.0 | $52,\!283,\!443.2$ | 0.22 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 2.5 | 16.2 | 2.5 | 120.3 | 120.0 |
| 75.0 | $75,\!852,\!661.7$ | 0.44 | 0.22 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.0 | 15.9 | 1.9 | 120.3 | 120.0 |
| 90.0 | 88,637,353.5 | 0.15 | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.3 | 16.1 | 1.8 | 41.5 | 120.0 |
| 95.0 | $92,\!604,\!309.4$ | 0.07 | 0.07 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 3.3 | 15.4 | 1.5 | 90.2 | 120.0 |
| Avg | | 0.27 | 0.10 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 2.1 | 12.8 | 2.0 | 84.6 | 120.0 |
| Min | | 0.05 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.3 | 1.4 | 25.6 | 120.0 |
| Max | | 0.72 | 0.36 | 0.00 | 0.00 | 0.00 | 0.02 | 0.01 | 3.3 | 16.2 | 3.0 | 120.7 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 19 |
| Running time in seconds for writing input file (t^{write}) | 1.2 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0300_100.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 300 |
| Density (Δ) | 100.0~% |
| Edges (m) | 44,850 |

| | | Rı | ınnin | g tim | ne (s) | | | | | | | | |
|-----------------|--------------------------------|----------|---------------|-------------------|--------|------|------------------|----------------|--------|--------------|------------|-------------|---------------|
| γ | Best OFV | | eviatio GR | QKBP* | | | | Gurobi | Hevaly | | | | |
| $\frac{1}{2.5}$ | 3,954,022.0 | <u> </u> | | DP 0.00 | | 0.00 | 0.00 | - | 0.6 | 6.5 | 1.4 | 14.2 | 120.0 |
| 5.0 | 7,543,680.9 | 1.16 | | 0.00 | | 0.00 | 0.00 | | 0.8 | 8.7 | 1.4 | 48.9 | 120.0 120.0 |
| 10.0 | 14,538,477.6 | 0.83 | 0.02 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 1.1 | 10.6 | 1.6 | 86.3 | 120.0 |
| 25.0 | 35,493,957.2 | | | 0.00 | | 0.00 | 0.03 | | | 14.2 | 1.7 | 54.5 | 120.0 |
| 50.0 | 68,925,411.6 | 0.28 | 0.0- | 0.00 | | 0.00 | 0.04 | | | 16.1 | 2.0 | 120.3 | 120.0 |
| 75.0 | 102,263,704.4 120,661,324.4 | 0.29 | 0.00 | 0.00 | | 0.00 | 0.00 0.01 | $0.00 \\ 0.00$ | 0.0 | 16.1 15.6 | 1.8 1.5 | 62.1 44.2 | 120.0 120.0 |
| | 125,950,486.8 | 00 | | 0.00 | | 0.00 | 0.01 | | _ | 15.7 | | 13.2 | 120.0 120.0 |
| Avg | | 0.37 | 0.07 | 0.00 | 0.00 | 0.00 | 0.01 | 0.00 | 2.0 | 12.9 | 1.6 | 55.5 | 120.0 |
| Min | | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.6 | 6.5 | 1.4 | 13.2 | 120.0 |
| Max | | 1.16 | 0.46 | 0.00 | 0.00 | 0.00 | 0.04 | 0.01 | 3.4 | 16.1 | 2.0 | 120.3 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 18 |
| Running time in seconds for writing input file (t^{write}) | 1.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.2 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0500_005.txt$

| Property of graph | Value |
|--------------------|-------|
| Nodes (n) | 500 |
| Density (Δ) | 5.0 % |
| Edges (m) | 6,367 |

| | | Running time (s) | | | | | | | | | | | |
|----------|--------------------|------------------|------|------|--------|--------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 558,061.0 | 1.76 | 1.48 | 3.88 | inf | 0.00 | 0.00 | 0.01 | 1.5 | 40.5 | 120.0 | 3.6 | 35.0 |
| 5.0 | 1,128,973.8 | 0.35 | 0.08 | 0.79 | \inf | 0.00 | 0.08 | 0.00 | 2.4 | 54.2 | 120.0 | 2.3 | 120.0 |
| 10.0 | 2,230,939.1 | 0.39 | 0.22 | 0.42 | \inf | 0.00 | 0.00 | 0.01 | 3.4 | 76.1 | 120.0 | 3.8 | 120.0 |
| 25.0 | 5,452,739.2 | 0.15 | 0.12 | 0.36 | \inf | 0.00 | 0.00 | 0.01 | 5.7 | 110.4 | 120.0 | 2.2 | 40.0 |
| 50.0 | $10,\!669,\!402.8$ | 0.06 | 0.03 | 0.06 | \inf | 0.00 | 0.00 | 0.01 | 8.3 | 109.3 | 120.0 | 1.1 | 58.0 |
| 75.0 | $15,\!422,\!748.8$ | 0.03 | 0.03 | 0.03 | \inf | 0.00 | 0.00 | 0.00 | 10.3 | 109.5 | 120.0 | 1.9 | 42.0 |
| 90.0 | 17,896,753.9 | 0.04 | 0.00 | 0.00 | \inf | 0.00 | 0.02 | 0.00 | 11.2 | 103.1 | 120.0 | 1.0 | 120.0 |
| 95.0 | 18,573,898.0 | 0.00 | 0.00 | 0.00 | inf | 0.00 | 0.00 | 0.00 | 11.8 | 94.5 | 120.0 | 0.5 | 1.0 |
| Avg | | 0.35 | 0.24 | 0.69 | inf | 0.00 | 0.01 | 0.01 | 6.8 | 87.2 | 120.0 | 2.1 | 67.0 |
| Min | | 0.00 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 1.5 | 40.5 | 120.0 | 0.5 | 1.0 |
| Max | | 1.76 | 1.48 | 3.88 | \inf | 0.00 | 0.08 | 0.01 | 11.8 | 110.4 | 120.0 | 3.8 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 29 |
| Running time in seconds for writing input file (t^{write}) | 1.7 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.3 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0500_010.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 500 |
| Density (Δ) | 10.0 % |
| Edges (m) | 12,399 |

