

Detecting Empty Wireframe Objects on Micro-Air Vehicles

Applied for Visual Target Detection in Autonomous Drone Racing

by

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Preface

Preface...

*P. Duernay
Delft, January 2013*

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Summary

Glossary

AP Average Precision

CAD Computer Aided Design

CNN Convolutional Neural Network

CPU Central Processing UniT

DPM Deformable Part Model

DR Domain Randomization

DSC Depthwise Separable Convolution

EWFO Empty Wire Frame Objects

FoV Field of View

FPV First Person View

GAN Generative Adversial Network

GPS Global Positioning System

GPU Graphical Processing Unit

HOG Histogram of Oriented Gradients

IR Infrared

IMU Inertial Measurement Unit

IROS International Conference of Intelligent Robots

LIDAR Light Detection And Ranging

MAV Micro-Air Vehicle

mAP Mean Average Precision

NED North-East-Down

IoU Intersection over Union

FCN Fully Convolutional Network

PCA Principal Component Analysis

RPN Region Proposal Network

SIFT Scale Invariant Feature Transform

SSD Single Shot Multibox Detector

SVM Support Vector Machine

TO Target Object

WRN Wide Residual Network

Yolo You only look once

Chapter 1

Introduction

Micro-Air Vehicles (MAVs) such as a Quadrotor-MAV displayed in Figure 1.1 are an emerging technology that supports society in a wide range of consumer, industrial and safety applications. For example MAVs are used to deliver medicine [45], fight fires [27] or even find survivors in disaster situations [24].

Especially in emergency scenarios the fast and safe flight of MAVs is crucial to deliver help quickly and save human lives. However, due to the complexity of such missions as well as the difficulty to control an MAV in disaster scenarios, often multiple human operators are required in order to ensure safe operation [36]. With humans in the loop a constant connection between the MAV and the operators is required which not only uses energy and requires infrastructure but also significantly increases the reaction time. Enabling MAVs to fly more autonomously could allow human operators to control more MAVs and thus to improve the support in emergency situations.

A major challenge on the way to the full autonomous flight of MAVs is the accurate estimation of the MAV's state within its environment. The system is highly dynamic so position and orientation can change rapidly. At the same time noise introduced by motor vibrations makes the position estimation with only on-board Inertial Measurement Units (IMUs) too inaccurate [35]. Light Detection And Ranging (LIDAR)-sensors can capture long and wide range 3D information but the sensors are typically heavy and require a significant amount of energy. Infrared (IR) sensors can cover distance information but are often limited in their Field of View (FoV) as well as in their range. External infrastructure like Global Positioning System (GPS) and optical tracking systems can provide accurate measurements but there is no guarantee that such systems are present in real world applications. Cameras on the other hand are cheap, lightweight and can measure long range distance information. This makes them a suitable choice as a sensor for on-board state estimation on light



Figure 1.1: An example of a Quadrotor-MAV-Platform that is used in this thesis.

MAVs [9].

However, the signal delivered by the camera is high dimensional and can not directly be interpreted as position or orientation measurements. Computer Vision algorithms are required to interpret the image and extract relevant information. This can be done by designing an algorithm manually or learning the image processing from annotated examples. In particular Deep Learning based methods aim to combine whole Computer Vision pipelines into one mapping that transforms the raw input image into a task dependent output. Experiments have shown how Deep Learning based methods outperform traditional Machine Learning approaches and manually crafted algorithms [40]. This made them the predominant choice for almost any vision task.

The hereby used Convolutional Neural Networks (CNNs) are designed in a hierarchical way, using multiple layers that are evaluated sequentially. An example architecture is displayed in Figure 1.2. The network transforms an image of size 224x224 from its input (left) to a task dependent output (right). In this case a classification network predicting 1000 class probabilities is displayed. Each layer applies a non-linear transformation for which the parameters are learned during training. By stacking more layers on top of each other (deepening) and increasing the number of nodes D per layer (widening), highly non-linear functions can be modelled.

Experiments have shown the superior performance of particularly deep/wide models [14, 15, 47, 58]. However, this model flexibility assumed to be the reason for their superior performance also leads to immense requirements in computational resources. For example a state-of-the-art Computer Vision model [15] contains 60.2 million parameters and one inference requires 11.3 billion floating point operations [52].



Figure 1.2: Example Architecture of a CNN.

Robotic platforms like MAVs have limited resources in terms of processing power and battery life. Hence, the use of CNNs on such devices is still an open challenge. Research has addressed to reduce the number of computations in Deep Learning models on multiple levels[12, 19, 30, 44, 58, 59]. However, the investigation of relatively shallow models with less than ten layers received only little attention by the research community.

This work investigates the deployment of a Deep Learning based Computer Vision pipeline on a MAV. The method is applied in the challenging scenario of Autonomous Drone Racing at the International Conference of Intelligent Robots (IROS) 2018. Within the race court several metal gates are placed and need to be passed one after another. Detecting the gates allows to estimate the MAV's relative position and to calculate the flying trajectory. An overview of the race court and the racing gates at the IROS 2016 Autonomous Drone Race can be seen in Figure 1.3.

Reference
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Method
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published

The thesis builds on previous work by Ozo et. al which uses a manually crafted image processing method to detect the racing gates. Although fast to execute the method is very sensitive to illumination changes.



Figure 1.3: Example Images of the IROS 2016 Autonomous Drone Race

Moreover, the algorithm fails when the objects are too far away or the frame is very thin. In order to develop a more robust method, this thesis investigates a learning based approach to the detection of racing gates.

Object Detection is one of the most intensively studied topics in Computer Vision. However, the objects investigated are usually solid and contain complex shapes. For example a pedestrian consist of body parts and a face. A box that surrounds the object mostly contains parts with distinctive shape an/or texture. A Computer Vision model can use these features for detection. The racing gates in contrast are of different nature. As can be seen in Figure 1.3 a box that surrounds the object would largely contain background. Hence, this part can not be used as a hint whether an object is present. Instead it can contain other objects even other gates that might distract a detector. Additionally, the object parts themselves are of very thin structure and can be hardly visible. Thus, a detector needs to make use of fine-grain structures, while ignoring the majority of the image. This introduces a particular vision task that even humans have a hard time at solving¹ and that affects the training and design of a Computer Vision pipeline that aims to detect these kind of objects.

This thesis defines a class of objects as **Empty Wire Frame Objects (EWFO)** studies methods for their detection. The definition is given as follows:

Definition - Empty Wireframe Objects

1. **Empty.** The object parts are sparse. The bounding box around the object is largely occupied by background.
2. **Wireframe** The object does not consist of complex but only basic geometric shapes like corners, lines and edges. The object parts can be spread over large parts of the image.

The detection of EWFO is studied in the examples of the IROS drone race gates. These can be seen can be seen in Figure 1.4. The image shows the *Closed Gate* as well as the *Jungle Gate*. Thereby the orange part is considered to be the object of interest. To the best of the authors knowledge EWFO have not been particularly addressed in Computer Vision. In [10] and [31] the authors also detect racing gates, however the used objects contain more structure than the ones investigated in this thesis. Jung et al. present a framework to detect similar objects in [25] and [26] but do not study the particular effects of the object shape. This work particularly addresses the implications of the object shape in using a Deep Learning based detection system for EWFO.

A drawback of Deep Learning based vision systems is their need for vast amounts of annotated examples, which is not always available. Racing gates for example are not an object that appears often in everyday life

¹The unconvinced reader can try to count the number of gates visible in the right image of Figure 1.3



Figure 1.4: Example Images of the Empty Wire Frame Objects investigated in this thesis.

and therefore not many example images exist. To this end no publicly available dataset can be used to train a Computer Vision system for EWFO. Since a large part of the object consists of background, it is particularly crucial that the training set covers a large variety of backgrounds. Otherwise, it is likely that a model uses the background for prediction and only works in a particular domain (Overfitting).



Figure 1.5: Example of the Cyberzoo dataset. On the left an image while the MAV is hovering, on the right an image during a turn manoeuvre.

In Chapter 1 example images of the target domain of this work are displayed. The images are taken during a test flight at a test environment. The left image shows an example when the MAV is hovering and thus is in a very stable position. The object in this case is clearly visible as a single orange square. In contrast the right image shows a close up example during a turn manoeuvre. Here it can be seen how the used wide angle lens causes distortion and thus the lines appear as circular shape. Furthermore, large parts of the image including the horizontal bars of the object in the back appear blurred due to the circular velocity of the MAV. In addition, the light conditions of the environment significantly influence the object appearance.

While it is possible to remove lens and sensor effects in post-processing, this can lead to information loss and requires on-board resources. Instead it is computationally more efficient to perform the detection on the raw image data. However, sensor effects have been shown to significantly influence the performance of neural networks [2, 8]. Furthermore, they can lead to varying object appearance on different MAVs. This further complicates the collection of annotated examples.

Another option is the artificial generation of data. By synthetically generating samples with corresponding labels, the theoretical amount of training data is infinite. Moreover, the generation allows to incorporate domain specific properties such as motion blur or image distortion. Hence, data generation is particularly

useful for the detection of MAVs on EWFOs where a large variety of backgrounds is required while samples are difficult to obtain. Finally, as MAV are brittle vehicles and mistakes in development can lead to damage on hardware, engineers and researchers often use simulators to evaluate their systems before transferring them to the real work. Thus the basic infrastructure required to generate data is often already available.

Yet introduces the generation of data its own challenges. First and foremost because the generation process in itself is based on model assumptions. If these do not sufficiently capture the real world, a model trained in such an environment might be heavily biased and perform poorly in the real world. Secondly, because the generation of visual data is computationally intense. Despite advances in Computer Graphics can virtual environments not yet fully capture the real world. Hence, this work investigates the use of data generation in order to detect EWFOs on MAVs.

Without an accurate detection of the racing gate, the MAV is not able to determine its current position and thus to calculate its flying trajectory. On the other hand, with an algorithm that requires less computational resources a lighter MAV can be built. This allows faster and more aggressive trajectories as well as longer battery life. Moreover, the vision system is part of a greater state estimation and control system which also includes further sensor measurements. Depending on the remaining part of the system, faster and less accurate detections can be more useful than slow but accurate detections. Hence, the trade-off between accuracy and inference speed is of particular interest for this application and is addressed in this work.

1.1 Research Question

This section summarizes the research question addressed in this thesis. Furthermore it describes how the question is split in multiple subquestions that are addressed in the individual chapters.

How can we learn a CNNs to detect EWFO on MAVs using synthetic data?

RQ1 How can data be generated to train a detection model for EWFO detection on a MAVs?

RQ2 What kind of architecture is suitable to detect EWFOs?

RQ3 What are the trade-offs in detection performance and inference time when a detection model for EWFOs is deployed on a MAV?

RQ4 Can the gained insights be used to build a lightweight and robust detection model for racing gates in the IROS Autonomous Drone Race?

Put some results at the end.

1.2 Results/Contributions

1.3 Outline

Refactor contributions once done

The thesis is structured as displayed in Figure 1.6. Chapter 2 describes the metrics and systems used for evaluation. ??, Chapter 4, ?? and ?? address the individual research questions. Each chapter contains an introduction to the topic, the methodology used in this thesis and experiments that have been carried out. ?? describes methods to generate synthetic data for machine learning. It concludes with the datasets used for the remaining parts of this thesis. Chapter 4 describes object detection and evaluates current methods in the



Figure 1.6: Thesis Outline

application for EWFOs. ?? illustrates and evaluates measures to reduce computations and optimize an object detection system for a particular hardware. It investigates the trade-off between detection performance and inference time. ?? describes how the gained insights are used to develop a detector for racing gates at the IROS 2018 Autonomous Drone Race. It also compares the current method to a traditional image processing method in terms of speed and detection performance. ?? discusses the overall results and formulates a conclusion.

Chapter 2

Background

This chapter describes background knowledge required to understand the remaining parts of the thesis. It introduces the target system for this work as well as datasets and metrics used for evaluation. Furthermore, it discusses related work in Object Detection and Data Generation.

2.1 System Overview

A MAV consist of multiple components of Software that are responsible for higher and lower level tasks. Figure 2.1 illustrates these components in the example of the target platform of this thesis. On the lowest level drivers read out sensors such as the camera and an IMU or communicate with a ground station. A low level control loop is responsible for controlling the local state of the MAV such as altitude and attitude. A higher level control loop controls the global state of the MAV which is the position and the flying trajectory.



Figure 2.1: Control Loop

The high level control loop of this work is described in further detail. A first step detects the racing gate and yields the corner coordinates. These are used to estimate the relative position of the MAV towards the gate. In the second step the visual measurements are fused with measurements of other sensors. In this case IMU and a sonar deliver altitude and attitude data. This step yields a global position estimate of the MAV. Combined with prior knowledge about the race court, the desired attitude and altitude required to fly the trajectory is calculated. The results are send as set points to the low level controller.

The hardware platform used to run the high level control loop is the *JeVois* smart camera. It contains a 1.3 MP camera with 65 degree field of view. The processing units are a quad core ARM Cortex A7 processor with 1.35 GHz and a dual core MALI-400 GPU with 233 Mhz. In order to extent the field of view a 120 degree wide angle lens is mounted. In Figure 2.2 the camera is shown.

