Week 6 - Data Science II

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01/02/2022

Today: Cross validation and resampling methods.

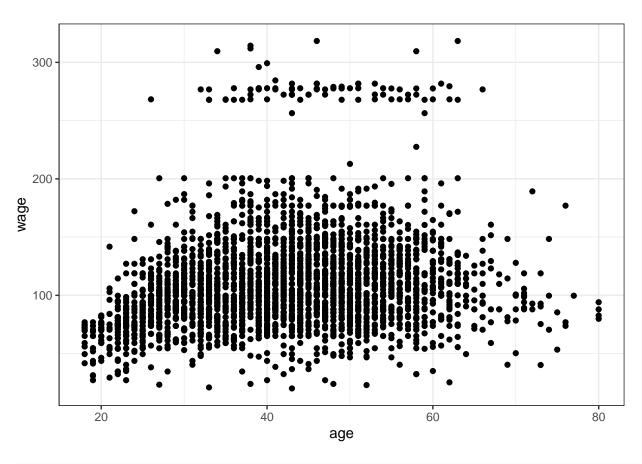
Loading required package: lattice

Note: The standard training data to testing data ratio is 70% to 30%. Note: The central limit theorem states that the average of averages in a data set tends to be normally distributed.

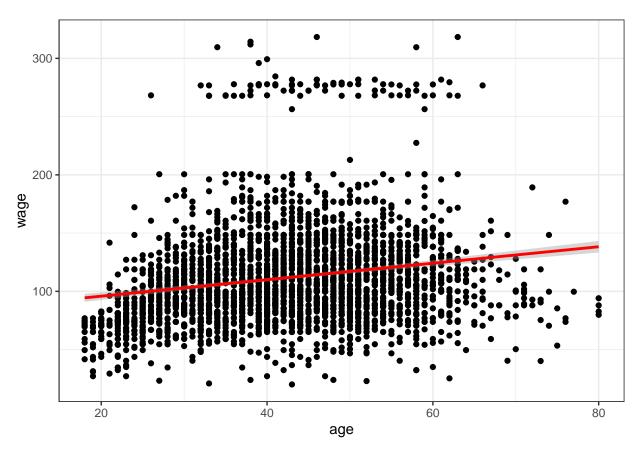
```
# Applied Data Science II - Week 6
# Today we are going to talk about SPLINES and GAMS!
#
# # -----
# Load your libraries!
# # -----
library(ISLR2)
library(tidyverse)
## -- Attaching packages ------ tidyverse 1.3.1 --
## v ggplot2 3.3.5 v purrr 0.3.4
## v tibble 3.1.6 v dplyr 1.0.7
## v tidyr 1.1.4
                v stringr 1.4.0
## v readr
         2.1.1
                 v forcats 0.5.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
library(caret)
```

```
##
## Attaching package: 'caret'
## The following object is masked from 'package:purrr':
##
##
       lift
library(splines)
library(npreg)
library(mgcv)
## Loading required package: nlme
##
## Attaching package: 'nlme'
## The following object is masked from 'package:dplyr':
##
##
       collapse
## This is mgcv 1.8-38. For overview type 'help("mgcv-package")'.
library(PerformanceAnalytics)
## Loading required package: xts
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##
       as.Date, as.Date.numeric
##
## Attaching package: 'xts'
## The following objects are masked from 'package:dplyr':
##
##
       first, last
##
## Attaching package: 'PerformanceAnalytics'
```

```
## The following object is masked from 'package:graphics':
##
##
       legend
# # -----
# Splines!
# Let's start by checking out the Wage dataset. It's not very fancy, but it's useful for teach
# This dataset is just wages and other data for a group of 3000 male workers in the Mid-Atlant
attach(Wage)
head(Wage)
##
          year age
                             maritl
                                        race
                                                    education
                                                                           region
## 231655 2006 18 1. Never Married 1. White
                                                 1. < HS Grad 2. Middle Atlantic
## 86582 2004 24 1. Never Married 1. White 4. College Grad 2. Middle Atlantic
## 161300 2003 45
                       2. Married 1. White 3. Some College 2. Middle Atlantic
                         2. Married 3. Asian 4. College Grad 2. Middle Atlantic
## 155159 2003 43
                50
## 11443 2005
                        4. Divorced 1. White
                                                   2. HS Grad 2. Middle Atlantic
## 376662 2008 54
                       2. Married 1. White 4. College Grad 2. Middle Atlantic
                                 health health_ins logwage
##
                jobclass
## 231655 1. Industrial
                                              2. No 4.318063 75.04315
                               1. <=Good
                                             2. No 4.255273 70.47602
## 86582 2. Information 2. >=Very Good
## 161300 1. Industrial 1. <=Good 1. Yes 4.875061 130.98218
## 155159 2. Information 2. >=Very Good 1. Yes 5.041393 154.68529
## 11443 2. Information 1. <=Good 1. Yes 4.318063 75.04315
## 376662 2. Information 2. >=Very Good 1. Yes 4.845098 127.11574
# Let's take a look at a plot between wages and age...
Wage %>%
        ggplot(aes(x = age, y = wage)) +
        geom_point() +
        theme_bw()
```