| | | Running time (s) | | | | | | | | | | | |
|----------|--------------------|------------------|------|------|--------|--------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 1,084,012.7 | 0.23 | 0.38 | 0.57 | inf | 0.00 | 0.00 | 0.01 | 1.5 | 39.2 | 120.0 | 17.0 | 68.0 |
| 5.0 | 2,087,950.0 | 0.00 | 0.09 | 0.45 | \inf | 0.00 | 0.00 | 0.01 | 2.3 | 55.6 | 120.0 | 19.2 | 83.0 |
| 10.0 | 4,020,257.3 | 0.39 | 0.22 | 0.12 | \inf | 0.00 | 0.14 | 0.01 | 3.4 | 72.8 | 120.0 | 32.1 | 120.0 |
| 25.0 | $10,\!123,\!775.8$ | 0.00 | 0.12 | 0.07 | \inf | 0.00 | 0.00 | 0.01 | 5.5 | 103.8 | 120.0 | 26.3 | 120.0 |
| 50.0 | 20,091,488.2 | 0.04 | 0.04 | 0.02 | \inf | 0.00 | 0.04 | 0.01 | 7.9 | 108.9 | 120.0 | 12.1 | 120.0 |
| 75.0 | $29,\!194,\!379.6$ | 0.13 | 0.04 | 0.00 | \inf | 0.00 | 0.01 | 0.00 | 9.5 | 110.7 | 120.0 | 5.8 | 120.0 |
| 90.0 | 34,046,724.2 | 0.04 | 0.01 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 10.4 | 98.4 | 120.0 | 5.1 | 120.0 |
| 95.0 | $35,\!437,\!662.4$ | 0.02 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 10.6 | 88.9 | 120.0 | 1.5 | 9.0 |
| Avg | | 0.11 | 0.11 | 0.15 | inf | 0.00 | 0.02 | 0.01 | 6.4 | 84.8 | 120.0 | 14.9 | 95.0 |
| Min | | 0.00 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 1.5 | 39.2 | 120.0 | 1.5 | 9.0 |
| Max | | 0.39 | 0.38 | 0.57 | \inf | 0.00 | 0.14 | 0.01 | 10.6 | 110.7 | 120.0 | 32.1 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-----------------------|
| Number of breakpoints | 26 |
| Running time in seconds for writing input file (t^{write}) | 1.7 |
| Running time in seconds for executing parametric cut procedure (t^{cu} | $^{\mathrm{lt}})$ 0.3 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

File dispersion-qkp-wgeo_0500_025.txt

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 500 |
| Density (Δ) | 25.0 % |
| Edges (m) | 31,118 |

| | | Running time (s) | | | | | | | | | | | |
|----------|--------------------|------------------|------|------|--------|--------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 2,581,885.1 | 0.30 | 0.24 | 0.00 | \inf | 0.00 | 0.50 | 0.01 | 1.7 | 42.5 | 120.0 | 22.3 | 120.0 |
| 5.0 | 5,160,148.6 | 0.41 | 0.28 | 0.00 | \inf | 0.00 | 0.10 | 0.00 | 2.5 | 56.6 | 120.0 | 19.9 | 120.0 |
| 10.0 | $10,\!016,\!504.2$ | 0.58 | 0.12 | 0.00 | \inf | 0.00 | 0.06 | 0.01 | 3.5 | 73.7 | 120.0 | 91.7 | 120.0 |
| 25.0 | $24,\!853,\!019.8$ | 0.08 | 0.03 | 0.03 | \inf | 0.00 | 0.01 | 0.01 | 5.7 | 103.2 | 120.0 | 43.4 | 120.0 |
| 50.0 | 48,993,908.6 | 0.14 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.01 | 7.9 | 108.0 | 120.0 | 67.4 | 120.0 |
| 75.0 | $72,\!048,\!838.2$ | 0.24 | 0.00 | 0.00 | \inf | 0.00 | 0.09 | 0.00 | 9.5 | 108.5 | 120.0 | 59.2 | 120.0 |
| 90.0 | 84,301,112.3 | 0.07 | 0.05 | 0.00 | \inf | 0.00 | 0.02 | 0.00 | 10.2 | 97.8 | 120.0 | 9.7 | 120.0 |
| 95.0 | 87,707,536.1 | 0.02 | 0.02 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 10.5 | 89.6 | 120.0 | 17.9 | 120.0 |
| Avg | | 0.23 | 0.09 | 0.00 | \inf | 0.00 | 0.10 | 0.01 | 6.4 | 85.0 | 120.0 | 41.4 | 120.0 |
| Min | | 0.02 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 1.7 | 42.5 | 120.0 | 9.7 | 120.0 |
| Max | | 0.58 | 0.28 | 0.03 | \inf | 0.00 | 0.50 | 0.01 | 10.5 | 108.5 | 120.0 | 91.7 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 16 |
| Running time in seconds for writing input file (t^{write}) | 1.9 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.3 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0500_050.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 500 |
| Density (Δ) | 50.0 % |
| Edges (m) | 62,463 |

| | | Running time (s) | | | | | | | | | | | |
|----------|---------------------|------------------|------|------|--------|--------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 4,702,038.2 | 0.52 | 0.40 | 0.00 | \inf | 0.12 | 0.00 | 0.01 | 1.7 | 45.4 | 120.0 | 120.1 | 120.0 |
| 5.0 | $9,\!564,\!042.5$ | 0.58 | 0.07 | 0.00 | \inf | 6.43 | 0.21 | 0.01 | 2.6 | 57.1 | 120.0 | 120.1 | 120.0 |
| 10.0 | 18,747,885.1 | 0.00 | 0.00 | 0.00 | \inf | 1.18 | 0.08 | 0.01 | 3.6 | 78.5 | 120.0 | 120.1 | 120.0 |
| 25.0 | 47,909,716.0 | 0.11 | 0.04 | 0.00 | \inf | 6.50 | 0.00 | 0.01 | 5.7 | 103.4 | 120.0 | 120.1 | 120.0 |
| 50.0 | 96,893,829.3 | 0.06 | 0.00 | 0.00 | \inf | 0.42 | 0.03 | 0.01 | 8.2 | 106.5 | 120.0 | 120.1 | 120.0 |
| 75.0 | $143,\!539,\!160.9$ | 0.17 | 0.02 | 0.00 | \inf | 0.00 | 0.11 | 0.00 | 9.9 | 106.3 | 120.0 | 57.7 | 120.0 |
| 90.0 | $168,\!210,\!283.3$ | 0.06 | 0.06 | 0.00 | \inf | 0.00 | 0.07 | 0.00 | 10.8 | 103.6 | 120.0 | 56.4 | 120.0 |
| 95.0 | $175,\!198,\!752.3$ | 0.10 | 0.09 | 0.00 | inf | 0.00 | 0.00 | 0.00 | 11.0 | 91.4 | 120.0 | 64.7 | 120.0 |
| Avg | | 0.20 | 0.08 | 0.00 | \inf | 1.83 | 0.06 | 0.01 | 6.7 | 86.5 | 120.0 | 97.4 | 120.0 |
| Min | | 0.00 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 1.7 | 45.4 | 120.0 | 56.4 | 120.0 |
| Max | | 0.58 | 0.40 | 0.00 | \inf | 6.50 | 0.21 | 0.01 | 11.0 | 106.5 | 120.0 | 120.1 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 14 |
| Running time in seconds for writing input file (t^{write}) | 2.2 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.3 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0500_075.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 500 |
| Density (Δ) | 75.0~% |
| Edges (m) | 93,428 |

