# Stats C183-Project6

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Spring 2022

#### PART A Downloading the training data

```
train <- read.csv("stockDataTrain.csv", sep=",", header=TRUE)</pre>
```

Computing the returns

```
returns <- (train[-1,3:ncol(train)]-train[-nrow(train),3:ncol(train)])/train[-nrow(train),3:ncol(train)]
```

Separating the returns with the index

```
rr <- returns[,-1]
index <- returns[,1]
head(rr) #gives the returns without the index</pre>
```

```
##
                      AAPL
                                 NVDA
                                              TSLA
                                                          MSFT
                                                                      AMD
             TSM
     0.067966914 0.05121871
                           0.17070078 0.3494846108
                                                    0.01242055
                                                               0.08163265
     0.107913530 0.02605846 -0.02117160 -0.1485233998
                                                    0.07797878
                                                               0.08086253
     0.003996158 0.09939605
                           0.03126701 -0.0026864956 -0.01439350
     0.022885268 0.07271754
                           0.02869540 -0.0005771803
                                                    0.01336632 -0.02200489
     0.040369884 0.03340213 -0.01971600
                                      0.1554122309
                                                    0.02574914
## 7 -0.064983478 0.02873098 -0.05609494 -0.0698158987
                                                    0.03501199 -0.06682578
            GOOG
                                   NFLX
                                              TWTR
     0.028911726 -0.050688595
## 2
  3 -0.082750882 -0.120070072 -0.21003972 -0.1500638
                                                   0.014214828 -0.031921145
  4 -0.054419409 -0.007636172 -0.08519163 -0.1649882
                                                   0.023142138
                                                               0.039089837
     0.063095775
                 0.058882570
                             0.29744751 -0.1675648
                                                   0.014654464
                                                               0.008500881
    0.027487499
                 0.063033208
                             0.05449585
                                        0.2629470
                                                   0.006593393
                                                               0.028352277
## 7 -0.006396881
                 0.079655237 -0.04058098
                                         0.1030021 -0.056144736
                                                               0.005109618
##
             PLD
                        AMT
                                    CCI
                                                           EQIX
     0.062693927 0.007294700 0.069616931
                                        0.072403346
                                                     0.02570208 0.014157854
## 3 -0.008740028 0.004909937 -0.027931708 -0.003017811 -0.02695303 0.029014868
     0.003202099 0.020153397 -0.009602118 0.050427962
                                                     0.01606782 0.058557368
     0.021658586 0.077430553
                            0.054997968 -0.017834140
                                                     0.05825051 0.002218882
## 6 -0.010118024 0.003905081 -0.032190846 -0.005975265
                                                     0.05705641 0.003683868
     0.001015610 0.053068066
                             0.003718001 0.009755617
                                                     0.02108652 0.015318362
                                                  ABT
##
             JNJ
                         UNH
                                      MRK
                                                             ABBV
     0.041256890
                 0.069036430
                             0.0758923301
                                           0.091173470
                                                       0.042316607
                                                                   0.06708666
  3
     0.073999511
                 0.061085122 -0.0038603275 -0.031925690
                                                       0.009624971 -0.01504280
     0.031151227 -0.081459836 0.0399720579
                                           0.005972766
                                                       0.013229588
```

```
## 6 0.038331612 0.026623209 -0.0001728946 0.022244611 0.038836598 0.02922433
## 7 -0.043299888 -0.003903819 -0.0114363785 0.029828673 -0.072643602 -0.02045492
                                                    MDLZ
##
              WMT
                           PG
                                       PEP
                   0.03438440 -0.003608634
                                            0.0387670709
     0.0002677824
                                                          0.010047332
## 2
##
     0.0231594815
                   0.02466324
                               0.042837588
                                            0.0152805604
                                                          0.012041789
     0.0496429779  0.02419383  0.035893769  0.0360825217
                                                          0.063454976
## 5 -0.0368834760 -0.01350660 0.028408101 0.0552597191
                                                          0.002942074
## 6 -0.0160899923 -0.02723131 0.011434796 -0.0002659565
                                                          0.035443670
## 7 -0.0198480014 -0.01615955 -0.006503135 -0.0386491729 -0.065498296
##
               EL
## 2 0.001454896
## 3 -0.025584005
## 4 0.085077885
## 5 0.055808312
## 6 -0.028230138
## 7 -0.010772920
```

#### index #qives the returns of the index

```
##
   [1]
       0.0431170300 0.0069321656 0.0062007890 0.0210302800
                                                           0.0190583317
##
   [6] -0.0150798306  0.0376552955 -0.0155138372  0.0232014608
                                                           0.0245335888
  [11] -0.0041885879 -0.0310408058
                                 0.0548925110 -0.0173961069
                                                           0.0085208197
                                 0.0197420297 -0.0625808182 -0.0264428316
  [16]
       0.0104913824 -0.0210116724
## [21]
        ## [26]
        0.0659911146 0.0026993985
                                 0.0153246024 0.0009109211
                                                           0.0356098011
  [31] -0.0012192431 -0.0012344508 -0.0194256793 0.0341745222
                                                           0.0182007622
  [36]
        0.0178843582 0.0371981603 -0.0003891972 0.0090912085
                                                           0.0115762514
  [41]
        0.0048137751 0.0193488261
                                 0.0005464328 0.0193029785
                                                           0.0221881353
        0.0280826277 0.0098316305
  [46]
                                 0.0561787044 -0.0389473721 -0.0268844986
##
  [51]
       0.0027187751 0.0216083420
                                 0.0048424360 0.0360215562
                                                           0.0302632115
##
  [56]
       0.0042942871 -0.0694033560 0.0178593568 -0.0917768946
```

# BREAKPOINT 1: This is the first approach for finding X for the Multigroup Model

```
group1 = rr[1:6]
group2 = rr[7:12]
group3 = rr[13:18]
group4 = rr[19:24]
group5 = rr[25:30]

cor.matrix = cor(rr)
head(cor.matrix)
```

```
##
                TSM
                         AAPL
                                    NVDA
                                                TSLA
                                                           MSFT
                                                                       AMD
## TSM 1.000000000 0.4881521 0.51335805 0.002352407 0.5610358 0.28976420
  AAPL 0.488152139 1.0000000 0.46607525 0.132955720 0.3883190 0.25508531
## NVDA 0.513358050 0.4660753 1.000000000 0.091198792 0.4424173 0.41682653
  TSLA 0.002352407 0.1329557 0.09119879 1.000000000 0.1000357 0.05088927
## MSFT 0.561035768 0.3883190 0.44241733 0.100035732 1.0000000 0.31061651
## AMD 0.289764204 0.2550853 0.41682653 0.050889269 0.3106165 1.00000000
##
              GOOG
                           FB
                                   NFLX
                                               TWTR.
                                                             CHT
                                                                     CMCSA
## TSM 0.41812563 0.09204639 0.2320642 -0.04916528 0.29111913 0.2885973
## AAPL 0.29738400 0.32209593 0.2715191 0.25514918 0.21085202 0.2562311
```

```
## NVDA 0.40521256 0.20242695 0.3525203 0.09768510 0.14273033 0.2786302
## TSLA 0.08753646 0.22938963 0.2598298 0.20023724 0.07437638 0.1848653
  MSFT 0.58646897 0.30209522 0.3194192 -0.01034658 -0.04565052 0.3746506
       0.29352490 0.12997820 0.1645240 -0.06180246
                                                     0.08940778 0.1971629
##
              PI.D
                         AMT
                                    CCT
                                                 PSA
                                                           EQIX
                                                                      WELL.
## TSM
       0.2988845 0.33037283 0.29291604
                                         0.04869060 0.34303613
                                                                0.1365636
## AAPL 0.2801479 0.38915377 0.31429053
                                         0.22728323 0.15500742 0.1184767
## NVDA 0.2763530 0.02292159 0.15452519
                                         0.02401534 0.26038486 -0.1047239
## TSLA 0.1021972 0.16292178 0.08453724 0.07435971 0.12163911 0.1855199
  MSFT 0.2613861 0.35657676 0.16885831 0.04307035 0.42383415 -0.1077074
       0.3591972 0.17342958 0.12253440 -0.04786822 0.09538971
                                                                 0.1876068
##
              JNJ
                        UNH
                                   MRK
                                              ABT
                                                        ABBV
                                                                   AZN
                                                                               WMT
## TSM
       0.4138310 0.2149548 0.16602888 0.4699059 0.25686311 0.2791651 0.27269290
## AAPL 0.1814671 0.1984693 0.12514394 0.4012236 0.08962962 0.1754471 0.14238957
## NVDA 0.1024046 0.2166770 0.06681852 0.2746761 0.25477425 0.1901820 0.10781126
## TSLA 0.0844957 0.1872566 0.19167680 0.2124842 0.20815838 0.1398365 0.06704248
  MSFT 0.3621385 0.1537371 0.19315174 0.4152522 0.38224601 0.1435684 0.09182490
       0.3030626 0.3335709 0.34979807 0.4516329 0.38781251 0.1379067 0.03907121
                                     MDLZ
##
                 PG
                            PEP
                                                  KΩ
                                                             EI.
## TSM
         0.22332488 0.331596563 0.2746476 0.4295469 0.25282221
## AAPL 0.14023665 0.220589041 0.1558214 0.1710399 0.23472668
## NVDA -0.07196894 0.009185657 0.1425258 0.1295878 0.13086183
## TSLA 0.08356726 0.119718469 0.1349797 0.2218584 0.11535336
        0.19265238 0.348626415 0.3954915 0.4343138 0.19395054
## MSFT
## AMD
         0.16057256 0.222287672 0.1800234 0.1311243 0.08478151
means = colMeans(rr)
means
##
                                      NVDA
                                                   TSLA
                                                                MSFT
                                                                               AMD
            TSM
                        AAPL
##
   0.018022831
                 0.017597560
                              0.044567996
                                            0.016879280
                                                         0.020687995
                                                                      0.043437846
##
           GOOG
                          FΒ
                                      NFLX
                                                   TWTR
                                                                 CHT
                                                                             CMCSA
   0.011206214
                 0.014473364
                              0.034101355
                                           -0.003696091
                                                         0.007410518
                                                                      0.006931851
##
            PLD
                         AMT
                                       CCI
                                                    PSA
                                                                EQIX
                                                                              WELL
##
   0.011089250
                 0.014264652
                              0.011227455
                                            0.008176040
                                                         0.015260709
                                                                      0.009094911
##
            JNJ
                         UNH
                                      MRK
                                                    ABT
                                                                ABBV
                                                                               AZN
##
   0.009525905
                 0.023671961
                              0.010107381
                                            0.015006148
                                                         0.016591625
                                                                      0.008827518
##
            WMT
                          PG
                                       PEP
                                                   MDLZ
                                                                  KO
                                                                                EL
   0.007404403
                 0.006624564
                              0.008565794
                                           0.006095891
                                                         0.007265480
                                                                      0.013236073
library(matrixStats)
sd = colSds(as.matrix(rr[sapply(rr,is.numeric)]))
```