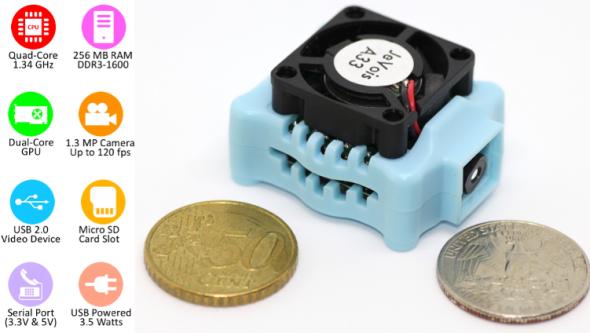


Figure 2.2: JeVois Camera

2.1.1 Baseline Algorithm

Within this work the first step of the aforementioned pipeline is addressed. It aims to replace the current baseline algorithm *SnakeGate*, a low-level image processing algorithm. Its scheme is summarized in and described in the following.

1. Filter image by colour threshold
2. Sample stochastically
3. Follow the pixels horizontally as long as they are within the colour threshold otherwise return to 2.
4. If a bar of sufficient length has been found repeat 3. vertically along one end of the line found in 3.
5. If a vertical bar is found the square is considered as gate candidate
6. Create local histogram around the corners of the gate candidate and choose the highest peak as gate corner.
7. Count the fraction of pixels within the color threshold in relation to the total number of pixels a long all edges of the gate candidate to determine the *color fitness*.
8. Gate candidates that exceed a chosen threshold are considered valid detections.

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JSnakeGate is fast to execute but lacks from several drawbacks. (1) it is colour dependent and thus very subtle to light changes. Hence it must be fine tuned according to light conditions in a certain room. Strong colour variations across the object cannot be handled by the method; (2) the method requires the full object to be visible; (3) the method cannot exploit context such as the pole of an object. These drawbacks motivate a learning based approach to be investigated in this thesis.

2.2 Datasets

A dataset has been recorded to serve as a benchmark for the developed methods. The dataset consists of 300 images recorded with the JeVois camera during flight and while remaining on ground. The samples stem



Figure 2.3: Examples of the three test domains. From left to right: *Basement*, *Cyberzoo* and *Hallway*

from three different rooms with varying light conditions. The rooms are referred to as *Basement*, *Cyberzoo* and *Hallway*. Example images for each room can be seen in Figure 2.3.

All environments are indoor scenes which are typical examples for GPS-denied areas, where vision based state estimation is required. The scenes contain two gates that are arranged in varying order. Hence up to two objects are visible and can overlap which means the gate farer away can be seen through the closer gate. Each of the rooms has different environmental conditions:

1. *Basement* is a bright environment illuminated by artificial light sources. The corridor in which the objects of interest are placed are narrow while also objects and persons are visible on the samples. The dataset contains 163 samples with 312 objects in total.
2. *Cyberzoo* is taken from a test environment for MAV flights. External light sources are covered such that an even illumination and dark background is created. Only in a small subset of images distractors like other objects or persons are visible. In total 88 samples stem from this room while 71 objects are present.
3. *Hallway* is a bright environment illuminated by a combination of artificial light sources as well as daylight that shines through the windows. The samples are taken with the windows as background. This leads to a very bright background such that the thin structure of the objects are hardly visible. The dataset contains 49 samples with a total of 86 objects.

2.3 Evaluation Metrics

The detection performance is evaluated in terms of precision and recall. These metrics are defined as:

Precision

$$p = \frac{\text{true positives}}{\text{true positives} + \text{false positives}}$$

Recall

$$r = \frac{\text{true positives}}{\text{true positives} + \text{false negatives}}$$

Where true positives are objects that are detected, false positives are detections although there is no object and false negatives are objects which have not been detected.

Hence, recall expresses how many of all objects are detected and therefore how complete the result is. Precision measures how many of the predicted objects are actually correct detections.

A correct detection is determined based on its overlap with a ground truth box. This is measured by the relation of Intersection over Union (IoU). In experiments we determine 0.6 as sufficient overlap for a detection.

The model used within this thesis associates a "confidence" value with each prediction that can trade off precision and recall. This is further explained in Chapter 4. By accepting more detections with a lower confidence threshold, the probability increases that one of the predictions is a true positive. Hence, it increases recall. However, it also increases the probability of false positives and thus lowers precision. In order to evaluate this trade-off, precision is plotted over recall at increasing confidence values.

As the learning of CNNs is stochastic, the mean across several trainings is reported. In order to determine the average precision recall trade-off the precision is interpolated across evenly distributed recall levels between 0 and 1 using:

$$p_{\text{interp}}(r) = \max_{r' \geq r} p(r')$$

Subsequently the mean at all recall levels can be calculated. A metric that combines the precision-recall trade-off is Average Precision (AP):

$$ap = \int_r p_{\text{interp}}(r) dr$$

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We denote precision, recall and average precision at a certain IoU threshold such as 60% as p_{60}, r_{60} and ap_{60} .

2.4 Related Work

This section describes previous work related to this thesis. Covered are methods to detect objects, reduce the inference time of CNNs and methods to train detectors in a simulated environment.

2.4.1 Detecting Objects

Object Detection is one of the central domains in Computer Vision. Giving a full review of all approaches is beyond the scope of this work. We mention some of the most important milestones relevant for this work.

On a high level Object Detection can be described by two individual goals: the description of what kind of object is seen (Classification), as well as where it is seen (Localization). Hence, an Object Detection pipeline transforms the raw image to a set of one or more areas and corresponding class labels. Images are high dimensional signals that can contain redundant and task irrelevant information. Performing detection in this space is difficult, also because the performance of machine learning models decreases when the feature space becomes too large (curse of dimensionality). Computer Vision pipelines usually apply a feature extraction stage, before the actual prediction is done. An overview is displayed in Figure 2.4.

1. The feature extraction stage extracts task relevant information from the image and infers an internal, more abstract representation of lower dimension.
2. The classification/localization stage produces the final output based on this representation.

An efficient feature extraction stage is thereby crucial for the success of an Object Detection pipeline. If the inferred representation is clearly separable, a simple classification stage can distinguish an object from the background. In contrast, even a flexible classifier cannot separate a highly overlapping feature space.

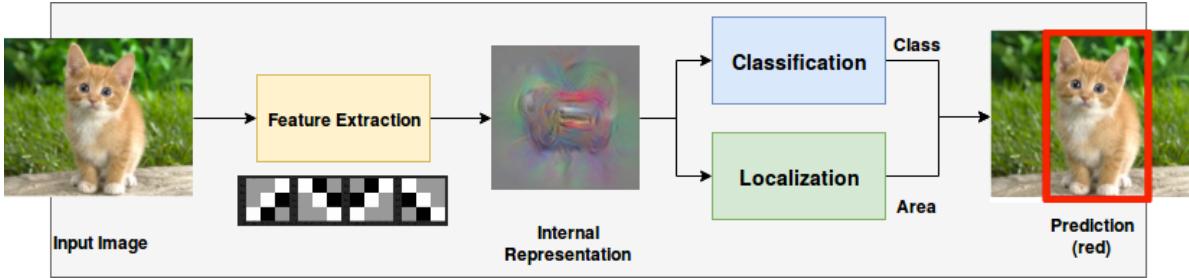


Figure 2.4: Object Detection Pipeline. An initial step extracts task relevant features of the input signal and derives an internal representation. Consecutively, classification determines what kind of object is present in the image, while localization determines where the object is located. The output consists of area(s) with class annotation.

Traditional Methods

The early attempts to Object Detection define objects in terms of basic volumetric shapes such as cubes and cylinders. During inference these features are extracted and compared to a database. However, in practice even recognizing these basic shapes proves to be difficult [3].

Later approaches focus more on appearance based features such as wavelets [37] which also applied in [55] for human face detection. Thereby the image is processed by a cascade of classifiers using a sliding window in multiple scales. The processing of an image patch is stopped when a classifier assigns background to that patch. The features can be computed with simple operations and thus the detector can be executed extremely fast. However, the used Haar-wavelets cannot efficiently encode large textures making the approach less suitable for more complex objects [3].

In contrast Histogram of Oriented Gradients (HOG) [7] and Scale Invariant Feature Transform (SIFT) [33] use the image gradient to cover shape information. In a sliding window local histograms based on the gradient orientation are calculated. Dalal and Triggs [7] use the feature for pedestrian detection.

A general challenge in Computer Vision is the combination of local image features such as corners and edges to a more global detection of an object. Especially, when parts of the object can be occluded or deformed and thus undergo large variations in appearance. In order to cope with these issues Felzenszwalb et al. [11] model pedestrians in individual parts and combine them in their proposed Deformable Part Model (DPM).

Traditional methods have in common that the individual steps of the detection pipeline are optimized separately. Furthermore, often the feature extractors and object models are designed manually. Hence, designing such a detector can result in cumbersome application dependent work. EWFO have sparse features and cameras on MAV can have a strong influence on the object appearance. Modelling this appearances manually is difficult. Also, the methods seem to have reached a limit in performance in the years of 2005-2012 where almost no improvement in performance was achieved.

CNNs-based Feature Extraction

A breakthrough in detection performance came with CNNs which emerged from Deep Learning research and subsequently became a popular feature extractor. CNNs can be seen as small neural networks that are applied locally on image patches in sliding window fashion. The outputs of the initial local operations (first layer) are further processed by higher layers until the desired output size is reached. The model parameters (weights) are trained using a loss function and the back-propagation algorithm.

The modular structure of CNNs allows to create highly non-linear models that can represent any function. However, this flexibility also introduces the challenge of choosing a suitable architecture. On a fundamental

level design parameters can be summarized in depth, width and kernel size.

Section 2.4.1 displays these parameters and introduces additional terminology necessary for the remaining parts of this chapter. The *kernel size* \mathbf{k} determines the spatial size of a kernel and therefore how big the patch is, the convolution is applied on. A layer usually contains multiple filters that are applied on its input. The amount of filters is also referred to as *width w*. The filters are applied in sliding window fashion which introduces the step size (*strides s*) as an additional parameter. The output of each convolution is concatenated and processed by the next layer. The amount of layers is also referred to as *depth*. In the image also the *receptive field* of a filter is visualized. This describes the image patch that is related to a certain feature response. The filter of the first layer (green) has a receptive field corresponding to its kernel size. The filter of the second layer (blue) combines the responses of the filters of the first layer at multiple spatial locations and thus has an increased receptive field.

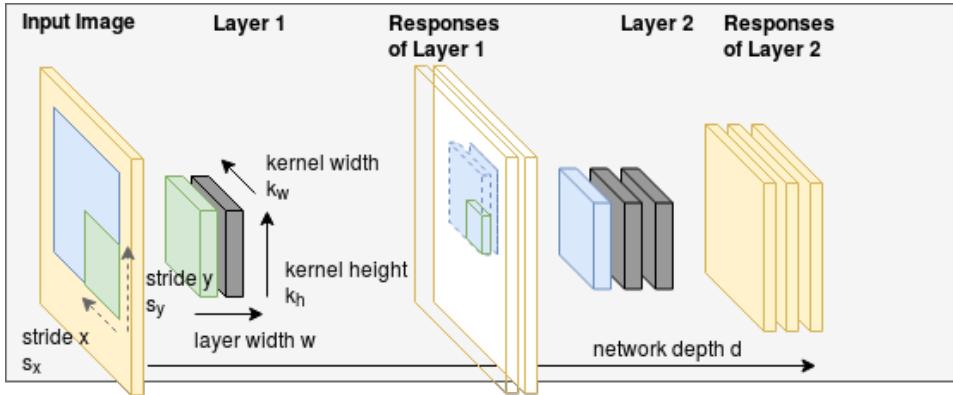


Figure 2.5: Notation in CNNs. The input image is convolved with a layer. One layer contains multiple kernels that are convolved in sliding window fashion with certain step size. The responses of the convolutions are collected and processed by the next layer. The receptive field is determined by which parts of the input image are part of the kernel response at layer x. The total amount of layers is also referred to as depth.

Among these parameters depth is considered one of the preliminary parameters to improve performance [14]. Simonyan and Zisserman [46] achieve first places in the 2014 ImageNet Classification challenge using a network that only contained filters of size 3-by-3 but up to 19 layers. Szegedy et al. [47] achieve similar performance using a network with 22 layers. The proposed network included an *Inception*-module, an architectural element that allows deeper networks at a constant computational budget.

Residual Connections. An issue that prevented training even deeper networks is the *vanishing gradient problem*. As the gradient distributes across nodes its magnitude gets smaller with increasing amount of nodes. Hence, the training becomes slow and the risk of converging in a local minima increases. This was addressed by He et al. [15] who propose the use of residual connections. Instead of propagating the gradient from the last to the first layer these connections allow the gradient to flow directly into all layers. This circumvents the vanishing gradient problem. The use of residual connections allowed to train a network 101 layers and improved on state of the art at that time.

