## Analyzing the Feature Importance of Different Variables on the Price of Ikea Products

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## List of Abbreviations

 ${\bf R}$  . . . . . . . . Statistical Programming Language

 ${f VIF}$  . . . . . . Variance Inflation Factor

MSE . . . . . . Mean Squared Error

 $\mathbf{IQR}$  . . . . . Interquartile Range

1

### Introduction

This project report is an examination at the Hamburg School of Business Administration in the module 'Data Business' as a part of a Bachelor of Science degree program. The students were given a data set and the task was to first explore the data and then choose a research question which was to be answered scientifically with the help of the statistical programming language R. The authors of this report were given a data set which contains Ikea products with different features, such as price, dimensional measures, name, category and designers of the product.

## Theoretical Background & Research Question

#### 2.1 Data Set

by P. Krück

The data set was obtained by a kaggle.com user (Reem Abdulrahman) by the means of webscraping techniques from the Saudi Arabian Ikea website in the furniture category on the 20th of April 2020. Noteworthy features include the name, category, price in Saudi Riyals, the designer and dimensions (width, height and depth). The data set has 13 variables and 2962 distinct observations after the removal of duplicates.

#### 2.2 Theoretical Background

#### 2.2.1 Random Forest Basics

by J. Pein

In order to analyze the feature importance in relation to the price variable, a

random forest regression model was chosen. A random forest consists of many decision trees, which predicts the response variable based on a majority decision process. In standard decision trees, each node is split to achieve the best performing model. In random forests however, the nodes are randomly split. Compared to linear regression, random forests not only take the mean and covariance structure into account, but also include deeper aspects of the data<sup>1</sup> resulting in a more advanced and robust model. To learn more about random forests, please see Breiman.<sup>2</sup>

#### 2.2.2 Overfitting

by P. Krück

In statistical modelling, overfitting refers to the phenomenon where an analysis model corresponds to closely to a given data set and thus fails to generalize to new data or future observations.

#### 2.2.3 Feature Importance

by J. Pein

There are different ways to measure feature importance. In this analysis permuting feature importance by a random forest algorithm is used. This algorithm leaves each feature out once while leaving all others unchanged, at each step calculating the mean squared error (MSE) of the predictions. This is done for every tree, calculating the overall MSE of each feature for the whole model.<sup>3</sup>

 $<sup>^1{\</sup>rm Gr\"{o}mping},$  "Variable Importance Assessment in Regression: Linear Regression versus Random Forest." 317.

<sup>&</sup>lt;sup>2</sup>"Random Forests."

 $<sup>^3</sup>$ Ibid., 23.

## 2.3 Research Question

#### by P. Krück

This paper explores the following research question:

How important are the different features of Ikea products in regard to their price?

The motivating forces for this research question are the possible implications for price determination of new items.

## Methods

### 3.1 Data Cleaning and Transformation

by P. Krück

To examine the given data set properly, the authors first had to restructure and reformat it. This initial data cleaning step included type conversion, value mutation, addition of newly calculated fields and the removal of irrelevant columns.

Concretely, name, category and designer were converted to categorical variables. In the designer column, blank strings and values prefixed by "IKEA of Sweden" were converted to missing values (NA). Furthermore, both the price and old price were converted to double values and the currency was changed from Saudi Arabian Riyals to Euros based on the exchange rate from the time the data set was obtained by the author (See section 2.2).

Interestingly, the data set had a peculiarity where some rows were exact duplicates except for values in the category vector. The authors considered

multiple approaches to handle these data duplications without losing information about the category of an item.

One considered option was to merge the two category values into one column value via comma separation (e.g. "a" and "b" converts to "a, b"). However, this approach leads to the creation of many combinatorial categories with a low count of items per category. Additionally, it reduces the item count per category where the category is not comma separated. Overall this would lead to having many small categories which increases the difficulty in applying a regression model due to overfitting (See section 2.2.2).

The second option was to create separate columns for the different values of category. The data set would then have observations with category one, two and three. While no information is lost utilizing this approach, most observations in the second and third category column would contain missing values, thus increasing the difficulty of analysis using a predefined model (See section 3.3).

The authors chose the option of selecting the observations where the category count occurred most frequently when considering duplicates. The most frequent categories could be retained without including more column vectors into the data set as in option two.

To better facilitate the comparison of the different sizes of furniture items, the size in cubic meters was computed based on the depth, width and height values, and added as a column vector for further analysis.