| | | Running time (s) | | | | | | | | | | | |
|----------|---------------------|------------------|------|------|--------|--------------|--------|------------------------------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | $ \overline{\text{QKBP}^*} $ | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 7,076,592.5 | 0.58 | 0.04 | 0.00 | inf | 2,418.75 | 0.04 | 0.01 | 1.7 | 42.5 | 120.0 | 120.1 | 120.0 |
| 5.0 | 14,158,194.6 | 0.10 | 0.06 | 0.00 | \inf | 1,612.72 | 0.00 | 0.01 | 2.4 | 56.8 | 120.0 | 120.1 | 120.0 |
| 10.0 | 28,229,742.7 | 0.11 | 0.00 | 0.00 | \inf | 7.32 | 0.17 | 0.01 | 3.5 | 73.8 | 120.0 | 120.1 | 120.0 |
| 25.0 | 71,497,396.7 | 0.00 | 0.00 | 0.00 | \inf | 5.39 | 0.10 | 0.01 | 5.6 | 103.0 | 120.0 | 120.1 | 120.0 |
| 50.0 | $145,\!346,\!118.0$ | 0.32 | 0.00 | 0.00 | \inf | 23.63 | 0.02 | 0.01 | 7.9 | 106.3 | 120.0 | 120.1 | 120.0 |
| 75.0 | $215,\!222,\!498.9$ | 0.17 | 0.00 | 0.00 | \inf | 0.07 | 0.16 | 0.01 | 9.4 | 108.7 | 120.0 | 120.1 | 120.0 |
| 90.0 | $252,\!337,\!180.7$ | 0.18 | 0.10 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 10.2 | 97.2 | 120.0 | 90.5 | 120.0 |
| 95.0 | 262,959,622.5 | 0.13 | 0.13 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 10.4 | 89.3 | 120.0 | 95.5 | 120.0 |
| Avg | | 0.20 | 0.04 | 0.00 | inf | 508.49 | 0.06 | 0.01 | 6.4 | 84.7 | 120.0 | 113.3 | 120.0 |
| Min | | 0.00 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 1.7 | 42.5 | 120.0 | 90.5 | 120.0 |
| Max | | 0.58 | 0.13 | 0.00 | \inf | $2,\!418.75$ | 0.17 | 0.01 | 10.4 | 108.7 | 120.0 | 120.1 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 12 |
| Running time in seconds for writing input file (t^{write}) | 2.4 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.3 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_0500_100.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 500 |
| Density (Δ) | 100.0~% |
| Edges (m) | 124,750 |

| | | Running time (s) | | | | | | | | | | | |
|----------|---------------------|------------------------------|------|------|--------|--------------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | $\overline{\mathrm{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 9,398,593.9 | 0.00 | 0.00 | 0.00 | inf | 3,166.00 | 0.00 | 0.01 | 1.7 | 43.2 | 120.0 | 120.1 | 120.0 |
| 5.0 | 18,962,077.3 | 0.08 | 0.00 | 0.00 | \inf | 1,280.97 | 0.18 | 0.01 | 2.5 | 56.4 | 120.0 | 120.1 | 120.0 |
| 10.0 | 38,360,551.2 | 0.30 | 0.07 | 0.00 | \inf | 644.98 | 0.04 | 0.01 | 3.6 | 73.9 | 120.0 | 120.1 | 120.0 |
| 25.0 | 96,012,175.0 | 0.01 | 0.00 | 0.00 | \inf | 287.33 | 0.02 | 0.01 | 5.8 | 106.0 | 120.0 | 120.1 | 120.0 |
| 50.0 | $190,\!519,\!222.4$ | 0.25 | 0.02 | 0.00 | \inf | 106.70 | 0.13 | 0.01 | 8.3 | 109.6 | 120.0 | 120.1 | 120.0 |
| 75.0 | $281,\!686,\!636.9$ | 0.16 | 0.01 | 0.00 | \inf | 32.76 | 0.06 | 0.00 | 9.9 | 110.6 | 120.0 | 120.1 | 120.0 |
| 90.0 | 330,405,009.5 | 0.00 | 0.00 | 0.00 | \inf | 0.00 | 0.19 | 0.00 | 11.2 | 98.7 | 120.0 | 86.0 | 120.0 |
| 95.0 | $344,\!823,\!907.4$ | 0.06 | 0.04 | 0.00 | inf | 0.00 | 0.11 | 0.00 | 11.1 | 90.0 | 120.0 | 94.9 | 120.0 |
| Avg | | 0.11 | 0.02 | 0.00 | inf | 689.84 | 0.09 | 0.01 | 6.8 | 86.0 | 120.0 | 112.7 | 120.0 |
| Min | | 0.00 | 0.00 | 0.00 | \inf | 0.00 | 0.00 | 0.00 | 1.7 | 43.2 | 120.0 | 86.0 | 120.0 |
| Max | | 0.30 | 0.07 | 0.00 | \inf | $3,\!166.00$ | 0.19 | 0.01 | 11.2 | 110.6 | 120.0 | 120.1 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 15 |
| Running time in seconds for writing input file (t^{write}) | 2.6 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.4 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_1000_005.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 1,000 |
| Density (Δ) | 5.0~% |
| Edges (m) | 24,926 |