#### Compute correlation fro each group

```
rho11 = (sum(cor.matrix[1:6,1:6]) - 6) / (36-6)
rho12 = (sum(cor.matrix[1:6,7:12])) / 36
rho13 = (sum(cor.matrix[1:6,13:18])) / 36
rho14 = (sum(cor.matrix[1:6,19:24])) / 36
rho15 = (sum(cor.matrix[1:6,25:30])) / 36

rho21 = rho12
rho22 = (sum(cor.matrix[7:12,7:12])-6) / (36-6)
```

```
rho23 = (sum(cor.matrix[7:12,13:18])) / 36
rho24 = (sum(cor.matrix[7:12,19:24])) / 36
rho25 = (sum(cor.matrix[7:12,25:30])) / 36
rho31 = rho13
rho32 = rho23
rho33 = (sum(cor.matrix[13:18,13:18])-6) / (36-6)
rho34 = (sum(cor.matrix[13:18,19:24])) / 36
rho35 = (sum(cor.matrix[13:18,25:30])) / 36
rho41 = rho14
rho42 = rho24
rho43 = rho34
rho44 = (sum(cor.matrix[19:24,19:24])-6) / (36-6)
rho45 = (sum(cor.matrix[19:24,25:30])) / 36
rho51 = rho15
rho52 = rho25
rho53 = rho35
rho54 = rho45
rho55 = (sum(cor.matrix[25:30,25:30])-6) / (36-6)
P = rbind(c(rho11, rho12, rho13, rho14, rho15),
          c(rho21,rho22,rho23,rho24,rho25),
          c(rho31,rho32,rho33,rho34,rho35),
          c(rho41,rho42,rho43,rho44,rho45),
          c(rho51,rho52,rho53,rho54,rho55))
Ρ
             [,1]
                        [,2]
                                  [,3]
                                            [,4]
## [1,] 0.3006055 0.2150248 0.1759939 0.2420958 0.1809633
## [2,] 0.2150248 0.1624972 0.1367383 0.1219426 0.1329181
## [3,] 0.1759939 0.1367383 0.3889642 0.2418283 0.3176168
## [4,] 0.2420958 0.1219426 0.2418283 0.2942266 0.2577317
## [5,] 0.1809633 0.1329181 0.3176168 0.2577317 0.3697981
Computing matrix A
N = 6 #6 stocks per group
row1 = c(1+(N*rho11)/(1-rho11), N*rho12/(1-rho11), N*rho13/(1-rho11), N*rho14/(1-rho11), N*rho15/(1-rho11))
row2 = c((N*rho21)/(1-rho22), 1+N*rho22/(1-rho22), N*rho23/(1-rho22), N*rho24/(1-rho22), N*rho25/(1-rho22))
row3 = c((N*rho31)/(1-rho33), N*rho32/(1-rho33), 1+N*rho33/(1-rho33), N*rho34/(1-rho33), N*rho35/(1-rho33))
row4 = c((N*rho41)/(1-rho44), N*rho42/(1-rho44), N*rho43/(1-rho44), 1+N*rho44/(1-rho44), N*rho45/(1-rho44))
row5 = c((N*rho51)/(1-rho55), N*rho52/(1-rho55), N*rho53/(1-rho55), N*rho54/(1-rho55), 1+N*rho55/(1-rho55))
A = rbind(row1,row2,row3,row4,row5)
            [,1]
                      [,2]
                                [,3]
                                          [,4]
                                                     [,5]
## row1 3.578849 1.844665 1.5098255 2.0769030 1.5524565
```

```
## row2 1.540471 2.164155 0.9796142 0.8736154 0.9522458
## row3 1.728153 1.342687 4.8193915 2.3746066 3.1188037
## row4 2.058132 1.036672 2.0558578 3.5013126 2.1910574
## row5 1.722908 1.265481 3.0239529 2.4538009 4.5207586
Computing Matrix C
Rf = 0.002
c1 = 0
for (i in 1:6){
  c1 = c1 + as.numeric((means[i]-Rf)/(sd[i]*(1-rho11)))
}
c2 = 0
for (i in 7:12){
  c2 = c2 + as.numeric((means[i]-Rf)/(sd[i]*(1-rho22)))
}
c3 = 0
for (i in 13:18){
  c3 = c3 + as.numeric((means[i]-Rf)/(sd[i]*(1-rho33)))
c4 = 0
for (i in 19:24){
  c4 = c4 + as.numeric((means[i]-Rf)/(sd[i]*(1-rho44)))
c5 = 0
for (i in 25:30){
  c5 = c5 + as.numeric((means[i]-Rf)/(sd[i]*(1-rho55)))
}
C \leftarrow rbind(c1,c2,c3,c4,c5)
C
           [,1]
##
## c1 2.1441207
## c2 0.9747475
## c3 1.8117479
## c4 1.8850972
## c5 1.2966100
cut off points for each group from phi
phi <- solve(A) %*% C
phi
##
               [,1]
## [1,] 0.41352603
## [2,] 0.02910834
## [3,] 0.18078681
## [4,] 0.27329112
## [5,] -0.14820211
c1s = c(rho11,rho12,rho13,rho14,rho15) %*% phi
```

c2s = c(rho21, rho22, rho23, rho24, rho25) %\*% phi

```
c3s = c(rho31, rho32, rho33, rho34, rho35) %*% phi
c4s = c(rho41,rho42,rho43,rho44,rho45) %*% phi
c5s = c(rho51,rho52,rho53,rho54,rho55) %*% phi
z1 \leftarrow numeric(0)
for(i in 1:6){
 z1[i] = 1/(sd[i]*(1-rho11)) * ((means[i]-Rf)/sd[i] - c1s)
z2 \leftarrow numeric(0)
for(i in 7:12){
 z2[i-6] = 1/(sd[i]*(1-rho22)) * ((means[i]-Rf)/sd[i] - c2s)
z3 \leftarrow numeric(0)
for(i in 13:18){
 z3[i-12] = 1/(sd[i]*(1-rho33)) * ((means[i]-Rf)/sd[i] - c3s)
z4 <- numeric(0)
for(i in 19:24){
 z4[i-18] = 1/(sd[i]*(1-rho44)) * ((means[i]-Rf)/sd[i] - c4s)
z5 \leftarrow numeric(0)
for(i in 25:30){
 z5[i-24] = 1/(sd[i]*(1-rho55)) * ((means[i]-Rf)/sd[i] - c5s)
}
Z = c(z1, z2, z3, z4, z5)
## [1] 1.11407657 0.30605812 1.83426225 -0.91364475 2.57355537 0.30604410
## [7] 0.57044088 1.36838082 1.02047402 -1.45348036 1.24172661 -0.97367581
## [13] 0.23049866 2.36731389 1.26184626 -1.32748109 2.37771834 -1.26134559
## [19] 0.02709128 7.72486088 -0.76403279 1.08979086 0.02397025 -1.85258929
## [25] -1.52256586 -1.43707250 0.43742731 -2.21948757 -0.51298672 2.04883197
X = Z/sum(Z)
X
## [1] 0.081402607 0.022362851 0.134024656 -0.066757588 0.188042833
## [6] 0.022361827 0.041680595 0.099983940 0.074563317 -0.106201937
## [11] 0.090729655 -0.071143897 0.016841923 0.172973319 0.092199744
```

BREAKPOINT 2 This is the Second approach to finding X for multigroup model Computing the variance of the market

```
exp_R_m = mean(index)
sigma_m2 <- var(index)</pre>
exp_R = colMeans(rr)
Optimal Portfolio from Multigroup Model
cormat <- cor(rr)</pre>
head(cormat)
##
                TSM
                         AAPL
                                    NVDA
                                                 TSLA
                                                           MSFT
                                                                       AMD
## TSM 1.000000000 0.4881521 0.51335805 0.002352407 0.5610358 0.28976420
## AAPL 0.488152139 1.0000000 0.46607525 0.132955720 0.3883190 0.25508531
## NVDA 0.513358050 0.4660753 1.00000000 0.091198792 0.4424173 0.41682653
## TSLA 0.002352407 0.1329557 0.09119879 1.000000000 0.1000357 0.05088927
## MSFT 0.561035768 0.3883190 0.44241733 0.100035732 1.0000000 0.31061651
## AMD 0.289764204 0.2550853 0.41682653 0.050889269 0.3106165 1.00000000
##
              GOOG
                           FB
                                   NFLX
                                                TWTR
                                                             CHT
## TSM 0.41812563 0.09204639 0.2320642 -0.04916528 0.29111913 0.2885973
## AAPL 0.29738400 0.32209593 0.2715191 0.25514918 0.21085202 0.2562311
## NVDA 0.40521256 0.20242695 0.3525203 0.09768510
                                                     0.14273033 0.2786302
## TSLA 0.08753646 0.22938963 0.2598298 0.20023724 0.07437638 0.1848653
## MSFT 0.58646897 0.30209522 0.3194192 -0.01034658 -0.04565052 0.3746506
       0.29352490 0.12997820 0.1645240 -0.06180246 0.08940778 0.1971629
##
              PLD
                         AMT
                                    CCI
                                                 PSA
                                                           EQIX
                                                                      WELL
## TSM 0.2988845 0.33037283 0.29291604 0.04869060 0.34303613
                                                                 0.1365636
## AAPL 0.2801479 0.38915377 0.31429053 0.22728323 0.15500742 0.1184767
## NVDA 0.2763530 0.02292159 0.15452519 0.02401534 0.26038486 -0.1047239
## TSLA 0.1021972 0.16292178 0.08453724 0.07435971 0.12163911
                                                                0.1855199
## MSFT 0.2613861 0.35657676 0.16885831 0.04307035 0.42383415 -0.1077074
       0.3591972 0.17342958 0.12253440 -0.04786822 0.09538971 0.1876068
##
              JNJ
                        UNH
                                   MRK
                                             ABT
                                                        ABBV
                                                                   A 7.N
                                                                              WMT
## TSM 0.4138310 0.2149548 0.16602888 0.4699059 0.25686311 0.2791651 0.27269290
## AAPL 0.1814671 0.1984693 0.12514394 0.4012236 0.08962962 0.1754471 0.14238957
## NVDA 0.1024046 0.2166770 0.06681852 0.2746761 0.25477425 0.1901820 0.10781126
## TSLA 0.0844957 0.1872566 0.19167680 0.2124842 0.20815838 0.1398365 0.06704248
## MSFT 0.3621385 0.1537371 0.19315174 0.4152522 0.38224601 0.1435684 0.09182490
       0.3030626 0.3335709 0.34979807 0.4516329 0.38781251 0.1379067 0.03907121
##
##
                 PG
                            PEP
                                     MDLZ
                                                 KO
         0.22332488 0.331596563 0.2746476 0.4295469 0.25282221
## TSM
## AAPL 0.14023665 0.220589041 0.1558214 0.1710399 0.23472668
## NVDA -0.07196894 0.009185657 0.1425258 0.1295878 0.13086183
        0.08356726 0.119718469 0.1349797 0.2218584 0.11535336
         0.19265238 0.348626415 0.3954915 0.4343138 0.19395054
## MSFT
## AMD
         0.16057256 0.222287672 0.1800234 0.1311243 0.08478151
stdev <- diag(cov(rr))^.5</pre>
for (i in 1:5){
  g_a = (i*6-5):(i*6)
```

 $cormat[g_a,g_a] \leftarrow (sum(cormat[g_a,g_a]) - 6)/30$ 

for (j in (i+1):5){

```
if (i >= 5){
      break
    }
    g_b = (j*6-5):(j*6)
    cormat[g_a,g_b] = mean(cormat[g_a, g_b])
    cormat[g_b,g_a] = mean(cormat[g_a,g_b])
  }
}
diag(cormat) = 1
head(cormat)
##
              TSM
                       AAPL
                                 NVDA
                                           TSLA
                                                     MSFT
                                                                AMD
                                                                         GOOG
## TSM 1.0000000 0.3006055 0.3006055 0.3006055 0.3006055 0.3006055 0.2150248
## AAPL 0.3006055 1.0000000 0.3006055 0.3006055 0.3006055 0.3006055 0.2150248
## NVDA 0.3006055 0.3006055 1.0000000 0.3006055 0.3006055 0.3006055 0.2150248
## TSLA 0.3006055 0.3006055 0.3006055 1.0000000 0.3006055 0.3006055 0.2150248
## MSFT 0.3006055 0.3006055 0.3006055 0.3006055 1.0000000 0.3006055 0.2150248
       0.3006055 0.3006055 0.3006055 0.3006055 0.3006055 1.0000000 0.2150248
                                 TWTR
                                            CHT
                                                    CMCSA
                                                                PLD
                                                                          TMA
##
               FB
                       NFI.X
## TSM 0.2150248 0.2150248 0.2150248 0.2150248 0.2150248 0.1759939 0.1759939
## AAPL 0.2150248 0.2150248 0.2150248 0.2150248 0.2150248 0.1759939 0.1759939
## NVDA 0.2150248 0.2150248 0.2150248 0.2150248 0.2150248 0.1759939 0.1759939
## TSLA 0.2150248 0.2150248 0.2150248 0.2150248 0.2150248 0.1759939 0.1759939
## MSFT 0.2150248 0.2150248 0.2150248 0.2150248 0.2150248 0.1759939 0.1759939
## AMD 0.2150248 0.2150248 0.2150248 0.2150248 0.2150248 0.1759939 0.1759939
                                                      JNJ
##
              CCI
                        PSA
                                 EQIX
                                           WELL
                                                                UNH
                                                                          MRK
## TSM 0.1759939 0.1759939 0.1759939 0.1759939 0.2420958 0.2420958 0.2420958
## AAPL 0.1759939 0.1759939 0.1759939 0.1759939 0.2420958 0.2420958 0.2420958
## NVDA 0.1759939 0.1759939 0.1759939 0.1759939 0.2420958 0.2420958 0.2420958
## TSLA 0.1759939 0.1759939 0.1759939 0.1759939 0.2420958 0.2420958 0.2420958
## MSFT 0.1759939 0.1759939 0.1759939 0.1759939 0.2420958 0.2420958 0.2420958
## AMD 0.1759939 0.1759939 0.1759939 0.1759939 0.2420958 0.2420958 0.2420958
##
              ABT
                       ABBV
                                  AZN
                                            WMT
                                                       PG
                                                                PEP
## TSM 0.2420958 0.2420958 0.2420958 0.1809633 0.1809633 0.1809633 0.1809633
## AAPL 0.2420958 0.2420958 0.2420958 0.1809633 0.1809633 0.1809633
## NVDA 0.2420958 0.2420958 0.2420958 0.1809633 0.1809633 0.1809633 0.1809633
## TSLA 0.2420958 0.2420958 0.2420958 0.1809633 0.1809633 0.1809633 0.1809633
## MSFT 0.2420958 0.2420958 0.2420958 0.1809633 0.1809633 0.1809633
## AMD 0.2420958 0.2420958 0.2420958 0.1809633 0.1809633 0.1809633 0.1809633
##
               ΚO
## TSM 0.1809633 0.1809633
## AAPL 0.1809633 0.1809633
## NVDA 0.1809633 0.1809633
## TSLA 0.1809633 0.1809633
## MSFT 0.1809633 0.1809633
## AMD 0.1809633 0.1809633
covmat = matrix(nrow = 30,ncol=30,dimnames= list(names(stdev),names(stdev)))
for (i in 1:30){
  for (j in 1:30){
    covmat[i,j] = cormat[i,j] * stdev[i] * stdev[j]
  }
```