Finally, the authors only selected columns that could have a potential impact on outcome of the analysis (See section 2.3) for further investigation. A detailed com-

**Table 3.1:** Initial Data Set formatting.

| name | category  | price | old_price    | sellable_online | other_colors | designer |  |
|------|-----------|-------|--------------|-----------------|--------------|----------|--|
| PAX  | Wardrobes | 20450 | No old price | TRUE            | No           | IKEA     |  |
| ELV  | Wardrobes | 7500  | SR 820       | TRUE            | No           | Ehlén    |  |
| ELV  | Wardrobes | 15720 | SR 1,755     | TRUE            | No           | Ehlén    |  |
| ELV  | Wardrobes | 9240  | SR 1,050     | TRUE            | No           | Ehlén    |  |
| ELV  | Wardrobes | 27450 | SR 3,130     | TRUE            | No           | Ehlén    |  |
| ELV  | Wardrobes | 12310 | SR 1,535     | TRUE            | No           | Ehlén    |  |

Table 3.2: Transformed Data Set formatting.

| name | category  | price_eur | old_price_eur | sellable_online | other_colors | designer | size_m3 |
|------|-----------|-----------|---------------|-----------------|--------------|----------|---------|
| PAX  | Wardrobes | 501.78    | NA            | TRUE            | FALSE        | Ehlén    | 3.12    |
| ELV  | Wardrobes | 184.03    | 201.2         | TRUE            | FALSE        | Ehlén    | NA      |
| ELV  | Wardrobes | 385.72    | 430.62        | TRUE            | FALSE        | Ehlén    | NA      |
| ELV  | Wardrobes | 226.72    | 257.64        | TRUE            | FALSE        | Ehlén    | NA      |
| ELV  | Wardrobes | 673.54    | 768.01        | TRUE            | FALSE        | Ehlén    | NA      |
| ELV  | Wardrobes | 302.05    | 376.64        | TRUE            | FALSE        | Ehlén    | NA      |

parison of the initial vs. transformed data structure can be seen in tables 3.1 and 3.2.

#### 3.2 Exploratory Data Analysis

by P. Krück

The following sections explore our data based on the eight step data exploration protocol proposed by Zuur et al.<sup>1</sup>

#### 3.2.1 Step 1: Outliers in Price and Independent Variables

by P. Krück

Outliers of the chosen variables can be observed for each variable (see figure 3.1). Web scraping code is written in a generic form which makes it generalizable to all applied pages. This removes the occurance of observation errors in the Ikea data set. Additionally, it is also unlikely that the outliers are due to falsely scraped items. To verify this hypothesis, the authors randomly tested outlier observations and manually checked them against the ikea website information. With a high

<sup>&</sup>lt;sup>1</sup>Zuur, "A protocol for data exploration to avoid common statistical problems."

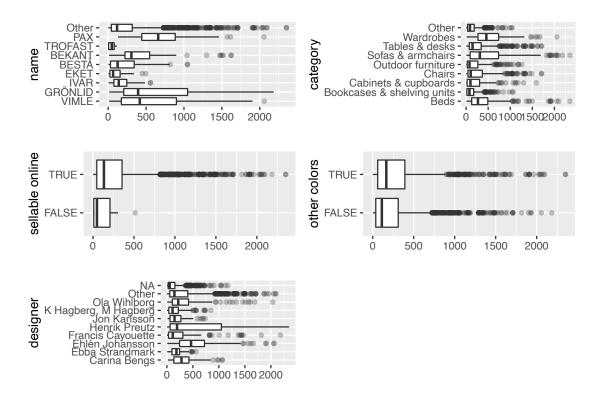


Figure 3.1: Boxplots for Price in Euro Based on Independent Variables

level of statistical confidence, the authors proceeded with further analysis without removing outliers as observation errors.

#### 3.2.2 Step 2: Homogeneity of Price

#### by P. Krück

The homogeneity (homoscedasticity) of variance for price is explored by the means of conditional boxplotting. Within each name, and within each category the variance is heterogenous (see fig. 3.2). However, looking at both name and category in conjunction, it is possible to explore homoscedasticity of variance for price.

Due to the limited scope and length of this paper, the authors were not able to inspect all variable combinations for the three categorical plus two logical variables of the data set  $(2^5 = 32)$ .