Wide-Residual Networks. However, later work by Zagoruyko and Komodakis [58] shows how residual networks do not behave like a single deep model but more like an ensemble of more shallow networks. Moreover, the study shows that similar performance can be achieved by particularly wide networks and residual connections. Being of similar performance the proposed Wide Residual Networks (WRNs) are computationally more efficient to execute.

While wide residual networks can achieve similar performance to deep residual networks with reduced inference time the computational requirements are still large. This work addresses the detection of EWFO with very limited resources. Hence, a network in which the vanishing gradient problem would appear is likely to be already too computationally expensive to be applied on a MAV.

Fully Convolution Networks. Instead the work focuses on much smaller networks that are fast to execute. Execution time is also the motivation for Fully Convolutional Networks (FCNs). Instead of using a fully connected layer in the last stage, these networks only apply local operations. This saves many computations in the last layer and enables the application of models on various input sizes.

Dilated Convolutions. However, FCN in combination with a small amount of layers introduce a limited receptive field. If the network is too shallow the last layer cannot take into account the whole input image. A way to increase the receptive field without increasing the number of computations is the use of sparse kernels, also called Atrous/Dilated convolutions.

Depthwise Separable Convolutions. Another line of research to reduce the number of computations in CNNs address the convolution operation. *MobileNet* [19] and *QuickNet* [12] make extensive use of Depthwise Separable Convolutions (DSCs). DSCs replace the original 3D-convolution by several 2D-convolutions followed by a pointwise convolution. This reduces the total number of operations from $N = k_w \cdot k_h \cdot w_n \cdot w_{n+1}$ to $N = (k_w \cdot k_h + w_n) + w_n \cdot w_{n+1}$. *MobileNetV2* [44] further includes linear bottlenecks to reduce the total number of operations. These are convolutions with a 1by1 kernel and linear activation.

Channel Shuffling. [59] addresses the computational costs of pointwise convolutions. Instead of applying a pointwise convolution on the whole input volume, group convolutions are applied on by dividing the channels in subsets. These channels are shuffled to enable cross-channel information propagation.

Dense Connections. *DenseNet* [20] proposes the use of dense connections in CNNs. Thereby the input of each convolutional layer does not only consist if its direct previous layer but of a concatenation of the activations of all its previous layers. By enabling feature reuse the total amount of parameters shall be reduced.

Despite a large amount of research conducted in finding suitable architectures there has not yet been a single way that always achieves a goal. It has been shown how models with a large amount of parameters combined with vast amounts of training data perform well on various vision tasks and objects. However, there is no guarantee that the found representation is also the most suitable/efficient one. The research resulted in a collection of rules an best practices that need to be considered with the task at hand. This work investigates the design of a CNN for the detection of EWFO.

CNN-based Object Detection

After showing promising results for Classification, CNNs where also applied for Object Detection. CNNs-based Object Detectors can broadly be grouped in two categories. The categories are introduced and finally compared in relevance to this work.

Two-Stage Detectors. Girshick et al. [13] use Selective Search [53] to extract object candidates from an image and classify each region with a CNN. However, this requires to run the whole network at various scales

and overlapping locations. Hence, the approach is computationally intense while many of the performed operations are redundant.

Follow up work aims to share computations for faster inference. Spatial Pyramid Pooling [?] allows to crop any region to a predefined size. Thus a CNN does not have to be run at overlapping regions anymore but the extracted features can be reused and need to be only computed once. This leads to a vast reduction in computations and leaves the region proposal algorithm as a computational bottleneck.

With the Region Proposal Network (RPN)[42] region proposals and feature extraction is combined in a single stage. The whole stage is framed as a regression problem by predicting object probability for a predefined set of bounding boxes so called anchor/prior or default boxes. Predefining the total amount of possible locations and bounding box dimensions would lead to an intractable amount of parameters and computations. Hence, the most common object appearances are defined and the network not only predicts an object probability for each box but also how to adapt location and dimensions to better fit the predicted object. Combining feature extraction and region proposals in a single network led to 213x speed up.

Being currently the method with the best performance in terms of Mean Average Precision (mAP) two stage approaches would be a valid choice for the detection of EWFO. However, their two stage character makes the inference time relatively slow, which is not suitable for the application on a MAV. Also, this work investigates the detection of a single object. For this application the RPN can be used directly.

One-Stage Detectors. One stage detectors aim to further combine multiple stages of the Object Detection task into a single network. Therefore the whole pipeline is framed as a regression task. This leads to the question how to discretize the input image.

The first one stage detector You only look once (Yolo)[48] divides the input image in a fixed grid and predicts class probabilities for each grid cell. As this limits the amount of bounding box coordinates significantly the network also predicts global bounding box coordinates and a object probability for each box. As a last step a postprocessing algorithm fuses the output to the final prediction. Being a breakthrough as the first one stage detector the approach is limited to predict a single class for each grid cell. Furthermore, the approach of predicting bounding box coordinates globally proved hard for the network to learn and resulted in high localization errors.

Better results could be achieved by predicting offsets to predefined regions as in the concept of the aforementioned anchor boxes. Single Shot Multibox Detector (SSD) [32] extends the anchor box approach to perform the whole Object Detection task. Therefore the network not only predicts bounding box coordinate offsets and object probability but also a class probability for each anchor box.

An issue that arises with discretization of the object detection task is that objects can appear at different scales. For small objects it is required to have a high resolution of bounding box locations to have a sufficient representation of the input image. For example many small objects can appear next to each other. A too coarse resolution could not capture the fact that there are multiple objects present. Furthermore, it is required to take into account fine grain features to predict such an object. In contrast, for large objects small changes in location do not make a difference. In contrary, a too fine resolution can cause the detector focus on noise and thus lead to bad predictions or unstable training. Therefore, SSD introduces the prediction of objects at multiple output grids at different layers of the network. Thus, the output grid can be defined depending on the object size and the network can extract features based on the object scale. Follow up work in [41, 48] also included the concept of anchor boxes and prediction layers at multiple scales, making SSD and Yolo converge to a very similar solution.

In [21] one and two stage detectors are compared in terms of accuracy as well as resource requirements. While two stage detectors with very deep networks tend to achieve the best performance, one stage detectors are

generally faster. The experiments also show how the inference time of two stage detectors can be reduced without loosing too much accuracy when the amount of bounding box proposals is limited. However, single shot detectors are still the fastest method with the lowest memory profile. Furthermore, for the single class case the region proposal stage of a two stage detector can be used directly. Hence, in this work we investigate the detection of a EWFO with a one stage detector. The *TinyYoloV3* architecture is 9-layer network with a suitable size to be applied on a MAV. This work uses this approach as the baseline model.

The anchor box concept allows to incorporate prior knowledge about possible objects but also introduces additional hyperparameters that need to be tuned for an application. Therefore the alternative approach of *CornerNet*[29] avoids the anchor box concept by defining objects as paired key points. Each bounding box is defined as two corners. The network predicts a heatmap with potential corner locations as well as which corners belong together. This would be an interesting approach for the detection of EWFO. However, as the publication was quite recent the approach could not be taken into account.

Attention Models

A research direction which is fundamentally different to the approaches seen so far are models based on visual attention. Instead of processing the whole input image at once, the aim is to process only relevant image patches. Typically a model processes an image crop and decides which location to evaluate next until enough information is gathered for the final prediction. Examples for the approach can be found in [1, 4, 22].

Attention models are promising as their computational complexity can be controlled independently from the number of pixels in the input image. However, to this end successes have mostly been demonstrated on digit recognition like the MNIST dataset. Scaling the approach to real world problems proves to be difficult. Furthermore, the features of an EWFOs are sparse, while most part of the image does not provide hints where to look for an object. Therefore, we assume the approach less applicable for the detection of EWFOs.

2.4.2 Reducing Inference Time

Computer Vision research typically focuses on detection accuracy rather than inference speed. However, for the deployment on a MAV resource consumption is an important parameter. The following describes research topics that concern the reduction of inference time.

Weight Quantization

The hardware of most embedded Central Processing Unit (CPU) support only integer operations and thus rely on software to perform floating point operations. Hence, weight quantization is another line of research to reduce the inference time of deep networks on mobile devices. By mimicking the quantization effects during training, the network learns to deal with these kind of artefacts. However, the target platform of this work supports hardware accelerated floating point multiplications. While weight quantization could still be used to accelerate the network it would require serious low level operation optimization. This work addresses the optimization on a more high level architectural basis.

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Knowledge Distillation

Knowledge Distillation [17] is way to create a smaller model based on a trained bigger model or an ensemble of models. Thereby the smaller student-network is trained to mimic the output of the final and intermediate activations of the teacher-network. *FitNet* extends the approach to create a thinner/deeper network based on

a trained network thereby reducing parameters without loosing performance. In [?] the approach is applied to the task of Object Detection. In [56] knowledge distillation is combined with weight quantization in order to obtain a faster and more efficient model.

The approaches have in common that a very complex function learned from a deep model is aimed to be compressed in a more efficient model. Training the smaller model directly leads to a lower performance than using the distillation approach. We assume this is successfully as the network architectures used are generally deep. Even [56] which speaks of very tiny networks uses the VGG-architecture with 23 layers. These architectures are prohibitive to be deployed on small scale MAVs. We investigate a network size of around 10 layers. Such networks are easier to train and our experiments show we can reduce the width of the model by simply training the network on the task. Therefore we do not investigate this approach further.

2.4.3 Generating Data

Related methods vary from changing low level properties of the image over using CAD models in combination with real background up to rendering full 3D-environments. Often various combinations of synthesized and real data are applied.

Low-Level Image Augmentation

A common part of current Computer Vision pipelines is to augment a given data set by transforming low level properties of the image. By artificially increasing variations in the input signal, a model that is more invariant to the augmented properties shall be obtained.

Krizhevsky et al. [28] use Principal Component Analysis (PCA) to incorporate colour variations. Howard [18] shows how several image transformations can improve the performance of a CNN-based Classification model. The proposed pipeline includes variations in the crop of the input image as well as variations in brightness, color and contrast. In CNN-based Object Detection Szegedy et al. [48] uses random scaling and translation of the input image, as well as random variations in saturation and exposure. Liu et al. [32] additionally crop and flip each image with a certain probability.

Since most methods use image augmentation and Krizhevsky et al. [28] mentions it to be the particularly reason for superior performance at ILSVRC2012 competition it can be assumed to be beneficial for Computer Vision models. Unfortunately, none of the publications measures the improvements gained by the different operations.

While the aforementioned approaches add artificial variation to the input data, Carlson et al.[5] augment the image based on a physical camera model. The proposed pipeline is applied for Object Detection and incorporates models for sensor and lens effects like chromatic aberration, blur, exposure and noise. While being of minor effect for the augmentation of real data (0.1% - 1.62% mAP70) the reported results show an improvement when training on fully synthesized datasets. Here the reported gains vary between 1.26 and 6.5 % mAP70.

Low-level image augmentation is a comparatively cheap method to increase the variance in a dataset. However, it cannot create totally new samples or view points. Furthermore, it cannot change the scene in which an object is placed. Therefore it needs a sufficiently large base dataset that is augmented. This work addresses the case when no real training data is available. Hence, low-level image augmentation is incorporated in the training process but can not be the only method applied.

Augmenting Existing Images with CAD - Models

In order to create new view points Computer Aided Design (CAD)-models can be used. These models describe 3D-shape of an object and can be placed on existing images to augment or increase a dataset.

Peng et al.[39] study the use of CAD-models in the context of CNN-based Object Detection. The authors particularly address how image cues like texture, colour and background affects the detection performance. The experiments show how the used CNNs are relatively insensitive towards context but use shape as primary, texture and colour as secondary most important features. This enables competitive performance even when the object of interest is placed only on uniformly covered backgrounds. However, the study only covers solid objects such as birds, bicycles and airplanes. EWFO are substantially different and we hypothesize that other image cues must be relevant.

Madaan et al.[34] study the segmentation of wires based on synthetic training. As wires similarly to EWFO only consist of thin edges, the application is quite close to this work. However, the experiments focus on a single domain, namely sky images and thus the variations in background are comparatively small. We hypothesize that EWFO are particularly sensitive to such variations and address the application in multiple domains.

Hinterstoisser et al. [16] propose to use a base network that has been trained on real images and to continue training on images with CAD-models. During training the base network is frozen and only the last layers are updated. The method does not use real data but requires a suitable base network. As most available feature extractors (further discussed in Chapter 4) are of a size that is computationally prohibitive for MAV the method is not really applicable for this work.

The use of CAD-models in combination with real backgrounds allows to generate totally new view points for the object of interest. Furthermore, the image background consists of real data and thus the synthetic textures only concern the rendered object. However, the geometric properties like perspective as well as the physical properties like object placement are violated and therefore create an artificial scene. Despite this fact, literature shows that such images can benefit model performance in various cases. Yet, most of the approaches still use real data and/or focus on solid objects with rich textures and complex shape. We hypothesize that since EWFO do not provide these kind of structures the results do not apply in the same way. Hence, we incorporate the method to generate data and investigate how it can be applied for the detection of EWFO.