# # diag(covmat) = 1 head(covmat)

```
TSLA
                TSM
                           AAPL
                                       NVDA
                                                                MSFT
## TSM
       0.004062383 0.001376484 0.002294916 0.002250663 0.001154369 0.003323834
## AAPL 0.001376484 0.005161405 0.002586784 0.002536904 0.001301183 0.003746562
## NVDA 0.002294916 0.002586784 0.014346924 0.004229601 0.002169370 0.006246379
  TSLA 0.002250663 0.002536904 0.004229601 0.013798960 0.002127538 0.006125931
  MSFT 0.001154369 0.001301183 0.002169370 0.002127538 0.003630068 0.003142001
        0.003323834 0.003746562 0.006246379 0.006125931 0.003142001 0.030095678
                               FΒ
                GOOG
##
                                         NFLX
                                                     TWTR.
## TSM
        0.0007907413 0.0008439148 0.001800865 0.001939292 0.0004469362
## AAPL 0.0008913083 0.0009512445 0.002029900 0.002185933 0.0005037778
## NVDA 0.0014860157 0.0015859430 0.003384310 0.003644452 0.0008399133
## TSLA 0.0014573611 0.0015553615 0.003319051 0.003574177 0.0008237174
## MSFT 0.0007474831 0.0007977477 0.001702347 0.001833202 0.0004224861
        0.0021522666 0.0022969960 0.004901655 0.005278432 0.0012164860
               CMCSA
##
                              PLD
                                           AMT
                                                         CCT
        0.0008020364 0.0005877306 0.0005732038 0.0005138900 0.0005476926
## AAPL 0.0009040399 0.0006624785 0.0006461042 0.0005792469 0.0006173485
## NVDA 0.0015072422 0.0011045039 0.0010772041 0.0009657377 0.0010292617
## TSLA 0.0014781783 0.0010832059 0.0010564326 0.0009471155 0.0010094146
## MSFT 0.0007581603 0.0005555782 0.0005418461 0.0004857772 0.0005177305
        0.0021830099 0.0015997051 0.0015601655 0.0013987234 0.0014907282
                EQIX
                             WELL
                                           JNJ
                                                        UNH
       0.0006076410 0.0006585690 0.0006100724 0.0007408762 0.0007687610
## TSM
  AAPL 0.0006849212 0.0007423263 0.0006876618 0.0008351013 0.0008665326
## NVDA 0.0011419210 0.0012376284 0.0011464902 0.0013923057 0.0014447088
## TSLA 0.0011199015 0.0012137634 0.0011243827 0.0013654581 0.0014168507
## MSFT 0.0005743995 0.0006225414 0.0005766979 0.0007003459 0.0007267053
## AMD 0.0016538980 0.0017925156 0.0016605159 0.0020165420 0.0020924399
                            ABBV
##
                 ABT
                                          AZN
                                                        WMT
                                                                      PG
## TSM 0.0008628042 0.001179512 0.0010276903 0.0006246802 0.0004618618
## AAPL 0.0009725362 0.001329523 0.0011583927 0.0007041275 0.0005206017
## NVDA 0.0016214412 0.002216620 0.0019313066 0.0011739422 0.0008679625
## TSLA 0.0015901752 0.002173877 0.0018940655 0.0011513053 0.0008512258
## MSFT 0.0008156037 0.001114986 0.0009714696 0.0005905065 0.0004365952
## AMD
       0.0023484097 0.003210435 0.0027972024 0.0017002759 0.0012571111
##
                 PEP
                             MDLZ
                                            KO
                                                         EL
## TSM 0.0004649805 0.0005818332 0.0004351805 0.0005938492
## AAPL 0.0005241170 0.0006558311 0.0004905271 0.0006693753
## NVDA 0.0008738235 0.0010934211 0.0008178213 0.0011160024
## TSLA 0.0008569737 0.0010723368 0.0008020514 0.0010944827
## MSFT 0.0004395433 0.0005500035 0.0004113736 0.0005613621
## AMD 0.0012655998 0.0015836533 0.0011844891 0.0016163588
R_f = 0.002
R = \exp_R - R_f
X_alloc = (solve(covmat)%*%R)/ as.numeric(rep(1,30) %*% solve(covmat) %*% R)
X alloc
```

```
[,1]
##
## TSM
          0.081402607
## AAPL
         0.022362851
## NVDA
         0.134024656
## TSLA
        -0.066757588
## MSFT
          0.188042833
## AMD
          0.022361827
## GOOG
          0.041680595
## FB
          0.099983940
## NFLX
          0.074563317
## TWTR
        -0.106201937
## CHT
          0.090729655
## CMCSA -0.071143897
## PLD
          0.016841923
## AMT
          0.172973319
## CCI
          0.092199744
## PSA
         -0.096995507
## EQIX
         0.173733544
## WELL
        -0.092163161
## JNJ
          0.001979488
## UNH
          0.564435002
## MRK
         -0.055825840
## ABT
          0.079628114
## ABBV
          0.001751442
## AZN
         -0.135363764
## WMT
         -0.111249830
## PG
         -0.105003059
## PEP
          0.031961648
## MDLZ -0.162172043
         -0.037482573
## KO
## EL
          0.149702693
port_exp_R = as.numeric(t(X_alloc)%*%exp_R)
port_stdev = as.numeric(t(X_alloc) %*% covmat %*% X_alloc)^.5
port_exp_R
## [1] 0.03362654
port_stdev
## [1] 0.04807148
Breakpoint 3 Project 5 a.
train <- read.csv("stockDataTrain.csv", sep=",", header=TRUE)</pre>
returns <- (train[-1,3:ncol(train)]-train[-nrow(train),3:ncol(train)])/train[-nrow(train),3:ncol(train)]
rr <- returns[,-1]</pre>
index <- returns[,1]</pre>
head(rr)
```

```
AAPL
                                 NVDA
                                               TSLA
                                                          MSFT
##
## 2 0.067966914 0.05121871 0.17070078 0.3494846108 0.01242055 0.08163265
## 3 0.107913530 0.02605846 -0.02117160 -0.1485233998 0.07797878
    0.003996158 0.09939605 0.03126701 -0.0026864956 -0.01439350
                                                                0.01995012
     0.022885268 0.07271754 0.02869540 -0.0005771803 0.01336632 -0.02200489
## 6 0.040369884 0.03340213 -0.01971600 0.1554122309 0.02574914 0.04750000
## 7 -0.064983478 0.02873098 -0.05609494 -0.0698158987 0.03501199 -0.06682578
            GOOG
                          FB
                                   NFI.X
                                              TWTR
                                                           CHT
                                                                      CMCSA
## 2 0.029365727 0.094134553 0.08868150 -0.1486822 0.028911726 -0.050688595
## 3 -0.082750882 -0.120070072 -0.21003972 -0.1500638 0.014214828 -0.031921145
## 4 -0.054419409 -0.007636172 -0.08519163 -0.1649882 0.023142138 0.039089837
## 5 0.063095775 0.058882570 0.29744751 -0.1675648 0.014654464 0.008500881
## 6 0.027487499 0.063033208 0.05449585 0.2629470 0.006593393 0.028352277
## 7 -0.006396881 0.079655237 -0.04058098 0.1030021 -0.056144736
                                                                0.005109618
             PLD
                        AMT
                                    CCI
                                                 PSA
                                                           EQIX
## 2 0.062693927 0.007294700 0.069616931 0.072403346 0.02570208 0.014157854
## 3 -0.008740028 0.004909937 -0.027931708 -0.003017811 -0.02695303 0.029014868
## 4 0.003202099 0.020153397 -0.009602118 0.050427962 0.01606782 0.058557368
## 5 0.021658586 0.077430553 0.054997968 -0.017834140 0.05825051 0.002218882
## 6 -0.010118024 0.003905081 -0.032190846 -0.005975265 0.05705641 0.003683868
## 7 0.001015610 0.053068066 0.003718001 0.009755617 0.02108652 0.015318362
             JN.J
                         UNH
                                      MRK
                                                  ABT
## 2 0.041256890 0.069036430 0.0758923301 0.091173470 0.042316607 0.06708666
     0.073999511 0.061085122 -0.0038603275 -0.031925690 0.009624971 -0.01504280
    0.031151227 -0.081459836 0.0399720579 0.005972766 0.013229588 0.21840318
    0.001678525 0.061167487 -0.0119534510 0.038916678 0.052538949 -0.08665395
    ## 7 -0.043299888 -0.003903819 -0.0114363785
                                          0.029828673 -0.072643602 -0.02045492
                          PG
                                     PEP
                                                  MDLZ
             WMT
                                                                ΚO
    0.0002677824
                 0.03438440 -0.003608634 0.0387670709
                                                       0.010047332
    0.0231594815
                  0.02466324 0.042837588
                                         0.0152805604
                                                       0.012041789
## 4 0.0496429779 0.02419383 0.035893769
                                         0.0360825217
                                                       0.063454976
## 5 -0.0368834760 -0.01350660 0.028408101 0.0552597191
                                                       0.002942074
## 6 -0.0160899923 -0.02723131 0.011434796 -0.0002659565 0.035443670
## 7 -0.0198480014 -0.01615955 -0.006503135 -0.0386491729 -0.065498296
##
## 2 0.001454896
## 3 -0.025584005
## 4 0.085077885
## 5 0.055808312
## 6 -0.028230138
## 7 -0.010772920
```

#### index

```
## [1] 0.0431170300 0.0069321656 0.0062007890 0.0210302800 0.0190583317
## [6] -0.0150798306 0.0376552955 -0.0155138372 0.0232014608 0.0245335888
## [11] -0.0041885879 -0.0310408058 0.0548925110 -0.0173961069 0.0085208197
## [16] 0.0104913824 -0.0210116724 0.0197420297 -0.0625808182 -0.0264428316
## [21] 0.0829831178 0.0005048693 -0.0175301852 -0.0507353220 -0.0041283604
## [26] 0.0659911146 0.0026993985 0.0153246024 0.0009109211 0.0356098011
## [31] -0.0012192431 -0.0012344508 -0.0194256793 0.0341745222 0.0182007622
## [36] 0.0178843582 0.0371981603 -0.0003891972 0.0090912085 0.0115762514
## [41] 0.0048137751 0.0193488261 0.0005464328 0.0193029785 0.0221881353
```

```
## [46] 0.0280826277 0.0098316305 0.0561787044 -0.0389473721 -0.0268844986

## [51] 0.0027187751 0.0216083420 0.0048424360 0.0360215562 0.0302632115

## [56] 0.0042942871 -0.0694033560 0.0178593568 -0.0917768946

sigma_m2 <- var(index)
```

Calculating the betas, alphas, sigmas, and the variance of betas through linear regression model

```
beta2 <- rep(0,30)
alpha2 <- rep(0,30)
sigma_e2 <- rep(0,30)

var_beta2 <- rep(0,30)

for(i in 1:30){
    q <- lm(data=rr, formula=rr[,i] ~ index)
    beta2[i] <- q$coefficients[2]
    alpha2[i] <- q$coefficients[1]
    sigma_e2[i] <- summary(q)$sigma^2
    var_beta2[i] <- vcov(q)[2,2]
}</pre>
```

#### beta2

```
## [1] 1.1575430 1.1546817 2.0393210 0.7257803 1.2465438 3.3617924 1.0647161 ## [8] 0.6993114 1.2186013 0.2482677 0.1143192 1.0719706 0.9615390 0.6452853 ## [15] 0.4331112 0.3109568 0.7489639 0.3200383 0.6801403 0.8557822 0.7613453 ## [22] 1.2635732 1.4733349 0.5777802 0.3278997 0.3664477 0.6786786 0.8151057 ## [29] 0.5684855 0.6411576
```

#### alpha2

```
[1]
##
      0.0107539160 \quad 0.0103466129 \quad 0.0317618618 \quad 0.0123216653 \quad 0.0128601908
##
  [6]
      ## [11]
      0.0066926391 0.0002002969 0.0050511629 0.0102125141 0.0085076868
## [16]
      ## [21]
      0.0053264319 0.0070714054
                            0.0073396613 0.0051992860
                                                  0.0053453223
  [26]
      0.0043234165 \quad 0.0043039592 \quad 0.0009773474 \quad 0.0036956149 \quad 0.0092098549
```

## sigma\_e2

```
## [1] 0.002801742 0.003926622 0.010464609 0.013517433 0.002149154 0.019389460

## [7] 0.002260526 0.003372151 0.016093300 0.020312993 0.001069156 0.002342581

## [13] 0.001874361 0.002243112 0.001949121 0.002329658 0.002428271 0.003405539

## [19] 0.001130768 0.001617797 0.001949505 0.001594339 0.003787930 0.004181755

## [25] 0.002877866 0.001498124 0.001195860 0.001928903 0.001127292 0.002288760
```