| | | Dev | viation | Running time (s) | | | | | | | | | |
|----------|--------------------|----------------------------|---------|------------------|--------|--------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | $\overline{\text{QKBP}^*}$ | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 2,097,668.7 | 0.27 | 0.19 | \inf | \inf | 0.00 | 0.66 | 0.02 | 10.2 | 120.0 | 120.0 | 54.7 | 120.0 |
| 5.0 | $4,\!133,\!456.0$ | 0.20 | 0.05 | \inf | \inf | 0.00 | 0.12 | 0.01 | 15.4 | 120.0 | 120.0 | 63.0 | 120.0 |
| 10.0 | 8,257,446.2 | 0.15 | 0.06 | \inf | \inf | 0.00 | 0.11 | 0.02 | 23.0 | 120.0 | 120.0 | 58.7 | 120.0 |
| 25.0 | 20,679,798.2 | 0.07 | 0.00 | \inf | \inf | 0.00 | 0.03 | 0.03 | 37.4 | 120.0 | 120.0 | 120.3 | 120.0 |
| 50.0 | 40,900,913.2 | 0.05 | 0.01 | \inf | \inf | 0.00 | 0.08 | 0.01 | 51.9 | 120.0 | 120.0 | 13.6 | 120.0 |
| 75.0 | 59,586,465.8 | 0.01 | 0.00 | \inf | \inf | 0.00 | 0.05 | 0.01 | 63.5 | 120.0 | 120.0 | 13.6 | 120.0 |
| 90.0 | 69,335,143.9 | 0.01 | 0.00 | \inf | \inf | 0.00 | 0.00 | 0.01 | 67.6 | 120.0 | 120.0 | 3.6 | 94.0 |
| 95.0 | $72,\!114,\!236.0$ | 0.01 | 0.00 | \inf | \inf | 0.00 | 0.00 | 0.01 | 69.8 | 120.0 | 120.0 | 4.2 | 88.0 |
| Avg | | 0.10 | 0.04 | \inf | inf | 0.00 | 0.13 | 0.02 | 42.4 | 120.0 | 120.0 | 41.5 | 112.8 |
| Min | | 0.01 | 0.00 | \inf | \inf | 0.00 | 0.00 | 0.01 | 10.2 | 120.0 | 120.0 | 3.6 | 88.0 |
| Max | | 0.27 | 0.19 | \inf | \inf | 0.00 | 0.66 | 0.03 | 69.8 | 120.0 | 120.0 | 120.3 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 20 |
| Running time in seconds for writing input file (t^{write}) | 3.6 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.5 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_1000_010.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 1,000 |
| Density (Δ) | 10.0~% |
| Edges (m) | 49,500 |

| | | Running time (s) | | | | | | | | | | | |
|----------|---------------------|------------------|------|--------|--------|--------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 4,094,690.2 | 0.17 | 0.15 | \inf | \inf | 0.00 | 0.28 | 0.01 | 9.8 | 120.0 | 120.0 | 85.2 | 120.0 |
| 5.0 | 8,106,253.8 | 0.08 | 0.02 | \inf | \inf | 0.00 | 0.10 | 0.01 | 14.9 | 120.0 | 120.0 | 69.9 | 120.0 |
| 10.0 | 16,208,280.2 | 0.00 | 0.03 | \inf | \inf | 0.00 | 0.03 | 0.02 | 22.5 | 120.0 | 120.0 | 80.0 | 120.0 |
| 25.0 | $39,\!835,\!229.4$ | 0.02 | 0.01 | \inf | \inf | 0.00 | 0.13 | 0.02 | 35.7 | 120.0 | 120.0 | 30.3 | 120.0 |
| 50.0 | 77,902,137.5 | 0.02 | 0.01 | \inf | \inf | 0.00 | 0.02 | 0.03 | 51.1 | 120.0 | 120.0 | 121.1 | 120.0 |
| 75.0 | $114,\!534,\!934.7$ | 0.01 | 0.00 | \inf | \inf | 0.00 | 0.06 | 0.01 | 61.7 | 120.0 | 120.0 | 13.1 | 120.0 |
| 90.0 | $134,\!305,\!637.5$ | 0.03 | 0.00 | \inf | \inf | 0.00 | 0.09 | 0.01 | 65.6 | 120.0 | 120.0 | 13.3 | 120.0 |
| 95.0 | 140,105,204.9 | 0.09 | 0.01 | \inf | \inf | 0.00 | 0.04 | 0.01 | 66.9 | 120.0 | 120.0 | 11.0 | 120.0 |
| Avg | | 0.05 | 0.03 | \inf | \inf | 0.00 | 0.09 | 0.01 | 41.0 | 120.0 | 120.0 | 53.0 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.02 | 0.01 | 9.8 | 120.0 | 120.0 | 11.0 | 120.0 |
| Max | | 0.17 | 0.15 | \inf | \inf | 0.00 | 0.28 | 0.03 | 66.9 | 120.0 | 120.0 | 121.1 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 20 |
| Running time in seconds for writing input file (t^{write}) | 3.7 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.5 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

File dispersion-qkp-wgeo_1000_025.txt

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 1,000 |
| Density (Δ) | 25.0 % |
| Edges (m) | 124,346 |

| | | De | Running time (s) | | | | | | | | | | |
|----------|---------------------|-------|------------------|--------|--------|----------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 9,993,687.5 | 0.01 | 0.01 | inf | inf | 2,785.20 | 0.00 | 0.03 | 10.7 | 120.0 | 120.0 | 120.1 | 120.0 |
| 5.0 | 19,788,228.4 | 0.00 | 0.00 | \inf | \inf | 1,650.03 | 0.33 | 0.01 | 16.0 | 120.0 | 120.0 | 120.1 | 120.0 |
| 10.0 | 39,504,344.0 | 0.28 | 0.00 | \inf | \inf | 803.85 | 0.05 | 0.02 | 23.3 | 120.0 | 120.0 | 120.1 | 120.0 |
| 25.0 | 98,585,900.1 | 0.09 | 0.00 | \inf | \inf | 311.23 | 0.15 | 0.03 | 37.5 | 120.0 | 120.0 | 120.1 | 120.0 |
| 50.0 | $198,\!616,\!197.0$ | 0.03 | 0.00 | \inf | \inf | 121.30 | 0.09 | 0.02 | 52.5 | 120.0 | 120.0 | 120.1 | 120.0 |
| 75.0 | $292,\!869,\!748.1$ | 0.02 | 0.00 | \inf | \inf | 0.00 | 0.14 | 0.01 | 63.4 | 120.0 | 120.0 | 36.4 | 120.0 |
| 90.0 | $343,\!021,\!553.1$ | 0.02 | 0.00 | \inf | \inf | 0.00 | 0.06 | 0.01 | 69.2 | 120.0 | 120.0 | 32.6 | 120.0 |
| 95.0 | 357,709,491.6 | 0.03 | 0.00 | \inf | \inf | 0.00 | 0.09 | 0.01 | 69.8 | 120.0 | 120.0 | 29.7 | 120.0 |
| Avg | | 0.06 | 0.00 | inf | inf | 708.95 | 0.11 | 0.02 | 42.8 | 120.0 | 120.0 | 87.4 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.00 | 0.01 | 10.7 | 120.0 | 120.0 | 29.7 | 120.0 |
| Max | | 0.28 | 0.01 | \inf | \inf | 2,785.20 | 0.33 | 0.03 | 69.8 | 120.0 | 120.0 | 120.1 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 11 |
| Running time in seconds for writing input file (t^{write}) | 4.5 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.6 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_1000_050.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 1,000 |
| Density (Δ) | 50.0 % |
| Edges (m) | 250,545 |