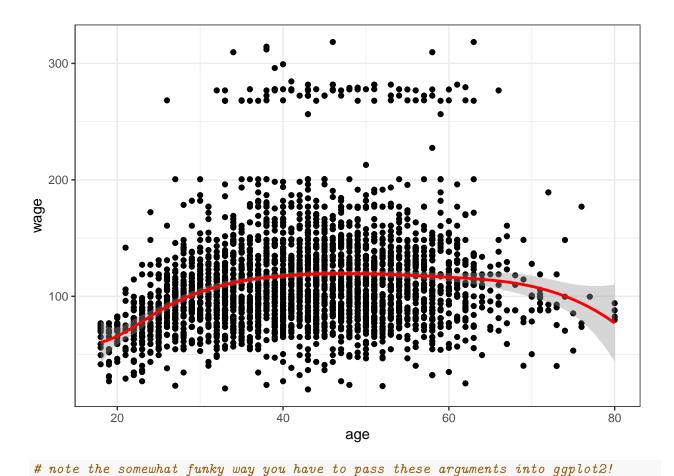
'geom_smooth()' using formula 'y ~ x'



We can also just run the math and see that the fit probably won't be great:
summary(lm(wage ~ age, data = Wage))

```
##
## Call:
## lm(formula = wage ~ age, data = Wage)
##
## Residuals:
##
       Min
                 1Q
                      Median
                                   3Q
                                           Max
## -100.265 -25.115
                     -6.063
                              16.601 205.748
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 81.70474
                          2.84624
                                    28.71
                                            <2e-16 ***
                                    10.92
## age
               0.70728
                          0.06475
                                            <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 40.93 on 2998 degrees of freedom
## Multiple R-squared: 0.03827, Adjusted R-squared: 0.03795
## F-statistic: 119.3 on 1 and 2998 DF, p-value: < 2.2e-16
```

```
# Yep, not super great.
# So since we suspect some nonlinearity here, we can use a spline!
# To use a spline is straightforward - you can call the bs() function (from the spline library
# and this lets you manually add in "knots" to your spline regression!
spline_regression <- lm(wage \sim bs(age, knots = c(25, 40, 60)), data = Wage)
# the bs() function changes everything, it stands for B-spline analysis
# the knots parameter is the position of the knots we would like to see
# for information on the relationship between the number of knots and the degrees of freedom,
# and, as we can see - the fit is better!
summary(spline_regression)
##
## Call:
## lm(formula = wage ~ bs(age, knots = c(25, 40, 60)), data = Wage)
##
## Residuals:
##
       Min
                10 Median
                                3Q
                                       Max
## -98.832 -24.537 -5.049 15.209 203.207
##
## Coefficients:
##
                                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                     60.494
                                                 9.460
                                                         6.394 1.86e-10 ***
## bs(age, knots = c(25, 40, 60))1
                                      3.980
                                                12.538
                                                         0.317 0.750899
## bs(age, knots = c(25, 40, 60))2
                                                 9.626 4.636 3.70e-06 ***
                                     44.631
## bs(age, knots = c(25, 40, 60))3
                                     62.839
                                                10.755 5.843 5.69e-09 ***
## bs(age, knots = c(25, 40, 60))4
                                     55.991
                                                10.706
                                                         5.230 1.81e-07 ***
## bs(age, knots = c(25, 40, 60))5
                                     50.688
                                                14.402
                                                         3.520 0.000439 ***
## bs(age, knots = c(25, 40, 60))6
                                     16.606
                                                19.126
                                                       0.868 0.385338
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 39.92 on 2993 degrees of freedom
## Multiple R-squared: 0.08642,
                                    Adjusted R-squared: 0.08459
## F-statistic: 47.19 on 6 and 2993 DF, p-value: < 2.2e-16
# we can also visualize it!
Wage %>%
        ggplot(aes(x = age, y = wage)) +
        geom_point() +
        theme_bw() +
        geom_smooth(method = "lm", color = "red",
                    formula = y ~ bs(x, knots = c(25, 40, 60)))
```