VAR Covariance Matrix for SIM

```
var_i <- sigma_e2 + beta2^2*var(index)
covmat <- beta2 %*% t(beta2)
covmat <- covmat * as.numeric(var(index))
# covmat <- covmat + diag(var_i)
covmat <- covmat + diag(sigma_e2)
rownames(covmat) <- names(rr)
colnames(covmat) <- names(rr)
head(covmat)</pre>
```

```
##
                 TSM
                             AAPL
                                         NVDA
                                                      TSLA
                                                                  MSFT
                                                                                AMD
## TSM 0.0041106888 0.0013057112 0.002306059 0.0008207105 0.001409589 0.003801506
## AAPL 0.0013057112 0.0052291052 0.002300359 0.0008186818 0.001406104 0.003792110
## NVDA 0.0023060592 0.0023003589 0.014527348 0.0014459007 0.002483367 0.006697369
## TSLA 0.0008207105 0.0008186818 0.001445901 0.0140320188 0.000883813 0.002383547
## MSFT 0.0014095886 0.0014061043 0.002483367 0.0008838130 0.003667122 0.004093795
## AMD 0.0038015065 0.0037921096 0.006697369 0.0023835472 0.004093795 0.030429979
##
                GOOG
                               FΒ
                                          NFLX
                                                       TWTR
                                                                     CHT
## TSM 0.0012039783 0.0007907797 0.0013779914 0.0002807405 1.292718e-04
## AAPL 0.0012010023 0.0007888249 0.0013745851 0.0002800466 1.289523e-04
## NVDA 0.0021211293 0.0013931695 0.0024276997 0.0004945994 2.277468e-04
## TSLA 0.0007548953 0.0004958194 0.0008640016 0.0001760245 8.105353e-05
## MSFT 0.0012965494 0.0008515809 0.0014839419 0.0003023260 1.392112e-04
       0.0034966522 0.0022966205 0.0040020292 0.0008153402 3.754375e-04
## AMD
##
               CMCSA
                              PLD
                                           AMT
                                                        CCI
                                                                     PSA
## TSM 0.0012121817 0.0010873060 0.0007296871 0.0004897611 0.0003516292
## AAPL 0.0012091853 0.0010846183 0.0007278834 0.0004885504 0.0003507600
## NVDA 0.0021355817 0.0019155798 0.0012855386 0.0008628449 0.0006194887
## TSLA 0.0007600388 0.0006817416 0.0004575143 0.0003070805 0.0002204717
## MSFT 0.0013053835 0.0011709064 0.0007857910 0.0005274176 0.0003786651
## AMD 0.0035204767 0.0031578066 0.0021191925 0.0014223878 0.0010212185
##
                EQIX
                             WELL
                                           JNJ
                                                        UNH
                                                                     MRK
## TSM 0.0008469266 0.0003618985 0.0007691010 0.0009677164 0.0008609274
## AAPL 0.0008448331 0.0003610039 0.0007671999 0.0009653243 0.0008587992
## NVDA 0.0014920873 0.0006375808 0.0013549768 0.0017048909 0.0015167534
## TSLA 0.0005310236 0.0002269106 0.0004822269 0.0006067589 0.0005398021
## MSFT 0.0009120448 0.0003897240 0.0008282354 0.0010421219 0.0009271221
## AMD 0.0024596851 0.0010510431 0.0022336604 0.0028104889 0.0025003469
##
                 ABT
                            ABBV
                                          AZN
                                                       WMT
                                                                     PG
## TSM 0.0014288455 0.001666043 0.0006533524 0.0003707881 0.0004143781
  AAPL 0.0014253135 0.001661925 0.0006517374 0.0003698716 0.0004133538
## NVDA 0.0025172928 0.002935180 0.0011510547 0.0006532423 0.0007300377
  TSLA 0.0008958871 0.001044610 0.0004096524 0.0002324844 0.0002598154
  MSFT 0.0015387061 0.001794142 0.0007035871 0.0003992972 0.0004462387
  AMD 0.0041497221 0.004838604 0.0018974976 0.0010768609 0.0012034570
                 PEP
                             MDLZ
                                            ΚO
##
                                                         EL
## TSM 0.0007674481 0.0009217195 0.0006428420 0.0007250195
## AAPL 0.0007655511 0.0009194412 0.0006412530 0.0007232273
## NVDA 0.0013520648 0.0016238551 0.0011325378 0.0012773154
## TSLA 0.0004811905 0.0005779188 0.0004030624 0.0004545877
## MSFT 0.0008264554 0.0009925884 0.0006922686 0.0007807645
## AMD 0.0022288600 0.0026769025 0.0018669729 0.0021056366
```

```
Rf <- 0.002
R_ibar <- colMeans(rr)</pre>
R <- R_ibar-Rf
R ibar
##
             TSM
                         AAPL
                                       NVDA
                                                     TSLA
                                                                   MSFT
                                                                                  AMD
##
    0.018022831
                  0.017597560
                                0.044567996
                                             0.016879280
                                                            0.020687995
                                                                         0.043437846
##
           GOOG
                            FB
                                       NFLX
                                                     TWTR
                                                                    CHT
                                                                                CMCSA
                                0.034101355 -0.003696091
##
    0.011206214
                  0.014473364
                                                           0.007410518
                                                                         0.006931851
##
             PLD
                          AMT
                                        CCI
                                                      PSA
                                                                   EQIX
##
    0.011089250
                  0.014264652
                                0.011227455
                                             0.008176040
                                                            0.015260709
                                                                         0.009094911
             JNJ
                          UNH
                                        MRK
                                                      ABT
                                                                   ABBV
##
                                                                                  AZN
                                                                         0.008827518
    0.009525905
                  0.023671961
                                0.010107381
                                              0.015006148
                                                            0.016591625
##
##
             WMT
                           PG
                                        PEP
                                                     MDLZ
                                                                     ΚO
##
    0.007404403
                  0.006624564
                                0.008565794
                                             0.006095891
                                                           0.007265480
                                                                         0.013236073
df <- data.frame(matrix(ncol=6,nrow=0))</pre>
df <- cbind(colnames(rr),alpha2,beta2,R_ibar,sigma_e2,(R_ibar - Rf)/beta2)</pre>
df = data.frame(df)
colnames(df) <- c("stock", "alpha", "beta", "expected return of stock", "sigma^2", "excess return to beta ra
df = df[order(df$`excess return to beta ratio`,decreasing=TRUE),]
df = cbind(df,(R_ibar-Rf)*beta2/sigma_e2,cumsum((R_ibar-Rf)*beta2/sigma_e2),beta2^2/sigma_e2,cumsum(bet
df <- cbind(df,(sigma_m2*df$`cumsum((R_ibar - Rf) * beta2/sigma_e2)`)/(1+sigma_m2*df$`cumsum(beta2^2/si
colnames(df) <- c("stock", "alpha", "beta", "expected return of stock", "sigma^2", "excess return to beta ra
#if short sales allowed:
C_star_allowed <- df$C[length(df$C)]</pre>
#if short sales not allowed
C_star <- df$C[which(df$`excess return to beta ratio` > df$C)[length(which(df$`excess return to beta ra
  a.
df
##
         stock
                                alpha
                                                    beta expected return of stock
```

```
## CHT
           CHT
                0.00669263907115864 0.114319164853984
                                                             0.00741051846790379
          NFLX
                 0.0264490179120803 1.21860131508328
## NFLX
                                                              0.0341013549289067
## UNH
           UNH
                 0.0182979847323322  0.855782220524718
                                                              0.0236719605219577
## WELL
          WELL
                0.00708519669666882 0.320038264897381
                                                             0.00909491113810431
## CCI
           CCI
                0.00850768680190838 \quad 0.43311118812552
                                                              0.0112274547327908
## NVDA
          NVDA
                 0.0317618618371258 2.03932104594676
                                                              0.0445679959976041
## TSLA
          TSLA
                  0.012321665289032 0.725780263879404
                                                              0.0168792799170672
## PSA
           PSA
                 0.0062233532243196 0.310956795445091
                                                             0.00817603960908326
           AMT
                 0.0102125141479574 0.645285339536314
## AMT
                                                              0.0142646523075258
## FB
            FΒ
                 0.0100819626761704 0.699311446269394
                                                              0.0144733635390621
## EQIX
          EQIX
                 0.0105575103587186 0.74896393799576
                                                              0.0152607093427123
## EL
                0.00920985493494317 0.641157624276606
                                                              0.0132360726659958
## WMT
           WMT
                0.00534532228914836 0.327899680310383
                                                             0.00740440332770216
## MSFT
          MSFT
                 0.0128601907820131 1.24654376313014
                                                              0.0206879953835887
## TSM
           TSM
                 0.0107539159973098
                                     1.15754297987532
                                                              0.0180228306815699
          AAPL
## AAPL
                 0.0103466129290547
                                     1.15468167334493
                                                               0.017597559733576
            PG
## PG
                 0.0043234164772652 0.36644768499596
                                                             0.00662456382538972
```

```
## AMD
           AMD
                 0.0223271122321973 3.36179235105671
                                                               0.0434378460977005
           AZN
                 0.0051992860102525 0.577780172496018
                                                              0.00882751826870652
##
  A 7.N
                0.00525489157321153 0.680140337002439
   JNJ
           JNJ
                                                              0.00952590540936918
## MRK
           MRK
                0.00532643189611972 0.761345276707195
                                                               0.0101073808179862
##
   ABT
           ABT
                0.00707140541624719
                                      1.26357320932821
                                                               0.0150061482427406
                0.00733966128709105
   ABBV
          ABBV
                                      1.47333490790803
                                                               0.0165916250872423
##
                    0.00430395919008 0.678678633758669
##
  PEP
           PEP
                                                              0.00856579410471387
## PI.D
           PLD
                 0.0050511628986216
                                        0.9615390329351
                                                               0.0110892498789807
##
  ΚO
            ΚO
                0.00369561494741026 0.568485507793538
                                                              0.00726548036686501
##
  GOOG
          GOOG
                0.00452021588076655
                                      1.06471610489039
                                                               0.0112062142963412
  MDLZ
          MDLZ 0.000977347440130093 0.815105726862176
                                                              0.00609589084648479
   CMCSA CMCSA 0.000200296894146275
##
                                      1.07197058062099
                                                              0.00693185056432624
##
   TWTR.
          TWTR -0.00525511449052535 0.248267714738308
                                                             -0.00369609087873399
##
                      sigma^2 excess return to beta ratio
                                                                   Col1
                                                                              Col2
##
  CHT
                                                             6.61985098
                                                                          6.619851
         0.00106915625998746
                                        0.0473281839909736
##
   NFLX
          0.0160932997123741
                                        0.0263427870391827
                                                             4.58669520
                                                                         11.206546
                                                                         19.502108
##
  UNH
         0.00161779675597616
                                        0.0253241537416723
                                                             8.29556175
   WELL
         0.00340553940263042
                                        0.0221689463926423
                                                             0.79890079
                                                                         20.301009
  CCI
##
         0.00194912078269453
                                        0.021305048185725
                                                           10.83933856
                                                                         31.140347
## NVDA
          0.0104646089943664
                                        0.0208736118730348
                                                            7.18459591
                                                                         38.324943
##
  TSLA
          0.0135174326719554
                                        0.0205010809160547
                                                             4.33616091
                                                                         42.661104
## PSA
         0.00232965769528159
                                        0.0198614074352134
                                                             2.58670674
                                                                         45.247811
## AMT
                                        0.0190065565666483
         0.00224311178209009
                                                             2.43074783
                                                                         47.678559
##
  FB
         0.00337215106808481
                                        0.0178366357444935
                                                           -0.06961827
                                                                         47.608940
##
  EQIX
         0.00242827072727569
                                        0.0177054043191962
                                                             0.57851782
                                                                         48.187458
##
  EL
         0.00228875970907348
                                        0.0175246651378014
                                                             2.25682645
                                                                         50.444285
  WMT
         0.00287786636238358
##
                                        0.0164818804415621
                                                             4.66274557
                                                                         55.107030
##
  MSFT
         0.00214915365616709
                                        0.0149918486108037
                                                             3.52822378
                                                                         58.635254
         0.00280174209968681
                                                             2.05041879
##
  TSM
                                        0.0138421043193539
                                                                         60.685673
## AAPL
         0.00392662158494458
                                        0.0135081036563024
                                                             0.82436209
                                                                         61.510035
## PG
         0.00149812400535767
                                        0.0126199837377625
                                                             4.09006829
                                                                         65.600103
##
   AMD
           0.019389459862153
                                        0.0123261170740291
                                                             0.66674990
                                                                         66.266853
##
   AZN
          0.0041817551179446
                                        0.0118168095648065
                                                             4.52672066
                                                                         70.793574
##
   JNJ
         0.00113076821477706
                                        0.0110652243366977 11.46403492
                                                                         82.257609
  MRK
          0.0019495052350728
                                        0.0106487569648431
                                                             3.16619621
##
                                                                         85.423805
  ABT
                                                           10.30785601
##
         0.00159433935288406
                                        0.0102931497334099
                                                                         95.731661
   ABBV
         0.00378792990865251
                                      0.00990380734816146
                                                             5.67548796 101.407149
## PEP
                                      0.00967437867956898
                                                             0.94333708 102.350486
         0.00119585975184197
  PLD
         0.00187436101741367
                                                             0.61576943 102.966255
##
                                      0.00945281425678135
          0.0011272920141441
## KO
                                      0.00926229480730637
                                                             1.13118854 104.097444
   GOOG
         0.00226052603629044
                                      0.00864663759104967
                                                             3.72624312 107.823687
  MDLZ
          0.0019289030498278
                                                             1.73082006 109.554507
##
                                      0.00502498106871644
   CMCSA 0.00234258097732937
                                      0.00460073312969953
                                                             2.65534506 112.209852
##
   TWTR.
          0.0203129932936262
                                      -0.0229433411619311
                                                            3.14759720 115.357449
##
                Co13
                           Co14
## CHT
                       478.2402 0.004407674
          478.240217
##
  NFLX
          339.551377
                      817.7916 0.006085740
## UNH
          397.418607 1215.2102 0.008710723
## WELL
           38.968716 1254.1789 0.008912431
##
  CCI
          723.015476 1977.1944 0.010377189
          582.875846 2560.0702 0.010694173
##
  NVDA
## TSLA
          501.485214 3061.5555 0.010442825
## PSA
          145.022121 3206.5776 0.010696302
## AMT
           92.273753 3298.8513 0.011030312
```

```
## FB
            3.034356 3301.8857 0.011006480
           12.223537 3314.1092 0.011108832
## EQIX
          490.536266 3804.6455 0.010447634
## EL
          493.265333 4297.9108 0.010355423
## WMT
## MSFT
          185.631930 4483.5427 0.010647028
           96.240984 4579.7837 0.010830083
## TSM
           41.505724 4621.2895 0.010896488
## AAPL
## PG
          231.006771 4852.2962 0.011164173
## AMD
           30.075850 4882.3721 0.011220214
## AZN
          409.094341 5291.4664 0.011210174
##
  JNJ
          452.691728 5744.1581 0.012154243
## MRK
          297.330123 6041.4883 0.012090886
## ABT
         1001.428744 7042.9170 0.011867705
## ABBV
          573.061224 7615.9782 0.011737441
## PEP
           79.830100 7695.8083 0.011738168
## PLD
           37.360387 7733.1687 0.011758406
           89.634707 7822.8034 0.011767136
## KO
## GOOG
          385.166143 8207.9696 0.011679821
          344.443100 8552.4127 0.011440452
## MDLZ
## CMCSA
          286.683280 8839.0960 0.011377139
## TWTR
          179.609549 9018.7055 0.011487089
\# C\_star \leftarrow df C[nrow(df)]
# C_star
\#z \leftarrow (as.numeric(df\$beta) / as.numeric(df\$`sigma^2`)) * (as.numeric(df\$`excess return to beta ratio`)
# # 2
\# alloc \leftarrow z / sum(z)
# names(alloc) <- row.names(df)</pre>
# alloc <- alloc[colnames(rrr)] #reordering stocks</pre>
# alloc
# sigma_m2 * (alloc%*%beta2) * ((alloc %*% colMeans(rrr) - Rf)/ (alloc%*%covmat %*% alloc))
  b.
```