Fully Synthesizing Environments

A more realistic placement of objects can be achieved when fully synthesizing environments. The object of interest can be placed according to physical laws, shadows fall correctly and geometric properties of an image are followed. However, if the graphical models do not fully capture the details of real world objects, the generated data might look too artificial.

Johnson-Roberson et al. [23] use a powerful graphical engine and a highly detailed environment to train an Object Detection model entirely in simulation. The results show an improvement towards data annotated by humans especially when using vast amounts of simulated data.

In order to create realistic environments intense manual work is required for the design. In contrast [43, 49, 50] use a relatively simple environment but a high degree of randomization to address the reality gap. The aim is to learn an abstract representation by strongly varying textures, light conditions and object locations. Tobin et al. introduced this technique as Domain Randomization (DR). The drawback of the approach is that a too high degree of randomization may omit pattern in the target domain that could otherwise be exploited by the model.

This work addresses the generation of data for the detection of EWFO on MAVs in GPS denied scenarios. Such scenarios cover a wide range of possible environmental conditions and the images taken from MAV cameras are peculiar. Hence the creation of a full environment is investigated in this work.

2.4.4 Transfer Learning

The field of transfer learning particularly addresses domain shifts in the modelling process. Hence, a common application is the learning from synthetic data.

A common approach in CNN-based models is the incorporation of a domain classifier in the model. By augmenting the data with domain labels, the classifier learns to distinguish the two domains. Subsequently a gradient reverse layer is applied and thus the weights are updated in such a way that a domain agnostic representation is learned. Examples of the approach can be found in [6, 57].

While the aforementioned approaches require labelled samples from the target domain, Peng et al. [38] propose to include task-irrelevant samples and a source classifier. As a result no samples of the target domain are required.

While transfer learning provides the theoretical framework as well as methods to deal with domain shifts, it does not allow to generate data. Furthermore, it often requires samples of the target domain. This work addresses the case when no real data is used for training. The field is interesting to be incorporated in the data generation pipeline investigated in this thesis but it can not be used as a start off point. Hence, the use of transfer learning in the modelling process is denoted as future work.

2.4.5 Generative Adversarial Networks

Generative Adversarial Networks (GANs) [?] are a learning technique to generate new samples. The method uses two models a generator and a discriminator. While the generator generates samples the discriminator aims to distinguish the generated samples from a real dataset. Thereby the training goal of the generator is to maximize the error of the discriminator. Both models are updated with back propagation. The method shows promising results for image transformation or image syntheses but also for audio signals [?]. Yet to the authors knowledge GANs have not yet been applied to generate samples for Object Detection. Furthermore, the discriminator needs a training set for initialization. As for this work only a small amount of training samples are available, we do not investigate this approach for generating samples to detect EWFOs.

Chapter 3

Synthesizing Data for the Detection of EWFO on MAVs

This chapter addresses the generation of data for the detection of EWFO. In particular the following research question is addressed:

How can data be generated to train a detection model for EWFO detection on a MAVs?

The question is subdivided in three research questions to be addressed in this chapter:

RQ1.1 What role does context play for the detection EWFOs on MAVs?

RQ1.2 What role does the view perspective play for the detection EWFOs on MAVs?

RQ1.3 Can the incorporation of sensor effects or image augmentation benefit the detection performance?

The chapter starts by introducing terminology and the data generation pipeline. In the later sections each research question is addressed in several experiments. The chapter finishes with an overall conclusion.

3.1 Methodology

A data generation pipeline is implemented using OpenGL, UnrealEngine and AirSim. An overview can be seen in Figure 3.1. In the first step a scene is created in which the objects of interest as well as the camera are placed. In 3D space position and orientation (pose) of each object are determined by translation \mathbf{t} and rotation \mathbf{r} . The coordinate system is North-East-Down (NED).

A view projection yields an image through the lens of the camera. The coordinates of each point in 3D space are projected on the 2D image plane. A final post processing step can simulate further effects like lens distortion and sensor noise. This step is implemented using OpenCV and Python. All source code is made publicly available at <https://github.com/phildue/datagen.git>.

Within the pipeline environments for training and testing are created. A black environment serves as base to replace the background with existing images. Furthermore, three indoor base environments are created that fully simulate illumination and background. An overview can be seen in Figure 3.2. Within the environment light conditions, background textures, object locations can be changed manually. The environments are described in the following:

1. *Dark*: The environment is a room without windows, only containing artificial light sources.



Figure 3.1: Overview of the data generation process.

2. *Daylight*: The environment is a room with windows along all walls that allow daylight to illuminate the room. The windows can lead to strong variations in the contrast between different parts of the object.
3. *IROS*: The environment resembles the room of the IROS Autonomous Drone Race 2018. The light sources stem from a window front at one side of the room, as well as artificial light sources at the ceiling. Depending on the view point, the object might appear against bright or dark background.



Figure 3.2: The environments from left to right *Dark*, *Daylight*, *IROS2018*

The data generation pipeline is used to generate a test set in simulation. The test set is set up in the *IROS* environment and inspired by the race court of the IROS Autonomous Drone Race. The AirSim flight controller is used to simulate a flight of an MAV through the race court. The test set contains 550 images with a total of 1361 objects.

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It should be noted that when generating data with the described methods it is likely that samples appear in which only a corner of the object is visible or the view angle is in such a way that the object appears only as a thin line. In initial experiments these corner cases led to unstable training. Hence, some minimum requirements for the labels are set and samples/labels are removed if these are not met. Objects have to have a minimum size of 1% of the image area as well as an aspect ratio between 1/3 and 3/1. Furthermore, at least three corners have to be visible.

The models and training are implemented using the *Keras* framework with *tensorflow*-backend. For all train-

ings the Adam optimizer is applied using a learning rate of 0.001 for the first 60 epochs and a learning rate 0.0001 afterwards. A validation set containing 1% randomly sampled images from the training set is used. The training is stopped if the validation error does not decrease for more than 5 epochs or 100 epochs are reached.

Throughout the experiments the baseline TinyYoloV3 architecture is used. Thereby we simplify the loss function to a single class prediction. The exact model is described in Chapter 4. The input image resolution is 416x416.

3.2 Context

The context in which an object is placed consists of background as well as light conditions or other objects. It is determined in the first step of the data generation process. Theoretically CNNs can learn to exploit context for detection. Yet, the actual influence is not clear. For example the Object Detectors trained in [39] do not seem to make use of this image cue. Nevertheless, we investigate the importance of context for the detection of EWFOs. We hypothesize that due to the sparsity of their features and their emptiness context and background plays a more important role than for solid objects.

For the investigation we compare three methods to generate data: The placement of CAD-models on uniformly coloured backgrounds, on backgrounds taken from a dataset as well as from fully synthesized environments. In terms of geometric and physical properties the fully synthesized environments provide the most realism and hence should give the best results. However, as the graphical engine only contains a limited set of textures, the variance in background is way smaller than in the backgrounds taken from a dataset. Furthermore, the objects in the background are also rendered. Hence, when tested on real data this method could lead to better performance.

3.2.1 Experiments

Four datasets are generated with 20 000 samples each. Dataset I contains samples generated by placing CAD-models on uniformly coloured backgrounds; Dataset II contains samples generated by placing CAD-models on backgrounds taken from the Pascal VOC dataset, Dataset III contains samples from the *Dark* environment, Dataset IV contains samples from all virtual environments. A fourth model is trained on a combination of Dataset II and IV (equal proportion).

Within the environment the camera is placed at random locations following these distributions:

$$x = \mathcal{U}(-30, 30), \quad y = \mathcal{U}(-20, 20), \quad z = \mathcal{N}(-4.5, 0.5)), \quad \phi = \mathcal{U}(0, 0.1\pi), \quad \theta = \mathcal{U}(0, 0.1\pi), \quad \psi = \mathcal{N}(-\pi, \pi) \quad (3.1)$$

Where $\mathcal{U}(a, b)$ is a uniform distribution between a, b and $\mathcal{N}(\mu, \sigma^2)$ is a Gaussian distribution with mean μ and variance σ^2 .

The models are tested on the real datasets described in Section 2.2 as well as the simulated flight described in Section 3.1.

3.2.2 Results

Figure 3.3 display the results. It can be seen how using uniformly coloured backgrounds achieve almost no detection. Only on the simulated data a few objects could be detected.

In contrast using fully synthesized data achieves the best performance on the simulated data for low and high quality detections. It can be seen that almost all detections have an IoU of more than 60% and are thus good quality. On the real data the performance in low quality detections is comparable to the performance on the simulated data. However, in high quality detections the performance drops significantly to an equal level of using real backgrounds.

Using real backgrounds performs poorer than using a fully synthesized environment in almost every case. However, for higher quality detections the performance is competitive to using a fully synthesized environment. Combining both methods does achieve at most the performance of using fully synthesized data. However, in most cases the performance is worse.

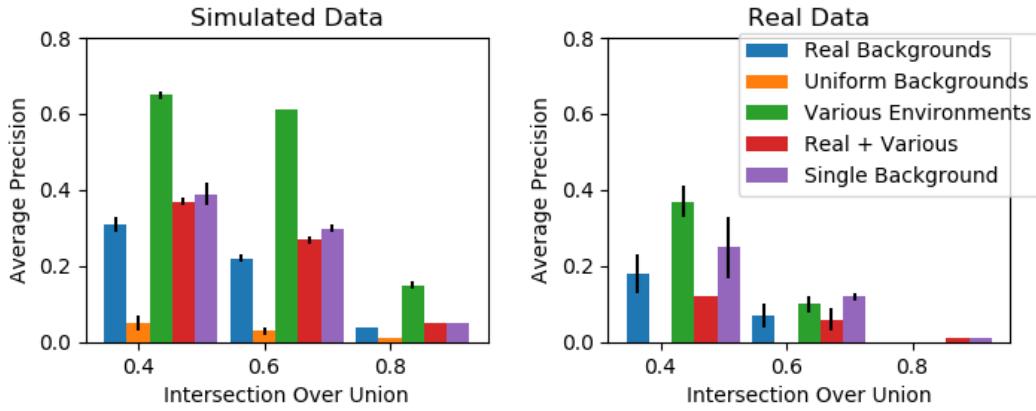


Figure 3.3: Results of different ways to generate context. Synthesizing more parts of the environment improves performance on both test sets. However, this only holds for weakly localized predictions.

3.2.3 Discussion

The results meet our hypothesis that using only uniformly coloured backgrounds is not enough to train an Object Detector for EWFO. Providing more variance in the background is crucial to improve performance.

Despite having not seen a single real background, the model trained on fully synthesized data achieves the best performance on the real data. Even a model trained in a single virtual environment achieves competitive performance. Hence, it seems that synthesizing correct geometric/physical properties is more important than providing a large variance in background. However, the margin gets small for higher quality detections. Thus, the simulation of geometric/physical properties does not help for good localization.

3.2.4 Conclusion

We investigated the role context plays for the detection of EWFOs on MAVs. We can conclude that providing some background is crucial for the detection. Otherwise the detector performs poorly in simulation as well as the real world. Furthermore, synthesizing the whole environment benefits the detection on real images. However, most of the additional detections have not very accurate bounding boxes.

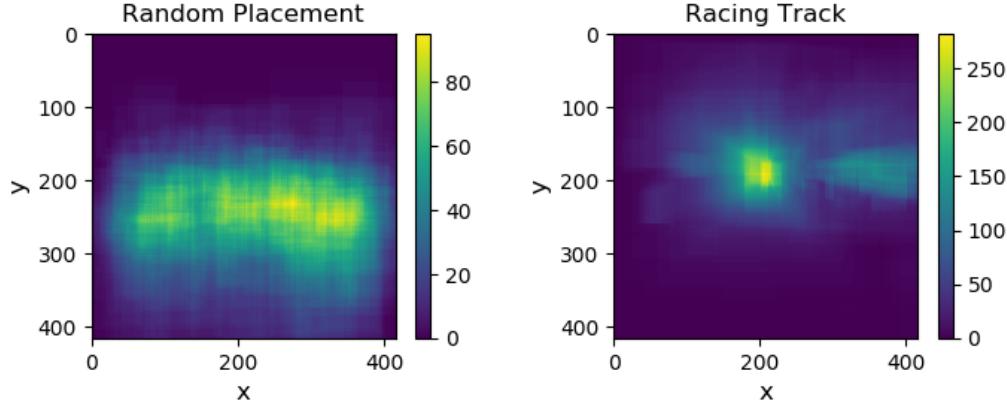


Figure 3.4: Object appearances when generating samples with random poses (left) and during a MAV flight. During the flight the object appears mostly centered on the horizontal line.