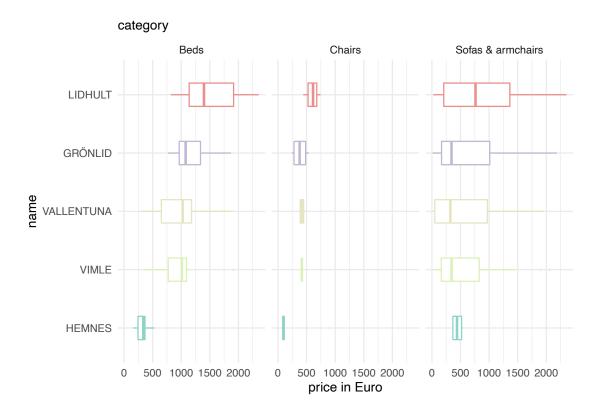


Figure 3.2: Homogeneity of Category for Selected Combinations of Name and Category

#### 3.2.3 Step 3: Normality

#### by P. Krück

No numerical variables (price, old\_price and size\_m3) are arranged along a normal distribution (see fig. 3.3), but rather follow an exponential decay  $(e^{-x})$ .

#### 3.2.4 Step 4: Missing Values

#### by P. Krück

All variables were examined for missing values. Only designer, size\_m3 and old\_price\_eur have missing values with percentages of 3.44%, 45.9% and 81% respectively (see fig. 3.4). The missing values for designer were deliberately set to NA by the authors in the case where the values contained digits, which is likely a scraping error. The NA values for the size can be explained due to the computation

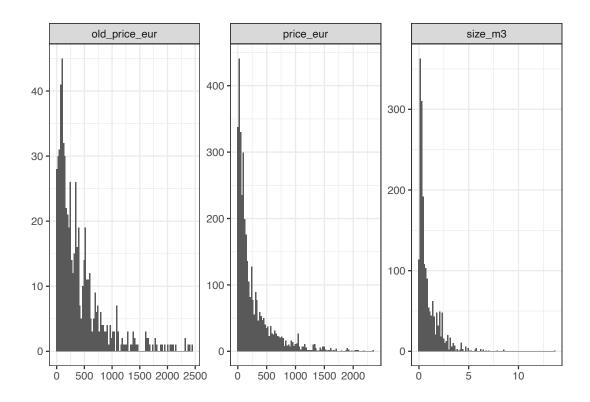


Figure 3.3: Histogram of Numerical Variables with a Bin Width of 100 Euro

**Table 3.3:** Variance Inflation Factors for Numerical Variables

| price_ | eur | old_price_eur | size_m3 |
|--------|-----|---------------|---------|
| 77     | .97 | 78.54         | 2.36    |

of this column vector. size\_m3 is the product of depth, width and height. If one of those three values is missing, the end result is also a missing value. In contrast, the abscence of the old price variables is due to the fact that most items are not on sale and thus do not have a missing value.

#### 3.2.5 Step 5: Collinearity between Independent Variables

#### by P. Krück

The old price has a rather high variance inflation factor (VIF) which corresponds to high multicollinearity (see table 3.3). Contrarily, size has a low VIF which translates to low multicollinearity among the other independent variables (see table 3.3).

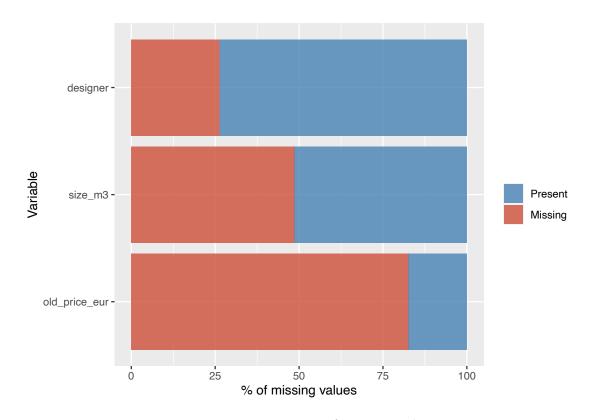


Figure 3.4: Percentage of Missing Values

## 3.2.6 Step 6: Relationship between Independent Variables and Price

#### by P. Krück

Inspecting the relationship between the independent variables and price, a strong correlation between old\_price\_eur and size\_m3 can be observed, while none can be detected for the other variables (see A.5). old\_price\_eur has a linear relationship (see fig. 3.5) whereas size\_m3 begins with a linear relationship as well, which is only disturbed by an outlier. (see fig. 3.6).