If short sales are allowed, the answer of the composition matches the  $z_i$  and  $x_i$  computed from covariance matrix of single index model in project 4, which is a good way to double check our work.

```
z_i_allowed <- (beta2/sigma_e2)*(((R_ibar - Rf)/beta2)-C_star_allowed)
x_i_allowed <- z_i_allowed/sum(z_i_allowed)
x_i_allowed</pre>
```

```
##
             TSM
                          AAPL
                                        NVDA
                                                      TSLA
                                                                     MSFT
                                                                                    AMD
                  0.033687943
                                0.103688140
##
    0.055152410
                                              0.027434045
                                                             0.115228543
                                                                           0.008246005
            GOOG
                            FΒ
                                        NFLX
                                                      TWTR
                                                                      CHT
##
                                                                                  CMCSA
   -0.075835640
                  0.074639392
                                0.063763382
                                              -0.023853411
##
                                                             0.217230531
                                                                          -0.178623842
##
             PLD
                           AMT
                                         CCI
                                                       PSA
                                                                     EQIX
                                                                                   WELL
##
   -0.059154112
                  0.122616728
                                0.123664093
                                              0.063360582
                                                             0.108717210
                                                                           0.056901605
                           UNH
                                         MRK
                                                                     ABBV
##
             JNJ
                                                       ABT
                                                                                    AZN
   -0.014383331
                  0.414901508
                               -0.018558158 -0.053636878 -0.034907550
                                                                           0.002582333
##
                            PG
                                         PEP
##
             WMT
                                                      MDLZ
                                                                       ΚO
                                                                                     EL
    0.032258895
                  0.015707810 -0.058314155 -0.154788774 -0.063596685
##
                                                                           0.095871382
```

If short sales are not allowed, the answer is a little different compared to when short sales are allowed.

```
z_i <- (beta2/sigma_e2)*(((R_ibar - Rf)/beta2)-C_star)
x_i <- z_i/sum(z_i)
x_i</pre>
```

```
AAPL
                                        NVDA
                                                       TSLA
                                                                     MSFT
                                                                                     AMD
##
             TSM
                                                                            0.009534856
                                 0.092802810
##
    0.053585865
                  0.033300200
                                               0.024583059
                                                              0.108091390
##
            GOOG
                            FΒ
                                        NFLX
                                                       TWTR
                                                                      CHT
                                              -0.020570677
                                                              0.190313037
##
   -0.059501874
                  0.067719257
                                 0.056467341
                                                                           -0.149045831
##
             PLD
                           AMT
                                          CCI
                                                        PSA
                                                                     EQIX
                                                                                    WELL
##
   -0.044426406
                  0.110525095
                                 0.110542284
                                               0.056905316
                                                             0.098724566
                                                                            0.050751020
##
             JNJ
                           UNH
                                         MRK
                                                        ABT
                                                                     ABBV
                                                                                     A 7.N
   -0.004296439
##
                  0.367921916
                                -0.010804623
                                              -0.035815191
                                                            -0.025039834
                                                                            0.004130464
##
             WMT
                            PG
                                          PEP
                                                       MDLZ
                                                                       KO
                                                                                      EL
    0.029599779
                  0.016993844 -0.042952070 -0.128802310 -0.048407407
                                                                            0.087170562
```

```
cov.matrix <- cov(rr)
# cov.matrix <- covmat
head(cov.matrix)</pre>
```