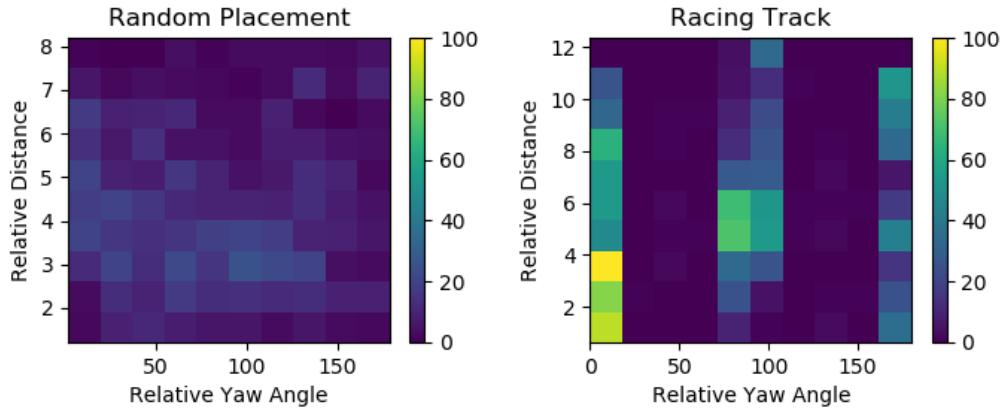


Figure 3.5: Histogram of object occurrences in yaw angle and distance relative to the camera. The random placement does rarely cover facing the object closely and frontally.

3.3 View

Another important property that influences the generated sample is the camera pose. It determines the view on the scene and therefore at which distance, angle and location the objects appear on the image.

A straightforward way is placing the camera randomly (within some margin) in order to cover a large variation of views on the object. That way the network can learn a general object representation and hopefully detect unseen objects from different view points. However, random placement might not resemble the real world sufficiently. An MAV does not appear at random places within a scene, especially not when it follows a racing track. We examine this by simulating a flight through a race court using AirSim's MAV model and analyzing the relative object poses. We compare these to the relative poses obtained when placing the camera randomly using the distributions from Equation (3.1).

Figure 3.4 shows the distribution of bounding boxes when created with random camera placement and when following a racing track. It can be seen how, when following the race track most of the objects are centered and distributed across the horizon, as camera focuses the next object frontally most of the time. In contrast, random placement leads to more evenly distributed object locations. This can also be seen in Figure 3.5 where a 2D histogram of the yaw angle and distance with respect to the camera is displayed. Thereby 0 corresponds to facing the object frontally, 180 degrees facing the object from the back. It is apparent how the

random placement covers a much larger range of relative angles, while in the racing track certain angles do not appear at all. Even more importantly the largest bins of the racing track is an angle of 0 and a distance between 0m and 4m. These bins are almost not present when placing the camera randomly. This is because close to the camera the field of view is small, while the area of the object faced frontally is big. Hence, the probability of an object ending up at this specific location is relatively low. Furthermore, when placing the camera randomly there are no samples further away than 8m. This is because in the race track the camera traverses the room from one end - where it can see almost all gates - to another. The probability that the randomly placed camera ends up in a similar position is relatively low.

The filters of CNNs are translation invariant by design but cannot inherently handle variation in rotation and scale. We hypothesize that the generation of samples with only one of the two methods can miss important object appearances. Random placement does not cover appearances that are typical for a autonomous drone race. On the other hand, only training on racing tracks might lead to a bias towards the created courses.

3.3.1 Experiments

In order to evaluate this hypothesis three models are trained on 20 000 samples each. Model I is trained when placing the camera randomly, following the distribution in Equation (3.1). Model II is trained on varying racing courts. Model III is trained on a combination of both datasets (equal proportion).

The models are tested on the real datasets described in Section 2.2 as well as the simulated flight described in Section 3.1.

3.3.2 Results

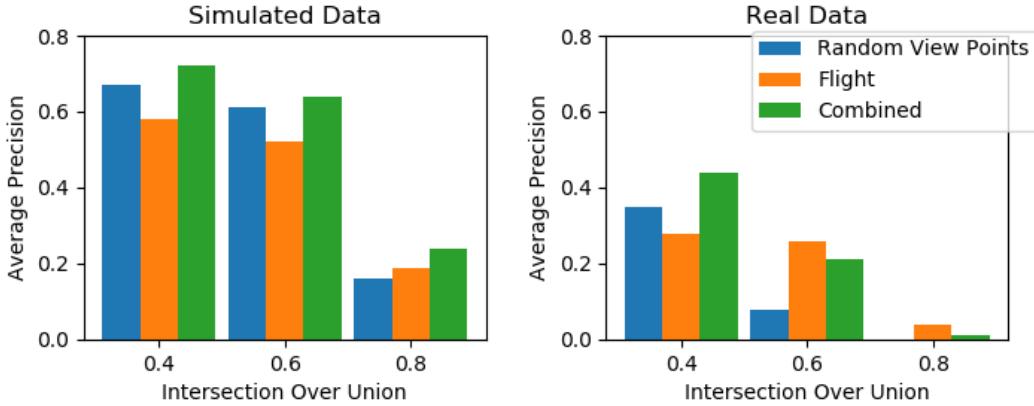


Figure 3.6: Average Precision for the three different models.

Figure 3.6 shows the average precision of the different models. It should be noted that *Random View Points* is the same model as *Various Environments* of Figure 3.3. On the simulated dataset there is only a minor difference between the three models in terms of average precision. In contrast on the real world dataset it can be seen how the models that include flight images perform better for higher quality detections. The best performance is achieved by the model that was trained on a combination of both datasets.

Figure 3.7 shows the performance of the different models in terms of recall on the simulated dataset at a confidence threshold of 0.5. It can be seen that the recall of the model only trained on racing tracks is lower than the recall of the other models. This holds particularly when the object is not faced frontally. Between the combined dataset and random placement only minor differences can be identified.

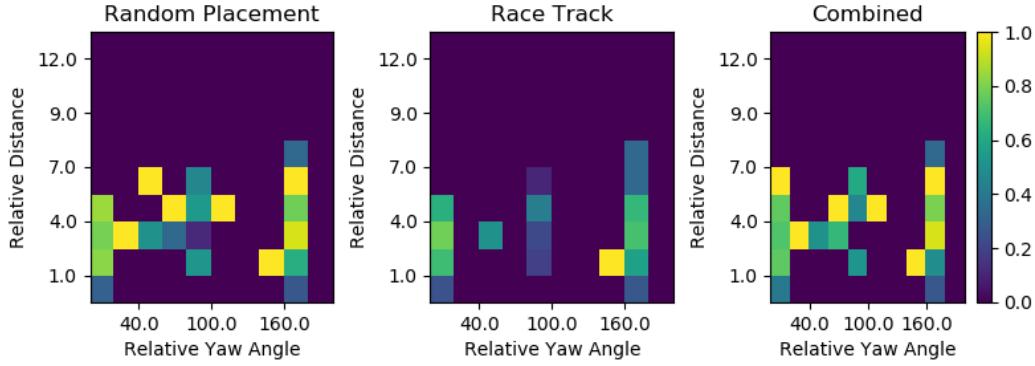


Figure 3.7: Recall on clusters depending on yaw angle and distance.

Despite the lower recall the model trained on racing tracks achieves comparable performance in terms of AP. This is explained by the higher precision achieved by the model.

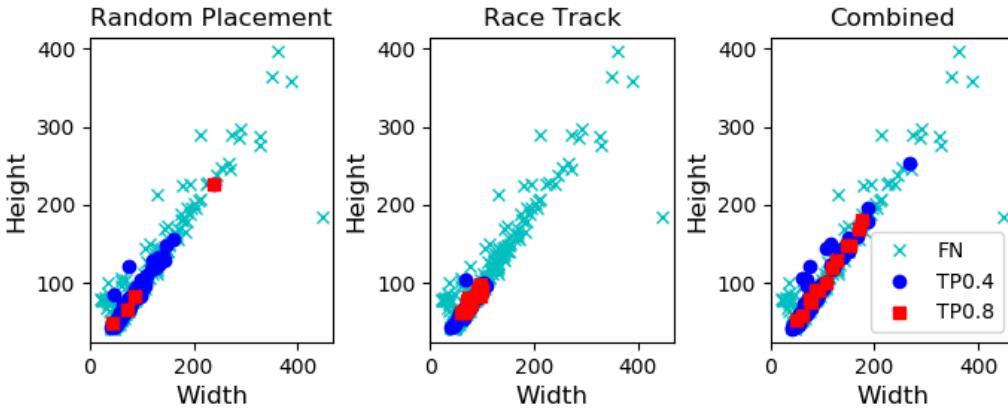


Figure 3.8: Detections on the real data shown with respect to width and height of the bounding box. The more top left a sample is located the closer it is to the camera. When Height > Width the object mostly has a yaw angle unequal to zero.

Figure 3.8 shows true positives at different IoU thresholds as well as false negatives of the real data. It can be seen how the models that cover more relative view angles in their training data have a broader range of detections. The model trained on racing tracks only detects objects at quite narrow field. It is also apparent how the model trained on a combination of both datasets not only detects the same objects as the other two models but also objects.

On the real as well as on the simulated data it can be seen that there is some distance were the model performs best. Objects that are very close or too far are not detected by any of the models.

3.3.3 Discussion

Even though one model is trained on various race courts, containing many samples with objects close to the camera there is no significant performance increase for those samples. Instead this model produces higher quality bounding boxes while overall detecting less objects. The model trained on random view points seems to detect more objects but the predicted bounding boxes are poorer. Hence, there seems to be a trade-off between detecting angles at more view points and the quality of the respected bounding boxes.

It can also be seen that the combined model learns to detect not only the same objects as the individual models but also totally new objects. Hence, it can be assumed covering more angles in the training set helps to generalize.

It can also be observed that the performance for objects that are close to the camera are quite poor for all models. This is potentially explained by the fact that less object context is available. For example the pole for closer objects is less visible. Also, the probability of having a part of the object out of view increases as the camera comes closer. Another issue could be the limited receptive field of the detection model. As the last node of the model cannot see the whole image and the object is empty, it is possible that the node responsible to predict the object does not see any of the object parts. This is further addressed in Chapter 4.

For larger distances the performance decreases again. This is explained by the fact that less details of the objects are visible as the camera moves further away.

3.3.4 Conclusion

We investigated the influence of the relative view for the detection of EWFO on MAV. We hypothesized that having a higher variance in view points will improve the detection and that including samples obtained from racing tracks is crucial for detecting close objects. However, we could not observe a direct relation between the view angles present during training and the model performance on different angles. Instead we observe that the model containing less angles in the training set produces less but higher quality bounding boxes. Furthermore, we observe that including the racing track images helps the model to generalize and improves performance on the real world dataset.

3.4 Image Augmentation

The final step applies low-level image transformations. It allows to further simulate sensor effects and increase the variance in the generated data.

In literature [18, 28, 32, 48] the application of image augmentation is a common tool to improve the detection performance. The experiments in [5] show how the incorporation of sensor effects particularly improves the performance of models learned on fully synthesized data. In the MAV domain sensor and lens effects have a significant influence on the obtained sample. Hence, we hypothesize that the incorporation of these effects will improve the performance of the trained models. A total of five image augmentation techniques are investigated.

Lens Distortion Lens distortion is a form of optical aberration which causes light to not fall in a single point but a region of space. For MAVs commonly used wide-angle lenses, this leads to barrel distortion and thus to straight lines appearing as curves in the image.

For this work a 120 wide angle lens is used. Especially, close objects undergo a strong variation in appearance. Hence, we hypothesize including this effect in the training process will improve the performance on the real world dataset.

The effect is applied using the model for wide-angle lenses from [54]. It models the removal of lens distortion as combination of radial and non-radial part, that is approximated with a second order Taylor expansion:

$$\begin{pmatrix} x_u \\ y_u \end{pmatrix} = f(x, y) = \begin{pmatrix} x(1 + \kappa_1 x^2 + \kappa_1(1 + \lambda_x) y^2 + \kappa_2(x^2 + y^2)^2) \\ y(1 + \kappa_1 x^2 + \kappa_1(1 + \lambda_y) y^2 + \kappa_2(x^2 + y^2)^2) \end{pmatrix} \quad (3.2)$$

Where:

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- x_u and y_u are the undistorted coordinates.
- $\kappa_1 \kappa_2$ control the radial distortion
- λ_x and λ_y control the tangential distortion

Applying the lens distortion to an image is done using the inverse of Equation (3.2). However, as there is no closed form solution, so the Newton-approximation.

An example with $\kappa_1 = 0.5, \kappa_2 = 0.5$ is displayed in Figure 3.11. It can be seen how the previously straight lines appear as circular shape.

Chromatic Aberration. Chromatic Aberration is caused when different wavelengths of light do not end up in the same locations of the visual sensor. This leads to a shift in the colour channels of the image.

In [5] including chromatic aberration significantly improves the performance of models that are trained on fully synthesized data. Hence, we hypothesize this will also help for our work.

Similarly to [5], chromatic aberration is applied by scaling the locations of the green channel, as well as applying translations on all channels. The model can be implemented as affine transformation of the pixel locations for each channel:

$$f(x_C, y_C) = \begin{pmatrix} S & 0 & t_x \\ 0 & S & t_y \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x_C \\ y_C \\ 1 \end{pmatrix} \quad (3.3)$$

Where C is one colour channel of the image.

