ETH Zurich Institut für Theoretische Informatik

Prof. Dr. Angelika Steger Prof. Dr. Emo Welzl

Prof. Dr. Peter Widmayer

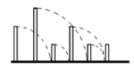
Algorithms Lab

Exercise – Dominoes

Playing with dominoes is a lot of fun. You can, for example, place them in long lines so that when the first tile is toppled, it topples the second, which topples the third, etc., resulting in all of the tiles falling.

In this problem, you are dealing with a special kind of domino set, in which the tiles are of different heights. Your task is to determine, given an arrangement of these tiles in a line, how many of the domino tiles will fall after toppling the left-most domino.

More precisely, we have the following set-up: the dominoes are placed at successive points on the integer line, the first at position 1, the second at 2, and so on. If a tile of height h at position i is toppled, this causes the tiles at all positions j such that j - i < h to fall as well.



Input The first line of the input contains a positive integer $t \le 10$ denoting the number of test cases. Each of the t test cases is described as follows:

- It starts with a line containing the number $1 \le n \le 1\,000\,000$ of dominoes,
- The next line contains n integers separated by spaces, where the i-th integer represents the height $1 \le h_i < 2^{31}$ of the domino tile placed at the i-th position.

Output The output should consist, for each test case, of a single line containing the number of domino tiles that will fall after toppling the leftmost tile in this testcase.

Points There are two test sets, worth 100 points in total.

- 1. For the first test set, worth 50 points, you may assume that $n \le 1000$.
- 2. For the second test set, worth 50 points, there are no additional assumption.

Corresponding sample test sets are contained in test i. in/out for $i \in \{1, 2\}$.

Hint: Please add the command std::ios_base::sync_with_stdio(false) as the first line of your main function. It will make reading the input and writing the output much faster.

Sample Input

Sample Output

5 3