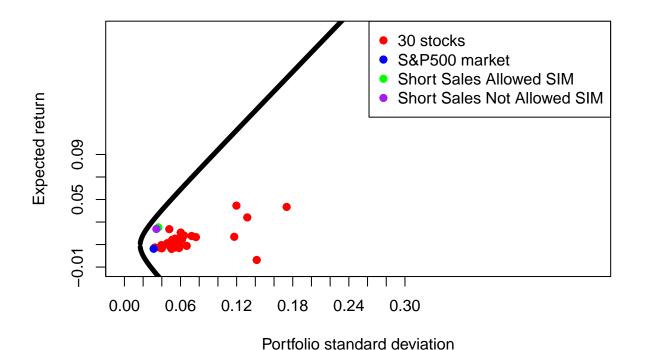
```
##
                 TSM
                                        NVDA
                                                     TSLA
                                                                 MSFT
                                                                               AMD
                            AAPI.
## TSM 4.062383e-03 0.002235268 0.003919135 1.761271e-05 0.002154460 0.003203961
  AAPL 2.235268e-03 0.005161405 0.004010693 1.122055e-03 0.001680854 0.003179227
## NVDA 3.919135e-03 0.004010693 0.014346924 1.283192e-03 0.003192779 0.008661374
  TSLA 1.761271e-05 0.001122055 0.001283192 1.379896e-02 0.000708004 0.001037054
  MSFT 2.154460e-03 0.001680854 0.003192779 7.080040e-04 0.003630068 0.003246639
       3.203961e-03 0.003179227 0.008661374 1.037054e-03 0.003246639 0.030095678
  AMD
##
##
                GOOG
                               FΒ
                                         NFLX
                                                        TWTR
                                                                       CHT
       0.0015376332 0.0003612575 0.001943573 -4.434180e-04
## TSM
                                                             6.051009e-04
  AAPL 0.0012326992 0.0014249149 0.002563224
                                               2.593836e-03
                                                             4.940016e-04
## NVDA 0.0028003856 0.0014930262 0.005548375
                                               1.655664e-03
                                                             5.575223e-04
  TSLA 0.0005932909 0.0016592685 0.004010646 3.328376e-03
## MSFT 0.0020387217 0.0011207815 0.002528836 -8.821019e-05 -8.969531e-05
##
  AMD
       0.0029380051 0.0013884886 0.003750453 -1.517128e-03
                                                             5.058177e-04
              CMCSA
                                          AMT
                                                        CCI
##
                             PLD
                                                                      PSA
## TSM 0.001076460 0.0009981227 0.0010760083 0.0008552944
                                                            0.0001515250
  AAPL 0.001077286 0.0010545360 0.0014286508 0.0010344209
                                                            0.0007972601
## NVDA 0.001953092 0.0017343381 0.0001402959 0.0008479314
                                                            0.0001404484
## TSLA 0.001270848 0.0006290024 0.0009779647 0.0004549391
                                                            0.0004264907
## MSFT 0.001320988 0.0008251445 0.0010978204 0.0004660815
                                                            0.0001267023
  AMD
       0.002001670 0.0032649395 0.0015374327 0.0009738502 -0.0004054600
##
                EQIX
                              WELL
                                            JNJ
                                                         UNH
                                                                       MR.K
       0.0011843750
                      0.0005110208 0.0010428388 0.0006578176 0.0005272151
## AAPL 0.0006032473 0.0004997238 0.0005154489 0.0006846134 0.0004479273
## NVDA 0.0016894839 -0.0007364419 0.0004849562 0.0012461212 0.0003987402
## TSLA 0.0007740256 0.0012794605 0.0003924294 0.0010561565 0.0011217768
  MSFT 0.0013832868 -0.0003809920 0.0008626523 0.0004447379 0.0005797887
##
  AMD
       0.0008964220 0.0019107934 0.0020786828 0.0027784858 0.0030233136
                ABT
                            ABBV
                                          AZN
                                                        WMT
                                                                       PG
## TSM 0.001674696 0.0012514596 0.0011850485 0.0009413284
                                                            0.0005699788
## AAPL 0.001611777 0.0004922211 0.0008394886 0.0005540373 0.0004034379
## NVDA 0.001839648 0.0023327039 0.0015171674 0.0006993916 -0.0003451880
```

```
## TSLA 0.001395675 0.0018691396 0.0010940279 0.0004265306 0.0003930886
## MSFT 0.001398956 0.0017604554 0.0005761039 0.0002996365 0.0004647966
## AMD 0.004380990 0.0051427873 0.0015933901 0.0003671012 0.0011154614
##
                             MDLZ
                PEP
                                            ΚO
## TSM 8.520290e-04 0.0008830470 0.0010329745 0.0008296615
## AAPL 6.388837e-04 0.0005647143 0.0004636284 0.0008682439
## NVDA 4.435509e-05 0.0008611732 0.0005856416 0.0008070263
## TSLA 5.669415e-04 0.0007998516 0.0009833035 0.0006976679
## MSFT 8.467819e-04 0.0012020212 0.0009873010 0.0006016497
## AMD 1.554610e-03 0.0015754280 0.0008582701 0.0007572661
ones \leftarrow rep(1,30)
A <- t(ones) %*% solve(cov.matrix) %*% R_ibar
##
          [,1]
## [1,] 33.11504
B <- t(R_ibar) %*% solve(cov.matrix) %*% R_ibar
##
            [,1]
## [1,] 1.049438
C <- t(ones) %*% solve(cov.matrix) %*% ones</pre>
##
            [,1]
## [1,] 3530.478
D \leftarrow B*C - A^2
D
            [,1]
## [1,] 2608.411
Sigma30 <- cov(rr)
head(Sigma30)
                                        NVDA
##
                 TSM
                            AAPL
                                                     TSLA
                                                                 MSFT
## TSM 4.062383e-03 0.002235268 0.003919135 1.761271e-05 0.002154460 0.003203961
## AAPL 2.235268e-03 0.005161405 0.004010693 1.122055e-03 0.001680854 0.003179227
## NVDA 3.919135e-03 0.004010693 0.014346924 1.283192e-03 0.003192779 0.008661374
## TSLA 1.761271e-05 0.001122055 0.001283192 1.379896e-02 0.000708004 0.001037054
## MSFT 2.154460e-03 0.001680854 0.003192779 7.080040e-04 0.003630068 0.003246639
## AMD 3.203961e-03 0.003179227 0.008661374 1.037054e-03 0.003246639 0.030095678
                GOOG
                                                       TWTR
##
                               FΒ
                                         NFLX
## TSM 0.0015376332 0.0003612575 0.001943573 -4.434180e-04 6.051009e-04
## AAPL 0.0012326992 0.0014249149 0.002563224 2.593836e-03 4.940016e-04
```

```
## NVDA 0.0028003856 0.0014930262 0.005548375 1.655664e-03 5.575223e-04
## TSLA 0.0005932909 0.0016592685 0.004010646 3.328376e-03 2.849212e-04
## MSFT 0.0020387217 0.0011207815 0.002528836 -8.821019e-05 -8.969531e-05
        0.0029380051 0.0013884886 0.003750453 -1.517128e-03 5.058177e-04
              CMCSA
                             D.Id
                                           AMT
                                                        CCT
## TSM 0.001076460 0.0009981227 0.0010760083 0.0008552944
                                                             0.0001515250
## AAPL 0.001077286 0.0010545360 0.0014286508 0.0010344209
                                                             0.0007972601
## NVDA 0.001953092 0.0017343381 0.0001402959 0.0008479314
                                                             0.0001404484
## TSLA 0.001270848 0.0006290024 0.0009779647 0.0004549391
                                                             0.0004264907
## MSFT 0.001320988 0.0008251445 0.0010978204 0.0004660815
                                                             0.0001267023
        0.002001670 \ 0.0032649395 \ 0.0015374327 \ 0.0009738502 \ -0.0004054600
##
                EQIX
                               WELL
                                             JNJ
                                                          UNH
## TSM 0.0011843750 0.0005110208 0.0010428388 0.0006578176 0.0005272151
## AAPL 0.0006032473 0.0004997238 0.0005154489 0.0006846134 0.0004479273
## NVDA 0.0016894839 -0.0007364419 0.0004849562 0.0012461212 0.0003987402
## TSLA 0.0007740256 0.0012794605 0.0003924294 0.0010561565 0.0011217768
## MSFT 0.0013832868 -0.0003809920 0.0008626523 0.0004447379 0.0005797887
        0.0008964220 0.0019107934 0.0020786828 0.0027784858 0.0030233136
                ABT
##
                            ABBV
                                           AZN
                                                        WMT
                                                                        PG
## TSM
       0.001674696 0.0012514596 0.0011850485 0.0009413284
                                                             0.0005699788
## AAPL 0.001611777 0.0004922211 0.0008394886 0.0005540373
                                                             0.0004034379
## NVDA 0.001839648 0.0023327039 0.0015171674 0.0006993916 -0.0003451880
## TSLA 0.001395675 0.0018691396 0.0010940279 0.0004265306
                                                             0.0003930886
## MSFT 0.001398956 0.0017604554 0.0005761039 0.0002996365
                                                             0.0004647966
       0.004380990 0.0051427873 0.0015933901 0.0003671012 0.0011154614
                 PEP
                             MDLZ
                                             KO
## TSM 8.520290e-04 0.0008830470 0.0010329745 0.0008296615
## AAPL 6.388837e-04 0.0005647143 0.0004636284 0.0008682439
## NVDA 4.435509e-05 0.0008611732 0.0005856416 0.0008070263
## TSLA 5.669415e-04 0.0007998516 0.0009833035 0.0006976679
## MSFT 8.467819e-04 0.0012020212 0.0009873010 0.0006016497
## AMD 1.554610e-03 0.0015754280 0.0008582701 0.0007572661
sdev30 <- (diag(Sigma30))^.5</pre>
sdev30
                    AAPL
                                NVDA
                                           TSLA
                                                      MSFT
                                                                   AMD
                                                                             GOOG
          TSM
## 0.06373683 0.07184292 0.11977864 0.11746897 0.06025004 0.17348106 0.05769731
                    NFLX
                                TWTR
                                            CHT
                                                     CMCSA
                                                                  PLD
           FB
                                                                              AMT
## 0.06157717 0.13140208 0.14150259 0.03261119 0.05852146 0.05239503 0.05110000
          CCT
                     PSA
                               EQIX
                                           WELL
                                                       JNJ
                                                                  UNH
                                                                              MRK
  0.04581229 0.04882572 0.05417001 0.05871015 0.03953700 0.04801401 0.04982115
                                AZN
                                                        PG
##
          ABT
                    ABBV
                                            WMT
                                                                  PEP
                                                                             MDI.7.
## 0.05591581 0.07644070 0.06660160 0.05415978 0.04004342 0.04031382 0.05044494
                      EL
##
           ΚO
## 0.03773016 0.05148673
sdev_m = sigma_m2^{.5}
R m = mean(index)
R_allowed_SIM <- t(x_i_allowed) %*% R_ibar</pre>
sdev_allowed_SIM <- (t(x_i_allowed) %*% covmat %*% x_i_allowed)^.5</pre>
R_not_allowed_SIM <- t(x_i) %*% R_ibar</pre>
sdev_not_allowed_SIM <- (t(x_i) %*% covmat %*% x_i)^.5</pre>
```

```
popo = x_i
  b.
#Hyperbola:
#Efficient frontier:
    minvar <- 1/C
    minE <- A/C
    sdeff \leftarrow seq((minvar)^0.5, 1, by = 0.0001)
## Warning in from + (OL:n) * by: Recycling array of length 1 in array-vector arithmetic is deprecated.
    Use c() or as.vector() instead.
   options(warn = -1)
    y1 \leftarrow (A + sqrt(D*(C*sdeff^2 - 1)))*(1/C)
## Warning in C * sdeff^2: Recycling array of length 1 in array-vector arithmetic is deprecated.
    Use c() or as.vector() instead.
## Warning in D * (C * sdeff^2 - 1): Recycling array of length 1 in array-vector arithmetic is deprecat
    Use c() or as.vector() instead.
## Warning in sqrt(D * (C * sdeff^2 - 1)): NaNs produced
\#\# Warning in A + sqrt(D * (C * sdeff^2 - 1)): Recycling array of length 1 in array-vector arithmetic i
    Use c() or as.vector() instead.
## Warning in (A + \text{sqrt}(D * (C * \text{sdeff}^2 - 1))) * (1/C): Recycling array of length 1 in vector-array ar
   Use c() or as.vector() instead.
    y2 <- (A - sqrt(D*(C*sdeff^2 - 1)))*(1/C)
## Warning in C * sdeff^2: Recycling array of length 1 in array-vector arithmetic is deprecated.
    Use c() or as.vector() instead.
## Warning in D * (C * sdeff^2 - 1): Recycling array of length 1 in array-vector arithmetic is deprecat
     Use c() or as.vector() instead.
##
## Warning in sqrt(D * (C * sdeff^2 - 1)): NaNs produced
## Warning in A - sqrt(D * (C * sdeff^2 - 1)): Recycling array of length 1 in array-vector arithmetic i
    Use c() or as.vector() instead.
## Warning in (A - \text{sqrt}(D * (C * \text{sdeff}^2 - 1))) * (1/C): Recycling array of length 1 in vector-array ar
    Use c() or as.vector() instead.
```

```
options(warn = 0)
# plot(sdeff, y1, type = "n", xlim=c(0,0.3), ylim=c(-0.05,0.10), xlab="Portfolio standard deviation", ylim=c(-0.05,0.10)
plot(sdeff, y1, type = "n", xlim=c(0,0.5), ylim=c(-0.01,0.2), xlab="Portfolio standard deviation", ylab=
axis(1, at=seq(0, 0.3, 0.02))
axis(2, at=seq(-0.05, 0.10, 0.02))
    points(sdeff, y1, lwd=5,type = "1")
    points(sdeff, y2, lwd=5,type = "1")
    #min risk portfolio
    # points(sqrt(1/C), A/C, pch=19, col = "yellow")
    # #investors expected return portfolio
    # points(sd1,R1bar, pch = 19, col = "blue")
    #30 stocks
    points(sdev30,R_ibar, pch=19, col = "red")
    points(sdev_m,R_m,pch=19,col="blue")
    points(sdev_allowed_SIM, R_allowed_SIM,pch=19, col = "green")
    points(sdev_not_allowed_SIM,R_not_allowed_SIM, pch =19, col="purple")
    legend("topright",c("30 stocks", "S&P500 market", "Short Sales Allowed SIM", "Short Sales Not Allowed "
```



# #random weights
# # points(sd\_bar, r\_bar, pch=19, col = "green")
# points(sd\_bar, rp\_bar, pch=19, col = "green")
# #equal allocation portfolio
# points(sdp30\_equal, Rp30\_equal, pch=19, col="purple")

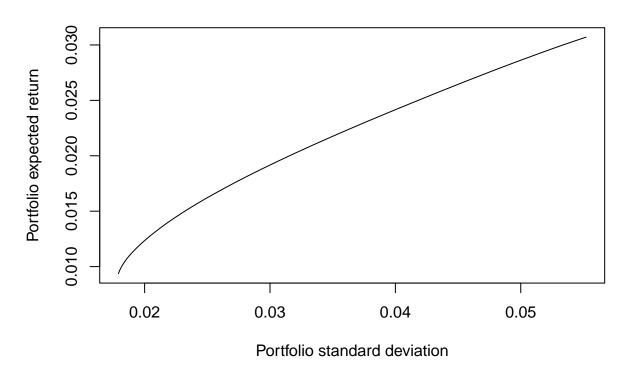
c.

```
a <- read.csv("stockDataTrain.csv", sep=",", header=TRUE)
r <- (train[-1,3:ncol(train)]-train[-nrow(train),3:ncol(train)])/train[-nrow(train),3:ncol(train)]
# #Stocks used:
# #Data
# 2015-01-31 to 2019-12-31
#Compute the betas:
covmat <- var(r)</pre>
beta <- covmat[1,-1] / covmat[1,1]
#Keep only the stocks with positive betas:
rrr \leftarrow r[,-c(1,which(beta\lt0)+1)]
#Note: which(beta<0) gives the element in the beta vector with negative beta and add 1 because
#the first column in the initial data set is the index. We also remove column 1 (index) from the initi
Rfr \leftarrow seq(-0.05,.01,0.0005)
#Initialize the two vectors:
rbar_opt <- rep(0,length(Rfr))</pre>
risk_opt <- rep(0,length(Rfr))</pre>
for(l in 1:length(Rfr)){
#Risk free asset:
rf <- Rfr[1]
#rf <- .002
\#Initialize
beta <- rep(0,ncol(rrr))</pre>
alpha <- rep(0,ncol(rrr))</pre>
mse <- rep(0,ncol(rrr))</pre>
Ribar <- rep(0,ncol(rrr))</pre>
Ratio <- rep(0,ncol(rrr))</pre>
stocknum <- rep(0,ncol(rrr))</pre>
#stock <- names(rrr)</pre>
#This for loop computes the required inputs:
for(i in 1:ncol(rrr)){
    q <- lm(data=rrr, formula=rrr[,i] ~ r[,1])</pre>
    beta[i] <- q$coefficients[2]</pre>
    alpha[i] <- q$coefficients[1]</pre>
     mse[i] <- summary(q)$sigma^2</pre>
    Ribar[i] <- q$coefficients[1]+q$coefficients[2]*mean(r[,1])</pre>
    Ratio[i] <- (Ribar[i]-rf)/beta[i]</pre>
    stocknum[i] <- i</pre>
}
```

```
#So far we have this table:
#xx <- (cbind(stock,alpha, beta, Ribar, mse, Ratio))</pre>
xx <- (data.frame(stocknum,alpha, beta, Ribar, mse, Ratio))
#Order the table based on the excess return to beta ratio:
A <- xx[order(-xx[,6]),]
col1 <- rep(0,nrow(A))</pre>
col2 <- rep(0,nrow(A))</pre>
col3 <- rep(0,nrow(A))</pre>
col4 <- rep(0,nrow(A))</pre>
col5 <- rep(0,nrow(A))</pre>
#Create the last 5 columns of the table:
col1 \leftarrow (A[,4]-rf)*A[,3]/A[,5]
col3 \leftarrow A[,3]^2/A[,5]
for(i in(1:nrow(A))) {
col2[i] <- sum(col1[1:i])</pre>
col4[i] \leftarrow sum(col3[1:i])
}
#So far we have:
cbind(A, col1, col2, col3, col4)
#Compute the Ci (col5):
for(i in (1:nrow(A))) {
col5[i] \leftarrow var(r[,1])*col2[i]/(1+var(r[,1])*col4[i])
}
#The final table when short sales allowed:
B <- cbind(A, col1, col2, col3, col4, col5)</pre>
rownames(B) <- NULL
#SHORT SALES NOT ALLOWED:
#First create a matrix up to the maximum of col5:
\#table1 \leftarrow cbind(A, col1, col2, col3, col4, col5)
\#table2 <- (B[1:which(col5==max(col5)), ], nrow=which(col5==max(col5)), ncol=ncol(B))
table2 <- B[1:which(col5==max(col5)), ]</pre>
#Compute the Zi:
z_{no\_short} \leftarrow (table2[,3]/table2[,5])*(table2[,6]-max(col5))
#Compute the xi:
x_no_short <- z_no_short/sum(z_no_short)</pre>
#Compute the mean and variance for each portfolio when short sales not allowed:
#First match the columns of the data with the composition of the portfolio:
r1 <- data.frame(rrr[,table2[,1]])</pre>
```

```
beta1 <- rep(0,ncol(r1))</pre>
sigma_e1 <- rep(0,ncol(r1))</pre>
alpha1 <- rep(0,ncol(r1))</pre>
for(i in 1:ncol(r1)){
    q1<- lm(r1[,i] ~ r[,1])
beta1[i] <- q1$coefficients[2]</pre>
sigma_e1[i] <- summary(q1)$sigma^2</pre>
alpha1[i] <- q1$coefficients[1]</pre>
means1 <- colMeans(r1)</pre>
\#means1 \leftarrow alpha1 + beta1*mean(r[,1])
#Construct the variance covariance matrix using SIM:
xx <- rep(0,ncol(r1)*(ncol(r1)))</pre>
                                               \#Initialize
varcovar <- matrix(xx,nrow=ncol(r1),ncol=ncol(r1)) #the variance covariance matrix</pre>
for (i in 1:ncol(r1)){
    for (j in 1:ncol(r1)){
        varcovar[i,j]=beta1[i]*beta1[j]*var(r[,1])
        if(i==j){varcovar[i,j]=beta1[i]^2*var(r[,1])+ sigma_e1[i]}
        }
rbar_opt[1] <- t(x_no_short) %*% means1</pre>
risk_opt[1] <- ( t(x_no_short) %*% varcovar %*% x_no_short )^.5</pre>
}
plot(risk_opt, rbar_opt, type="l", main="Efficient frontier when short sales not allowed", ylab="Portfo")
```