An example is displayed in Figure 3.10. It can be seen how the red and green channel are shifted relative to each other. Thus two bars appear in the image.

Blur Fast movement and sensor noise can lead to blurry images. This is particularly present in the domain of MAV/Autonomous Drone Racing. Hence, we hypothesize including this effect will improve the detection in the real world.

The effect is modelled using a Gaussian-filter. The image is convolved with a 2D-kernel build from:

$$k(x, y) = \frac{1}{2\sigma_x\sigma_y\pi} e^{-\frac{1}{2}(\frac{(x-\mu_x)^2}{\sigma_x^2} + \frac{(y-\mu_y)^2}{\sigma_y^2})} \quad (3.4)$$

Where σ_x and σ_y are the variance in direction x and y, used to model directional (motion) blur and μ_x, μ_y are at the kernel center. An example can be seen in Figure 3.12.

Exposure. Exposure is the time the sensor records light in order to create an image. Over- and Underexposure are caused when this time is too short or too long, leading to too dark or too bright images.

Cameras typically have Autoexposure-functionality which adapts the exposure time depending on light conditions. However, the adoption is not instant, sudden light changes can lead to over- or underexposure. This particularly applies during a fast flight. Hence, we hypothesize incorporating the effect in the data generation will improve the performance of the trained model. The effect is modelled following [5]:

$$f(S) = \frac{255}{1 + e^{-AS}} \quad (3.5)$$

whats a

where A is a constant term for contrast and S the exposure. The image can be re-exposed with:

$$I' = f(S + \Delta S) \quad (3.6)$$

where S is obtained from :

$$S = f^{-1}(I) \quad (3.7)$$

An example for overexposure is displayed in Figure 3.14. It can be seen how lighter areas appear particularly light, while dark areas remain dark.

Colour Variations The 3D-models and textures used in the simulator are limited and creating a large variation in environments or objects requires manual effort. An alternative method to increase the variation in colour and illumination is a scaling in HSV space. The objects in the real world dataset have a slightly different shape and different colour to the 3D-models of the data generation tool. We hypothesize including variations in HSV space will improve the performance on the real world dataset.

The variations are including with:

$$I^* = f(I) = SI \quad (3.8)$$

Where \mathbf{S} is a 3D-vector where each element stems from a uniform distribution. The distributions are:



Figure 3.9: Original Image.

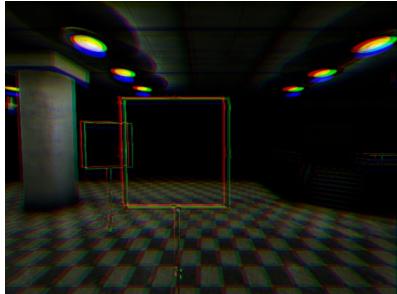


Figure 3.10: Chromatic Aberration.

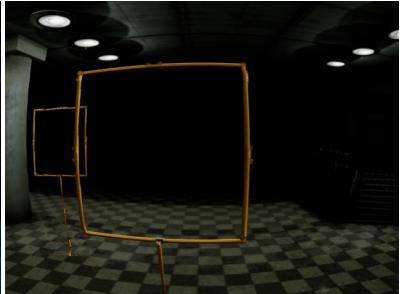


Figure 3.11: Lens Distortion.



Figure 3.12: Out-of-Focus blur.

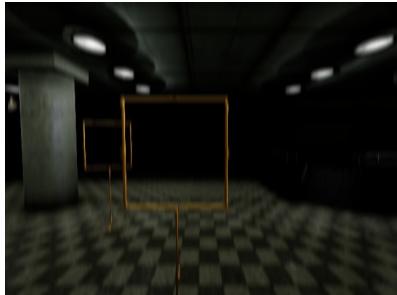


Figure 3.13: Vertical Motion Blur.

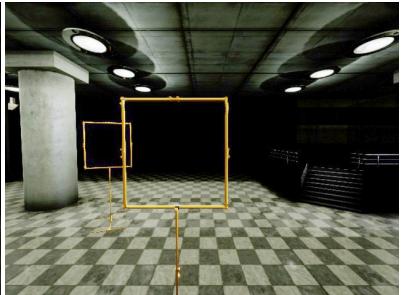


Figure 3.14: Exposure.

3.4.1 Experiments

Distortion

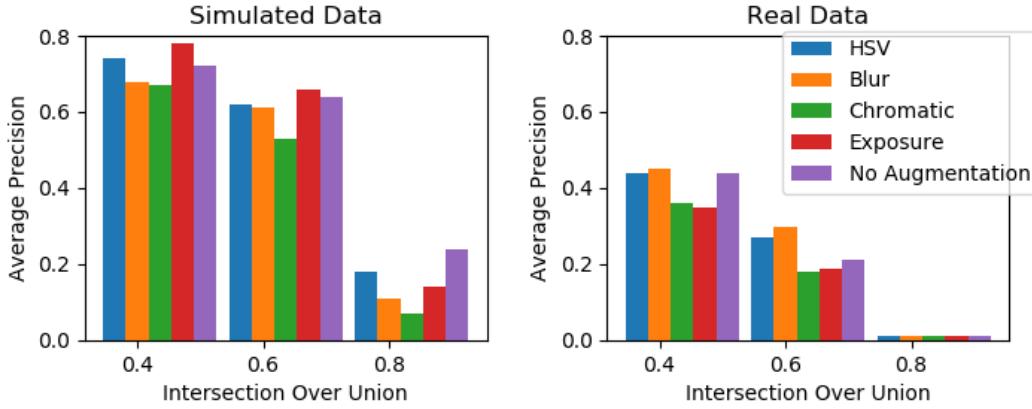


Figure 3.15: Performance in terms of Average Precision for different methods of image augmentation.

3.4.2 Results

Figure 3.15 shows the results in terms of average precision in the training domain. On the simulated data variations in exposure improve the performance of low quality predictions slightly compared to using no augmentation. However, using no data augmentation achieves the best performance for high quality detections. The other effects have only minor influence.

On the real data variations in HSV space as well as blurring improves the results compared to not using data augmentation. Incorporating chromatic aberration and variations in exposure lead to a deterioration in performance.

3.4.3 Discussion

In simulation the data augmentation has only a minor effect on low quality predictions, while the performance in high quality predictions decreases. As most effects are not really present in the test set this confirms that the models can learn a robust representation. Despite having more noise in the training data, the performance on the test set stays the same. However, the added noise leads to a lower quality in the predicted bounding boxes.

On the real data there is a stronger effect measurable. Variation in HSV and image blurring increase the performance compare to not using data augmentation. This meets our hypothesis that variations in HSV help to achieve a model that is more robust against changes in colour. Blur is one effect that can clearly be seen in the real world test set. Including this effect in the training process helped the model to perform better in the real world. Chromatic Aberration led to a significant improvement in [5] however, we cannot confirm these results. It is possible that our camera suffers only little from chromatic aberration and thus including the effect in the training does not further help the prediction. The same holds for variations in exposure.

3.4.4 Conclusion

We investigated whether including sensor effects present in the target domain in the data generation process can improve the detection. Therefore we modelled several effects that were observed when working with the camera or that improved the detection in experiments conducted in literature. Finally, image blurring improved the detection. Other effects led to a deterioration in performance.

We also investigated image augmentation by adding variations in HSV-space to evaluated whether this improves the robustness of the model, improving the performance on the real world dataset. We can confirm this hypothesis and conclude that this image augmentation should be part of the training process.

3.5 Conclusion

In this chapter the generation of data for the detection of EWFOs on MAVs was investigated. Finally, the initially formulated research questions can be answered:

put more numbers on the results

RQ1.1 What role does context play for the detection EWFOs on MAVs?

Without providing some variation in background, the trained model could not detect objects in simulation or the real world. However, when providing random images as background, the object could be detected sometimes. Hence, we conclude that at least some variation in background is required. Better results are obtained when the context is more realistic in terms of illumination and object placement even though when the environment is fully synthesized. Hence, we conclude that the model can make use of context and that creating a realistic synthesized environment is crucial for detection.

RQ1.2 What role does the view perspective play for the detection EWFOs on MAVs?

We observe that the models perform poorer on objects with very low and very high distance. We assume that this is because less context is present and the object parts are spread over larger distances in the image.

We could not identify a direct relation between the view perspective in training and during testing. Instead we see a trade-off in quality of bounding boxes in terms of detection and location and overall recall. The more angles are included in the training set the more objects can be detected however, more false positives are predicted and the dimensions of the bounding box are less accurate.

RQ1.3 Can the incorporation of sensor effects or image augmentation benefit the detection performance?

Image blurring improved the performance of the models in the real world. We assume that other effects are of minor influence in the camera used in this work. Thus modelling the respective effects did not help. In contrast motion blur seems to be of large influence. Incorporating this effect led to an improvement. Furthermore, we find that adding variations HSV-space improves the performance of the model in the real world.

Chapter 4

Detecting EWFO on MAV

CNN-based Object Detectors offer the advantage that they can be trained on any object given labelled training data is available. However, typically the architectures of CNNs are optimized for solid feature rich objects, such as planes, cars or faces. The predominant metrics optimized are precision and recall rather than inference speed. This work investigates the detection of EWFO on MAVs as part of a control loop. Hence, inference speed and computational requirements can be more important than detection performance. Furthermore, EWFOs differ substantially from objects usually used in Object Detection. This chapter investigates the detection of EWFOs with a CNNs. An off-the-shelf CNNs-based detector is optimized for the detection of EWFOs. Furthermore, the trade-off in detection performance and inference speed is studied in the example of the hardware used in this thesis. The research questions are summarized in the following:

RQ2 How can the architecture be optimized to detect EWFOs more efficiently?

RQ3 What are the trade-offs in detection performance and inference time when the detection model for EWFOs is deployed on a MAV?

4.1 Methodology

This work uses a typical one-stage detector with anchor boxes as baseline, namely the *YoloV3* detector with the *TinyYoloV3* network. The fundamental concept of one-stage detectors with anchor boxes is illustrated in ???. In this section the implementation with the *TinyYoloV3* network and its training goal are explained.

On a high level basis *YoloV3* maps the input image to a predefined set of anchor boxes which are visualized in ???. The anchors have a predefined width t_w , height t_h and center location c_x , c_y . For objects of different scales different image features are relevant. Furthermore, for small objects a more fine grain resolution is required to sufficiently distinguish between multiple small objects close to each other. Therefore, *YoloV3* uses two output grids $G = 2$ output grids, with a grid of $S_1 = 13$ for larger objects (red) and $S_2 = 26$ smaller objects (blue).

For each box the network predicts an object probability \hat{o} that classifies the class as object (1) or background (0). The original version of *YoloV3* further distinguishes between object classes, however this work considers the single class case. There we remove this output node from the prediction.

The predefined anchors only cover a subset of possible areas that can contain an object. Hence, *YoloV3* also predicts how to better adapt the anchor box to better fit the predicted object. These are the bounding box center \hat{x} , \hat{y} , its width w and height h . The predicted outputs are interpreted as offset to the predefined anchor box dimensions. Hence, the output for the anchor at grid i , cell j , anchor k is decoded as follows:

$$b_x = \hat{x}_{i,j,k} + t_{i,j,k}^x \quad b_y = \hat{y}_{i,j,k} + t_{i,j,k}^y \quad b_w = \hat{w}_{i,j,k} \cdot t_{i,j,k}^w \quad b_h = \hat{h}_{i,j,k} \cdot t_{i,j,k}^h \quad (4.1)$$

where t^x, t^y, t^w, t^h are the coordinates of the predefined anchor boxes and b_x, b_y, b_w, b_h are the final bounding box coordinates normalized to the image resolution.

In total this leads to 5 predicted parameters for each bounding box and thus to a mapping from the input image of 416x416x3 pixels to 12675 output nodes that predict 2535 boxes. In a last step boxes that contain the same class and have a high overlap are filtered such that only the boxes with the highest confidences remain.

This mapping is implemented with a CNNs as illustrated in Figure 4.1. It contains 10 convolutional, 6 pooling and 1 unpooling layer(s). After each convolutional layer batch normalization normalizes the output in order to simplify the training process. The input image with a resolution of 416x416x3 is processed by 5 layers that stepwise decrease the spatial resolution (max pooling) while increasing the width, leading to a intermediate volume of 26x26x512. This part can be seen as a common part that extracts features for objects at all scales. The architecture is a typical example of current CNNs. In the early layers the receptive field of the filters is small. Hence, the patterns that can be represented are not very complex and only a small amount of filters is used. As the network gets deeper more complex patterns can be present and more weights are required to encode these features. Hence, the width is increased. Research has shown that fixing kernels to a size of 3x3 and stacking them in deep layers is particularly efficient. This can also be seen in the *TinyYoloV3* architecture.

vgg

Convolving the wide volume of deeper layers such as the 26x26x512 output of layer 5 with a 3x3 kernel requires many computations. Therefore a common technique is to first compress the volume by applying a 1x1 kernel intermediately. Such *bottleneck* layers can be seen in layer 6-1 and 7-2.