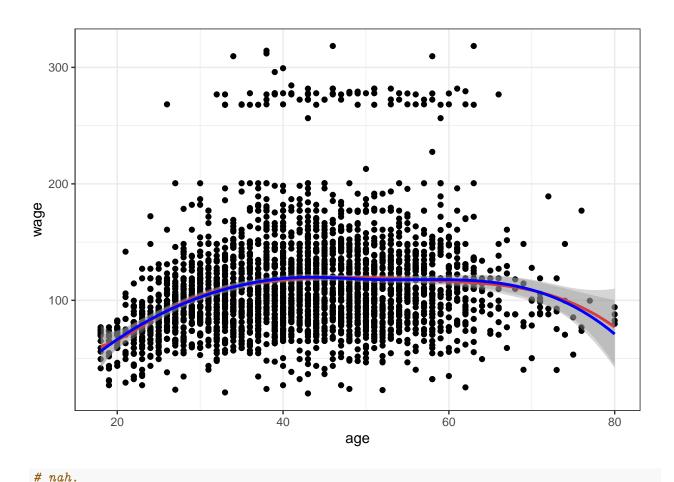
now, in the above, we SPECIFIED where to put the knots. We can achieve a similar result # by letting R choose for us! # Let's show that these produce a vector with the same dimensions... $\dim(bs(age, knots = c(25, 40, 60)))$

```
## [1] 3000 6
dim(bs(age, df = 6))
```

[1] 3000 6

```
# why 6?
# This df command produces a spline with six basis functions.
# This is because the bs() function naturally produces a a cubic spline which, when it has
# three knots, has seven degrees of freedom; six basis functions + one intercept.
# HOWEVER MANY KNOTS YOU WOULD LIKE IS: 2*knots = number of degrees of freedom.
attr(bs(age, df = 6), "knots")
```

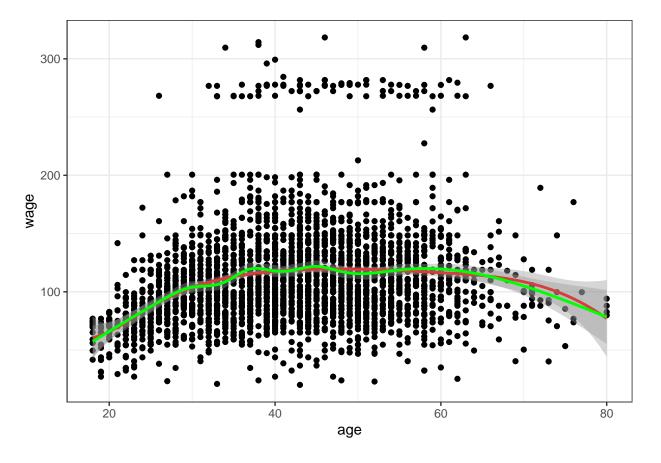
```
25%
          50%
##
                75%
## 33.75 42.00 51.00
# If we just let R choose...
summary(lm(wage ~ bs(age, df = 6), data = Wage))
##
## Call:
## lm(formula = wage ~ bs(age, df = 6), data = Wage)
## Residuals:
      Min
               1Q Median
                               3Q
## -99.681 -24.403 -5.202 15.441 201.413
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     56.314
                                 7.258
                                         7.759 1.17e-14 ***
## bs(age, df = 6)1
                     27.824
                                12.435
                                         2.238
                                                 0.0253 *
## bs(age, df = 6)2
                     54.063
                                 7.127
                                         7.585 4.41e-14 ***
                                 8.323 7.909 3.62e-15 ***
## bs(age, df = 6)3
                     65.828
## bs(age, df = 6)4
                     55.813
                                 8.724
                                         6.398 1.83e-10 ***
## bs(age, df = 6)5
                     72.131
                                13.745 5.248 1.65e-07 ***
## bs(age, df = 6)6
                     14.751
                                16.209
                                         0.910 0.3629
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 39.91 on 2993 degrees of freedom
## Multiple R-squared: 0.08729, Adjusted R-squared: 0.08546
## F-statistic: 47.71 on 6 and 2993 DF, p-value: < 2.2e-16
# slightly better! does it look all that different?
Wage %>%
       ggplot(aes(x = age, y = wage)) +
       geom_point() +
       theme_bw() +
       geom_smooth(method = "lm", color = "red",
                   formula = y \sim bs(x, knots = c(25, 40, 60))) +
       geom_smooth(method = lm, color = "blue",
                   formula = y \sim bs(x, df = 6))
```