| | | De | viatio | Running time (s) | | | | | | | | | |
|----------|---------------------|-------|--------|------------------|--------|----------|--------|------------------------------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | $ \overline{\text{QKBP}^*} $ | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 17,884,079.9 | 0.00 | 0.00 | \inf | \inf | 2,932.39 | 0.35 | 0.03 | 10.4 | 120.0 | 120.0 | 120.4 | 120.0 |
| 5.0 | 37,062,363.1 | 0.47 | 0.00 | \inf | \inf | 1,945.77 | 0.26 | 0.01 | 15.7 | 120.0 | 120.0 | 120.3 | 120.0 |
| 10.0 | 74,779,460.4 | 0.02 | 0.00 | \inf | \inf | 856.41 | 0.31 | 0.02 | 22.1 | 120.0 | 120.0 | 120.4 | 120.0 |
| 25.0 | 192,960,369.6 | 0.13 | 0.00 | \inf | \inf | 311.42 | 0.37 | 0.03 | 36.2 | 120.0 | 120.0 | 120.3 | 120.0 |
| 50.0 | 387,058,835.1 | 0.11 | 0.00 | \inf | \inf | 0.00 | 0.37 | 0.02 | 50.2 | 120.0 | 120.0 | 120.3 | 120.0 |
| 75.0 | 574,164,632.3 | 0.05 | 0.00 | \inf | \inf | 5.02 | 0.11 | 0.01 | 60.6 | 120.0 | 120.0 | 120.6 | 120.0 |
| 90.0 | 675,290,477.1 | 0.05 | 0.00 | \inf | \inf | 3.52 | 0.15 | 0.01 | 64.9 | 120.0 | 120.0 | 120.3 | 120.0 |
| 95.0 | $704,\!722,\!770.8$ | 0.06 | 0.00 | \inf | \inf | 1.84 | 0.03 | 0.01 | 65.6 | 120.0 | 120.0 | 120.3 | 120.0 |
| Avg | | 0.11 | 0.00 | inf | inf | 757.05 | 0.24 | 0.02 | 40.7 | 120.0 | 120.0 | 120.4 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.03 | 0.01 | 10.4 | 120.0 | 120.0 | 120.3 | 120.0 |
| Max | | 0.47 | 0.00 | \inf | \inf | 2,932.39 | 0.37 | 0.03 | 65.6 | 120.0 | 120.0 | 120.6 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 14 |
| Running time in seconds for writing input file (t^{write}) | 5.5 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.7 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_1000_075.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 1,000 |
| Density (Δ) | 75.0 % |
| Edges (m) | 374,402 |

| - | | Running time (s) | | | | | | | | | | | |
|---------------------------|---------------------|------------------|------|--------|--------|--------------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 27,658,495.8 | 0.00 | 0.00 | \inf | \inf | 2,472.82 | 0.84 | 0.03 | 11.0 | 120.0 | 120.0 | 120.4 | 120.0 |
| 5.0 | 56,356,737.3 | 0.00 | 0.00 | \inf | \inf | 1,443.26 | 0.46 | 0.01 | 15.8 | 120.0 | 120.0 | 120.4 | 120.0 |
| 10.0 | $113,\!215,\!508.7$ | 0.18 | 0.00 | \inf | \inf | 810.69 | 0.60 | 0.02 | 23.4 | 120.0 | 120.0 | 120.4 | 120.0 |
| 25.0 | 288,913,846.2 | 0.19 | 0.00 | \inf | \inf | 296.34 | 0.54 | 0.03 | 38.2 | 120.0 | 120.0 | 120.4 | 120.0 |
| 50.0 | 590,302,430.7 | 0.00 | 0.00 | \inf | \inf | 113.75 | 0.53 | 0.03 | 52.5 | 120.0 | 120.0 | 120.3 | 120.0 |
| 75.0 | 880,675,581.5 | 0.01 | 0.00 | \inf | \inf | 40.47 | 0.20 | 0.01 | 63.3 | 120.0 | 120.0 | 120.5 | 120.0 |
| 90.0 | 1,033,406,951.1 | 0.10 | 0.00 | \inf | \inf | 12.10 | 0.17 | 0.01 | 67.6 | 120.0 | 120.0 | 120.4 | 120.0 |
| 95.0 | 1,077,214,007.8 | 0.04 | 0.04 | \inf | inf | 6.10 | 0.00 | 0.01 | 69.3 | 120.0 | 120.0 | 120.4 | 120.0 |
| Avg | | 0.07 | 0.01 | \inf | \inf | 649.44 | 0.42 | 0.02 | 42.6 | 120.0 | 120.0 | 120.4 | 120.0 |
| $\overline{\mathrm{Min}}$ | | 0.00 | 0.00 | \inf | \inf | 6.10 | 0.00 | 0.01 | 11.0 | 120.0 | 120.0 | 120.3 | 120.0 |
| Max | | 0.19 | 0.04 | \inf | \inf | $2,\!472.82$ | 0.84 | 0.03 | 69.3 | 120.0 | 120.0 | 120.5 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 15 |
| Running time in seconds for writing input file (t^{write}) | 6.6 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.9 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_1000_100.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 1,000 |
| Density (Δ) | 100.0 % |
| Edges (m) | 499,500 |