From layer 5 the network splits to two branches responsible for smaller and larger objects. The lower branch extracts features for larger objects leading to a final grid of 13x13. The higher branch extracts features for smaller objects leading to a grid of 26x26. When Although not stated explicitly by the authors this is likely to compress the feature response of the previous layer and thus save computations.

In the final layer 15 output nodes are responsible to predict 3 bounding boxes for each grid cell. Thereby the nodes responsible for \hat{o} have a sigmoid-activation such that the response gets squashed between 0 and 1 thus can be interpreted as a probability. Similarly the nodes responsible for \hat{x} and \hat{y} have a sigmoid activation such that the output can be interpreted as coordinate normalized to the image size. For the output nodes of w and h *YoloV3* uses e^x -activation. This way the output is always larger than one while no adaption in bounding box width/height ($w = 1$) corresponds to no activation. Furthermore, the network can predict a large range of scales in a small range of activation which aims to simplify the learning process.

4.1.1 Training Goal

In order to train a CNN to predict the desired properties *YoloV3* quantifies the Object Detection task as the combined goal between localization and a classification:

$$\mathcal{L} = \lambda_{loc}\mathcal{L}_{loc} + \lambda_{obj}\mathcal{L}_{obj} + \lambda_{noobj}\mathcal{L}_{noobj} + \lambda_{class}\mathcal{L}_{class} \quad (4.2)$$

where \mathcal{L}_{loc} is the loss for bounding box dimensions, \mathcal{L}_{obj} the loss where a object is present, \mathcal{L}_{noobj} the loss where there is no object and \mathcal{L}_{class} the classification loss. λ are trade-off parameters between the multiple targets.

For a single class prediction this can be simplified to:

$$\mathcal{L} = \lambda_{loc}\mathcal{L}_{loc} + \lambda_{obj}\mathcal{L}_{obj} + \lambda_{noobj}\mathcal{L}_{noobj} \quad (4.3)$$

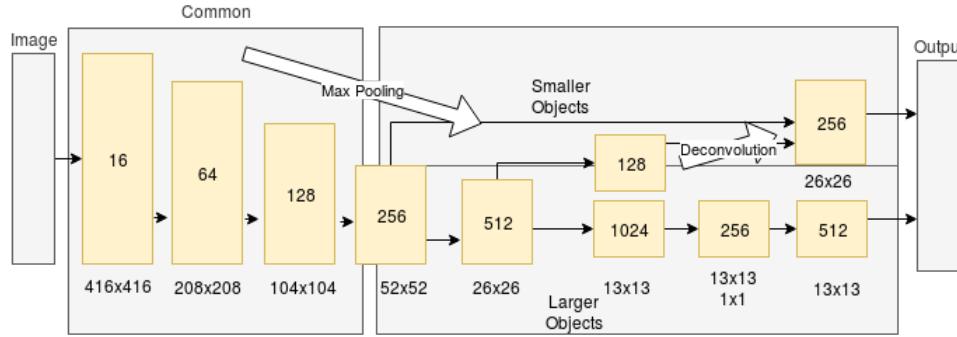


Figure 4.1: The architecture of the baseline *TinyYoloV3*. For each layer the amount of filters are displayed. The height of the boxes correspond to their spatial dimension. Arrows correspond to the forward pass in a network inference. In the common part the spatial resolution decreases each layer down to 26x26, while the width increases from 16 to 512. From layer 5 two branches focus on objects corresponding to different scales.

The object loss quantifies a binary classification loss. Hence, it is the difference between a predicted probability \hat{o} and an actual class label c . Where $o \in 0, 1$ and $\hat{o} \in (0, 1)$. In order to learn such a goal it is desirable that the weights of the network get updated significantly when the difference between truth and prediction are high. However, when prediction and truth are already close to each other the updates to the weights should be smaller otherwise the training might miss the optimal solution. A loss function that contains the desired properties and is used by *YoloV3* is the logarithmic loss which can be formulated as follows:

$$\mathcal{L}_{log} = -(o_{ij} \log(\hat{o}_{ijk}) + (1 - o_{ij}) \log(1 - \hat{o}_{ijk})) \quad (4.4)$$

where \hat{o}_{ij} is an output node with sigmoid activation assigned to anchor box i, j, k and o_{ij} the ground truth label assigned to that box. The logarithmic loss is calculated for each output grid G_i , for each grid cell S_j and each anchor box B_k . However, only the loss of the responsible anchor boxes are summed in the total loss calculation:

$$\mathcal{L}_{obj} = \sum_{i=0}^G \sum_{j=0}^{S_i^2} \sum_{k=0}^{B_i} \mathbb{1}_{ijk}^{obj} (-(c_{ijk} \log(\hat{c}_{ijk}) + (1 - c_{ijk}) \log(1 - \hat{c}_{ijk}))) \quad (4.5)$$

Thereby the binary variable $\mathbb{1}_{ijk}^{obj}$ is 1 if anchor at i, j, k is responsible to predict an object and 0 otherwise. The responsibility is determined by the IoU of an anchor box with a ground truth box. The box with the highest IoU with the ground truth box gets assigned responsible. \mathcal{L}_{obj} is defined vice versa but controlled by the $\mathbb{1}_{ijk}^{noobj}$ binary variable.

For the localization loss, similar to the classification loss, the weights should be updated significantly when the difference is high but less strongly when the difference is small. Furthermore, the loss should be invariant to direction. A loss that contains these properties is the squared distance between each bounding box parameter. However the squared distance does not make a difference between large and small boxes. For example, a deviation of 5 px for a small ground truth box with a width of 1 is treated equally to a deviation from a ground truth box with width 100. Therefore *YoloV3*, applies the square root on width and height to scale down very large box dimensions and thus balance the loss calculation. The localization loss is summarized in:

$$\mathcal{L}_{loc} = \sum_{i=0}^G \sum_{j=0}^{S_i^2} \sum_{k=0}^{B_i} \mathbb{1}_{ijk}^{obj} [(x_{ijk} - \hat{x}_{ijk})^2 + (y_{ijk} - \hat{y}_{ijk})^2 + (\sqrt{w_{ijk}} - \sqrt{\hat{w}_{ijk}})^2 + (\sqrt{h_{ijk}} - \sqrt{\hat{h}_{ijk}})^2] \quad (4.6)$$

where x_{ijk}, y_{ijk} are the ground truth center coordinates of anchor box i, j, k and w_{ijk}, h_{ijk} the corresponding width and height. $\hat{x}_{ijk}, \hat{y}_{ijk}, \hat{w}_{ijk}, \hat{h}_{ijk}$ are the predicted bounding box coordinates. $\mathbb{1}_{ijk}^{obj}$ is 1 if the set of output nodes at i, j, k is responsible to predict a certain object and 0 otherwise.

The model is implemented using *keras* with *tensorflow* backend.

4.1.2 Datasets

Throughout the experiments the same training and test set is used. For training 20 000 samples from the dataset created in Chapter 3 are used. For testing we use the test set described in Section 3.1.

For all trainings the Adam optimizer is applied using a learning rate of 0.001 for the first 60 epochs and a learning rate 0.0001 afterwards. A validation set containing 1% randomly sampled images from the training set is used. The training is stopped if the validation error does not decrease for more than 5 epochs or 100 epochs are reached.

4.2 Refining the architecture

TinyYoloV3 is optimized to detect solid feature rich objects of multiple classes with a low computational budget. This led to an architecture with 9 layers and a final width of 1024. Thereby the receptive field is of the last layer is 223 pixels. For solid objects this is of minor impact as even if the network only sees an object part it can still learn to recognize it. However, this does not apply for EWFOs which are empty and do not contain any information in the object centre. Instead it can confuse an output layer that is assigned responsible to detect such an object. We hypothesize that a larger receptive field will benefit the performance for objects of higher scale. Furthermore, EWFOs consist only of simple features. Hence we hypothesize that less filters are required to represent such an object and a thinner model can perform equally well than its wider counterpart. Finally, EWFOs are not very complex. Hence, we hypothesize that a shallower model should be able to learn the task equally well.

The anchor box concept introduces additional hyperparameters. By choosing the anchor box dimensions close to objects that appear in training/test set prior knowledge can be included. The better the anchor boxes fit the appearing object the less work has to be done by the network and hence performance can potentially be improved. Hence, we evaluate whether redesigned anchor boxes improve the network performance.

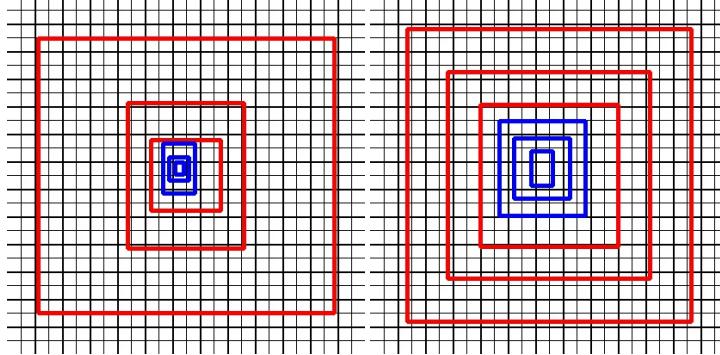


Figure 4.2: Visualization of the anchor parametrization. It can be seen the two output grids, where the grid for larger scale objects is drawn thicker. For both output grids the anchor at the center location is displayed. The anchor for smaller objects in blue, the anchors for larger objects in red. The left image shows the baseline *TinyYoloV3* anchors. The right image the anchors based on a k-means clustering of the training set.

4.2.1 Experiments

Initially an architecture evaluation is performed. Therefore different architectures are trained and evaluated in terms of **ap60!** (**ap60!**). As an architecture contains many parameters we can not simply vary each of them independently. Hence, three experiments are performed iteratively. We first describe them on a high level basis before explaining the exact changes. In a first step the width is decreased until a drop in performance is noticeable. In a second step the architecture with the lowest width but without performance drop is chosen and the depth is varied. Based on the results of this step we create a final model that combines the gained insights and tune the anchor boxes.

The scheme in which the architecture is changed is visualized in Figure 4.3. The width of the baseline model is decreased stepwise by a factor of two. When decreasing depth only convolutional layers are removed while the pooling layers are kept such that the spatial resolution stays the same. When increasing depth 2 layers are inserted stepwise at the end of both branches. The results show how depth is mainly relevant to detect objects of larger scale. Hence, the final model consist of 5 common layers, 15 layers on the branch to detect larger objects and 2 layers on the branch to detect small objects.

4.2.2 Results

Figure 4.4 shows the performance for thinner and wider networks. It is apparent how the performance only undergoes slight variations despite reducing the total number of weights by a factor 1000.

Figure 4.7 shows the distribution of object sizes in the bins used for evaluation. It can be seen that most objects in the test set are further away.

retrain one in the middle to get variance, it should be more linear

put some examples to show what each size actually means

4.2.3 Discussion

The overall performance is only slightly affected when reducing the number of weights in terms of width and height. We can assume that this is because the objects we investigate are of quite simple structure. Intuitively the features to be considered are color, lines and edges in certain combinations. Hence, it seems logical that only a few filters are necessary to represent these shapes.

The performance in terms of different object sizes varies significantly for models with varying depth. Only deeper networks are able to detect larger objects. However, the complexity of the object does not increase for closer objects. In contrary the closer the objects are, the less context is visible. A very close object consists "only" of an orange square. Hence, it is unlikely that increased flexibility is the reason for the increase in performance.

Instead it is more likely that the increased receptive field is the reason for the improved performance. In fact only the network with 14 layers has a receptive field of 414 and thus covers the whole image. Yet even this network cannot detect the largest objects. Thus the receptive field can not be the only reason for the lower performance on larger objects.

The current structure combines features distributed across space in a pyramid fashion. So 3-by-3 convolutions are performed layer by layer such until the whole image is covered. For EWFOs many of these steps are unnecessary as the objects are empty and the network should learn to ignore the empty part in the centre. It is possible that this structure gets confused by the parts that are present in the image centre.