Want to fit a spline of ANY degree (and not just a cubic one?) Use the NS function! This use

```
# "natural" splines which are even more flexible:
summary(lm(wage ~ ns(age, df = 12), data = Wage))
##
## Call:
## lm(formula = wage ~ ns(age, df = 12), data = Wage)
##
## Residuals:
                1Q Median
                                3Q
##
       Min
## -99.668 -24.334 -5.014 15.246 201.186
##
## Coefficients:
                      Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                        57.384
                                     6.921
                                             8.292 < 2e-16 ***
                                             6.930 5.12e-12 ***
## ns(age, df = 12)1
                                    7.188
                        49.813
## ns(age, df = 12)2
                        45.386
                                    9.318
                                             4.871 1.17e-06 ***
## ns(age, df = 12)3
                        66.918
                                    8.595
                                             7.785 9.52e-15 ***
## ns(age, df = 12)4
                        59.476
                                    8.747
                                             6.799 1.26e-11 ***
## ns(age, df = 12)5
                        60.372
                                    8.646
                                             6.983 3.55e-12 ***
```

```
## ns(age, df = 12)6
                       67.180
                                   9.009
                                           7.457 1.15e-13 ***
## ns(age, df = 12)7
                       58.753
                                   8.696
                                           6.756 1.69e-11 ***
## ns(age, df = 12)8
                                           6.765 1.60e-11 ***
                       57.421
                                   8.488
## ns(age, df = 12)9
                       61.185
                                   7.942
                                           7.704 1.78e-14 ***
## ns(age, df = 12)10
                                           7.020 2.73e-12 ***
                       55.098
                                   7.848
## ns(age, df = 12)11
                       67.378
                                  17.242
                                           3.908 9.52e-05 ***
## ns(age, df = 12)12
                        7.282
                                  12.226
                                           0.596
                                                    0.551
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 39.89 on 2987 degrees of freedom
## Multiple R-squared: 0.08973, Adjusted R-squared: 0.08607
## F-statistic: 24.54 on 12 and 2987 DF, p-value: < 2.2e-16
```



```
# But why have any silly constraints at all! Let's just use a SMOOTHING spline.
# Note: your textbook uses the smooth.spline function. We're going to use a different one
# from the npreg library as it gives you way more flexibility.
smooooooooth <- npreg::ss(age, wage, nknots = 16)</pre>
smooooooooth
##
## Call:
## npreg::ss(x = age, y = wage, nknots = 16)
## Smoothing Parameter spar = 0.3135218
                                           lambda = 1.097456e-05
## Equivalent Degrees of Freedom (Df) 6.441072
## Penalized Criterion (RSS) 4762520
## Generalized Cross-Validation (GCV) 1594.345
summary(smoooooooooth)
##
## Call:
## npreg::ss(x = age, y = wage, nknots = 16)
## Residuals:
##
      Min
                1Q Median
                                30
                                       Max
## -99.540 -24.432 -5.069 15.219 202.353
##
## Approx. Signif. of Parametric Effects:
               Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 106.21
                             1.446 73.424 0.00000 ***
                  27.01
                            12.026
                                     2.246 0.02478
## x
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Approx. Signif. of Nonparametric Effects:
##
                   Df Sum Sq Mean Sq F value Pr(>F)
                                        35.48
## s(x)
                4.441 250650
                                56439
```

Adjusted R-squared: 0.08635

1591

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

Residual standard error: 39.89 on 2994 degrees of freedom

F-statistic: 52.05 on 5.441 and 2994 DF, p-value: <2e-16

Residuals 2993.559 4762520

Multiple R-squared: 0.08804,

smooooooooth\$fit\$knot

```
[1] 18 22 26 30 34 38 42 46 50 54 58 62 66 70 74 80
# and, lastly, let's let the ss function actually choose the number of knots for us
# through cross-validation!
final_smooth <- npreg::ss(age, wage)</pre>
final smooth
##
## Call:
## npreg::ss(x = age, y = wage)
## Smoothing Parameter spar = 0.3169286
                                         lambda = 1.161449e-05
## Equivalent Degrees of Freedom (Df) 6.468966
## Penalized Criterion (RSS) 4762594
## Generalized Cross-Validation (GCV) 1594.4
summary(final_smooth)
##
## Call:
## npreg::ss(x = age, y = wage)
## Residuals:
     Min
             1Q Median
                            30
## -99.57 -24.43 -5.07 15.22 202.42
##
## Approx. Signif. of Parametric Effects:
              Estimate Std. Error t value Pr(>|t|)
                106.23
                            1.444 73.555 0.0000 ***
## (Intercept)
## x
                 27.09
                           11.920 2.273 0.0231
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Approx. Signif. of Nonparametric Effects:
##
                  Df Sum Sq Mean Sq F value Pr(>F)
                4.469 250220
## s(x)
                              55991
                                       35.19
                                                  0 ***
## Residuals 2993.531 4762594
                                1591
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 39.89 on 2994 degrees of freedom
```