| | | Running time (s) | | | | | | | | | | | |
|----------|---------------------|------------------|------|--------|--------|--------------|--------|-------|------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 36,867,381.1 | 0.24 | 0.00 | \inf | \inf | 2,668.33 | 0.90 | 0.03 | 10.5 | 120.0 | 120.0 | 120.4 | 121.0 |
| 5.0 | 75,092,164.0 | 0.31 | 0.00 | \inf | \inf | 1,702.11 | 0.94 | 0.01 | 15.4 | 120.0 | 120.0 | 120.5 | 121.0 |
| 10.0 | 152,189,862.7 | 0.20 | 0.00 | \inf | \inf | 1,065.76 | 0.49 | 0.02 | 24.2 | 120.0 | 120.0 | 120.4 | 121.0 |
| 25.0 | $393,\!457,\!775.1$ | 0.00 | 0.00 | \inf | \inf | 345.20 | 1.00 | 0.03 | 39.5 | 120.0 | 120.0 | 120.4 | 121.0 |
| 50.0 | $786,\!395,\!235.4$ | 0.02 | 0.00 | \inf | \inf | 116.19 | 0.59 | 0.02 | 56.8 | 120.0 | 120.0 | 120.6 | 121.0 |
| 75.0 | 1,160,864,584.9 | 0.13 | 0.00 | \inf | \inf | 43.84 | 0.33 | 0.01 | 66.7 | 120.0 | 120.0 | 120.5 | 121.0 |
| 90.0 | 1,360,479,209.5 | 0.11 | 0.00 | \inf | \inf | 17.26 | 0.23 | 0.01 | 70.9 | 120.0 | 120.0 | 120.5 | 121.0 |
| 95.0 | 1,419,830,579.9 | 0.09 | 0.00 | \inf | \inf | 8.20 | 0.02 | 0.01 | 72.0 | 120.0 | 120.0 | 120.5 | 120.0 |
| Avg | | 0.14 | 0.00 | \inf | \inf | 745.86 | 0.56 | 0.02 | 44.5 | 120.0 | 120.0 | 120.5 | 120.9 |
| Min | | 0.00 | 0.00 | \inf | \inf | 8.20 | 0.02 | 0.01 | 10.5 | 120.0 | 120.0 | 120.4 | 120.0 |
| Max | | 0.31 | 0.00 | \inf | \inf | $2,\!668.33$ | 1.00 | 0.03 | 72.0 | 120.0 | 120.0 | 120.6 | 121.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 16 |
| Running time in seconds for writing input file (t^{write}) | 7.8 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 1.0 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_2000_005.txt$

| Property of graph | Value |
|--------------------|--------|
| Nodes (n) | 2,000 |
| Density (Δ) | 5.0~% |
| Edges (m) | 99,390 |

| | | De | viation | Running time (s) | | | | | | | | | |
|----------|---------------------|-------|---------|------------------|--------|--------------|--------|-------|-------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 8,162,301.0 | 0.00 | 0.00 | \inf | inf | 3,386.64 | 0.16 | 0.06 | 63.8 | 120.0 | 120.0 | 120.1 | 120.0 |
| 5.0 | 16,061,052.8 | 0.00 | 0.04 | \inf | \inf | 10.19 | 0.18 | 0.04 | 99.1 | 120.0 | 120.0 | 120.1 | 120.0 |
| 10.0 | 31,862,810.5 | 0.03 | 0.00 | \inf | \inf | 4.44 | 0.25 | 0.06 | 120.0 | 120.0 | 120.0 | 120.1 | 120.0 |
| 25.0 | 79,902,717.2 | 0.01 | 0.00 | \inf | \inf | 1.95 | 0.15 | 0.10 | 120.0 | 120.0 | 120.0 | 120.1 | 120.0 |
| 50.0 | $159,\!101,\!626.8$ | 0.02 | 0.00 | \inf | \inf | 0.00 | 0.12 | 0.07 | 120.1 | 120.0 | 120.0 | 26.7 | 120.0 |
| 75.0 | $233,\!228,\!426.7$ | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.11 | 0.07 | 120.1 | 120.0 | 120.0 | 18.7 | 120.0 |
| 90.0 | 272,100,482.5 | 0.01 | 0.00 | \inf | \inf | 0.00 | 0.09 | 0.08 | 120.1 | 120.0 | 120.0 | 18.9 | 120.0 |
| 95.0 | 283,623,035.8 | 0.00 | 0.00 | inf | inf | 0.00 | 0.05 | 0.08 | 120.1 | 120.0 | 120.0 | 22.1 | 120.0 |
| Avg | | 0.01 | 0.01 | inf | inf | 425.40 | 0.14 | 0.07 | 110.4 | 120.0 | 120.0 | 70.8 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 0.00 | 0.05 | 0.04 | 63.8 | 120.0 | 120.0 | 18.7 | 120.0 |
| Max | | 0.03 | 0.04 | \inf | \inf | $3,\!386.64$ | 0.25 | 0.10 | 120.1 | 120.0 | 120.0 | 120.1 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 20 |
| Running time in seconds for writing input file (t^{write}) | 7.5 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 0.9 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_2000_010.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 2,000 |
| Density (Δ) | 10.0~% |
| Edges (m) | 199,944 |