# Efficient frontier when short sales not allowed



In part a, we used Rf <- 0.002

 $\mathrm{d}.$ 

```
#CONSTANT CORRELATION MODEL - EXAMPLE:
#Read the data:
data1 <- rrr
#Compute the average correlation:
rho \leftarrow (sum(cor(data1[1:30]))-30)/(30*29)
#Initialize the vectors:
col1 \leftarrow rep(0,30)
col2 \leftarrow rep(0,30)
col3 \leftarrow rep(0,30)
#Initialize the var-covar matrix:
y \leftarrow rep(0,30*30)
mat <- matrix(y, ncol=30, nrow=30)</pre>
#Compute necessary quantities:
Rbar <- colMeans(data1[1:30])</pre>
Rbar_f <- Rbar-0.0002</pre>
sigma <- ( diag(var(data1[1:30])) )^0.5</pre>
Ratio <- Rbar_f/sigma
```

```
#Initial table:
xx <- (cbind(Rbar, Rbar_f, sigma, Ratio))</pre>
#Order the table based on the excess return to sigma ratio:
aaa <- xx[order(-Ratio),]</pre>
#Create the last 3 columns of the table:
for(i in(1:30)) {
          col1[i] <- rho/(1-rho+i*rho)</pre>
          col2[i] <- sum(aaa[,4][1:i])</pre>
               }
#Compute the Ci:
for(i in (1:30)) {
           col3[i] <- col1[i]*col2[i]</pre>
                }
#Create the entire table until now:
xxx <- cbind(aaa, col1, col2, col3)</pre>
#SHORT SALES ALLOWED:
#Compute the Zi:
z \leftarrow (1/((1-\text{rho})*xxx[,3]))*(xxx[,4]-xxx[,7][nrow(xxx)])
#Compute the xi:
x \leftarrow z/sum(z)
#The final table:
aaaa <- cbind(xxx, z, x)</pre>
#SHORT SALES NOT ALLOWED:
#Find composition of optimum portfolio when short sales are not allowed:
aaaaa \leftarrow aaaa[1:which(aaaa[,7]==max(aaaa[,7])), ]
z_{no} \leftarrow (1/((1-rho)*aaaaa[,3]))*(aaaaa[,4]-aaaaa[,7][nrow(aaaaa)])
x_{no} \leftarrow z_{no}/sum(z_{no})
#Final table:
a_no <- cbind(aaaaa, z_no, x_no)
```

final table for short sales allowed

### aaaa

```
## UNH 0.023671961 0.023471961 0.04801401 0.48885647 0.21968758 0.4888565

## NVDA 0.044567996 0.044367996 0.11977864 0.37041658 0.18011791 0.8592730

## MSFT 0.020687995 0.020487995 0.06025004 0.34004946 0.15262704 1.1993225

## TSM 0.018022831 0.017822831 0.06373683 0.27963160 0.13241668 1.4789541
```

```
0.015260709  0.015060709  0.05417001  0.27802670  0.11693282  1.7569808
                      0.014064652 0.05110000 0.27523783 0.10469101 2.0322186
## AMT
          0.014264652
## ABT
          0.015006148
                       0.014806148 0.05591581
                                               0.26479360 0.09476949 2.2970122
## NFLX
          0.034101355
                      0.033901355 0.13140208
                                              0.25799709 0.08656571 2.5550093
## EL
          0.013236073
                       0.013036073 0.05148673
                                               0.25319287 0.07966909 2.8082022
                      0.043237846 0.17348106
                                               0.24923670 0.07379029 3.0574389
## AMD
          0.043437846
## AAPL
          0.017597560
                       0.017397560 0.07184292
                                               0.24216110 0.06871946 3.2996000
## CCI
          0.011227455
                       0.011027455 0.04581229
                                               0.24070951 0.06430075 3.5403095
## JNJ
          0.009525905
                       0.009325905 0.03953700
                                               0.23587789 0.06041596 3.7761874
## FB
          0.014473364
                       0.014273364 0.06157717
                                               0.23179636 0.05697383 4.0079838
## CHT
          0.007410518
                      0.007210518 0.03261119
                                               0.22110568 0.05390278 4.2290894
                      0.016391625 0.07644070
                                              0.21443582 0.05114588 4.4435253
## ABBV
          0.016591625
## PLD
          0.011089250
                      0.010889250 0.05239503 0.20782981 0.04865726 4.6513551
                      0.008365794 0.04031382
## PEP
          0.008565794
                                              0.20751680 0.04639958 4.8588719
          0.010107381
                       0.009907381 0.04982115
                                               0.19885894 0.04434212 5.0577308
## MRK
## GOOG
          0.011206214
                       0.011006214 0.05769731
                                               0.19075785 0.04245939 5.2484887
                                               0.18726348 0.04073001 5.4357522
## KO
          0.007265480
                      0.007065480 0.03773016
## PSA
          0.008176040
                      0.007976040 0.04882572
                                               0.16335733 0.03913600 5.5991095
                                              0.16043994 0.03766206 5.7595494
                      0.006424564 0.04004342
## PG
          0.006624564
## WELL
          0.009094911
                      0.008894911 0.05871015
                                               0.15150552 0.03629511 5.9110549
## TSLA
         0.016879280
                      0.016679280 0.11746897
                                               0.14198881 0.03502392 6.0530438
          0.007404403
                      0.007204403 0.05415978
                                               0.13302128 0.03383875 6.1860650
## WMT
                      0.008627518 0.06660160
                                               0.12953921 0.03273117 6.3156042
## AZN
          0.008827518
                       0.005895891 0.05044494 0.11687774 0.03169379 6.4324820
## MDLZ
          0.006095891
## CMCSA 0.006931851 0.006731851 0.05852146 0.11503216 0.03072016 6.5475141
        -0.003696091 -0.003896091 0.14150259 -0.02753371 0.02980455 6.5199804
##
              col3
## UNH
         0.1073957
                    7.86131157
                                0.460330091
## NVDA
        0.1547705
                   1.88404119
                                0.110322666
## MSFT
        0.1830491
                    3.09960415
                                0.181501655
## TSM
         0.1958382
                    1.71523296
                                0.100437864
## EQIX
        0.2054487
                    1.98018715
                                0.115952628
## AMT
         0.2127550
                    2.02921182
                                0.118823336
                    1.61507179
## ABT
         0.2176867
                                0.094572787
## NFLX
        0.2211762
                    0.62097995
                                0.036362349
                    1.46525657
## F.I.
         0.2237269
                                0.085800148
## AMD
         0.2256093
                    0.40564243
                                0.023752959
## AAPL
        0.2267467
                    0.85330092
                                0.049966228
         0.2276445
                    1.29754161
## CCT
                                0.075979363
## JNJ
         0.2281420
                    1.34687652
                                0.078868238
## FB
         0.2283502
                    0.77984790
                                0.045665084
         0.2279597
                    1.05240926
## CHT
                                0.061625296
## ABBV
        0.2272680
                    0.33715847
                                0.019742786
         0.2263222
                   0.33031340
## PLD
                                0.019341963
## PEP
         0.2254496
                    0.41935126
                                0.024555699
## MRK
         0.2242705
                   0.11662267
                                0.006829003
## GOOG
        0.2228476 -0.07923383 -0.004639648
## KO
         0.2213983 -0.23985447 -0.014045014
## PSA
         0.2191268 -0.81281730 -0.047595653
## PG
         0.2169165 -1.08445135 -0.063501565
        0.2145424 -0.93467550 -0.054731231
## WELL
## TSLA 0.2120013 -0.57096743 -0.033433797
## WMT
         0.2093287 -1.45058181 -0.084940847
## AZN
         0.2067171 -1.24660065 -0.072996444
```

```
## MDLZ 0.2038698 -1.96752632 -0.115211255
## CMCSA 0.2011407 -1.73640440 -0.101677588
## TWTR 0.1943251 -2.00929546 -0.117657105
```

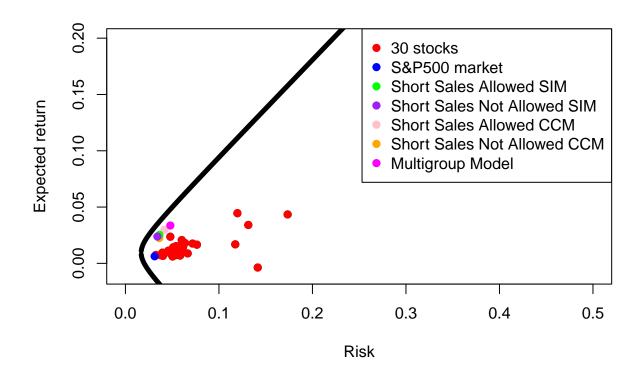
final table for short sales not allowed

a\_no

```
##
              Rhar
                         Rbar f
                                     sigma
                                               Ratio
                                                           col1
                                                                     co12
## UNH 0.023671961 0.023471961 0.04801401 0.4888565 0.21968758 0.4888565
## NVDA 0.044567996 0.044367996 0.11977864 0.3704166 0.18011791 0.8592730
## MSFT 0.020687995 0.020487995 0.06025004 0.3400495 0.15262704 1.1993225
## TSM 0.018022831 0.017822831 0.06373683 0.2796316 0.13241668 1.4789541
## EQIX 0.015260709 0.015060709 0.05417001 0.2780267 0.11693282 1.7569808
## AMT 0.014264652 0.014064652 0.05110000 0.2752378 0.10469101 2.0322186
## ABT 0.015006148 0.014806148 0.05591581 0.2647936 0.09476949 2.2970122
## NFLX 0.034101355 0.033901355 0.13140208 0.2579971 0.08656571 2.5550093
        0.013236073 0.013036073 0.05148673 0.2531929 0.07966909 2.8082022
       0.043437846 0.043237846 0.17348106 0.2492367 0.07379029 3.0574389
## AAPL 0.017597560 0.017397560 0.07184292 0.2421611 0.06871946 3.2996000
       0.011227455 0.011027455 0.04581229 0.2407095 0.06430075 3.5403095
       0.009525905 0.009325905 0.03953700 0.2358779 0.06041596 3.7761874
## .TN.T
## FB
        0.014473364 0.014273364 0.06157717 0.2317964 0.05697383 4.0079838
##
             col3
                          Z
                                     Х
                                             z_no
                                                         x_no
## UNH 0.1073957 7.8613116 0.46033009 6.95315146 0.408141927
## NVDA 0.1547705 1.8840412 0.11032267 1.51999958 0.089222212
## MSFT 0.1830491 3.0996041 0.18150166 2.37588003 0.139461402
## TSM 0.1958382 1.7152330 0.10043786 1.03110082 0.060524422
## EQIX 0.2054487 1.9801871 0.11595263 1.17523235 0.068984776
## AMT 0.2127550 2.0292118 0.11882334 1.17589650 0.069023761
## ABT 0.2176867 1.6150718 0.09457279 0.83524920 0.049028159
## NFLX 0.2211762 0.6209800 0.03636235 0.28914038 0.016972205
        0.2237269 1.4652566 0.08580015 0.61835074 0.036296472
## EL
## AMD
       0.2256093 0.4056424 0.02375296 0.15429274 0.009056805
## AAPL 0.2267467 0.8533009 0.04996623 0.24635994 0.014461043
       0.2276445 1.2975416 0.07597936 0.34573575 0.020294287
## CCI
## JNJ
       0.2281420 1.3468765 0.07886824 0.24400061 0.014322553
## FB
       0.2283502 0.7798479 0.04566508 0.07172163 0.004209977
```

e.

```
#Calculate the expected return and sd of the point of tangency
#when short sales allowed
sd_p_opt \leftarrow (t(x) %*% mat %*% x)^.5
R_p_opt <- t(x) %*% aaaa[,1]</pre>
#Calculate the expected return and sd of the point of tangency
#when short sales are not allowed
R_p_{opt_no} \leftarrow t(x_no) %*% aaaaa[,1]
#Plot all the stocks and the two tangency points:
plot(aaaa[,3], aaaa[,1], xlim=c(0,0.5), ylim=c(-0.01,0.2), xlab="Risk", ylab="Expected return")
points(sdeff, y1, lwd=5,type = "l")
points(sdeff, y2, lwd=5,type = "1")
points(sd_p_opt,R_p_opt, col="pink", pch=19)
points(sd_p_opt_no,R_p_opt_no, col="orange", pch=19)
#30 stocks
points(sdev30,R_ibar, pch=19, col = "red")
points(sdev_m,R_m,pch=19,col="blue")
points(sdev_allowed_SIM, R_allowed_SIM,pch=19, col = "green")
points(sdev_not_allowed_SIM,R_not_allowed_SIM, pch =19, col="purple")
points(port_stdev,port_exp_R,pch=19,col="magenta")
legend("topright",c("30 stocks","S&P500 market","Short Sales Allowed SIM","Short Sales Not Allowed SIM"
```