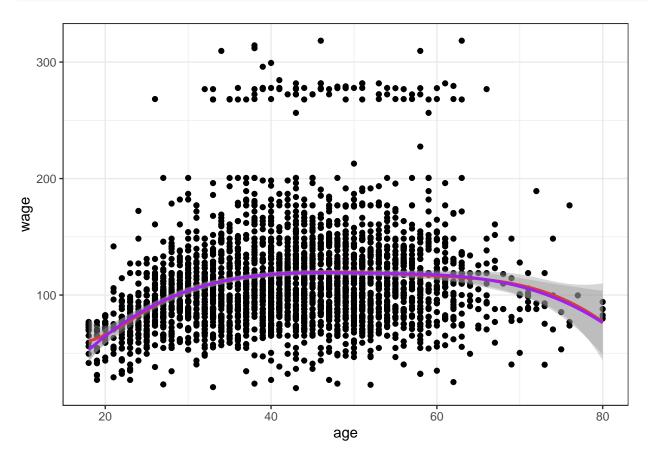
Multiple R-squared: 0.08803, Adjusted R-squared: 0.08632 ## F-statistic: 51.73 on 5.469 and 2994 DF, p-value: <2e-16

final_smooth\$fit\$knot

```
## [1] 18 19 20 21 22 23 25 26 27 28 29 30 32 33 34 35 36 38 39 40 41 42 43 45 46 ## [26] 47 48 49 50 52 53 54 55 56 58 59 60 61 62 63 65 66 67 68 69 70 72 73 74 75 ## [51] 76 80
```

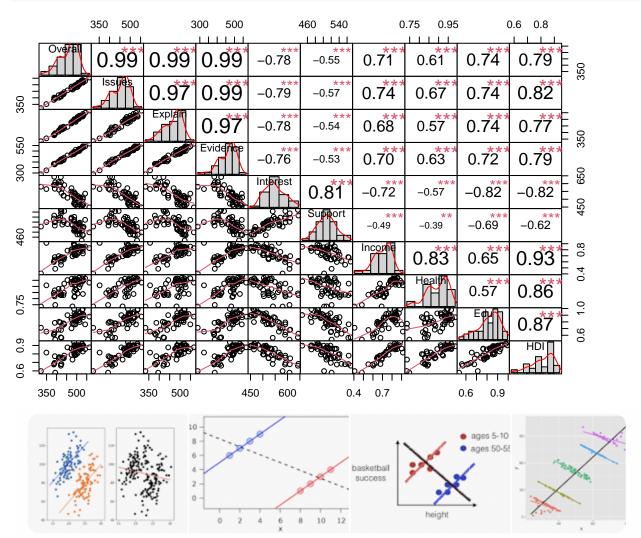
length(final_smooth\$fi\$knot)

[1] 52



```
# # -----
# Stop! Back to the lecture!
# Let's TALK ABOUT THEM GAMS
# Go ahead and download the dataset called "pisa_data.csv" from the Google Drive.
pisa_data <- read_csv("w6 data//pisa_data.csv")</pre>
## Rows: 65 Columns: 11
## -- Column specification --------
## Delimiter: ","
## chr (1): Country
## dbl (10): Overall, Issues, Explain, Evidence, Interest, Support, Income, Hea...
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
head(pisa_data)
## # A tibble: 6 x 11
    Country Overall Issues Explain Evidence Interest Support Income Health
    <chr>
               <dbl> <dbl>
                             <dbl>
                                     <dbl>
                                              <dbl>
                                                     <dbl> <dbl> <dbl> <dbl> <dbl>
## 1 Albania
                                                        NA 0.599 0.886 0.716
                 NA
                        NA
                               NA
                                        NA
                                                NA
## 2 Argenti~
                391
                       395
                               386
                                       385
                                               567
                                                       506 0.678 0.868 0.786
                       535
                              520
                                       531
                                                       487 0.826 0.965 0.978
## 3 Austral~
               527
                                               465
                       505
                                       505
                                                       515 0.835 0.944 0.824
## 4 Austria
                511
                               516
                                               507
## 5 Azerbai~
                382
                       353
                               412
                                       344
                                                612
                                                       542 0.566 0.78 NA
                                                       492 0.831 0.935 0.868
## 6 Belgium
                510
                       515
                               503
                                       516
                                                503
## # ... with 1 more variable: HDI <dbl>
# This is a nifty little dataset we've put together for you based on education.
# The data set has been constructed using average Science scores by country from
# the Programme for International Student Assessment (PISA) 2006, along with GNI per capita,
# Educational Index, Health Index, and Human Development Index from UN data.
# Drop nulls!
pisa_data <- pisa_data %>%
```

```
na.omit()
# Let's peek at the data with the chart.Correlation function
chart.Correlation(pisa_data[,2:11], histogram = TRUE, method = "pearson")
```



Simpson's paradox, also called Yule-Simpson effect, in statistics, an effect that occurs when the marginal association between two categorical variables is qualitatively different from the partial association between the same two variables after controlling for one or more other variables.