| | | De | viatio | Running time (s) | | | | | | | | | |
|----------|---------------------|-------|--------|------------------|--------|----------|--------|-------|-------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 15,158,237.1 | 0.09 | 0.00 | \inf | inf | 1,997.86 | 0.36 | 0.13 | 69.6 | 120.0 | 120.0 | 120.4 | 120.0 |
| 5.0 | 30,820,187.5 | 0.01 | 0.00 | \inf | \inf | 1,580.84 | 0.47 | 0.03 | 102.8 | 120.0 | 120.0 | 120.4 | 120.0 |
| 10.0 | 62,924,872.2 | 0.01 | 0.00 | \inf | \inf | 836.44 | 0.28 | 0.06 | 120.0 | 120.0 | 120.0 | 120.4 | 120.0 |
| 25.0 | $158,\!171,\!275.1$ | 0.00 | 0.00 | \inf | \inf | 283.48 | 0.25 | 0.06 | 120.0 | 120.0 | 120.0 | 120.3 | 120.0 |
| 50.0 | $314,\!268,\!401.3$ | 0.02 | 0.00 | \inf | \inf | 0.01 | 0.24 | 0.10 | 120.2 | 120.0 | 120.0 | 114.6 | 120.0 |
| 75.0 | $462,\!872,\!938.6$ | 0.02 | 0.00 | \inf | \inf | 5.72 | 0.18 | 0.07 | 120.0 | 120.0 | 120.0 | 120.6 | 120.0 |
| 90.0 | $542,\!046,\!348.4$ | 0.01 | 0.00 | \inf | \inf | 3.22 | 0.10 | 0.08 | 120.1 | 120.0 | 120.0 | 120.7 | 120.0 |
| 95.0 | 565,582,538.7 | 0.04 | 0.00 | \inf | \inf | 1.85 | 0.08 | 0.07 | 120.2 | 120.0 | 120.0 | 120.7 | 120.0 |
| Avg | | 0.02 | 0.00 | inf | inf | 588.68 | 0.24 | 0.08 | 111.6 | 120.0 | 120.0 | 119.8 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 0.01 | 0.08 | 0.03 | 69.6 | 120.0 | 120.0 | 114.6 | 120.0 |
| Max | | 0.09 | 0.00 | \inf | \inf | 1,997.86 | 0.47 | 0.13 | 120.2 | 120.0 | 120.0 | 120.7 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 12 |
| Running time in seconds for writing input file (t^{write}) | 8.2 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 1.0 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_2000_025.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 2,000 |
| Density (Δ) | 25.0 % |
| Edges (m) | 500,305 |

| | | De | viatio | Running time (s) | | | | | | | | | |
|----------|-------------------------|-------|--------|------------------|--------|--------------|--------|-------|-------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 37,986,132.3 | 0.06 | 0.00 | inf | inf | 2,327.06 | 1.54 | 0.13 | 65.3 | 120.0 | 120.0 | 121.0 | 121.0 |
| 5.0 | $76,\!528,\!469.4$ | 0.23 | 0.00 | \inf | \inf | 0.27 | 0.66 | 0.03 | 97.4 | 120.0 | 120.0 | 120.3 | 121.0 |
| 10.0 | 152,682,680.5 | 0.01 | 0.00 | \inf | \inf | 44.82 | 0.74 | 0.05 | 120.0 | 120.0 | 120.0 | 121.1 | 121.0 |
| 25.0 | 379,984,618.9 | 0.01 | 0.00 | \inf | \inf | 72.94 | 0.98 | 0.10 | 120.0 | 120.0 | 120.0 | 120.4 | 121.0 |
| 50.0 | $760,\!656,\!415.4$ | 0.01 | 0.00 | \inf | \inf | 0.11 | 0.82 | 0.08 | 120.0 | 120.0 | 120.0 | 120.6 | 120.0 |
| 75.0 | $1,\!127,\!172,\!236.1$ | 0.00 | 0.00 | \inf | \inf | 5.22 | 0.29 | 0.07 | 120.0 | 120.0 | 120.0 | 120.4 | 120.0 |
| 90.0 | $1,\!325,\!660,\!720.7$ | 0.00 | 0.00 | \inf | \inf | 3.72 | 0.22 | 0.07 | 120.1 | 120.0 | 120.0 | 120.5 | 121.0 |
| 95.0 | $1,\!383,\!523,\!525.9$ | 0.00 | 0.00 | \inf | \inf | 2.18 | 0.08 | 0.07 | 120.1 | 120.0 | 120.0 | 120.5 | 120.0 |
| Avg | | 0.04 | 0.00 | inf | inf | 307.04 | 0.67 | 0.07 | 110.4 | 120.0 | 120.0 | 120.6 | 120.6 |
| Min | | 0.00 | 0.00 | \inf | \inf | 0.11 | 0.08 | 0.03 | 65.3 | 120.0 | 120.0 | 120.3 | 120.0 |
| Max | | 0.23 | 0.00 | \inf | \inf | $2,\!327.06$ | 1.54 | 0.13 | 120.1 | 120.0 | 120.0 | 121.1 | 121.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 11 |
| Running time in seconds for writing input file (t^{write}) | 11.0 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 1.3 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_2000_050.txt$

| Property of graph | Value |
|--------------------|---------|
| Nodes (n) | 2,000 |
| Density (Δ) | 50.0 % |
| Edges (m) | 999,892 |

| | | Running time (s) | | | | | | | | | | | |
|----------|-------------------------|------------------|------|--------|--------|--------------|--------|-------|-------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 74,893,413.0 | 0.00 | 0.00 | \inf | \inf | 3,291.19 | 2.03 | 0.14 | 66.9 | 120.0 | 120.0 | 122.0 | 122.0 |
| 5.0 | 152,454,540.0 | 0.07 | 0.00 | \inf | \inf | 1,590.20 | 2.15 | 0.03 | 99.3 | 120.0 | 120.0 | 123.7 | 122.0 |
| 10.0 | 308,930,505.6 | 0.03 | 0.00 | \inf | \inf | 850.73 | 1.83 | 0.06 | 120.0 | 120.0 | 120.0 | 124.1 | 122.0 |
| 25.0 | 767,501,379.1 | 0.07 | 0.00 | \inf | \inf | 327.32 | 2.14 | 0.10 | 120.0 | 120.0 | 120.0 | 120.8 | 122.0 |
| 50.0 | $1,\!556,\!100,\!760.9$ | 0.02 | 0.00 | \inf | \inf | 112.36 | 1.22 | 0.10 | 120.1 | 120.0 | 120.0 | 120.6 | 122.0 |
| 75.0 | $2,\!317,\!855,\!526.8$ | 0.00 | 0.00 | \inf | \inf | 37.77 | 0.75 | 0.07 | 120.0 | 120.0 | 120.0 | 120.9 | 122.0 |
| 90.0 | 2,729,925,869.9 | 0.00 | 0.00 | \inf | \inf | 13.87 | 0.17 | 0.07 | 120.1 | 120.0 | 120.0 | 120.7 | 122.0 |
| 95.0 | $2,\!852,\!413,\!656.9$ | 0.05 | 0.00 | \inf | \inf | 7.50 | 0.10 | 0.07 | 120.1 | 120.0 | 120.0 | 120.8 | 122.0 |
| Avg | | 0.03 | 0.00 | inf | inf | 778.87 | 1.30 | 0.08 | 110.8 | 120.0 | 120.0 | 121.7 | 122.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 7.50 | 0.10 | 0.03 | 66.9 | 120.0 | 120.0 | 120.6 | 122.0 |
| Max | | 0.07 | 0.00 | \inf | \inf | $3,\!291.19$ | 2.15 | 0.14 | 120.1 | 120.0 | 120.0 | 124.1 | 122.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 12 |
| Running time in seconds for writing input file (t^{write}) | 15.0 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 2.0 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_2000_075.txt$