#### PART B 1.

#### index

```
0.0431170300 \quad 0.0069321656 \quad 0.0062007890 \quad 0.0210302800
                                                               0.0190583317
##
    [6] -0.0150798306  0.0376552955 -0.0155138372  0.0232014608
                                                               0.0245335888
  [11] -0.0041885879 -0.0310408058
                                   0.0548925110 -0.0173961069
                                                               0.0085208197
  [16]
        0.0104913824 -0.0210116724
                                    0.0197420297 -0.0625808182 -0.0264428316
  [21]
        0.0829831178
                     0.0005048693
                                   -0.0175301852 -0.0507353220
                                                              -0.0041283604
  [26]
##
        0.0659911146 0.0026993985
                                   0.0153246024
                                                 0.0009109211
                                                               0.0356098011
       -0.0012192431 -0.0012344508 -0.0194256793
                                                 0.0341745222
                                                               0.0182007622
  [36]
        ##
                                                 0.0090912085
                                                               0.0115762514
  [41]
        0.0048137751
                      0.0193488261
                                    0.0005464328
                                                 0.0193029785
                                                               0.0221881353
##
  [46]
        0.0280826277 0.0098316305
                                    0.0561787044 -0.0389473721 -0.0268844986
  [51]
        0.0027187751 0.0216083420
                                   0.0048424360 0.0360215562
        0.0042942871 -0.0694033560 0.0178593568 -0.0917768946
  ſ561
```

```
x
```

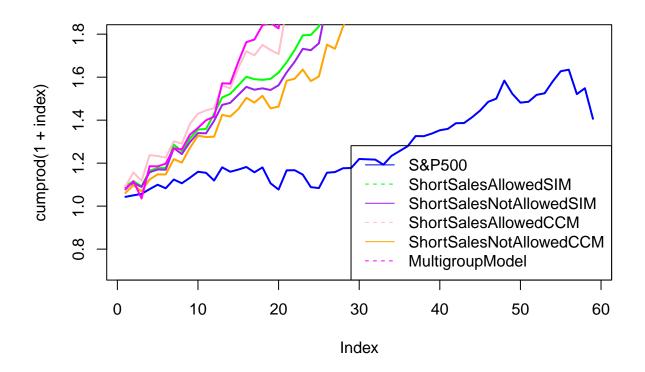
```
##
             UNH
                          NVDA
                                        MSFT
                                                        TSM
                                                                     EQIX
                                                                                     TMA
    0.460330091
                  0.110322666
                                 0.181501655
                                               0.100437864
                                                             0.115952628
                                                                           0.118823336
##
##
                          NFLX
                                          EL
                                                        AMD
                                                                     AAPL
                                                                                     CCI
             ABT
                  0.036362349
                                 0.085800148
##
    0.094572787
                                               0.023752959
                                                             0.049966228
                                                                            0.075979363
##
             JNJ
                            FΒ
                                          CHT
                                                       ABBV
                                                                      PLD
                                                                                     PEP
##
    0.078868238
                  0.045665084
                                 0.061625296
                                               0.019742786
                                                             0.019341963
                                                                            0.024555699
##
             MRK
                          GOOG
                                          ΚO
                                                        PSA
                                                                       PG
    0.006829003 \ -0.004639648 \ -0.014045014 \ -0.047595653 \ -0.063501565 \ -0.054731231
##
                                          AZN
##
            TSLA
                           WMT
                                                       MDLZ
                                                                    CMCSA
   -0.033433797 \ -0.084940847 \ -0.072996444 \ -0.115211255 \ -0.101677588 \ -0.117657105
```

We need to reorder them

```
reordered_x_ccm_allowed = x[colnames(rr)]
reordered_x_ccm_allowed
```

```
NVDA
##
           TSM
                       AAPL
                                                TSLA
                                                             MSFT
                                                                           AMD
   0.100437864
                0.049966228
                             0.110322666 -0.033433797
                                                                   0.023752959
##
                                                      0.181501655
##
          GOOG
                         FΒ
                                    NFLX
                                                TWTR
                                                              CHT
                                                                         CMCSA
##
  -0.004639648
                0.045665084
                             0.036362349 -0.117657105
                                                      0.061625296 -0.101677588
##
           PLD
                        AMT
                                     CCI
                                                 PSA
                                                             EQIX
##
   0.019341963
                0.118823336
                             0.075979363 -0.047595653
                                                      0.115952628 -0.054731231
##
           JNJ
                        UNH
                                     MRK
                                                 ABT
                                                             ABBV
   0.078868238
                0.460330091
                             0.006829003
                                         ##
##
           WMT
                         PG
                                     PEP
                                                MDLZ
                                                               ΚO
  -0.084940847 -0.063501565
                             0.024555699 -0.115211255 -0.014045014
                                                                  0.085800148
```

```
plot(cumprod(1+index), col="blue", lwd=2, type="l", ylim=c(0.7,1.8))
# points(cumprod(1+R_ibar), col="red", lwd=2, type="l")
r_allowed_sim <- as.matrix(rr) %*% x_i_allowed
r_not_allowed_sim <- as.matrix(rr) %*% x_i
r_allowed_ccm <- as.matrix(rr) %*% x_oi
r_not_allowed_ccm <- as.matrix(rr) %*% X_allowed
r_not_allowed_ccm <- as.matrix(rr[names(x_no)]) %*% x_no
r_multigroup <- as.matrix(rr) %*% X_allowed
points(cumprod(1+r_allowed_sim), col="green", lwd=2, type="l")
points(cumprod(1+r_not_allowed_sim), col="purple", lwd=2, type="l")
points(cumprod(1+r_not_allowed_ccm), col="pink", lwd=2, type="l")
points(cumprod(1+r_not_allowed_ccm), col="orange", lwd=2, type="l")
points(cumprod(1+r_multigroup), col="magenta", lwd=2, type="l")
legend('bottomright', lty=1:2, c('S&P500', 'ShortSalesAllowedSIM', 'ShortSalesNotAllowedSIM', 'ShortSalesA</pre>
```



# PART B 2.

```
comp <- cumprod(1+index)
geoMean_index <- comp[length(comp)]^(1/length(comp)) - 1
geoMean_index</pre>
```

# ## [1] 0.005795708

30 stocks in not a portfolio

```
# comp <- cumprod(1+R_ibar)
# geoMean_30stocks <- comp[length(comp)]^(1/length(comp)) - 1
# geoMean_30stocks</pre>
```

```
comp <- cumprod(1+r_allowed_sim)
geoMean_allowed_sim <- comp[length(comp)]^(1/length(comp)) - 1
geoMean_allowed_sim</pre>
```

# ## [1] 0.02460446

```
comp <- cumprod(1+r_not_allowed_sim)
geoMean_not_allowed_sim <- comp[length(comp)]^(1/length(comp)) - 1
geoMean_not_allowed_sim</pre>
```

# ## [1] 0.02321741

```
comp <- cumprod(1+r_allowed_ccm)</pre>
geoMean_allowed_ccm <- comp[length(comp)]^(1/length(comp)) - 1</pre>
geoMean_allowed_ccm
## [1] 0.02849642
comp <- cumprod(1+r_not_allowed_ccm)</pre>
geoMean_not_allowed_ccm <- comp[length(comp)]^(1/length(comp)) - 1</pre>
geoMean_not_allowed_ccm
## [1] 0.02182881
comp <- cumprod(1+r_multigroup)</pre>
geoMean_multigroup <- comp[length(comp)]^(1/length(comp)) - 1</pre>
geoMean_multigroup
## [1] 0.03181646
PART B 3. Sharpe Ratio of each Portfolio
For SIM when Short Sales are Allowed
(mean(r_allowed_sim) - Rf) / sdev_allowed_SIM
              [,1]
## [1,] 0.6410813
For SIM when Short Sales not Allowed
(mean(r_not_allowed_sim) - Rf) / sdev_not_allowed_SIM
              [,1]
## [1,] 0.6382121
For CCM with Short Sales Allowed
(t(reordered_x_ccm_allowed) %*% colMeans(rr) - Rf) / sd_p_opt
              [,1]
## [1,] 0.6680151
(mean(r_allowed_ccm)-Rf)/sd_p_opt
              [,1]
## [1,] 0.6680151
For CCM without Short Sales Allowed
```

```
(mean(r_not_allowed_ccm) - Rf) / sd_p_opt_no
##
              [,1]
## [1,] 0.5669022
For Multigroup Model
(mean(r_multigroup) - Rf) / port_stdev
## [1] 0.6579066
Here are Rm bar and sigma m
R_m = mean(index)
s_m2 <- var(index)</pre>
Differential Excess Return R_a_bar - R_a'_bar For SIM when Short Sales are Allowed
\# mean(r_allowed_sim) - (Rf + (R_m-Rf)/s_m2*sdev_allowed_SIM)
mean(r_allowed_sim) - Rf - ((R_m-Rf)/sdev_m) * sdev_allowed_SIM
##
               [,1]
## [1,] 0.01832064
For SIM when Short Sales not Allowed
\# \ mean(r\_not\_allowed\_sim) \ - \ (Rf \ + \ (R\_m-Rf)/s\_m2*sdev\_not\_allowed\_SIM)
mean(r_not_allowed_sim) - Rf - ((R_m-Rf)/sdev_m) * sdev_not_allowed_SIM
               [,1]
## [1,] 0.01714445
For CCM with Short Sales Allowed
\# (t(reordered\_x\_ccm\_allowed) \%*\% colMeans(rr)) - (Rf + (R\_m-Rf)/s\_m2* sd\_p\_opt)
# mean(r_allowed_ccm)-(Rf + (R_m-Rf)/s_m2*sd_p_opt)
mean(r_allowed_ccm) - Rf - ((R_m-Rf)/sdev_m) * sd_p_opt
##
               [,1]
## [1,] 0.02211854
For CCM without Short Sales Allowed
\# \ mean(r\_not\_allowed\_ccm) \ - \ (Rf \ + \ (R\_m-Rf)/s\_m2* \ sd\_p\_opt\_no)
mean(r_not_allowed_ccm) - Rf - ((R_m-Rf)/sdev_m) * sd_p_opt_no
## [1,] 0.01556331
For Multigroup Model
```

```
\# mean(r_multigroup) - (Rf + (R_m-Rf)/s_m2*port_stdev)
mean(r_multigroup) - Rf - ((R_m-Rf)/sdev_m) * port_stdev
## [1] 0.0250444
Treynor Measure SIM Short Sales Allowed
# (R_p_opt - Rf) / (t(beta)%*%x_i_allowed)
(mean(r_allowed_sim) - Rf) / (t(beta)%*%x_i_allowed)
##
                [,1]
## [1,] 0.03495135
SIM Short Sales Not Allowed
(mean(r_not_allowed_sim)-Rf)/ (t(beta)%*%x_i_allowed)
##
                [,1]
## [1,] 0.03274744
Jensen Differential Performance Index SIM Short Sales Allowed
\# R_p_{opt} - Rf - (R_m - Rf) * (t(beta)%*%x_i_allowed)
mean(r_allowed_sim) - Rf - (R_m - Rf) * (t(beta)%*%x_i_allowed)
##
                [,1]
## [1,] 0.02044384
SIM Short Sales Not Allowed
\# R_p_opt_no - Rf - (R_m-Rf)*(t(beta)%*%x_i)
\label{eq:mean} \texttt{mean}(\texttt{r\_not\_allowed\_sim}) \ - \ \texttt{Rf} \ - \ (\texttt{R\_m-Rf})*(\texttt{t(beta)}\%*\%\texttt{x\_i})
##
                [,1]
## [1,] 0.01882078
Part B 4.Fama's decomposition (net selectivity and diversification) for single index model when short sales
are not allowed
R_a = mean(r_not_allowed_sim)
\# R_a = R_p_opt_no
beta_a_double_prime = (sdev_not_allowed_SIM / sigma_m2^.5)
R_a_double_prime = Rf + ((R_m-Rf)/1)*beta_a_double_prime
R_from_net_selectivity = R_a - R_a_double_prime
R_from_net_selectivity
                [,1]
## [1,] 0.01714445
```

```
# beta_a = mean(beta)
beta_a = (t(beta)%*%x_i)
R_a_prime = Rf + ((R_m-Rf)/1)*beta_a
R_a_double_prime - R_a_prime
```

```
## [,1]
## [1,] 0.001676325
```

 $plot(c(1,beta_a,beta_a_double_prime,beta_a), \ c(R_m,R_a_prime,R_a_double_prime,R_p_opt_no), \\ xlab = "beta" \\ abline(lm(c(R_a_double_prime,Rf)~c(beta_a_double_prime,0)))$ 