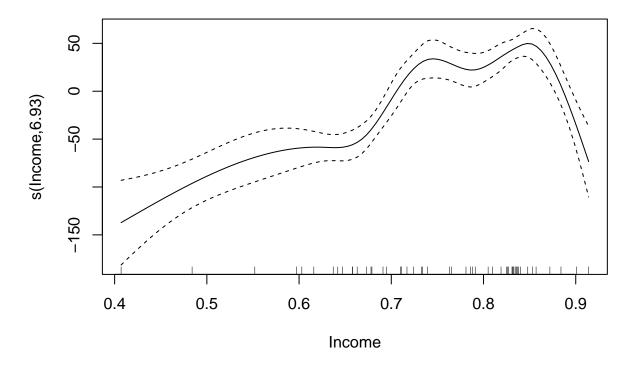
```
# okay, let's start simple and fit a linear model *first*. we're going to use the
# mgcv library to use the gam() function and not pass anything fancy in. Note that there are
# LOTS of libraries that use GAMs, so it's probably good to specifcy WHICH library you want to
# with ::
# Let's try predicting the overal score based solely on income.
```

```
pisa_lm_simple <- mgcv::gam(Overall ~ Income, data = pisa_data)</pre>
summary(pisa_lm_simple)
##
## Family: gaussian
## Link function: identity
##
## Formula:
## Overall ~ Income
## Parametric coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 206.36
                             37.89
                                    5.447 1.56e-06 ***
                 354.18
                             50.17
                                     7.060 4.84e-09 ***
## Income
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
##
## R-sq.(adj) = 0.489 Deviance explained = 49.9\%
## GCV = 1548.4 Scale est. = 1488.9
                                        n = 52
# okay, not terribly bad. The overal adjusted R2 isn't too shabby. Now let's try fitting
# a very straightforward GAM that takes advantage of splines.
pisa_gam_simple <- gam(Overall ~ s(Income, bs="cr"), data = pisa_data)</pre>
# Note: We again use the gam function as before for basic model fitting, but now we are using
# the s function within the formula to denote the smoothing spline terms. Within that function
# also specify the type of smooth, though a default is available. I chose bs = cr, denoting cu
# regression splines (how we started above!)
summary(pisa_gam_simple)
##
## Family: gaussian
## Link function: identity
##
## Formula:
## Overall ~ s(Income, bs = "cr")
##
## Parametric coefficients:
               Estimate Std. Error t value Pr(>|t|)
##
                             3.386
                                     139.1
                                             <2e-16 ***
## (Intercept) 471.154
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```

##

```
## Approximate significance of smooth terms:
## edf Ref.df F p-value
## s(Income) 6.935 7.787 25.77 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## R-sq.(adj) = 0.795 Deviance explained = 82.3%
## GCV = 703.74 Scale est. = 596.36 n = 52</pre>
```

plot(pisa_gam_simple)



```
# looks better! Now let's try multiple predictors - and this time, let's use a test and train
# approach to get a better idea of overall model performance.

# start linear...

set.seed(12345)
index <- createDataPartition(pisa_data$Overall, p = .8, list=FALSE)
training_data <- pisa_data[ index,]
test_data <- pisa_data[-index,]

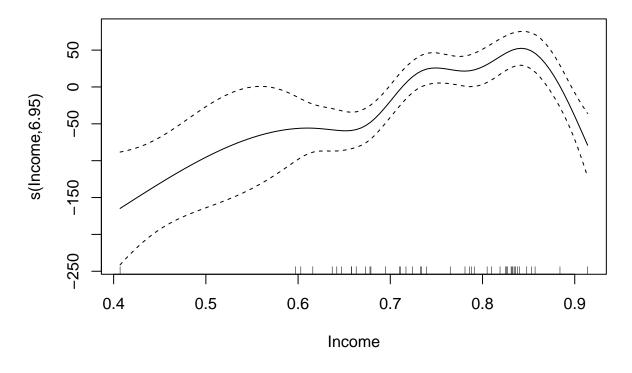
pisa_lm_multivariate <- mgcv::gam(Overall ~ Income + Edu + Health, data = training_data)
summary(pisa_lm_multivariate)</pre>
```

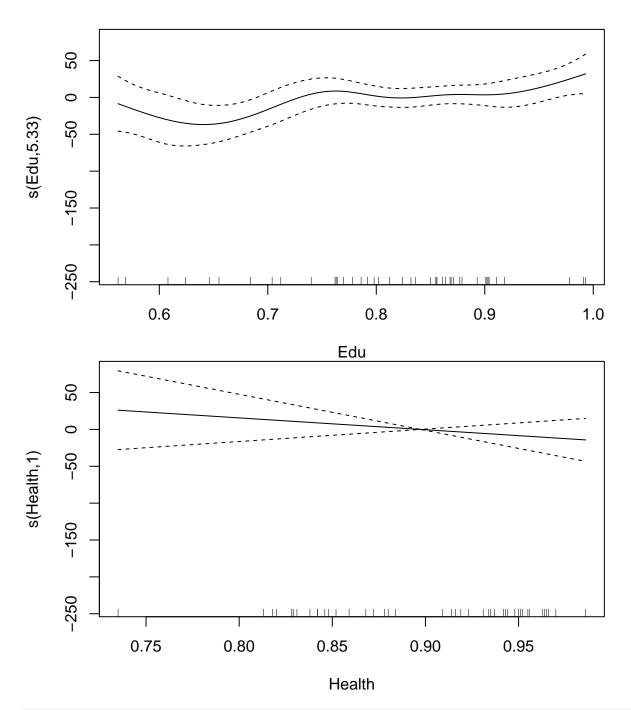
```
##
## Family: gaussian
## Link function: identity
```