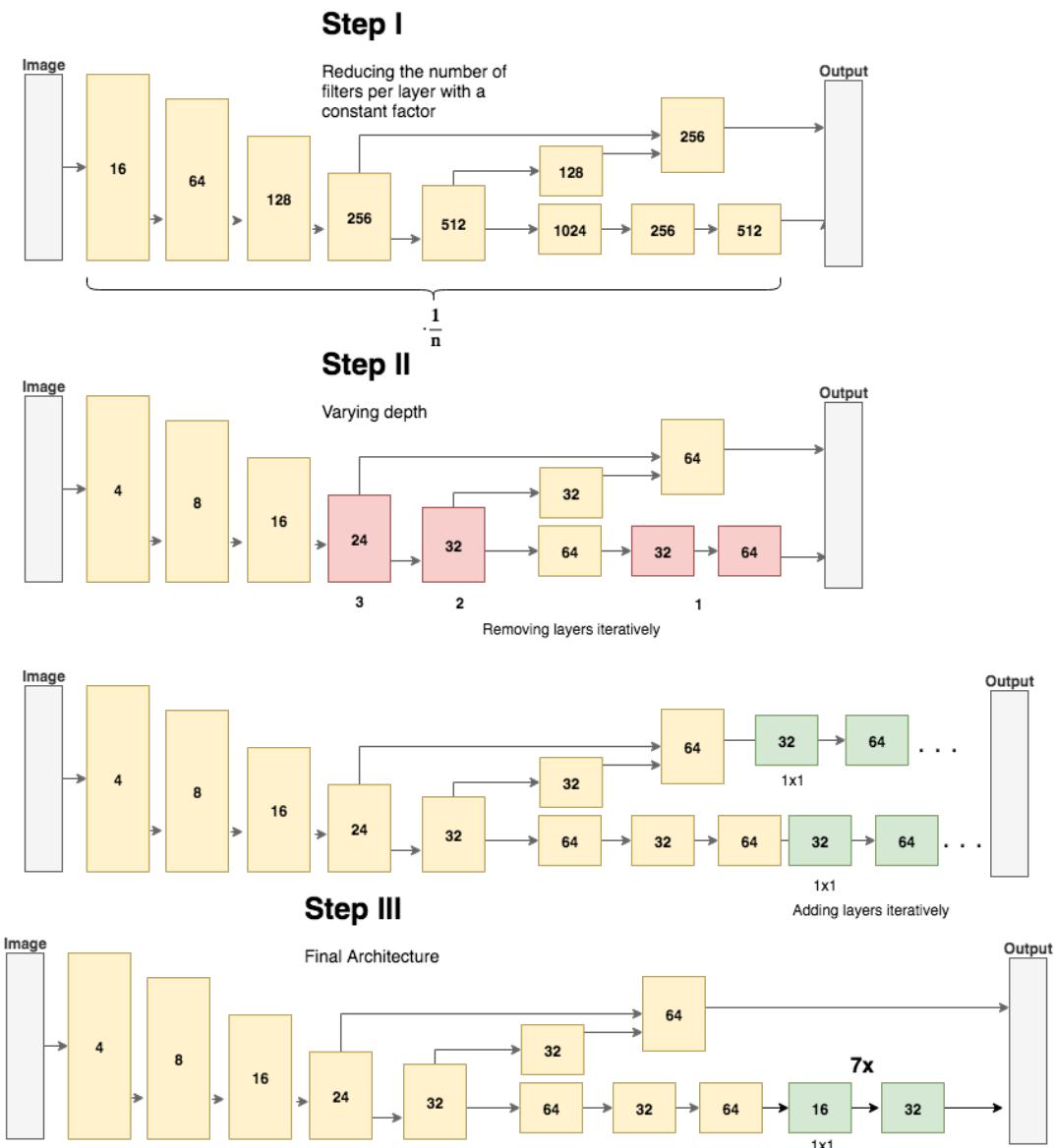


Figure 4.3: Architectural Changes when varying the depth. The upper graph shows in which order layers are removed. The lower graph shows how layers are added. Depth is increased by inserting two layers on each branch (green).

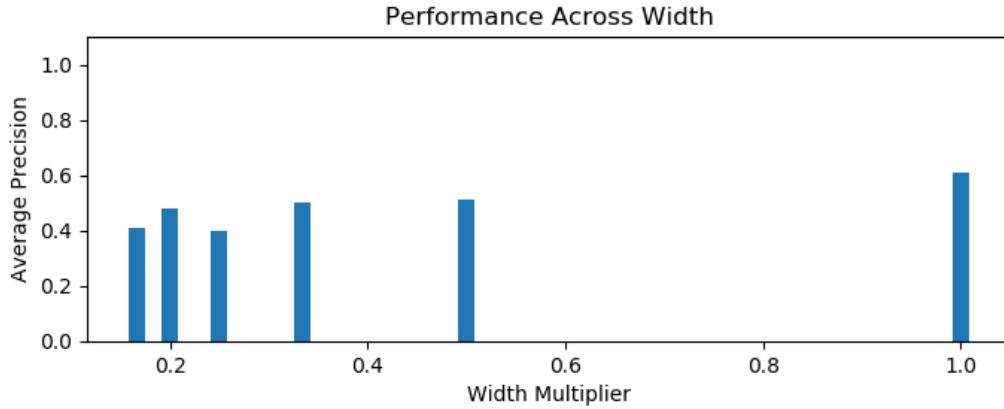


Figure 4.4: Performance in simulation when varying the amount of filters per layer. Starting from the baseline architecture with approximately 9 Mio. weights, the amount of filters per layer are decreased stepwise by a factor of 2. Only minor effects on performance can be seen, despite reducing the flexibility of the model.

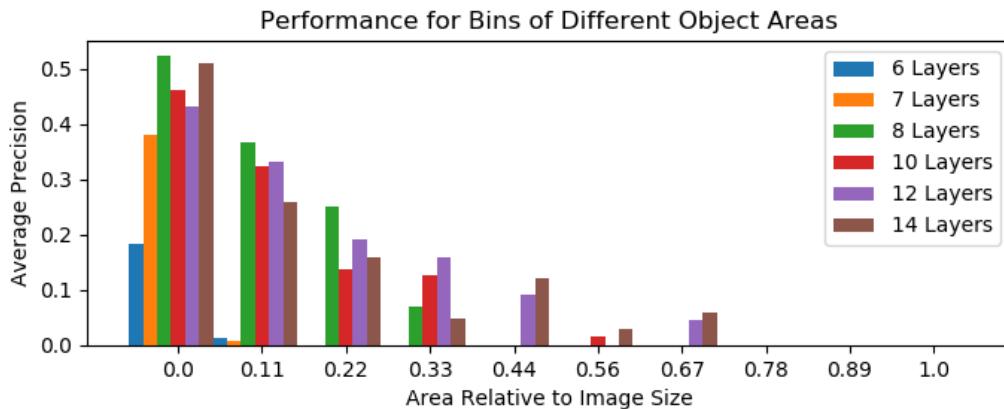


Figure 4.5: Performance in simulation of models with varying depth and for bins of different size. It can be seen that the performance for larger objects increases with the amount of layers.

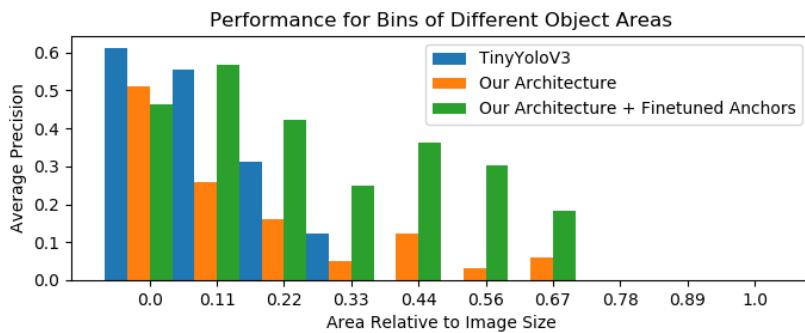


Figure 4.6: Architectural Changes when varying the depth. The upper graph shows in which order layers are removed. The lower graph shows how layers are added. Depth is increased by inserting two layers on each branch (green).

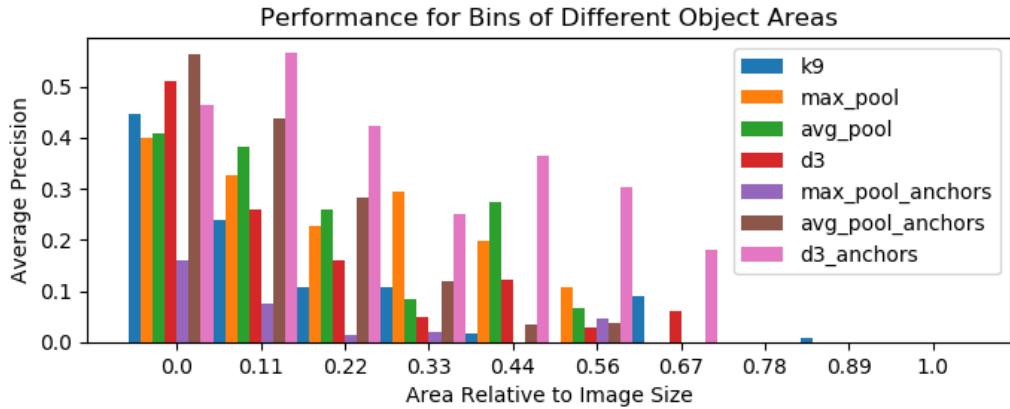


Figure 4.7: Label distribution in bins of different object size. As the field of view is larger for objects further away, the proportion of small objects is higher.

4.2.4 Conclusion

We investigated how width affects the performance for the detection of EWFOs. We hypothesized that due to the low variance in the investigated object and the simple features, less filters are required than in the baseline architecture. We can confirm this hypothesis as we see that the width can be decreased by a factor of 10 without loosing performance. This leads to a reduction of weights by a factor of 1000.

Furthermore, we investigated how depth affects the performance of the model. We hypothesized that a shallow network should be able to detect the object as it only consists of relatively simple features. We can see how depth is required in order to cover the whole input image. Hence, we cannot fully conclude whether depth is required for the increased flexibility or simply due to the receptive field.

4.3 Empty Objects

The experiments show how the performance of the network drops for larger objects while even a few layers are enough for small objects. This is the opposite as reported for example by . We hypothesize that this is due to the emptiness of EWFO. As the object gets larger, the features are spread further and further apart while more and more noise is present in the receptive field of the detector.

4.3.1 Experiment

A 7-by-7 max-pooling layer is inserted on the lower branch after layer 6. The model is compared to the architecture with 14 layers and a model where we replace the 3-by-3 kernel of layer 6 with a 9-by-9 kernel.

4.3.2 Results

4.4 Implementation on the MAV

Chapter 5

Discussion

In this work we investigated a learning based approach for the detection of EWFOs on MAVs. The research was motivated by several drawbacks of the manual crafted detection method: SnakeGate. The aim was to investigate whether a learning based Object Detector is more robust against, occlusion, out of view and changes in illumination. Our results show how the deep learning based detector outperforms SnakeGate especially in the cases of occlusion and out of view. The deep learning based detector can detect objects even when only 30% of the object is visible or when backlight leads to strong changes in colour appearance.

Yet the deep learning based detector introduces its own drawbacks. For example the bounding boxes are generally less accurate than of SnakeGate. We assume that the reason is the general structure of Yolo. CNNs collect "shallow" low level image features and combine them to a more deep representation of the image. Pooling layers reduce the spatial resolution to keep the number of computations tractable, however thereby also local information about the features gets lost. In the final layers information is present which features are present in that part of the image, however it is not clear where they come from. Future work should address how to reflect back from the deep representation to the low level features.

A main argument for deep learning detectors is the fact that they can be trained on any kind of object and thus make feature engineering unnecessary. Furthermore, the learned representation are often much better than the features crafted manually. A drawback is the computational requirements of CNNs. For this work no training data was available and the computational requirements were limited. By implementing a data generation pipeline and refining the architecture we could show how the deep learning based method outperforms the manually crafted one. However, this process was a vast amount of work and yet we have a severe drop in performance between the simulated and the real data. Hence, we have to wonder whether it would have not been more fruitful to invest time in feature engineering based on real data. It is questionable whether this is method would still perform better than the deep learning method. And yes for a new object it would required to be changed. But it would lead to a more transparent detector.

deep detector can be better extended but we loose track of whats going on, deep learning makes sense with the appropriate hardware and the appropriate data

Chapter 6

Conclusion

Appendix A

Appendix

A.1 Data Generation

This section describes how the ground truth labels are obtained when generating data.

A.1.1 Camera Model

The camera itself is modelled with the pinhole camera model that contains six parameters:

1. Focal length f_x, f_y
2. Central point c_x, c_y
3. Sensor skew s_x, s_y

The model can be summarized in the intrinsic camera matrix C :

$$C = \begin{bmatrix} \frac{f_x}{s_x} & 0 & c_x \\ 0 & \frac{f_y}{s_y} & c_y \\ 0 & 0 & 1 \end{bmatrix} \quad (\text{A.1})$$

The model projects 3D coordinates X to the image plane following:

$$X' = CX \quad (\text{A.2})$$

Where X are points described in homogeneous coordinates originating from the cameras position.

For data generation several tools are used. 3D Models for the Target Object (TO) are taken from ... OpenGL is used to render these objects and replace the background with a particular image. The Unreal Engine and AirSim are used to render a full scene.

Within the graphic engines, the objects can be placed in 3D space. From the known object shape the surrounding bounding box can be defined in 3D coordinates. Using the pinhole camera model described in Equation (A.1) the corresponding 2D coordinates on the image plane can be obtained with the following:

The camera position is described by its rotation matrix R and its translation vector t . Where R is obtained from the Euler angles with:

$$R =$$

The 3D coordinates of the objects relative to the camera can be obtained by applying the inverse transformation T of R and t with:

$$t' = R \times t$$

$$T = R^{-1} | - t'$$

$$X_{Cam} = T \times X$$

The full projection can then be expressed by the matrix multiplication:

$$X' = C \times T \times X$$

Where C is the intrinsic camera matrix defined in Equation (A.1).

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