| Property of graph | Value |
|--------------------|-----------|
| Nodes (n) | 2,000 |
| Density (Δ) | 75.0 % |
| Edges (m) | 1,499,336 |

| | | De | viatio | Running time (s) | | | | | | | | | |
|----------|-------------------------|-------|--------|------------------|--------|----------|--------|-------|-------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 111,777,087.1 | 0.26 | 0.00 | inf | inf | 3,161.04 | 3.29 | 0.13 | 65.4 | 120.0 | 120.0 | 123.0 | 120.0 |
| 5.0 | 227,586,687.5 | 0.00 | 0.00 | \inf | \inf | 1,674.65 | 3.22 | 0.03 | 96.7 | 120.0 | 120.0 | 120.9 | 120.0 |
| 10.0 | 463,811,780.0 | 0.04 | 0.00 | \inf | \inf | 913.33 | 2.68 | 0.05 | 120.0 | 120.0 | 120.0 | 121.8 | 120.0 |
| 25.0 | $1,\!151,\!478,\!894.8$ | 0.03 | 0.00 | \inf | \inf | 309.16 | 2.91 | 0.10 | 120.1 | 120.0 | 120.0 | 121.0 | 120.0 |
| 50.0 | $2,\!308,\!727,\!831.2$ | 0.00 | 0.00 | \inf | \inf | 111.00 | 2.46 | 0.09 | 120.1 | 120.0 | 120.0 | 122.8 | 120.0 |
| 75.0 | $3,\!422,\!995,\!480.4$ | 0.05 | 0.00 | \inf | \inf | 38.39 | 0.99 | 0.07 | 120.1 | 120.0 | 120.0 | 121.2 | 120.0 |
| 90.0 | 4,024,243,092.5 | 0.02 | 0.00 | \inf | \inf | 13.78 | 0.29 | 0.07 | 120.1 | 120.0 | 120.0 | 121.2 | 120.0 |
| 95.0 | $4,\!198,\!910,\!746.6$ | 0.00 | 0.00 | \inf | \inf | 5.71 | 0.08 | 0.07 | 120.2 | 120.0 | 120.0 | 122.0 | 120.0 |
| Avg | | 0.05 | 0.00 | \inf | inf | 778.38 | 1.99 | 0.08 | 110.3 | 120.0 | 120.0 | 121.7 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 5.71 | 0.08 | 0.03 | 65.4 | 120.0 | 120.0 | 120.9 | 120.0 |
| Max | | 0.26 | 0.00 | \inf | \inf | 3,161.04 | 3.29 | 0.13 | 120.2 | 120.0 | 120.0 | 123.0 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 11 |
| Running time in seconds for writing input file (t^{write}) | 18.8 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 2.6 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |

$File\ dispersion-qkp-wgeo_2000_100.txt$

| Property of graph | Value |
|--------------------|-----------|
| Nodes (n) | 2,000 |
| Density (Δ) | 100.0 % |
| Edges (m) | 1,999,000 |

| | | Deviation from best OFV (%) | | | | | Running time (s) | | | | | | |
|----------|-------------------------|-----------------------------|------|--------|--------|----------|------------------|-------|-------|-------|-------|--------|--------|
| γ | Best OFV | QKBP* | GR | DP | QK | Gurobi | Hexaly | QKBP* | GR | DP | QK | Gurobi | Hexaly |
| 2.5 | 146,032,229.0 | 0.25 | 0.00 | \inf | \inf | 2,910.50 | 3.90 | 0.14 | 73.5 | 120.0 | 120.0 | 121.3 | 120.0 |
| 5.0 | 298,463,595.0 | 0.00 | 0.00 | \inf | \inf | 1,848.74 | 3.28 | 0.03 | 109.3 | 120.0 | 120.0 | 122.7 | 120.0 |
| 10.0 | 610,589,901.0 | 0.04 | 0.00 | \inf | \inf | 927.61 | 3.64 | 0.06 | 120.1 | 120.0 | 120.0 | 124.1 | 120.0 |
| 25.0 | $1,\!552,\!122,\!124.4$ | 0.03 | 0.00 | \inf | \inf | 316.28 | 3.18 | 0.11 | 120.0 | 120.0 | 120.0 | 122.5 | 120.0 |
| 50.0 | $3,\!108,\!906,\!506.1$ | 0.00 | 0.00 | \inf | \inf | 107.83 | 2.21 | 0.08 | 120.0 | 120.0 | 120.0 | 122.7 | 120.0 |
| 75.0 | $4,\!618,\!504,\!994.4$ | 0.00 | 0.00 | \inf | \inf | 38.83 | 1.00 | 0.07 | 120.1 | 120.0 | 120.0 | 123.4 | 120.0 |
| 90.0 | $5,\!435,\!578,\!205.5$ | 0.02 | 0.00 | \inf | \inf | 13.26 | 0.42 | 0.07 | 120.0 | 120.0 | 120.0 | 121.3 | 120.0 |
| 95.0 | $5,\!676,\!339,\!787.3$ | 0.01 | 0.00 | \inf | \inf | 6.57 | 0.12 | 0.07 | 120.0 | 120.0 | 120.0 | 123.0 | 120.0 |
| Avg | | 0.04 | 0.00 | \inf | \inf | 771.20 | 2.22 | 0.08 | 112.9 | 120.0 | 120.0 | 122.6 | 120.0 |
| Min | | 0.00 | 0.00 | \inf | \inf | 6.57 | 0.12 | 0.03 | 73.5 | 120.0 | 120.0 | 121.3 | 120.0 |
| Max | | 0.25 | 0.00 | \inf | \inf | 2,910.50 | 3.90 | 0.14 | 120.1 | 120.0 | 120.0 | 124.1 | 120.0 |

^{*}The contribution in this paper

| QKBP-specific information | Value |
|---|-------|
| Number of breakpoints | 12 |
| Running time in seconds for writing input file (t^{write}) | 24.3 |
| Running time in seconds for executing parametric cut procedure (t^{cut}) | 3.4 |
| Running time in seconds for reading result file (t^{read}) | 0.0 |