```
##
## Formula:
## Overall ~ Income + Edu + Health
## Parametric coefficients:
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 48.97
                          100.46 0.488 0.62856
                          108.03 1.802 0.07909 .
## Income
                194.66
## Edu
                248.07
                           61.49 4.034 0.00024 ***
## Health
                 83.30
                           174.83 0.476 0.63632
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## R-sq.(adj) = 0.614 Deviance explained = 64.1%
## GCV = 1326.3 Scale est. = 1205.8 n = 44
# ...get rmse!
predictions_lm <- predict(pisa_lm_multivariate, test_data)</pre>
RMSE(predictions_lm, test_data$0verall)
## [1] 30.24088
# now let's go full GAMMMMMSSSSS
pisa_gam_multivariate <- gam(Overall ~ s(Income) + s(Edu) + s(Health), data = training_data)</pre>
summary(pisa_gam_multivariate)
##
## Family: gaussian
## Link function: identity
##
## Formula:
## Overall ~ s(Income) + s(Edu) + s(Health)
##
## Parametric coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 470.318
                            3.048
                                    154.3 <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Approximate significance of smooth terms:
              edf Ref.df
                             F p-value
## s(Income) 6.948 7.904 8.025 1.03e-05 ***
## s(Edu)
           5.334 6.305 2.219 0.0623 .
## s(Health) 1.000 1.000 0.953
```

[1] 25.23021

want to see how each of these effects is being modeled? use plot!
plot(pisa_gam_multivariate)





if you want it to be prettier, check out the visreg package!

```
# # -----
#
# Data Project Time!
#
# # ------
# Go into the Drive and open the file "walmart.csv".
# this is some data related to weekly store sales at a bunch of different walmart stores
```

```
# around the country. Your job is to use all the tools at your disposal (linear models,
# lasso models, ridge models, or GAMS) to try and have the BEST fitting model possible as base
# minimizing RMSE.
# You are trying to predict the weekly_sales based on the data available to you.
# good luck!
walmart <- read_csv("w6 data/walmart.csv")</pre>
## Rows: 6435 Columns: 8
## -- Column specification -----
## Delimiter: ","
## chr (1): date
## dbl (7): store, weekly_sales, holiday_flag, temperature, fuel_price, cpi, un...
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
head(walmart)
## # A tibble: 6 x 8
    store date
                      weekly_sales holiday_flag temperature fuel_price
     <dbl> <chr>
                             <dbl>
                                          <dbl>
                                                      <dbl>
                                                                 <dbl> <dbl>
##
## 1
        1 05-02-2010
                          1643691.
                                                       42.3
                                                                  2.57 211.
                                              0
## 2
        1 12-02-2010
                                                       38.5
                                                                  2.55 211.
                          1641957.
                                              1
## 3
       1 19-02-2010
                         1611968.
                                              0
                                                       39.9
                                                                  2.51 211.
## 4
       1 26-02-2010
                        1409728.
                                              0
                                                       46.6
                                                                  2.56 211.
## 5
       1 05-03-2010
                         1554807.
                                              0
                                                       46.5
                                                                  2.62 211.
## 6
        1 12-03-2010
                         1439542.
                                                       57.8
                                                                  2.67 211.
## # ... with 1 more variable: unemployment <dbl>
walmart_cleaned <- walmart %>%
        mutate(store = as.factor(store),
               holiday_flag = as.factor(holiday_flag),
               year = as.factor(lubridate::year(lubridate::dmy(date))),
               month = as.factor(lubridate::month(date))) %>%
        select(-c(date))
set.seed(12345)
index <- createDataPartition(walmart_cleaned$weekly_sales, p = .8, list=FALSE)
training_data <- walmart_cleaned[ index,]</pre>
test_data <- walmart_cleaned[-index,]</pre>
walmart_model <- gam(weekly_sales ~ store + holiday_flag +</pre>
                                     s(temperature) +
                                     s(fuel_price) + s(cpi) + s(unemployment) +
```

```
summary(walmart_model)
##
## Family: gaussian
## Link function: identity
##
## Formula:
  weekly_sales ~ store + holiday_flag + s(temperature) + s(fuel_price) +
       s(cpi) + s(unemployment) + year + month
##
##
## Parametric coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  1454624
                              257049
                                        5.659 1.61e-08 ***
## store2
                   376933
                               18781 20.070 < 2e-16 ***
## store3
                 -1193481
                               21059 -56.674 < 2e-16 ***
## store4
                                       1.220 0.222418
                   668728
                              548014
## store5
                               21643 -60.200 < 2e-16 ***
                 -1302932
## store6
                               20884 -2.662 0.007791 **
                   -55595
## store7
                  -723136
                               80315
                                      -9.004 < 2e-16 ***
## store8
                  -733813
                               23966 -30.619 < 2e-16 ***
## store9
                 -1101456
                               24143 -45.622 < 2e-16 ***
## store10
                   518738
                              547790
                                       0.947 0.343702
                               21201 -11.132 < 2e-16 ***
## store11
                  -236011
                              552588 -0.530 0.595852
## store12
                  -293097
                              547736
                                       1.122 0.262107
## store13
                   614313
## store14
                   765706
                              103027
                                       7.432 1.25e-13 ***
## store15
                  -847598
                              526213 -1.611 0.107296
## store16
                               80278 -10.316 < 2e-16 ***
                  -828160
                              547380 -0.928 0.353613
## store17
                  -507798
## store18
                  -374261
                              526884 -0.710 0.477533
## store19
                   -42418
                              526098 -0.081 0.935741
## store20
                   578201
                               27630 20.926 < 2e-16 ***
## store21
                  -804433
                               18745 -42.914 < 2e-16 ***
                              513460 -0.916 0.359463
## store22
                  -470571
## store23
                  -218273
                              525356 -0.415 0.677811
## store24
                  -118722
                              526448
                                      -0.226 0.821587
## store25
                  -822434
                               27997 -29.376 < 2e-16 ***
## store26
                              526290 -0.884 0.376873
                  -465109
## store27
                   274482
                              513129
                                       0.535 0.592730
                                       0.030 0.976006
## store28
                    16625
                              552728
## store29
                              527766 -1.752 0.079831 .
                  -924656
## store30
                 -1116328
                               18912 -59.028 < 2e-16 ***
## store31
                               18942
                                      -9.221 < 2e-16 ***
                  -174666
                               80188 -1.621 0.105048
## store32
                  -129996
## store33
                 -1105113
                              547800
                                      -2.017 0.043710 *
```

year + month, data = training_data)

549730 -0.674 0.500342

store34

-370518

```
## store35
                  -580067
                              513736 -1.129 0.258903
## store36
                 -1181026
                               19108 -61.810 < 2e-16 ***
## store37
                 -1034095
                               19068 -54.230 < 2e-16 ***
## store38
                              552602 -1.672 0.094545 .
                  -924065
                               19261 -4.889 1.05e-06 ***
## store39
                   -94166
## store40
                              525420 -1.235 0.216789
                  -649033
## store41
                   -82595
                               79726 -1.036 0.300255
## store42
                  -809127
                              547749 -1.477 0.139688
## store43
                               35975 -23.903 < 2e-16 ***
                  -859916
## store44
                 -1105192
                              547493 -2.019 0.043577 *
## store45
                              103073 -4.620 3.93e-06 ***
                  -476212
## holiday_flag1
                                8519
                                       3.081 0.002075 **
                    26246
## year2011
                               22025 -4.304 1.71e-05 ***
                   -94787
## year2012
                               35978 -3.748 0.000180 ***
                  -134851
## month2
                   118182
                               11837
                                       9.984 < 2e-16 ***
## month3
                    66011
                               13993
                                       4.717 2.45e-06 ***
## month4
                    67517
                               16244
                                       4.156 3.29e-05 ***
## month5
                    66405
                               18460
                                       3.597 0.000325 ***
                                       5.364 8.50e-08 ***
## month6
                               19786
                   106135
## month7
                    76267
                               21366
                                       3.570 0.000361 ***
## month8
                    87531
                               21520
                                       4.067 4.83e-05 ***
## month9
                    19603
                               20214
                                       0.970 0.332215
## month10
                    20247
                               18508
                                       1.094 0.274034
## month11
                               18928
                                       8.249 < 2e-16 ***
                   156146
## month12
                   307268
                               18794 16.349 < 2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Approximate significance of smooth terms:
                     edf Ref.df
                                    F p-value
## s(temperature)
                   2.838 3.614 5.863 0.000261 ***
## s(fuel_price)
                   4.486 5.631 5.376 3.34e-05 ***
## s(cpi)
                   7.496 8.250 4.836 2.91e-06 ***
## s(unemployment) 4.726 5.921 7.004 8.81e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## R-sq.(adj) = 0.939
                         Deviance explained =
## GCV = 1.998e+10 Scale est. = 1.9676e+10 n = 5151
predictions_gam <- predict(walmart_model, test_data)</pre>
RMSE(predictions_gam, test_data$weekly_sales)
```

[1] 138804.5