#### 3.2.7 Step 7: Interactions

#### by P. Krück

The interactions between different variables are explored by the use of con-

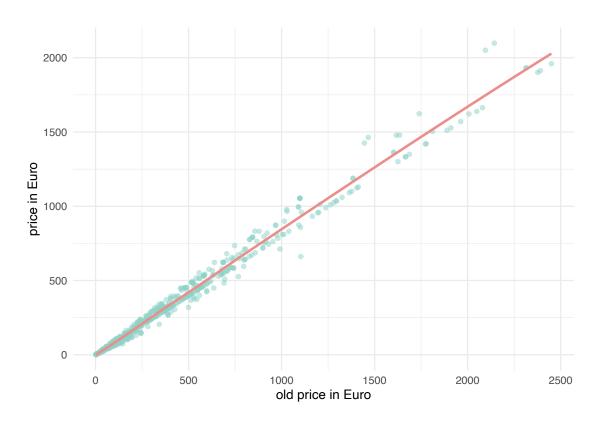


Figure 3.5: Relationship of Price and Old Price

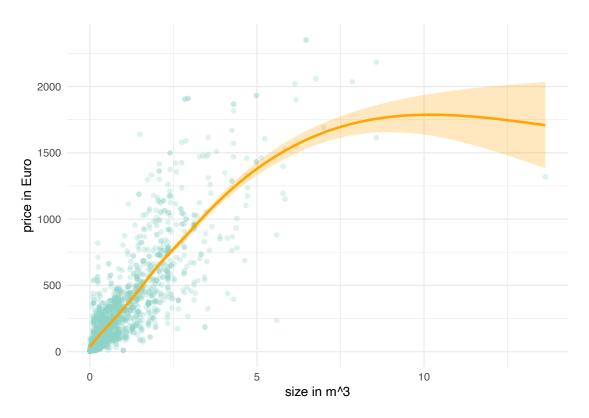


Figure 3.6: Relationship of Price and Size in Cubic Meters

ditioning plots (coplots). Utilizing this form of plotting the relationship of two numerical variables is explored by creating a matrix of plots subdivided by two categorical variables. In the given data set there are three numerical and three categorical variables which can be explored in this form of interaction. For the numerical variables, old\_price\_eur has such a strong relationship with price (see fig 3.5). A more detailed breakdown by the categorical variables would not reveal new information. This leaves the exploration of size\_m3 and price\_eur subdivided by designer, name and category resulting in  $\binom{3}{2} = 3$  combinations of coplots.

#### Interaction of size and price coplotted by designer and name

by P. Krück

It is unlikely that there is an interaction between size and price split by name and designer as is indicated by the non-parallelism of the fitted lines in the coplot (see figure A.6).

#### Problems with Coplot Development

by P. Krück

This section describes a programming error the authors ran into regarding coplotting.

Unfortunately, the authors of this papers weren't able to fully explore all combinations. Plotting designer and name works (see above) while the other two options would not plot properly. The authors could not fully debug the problem with these plots. The linear model predicted infinite values for some of the coplotted combinations for both amalgamations that would not render correctly. Dropping

all NA values left 354 observations and the coplot would correctly render for the combination of name and category while for name and designer it would not. The number of observations for name and category is rather low considering the additional categorical subdivision which lead the authors to discard it as an insignificant research finding. Still there seemed to be infinite values outputted by the linear method. The authors hypothesized that those values were caused by a division by 0 of the internal algorithm mechanics. This however proved to be wrong after applying the respective filters. The code for the two problematic plots can be viewed in Appendix chapter B.

The inclined reader is encouraged to dabble with the code. Sending any hints or even a solution to fix the code and fully render the plots would be highly appreciated by the authors.<sup>2</sup>

## 3.2.8 Step 8: Independence Observations of Response Variable Price

by P. Krück

The independence of observerations of the response variables assumes that "[...] information from any one observation should not provide information on another after the effects of other variables have been accounted for." The data cleaning step left the observed data set in a tidy format which implies that the observations are independent of eachother.<sup>4</sup>

<sup>&</sup>lt;sup>2</sup>Any questions, hints or solutions may kindly be sent to philip.krueck@myhsba.de.

<sup>&</sup>lt;sup>3</sup>Ibid., 11, ll.23–26.

 $<sup>^4</sup>$  "There are three interrelated rules which make a dataset tidy: Each variable must have its own column. Each observation must have its own row. Each value must have its own cell." (, Wickham, *R for Data Science*, 149, ll.4–7.)

#### 3.3 Random Forest Regression Model

by J. Pein

To analyze the feature importance of different variables on the price variable, a random forest model was chosen. In the given data set, categorical variables with lots of different values can be observed. Including all of those values in, for example, a linear regression model, would most likely lead to overfitting (see section 2.2.2). This is because the linear model would learn the immanent data structure of the sample, but would not be able to generalize from this. Thus, the authors chose the random forest model, because according to Breiman<sup>5</sup> it is robust against overfitting.

In this analysis, the R randomForest package was used, which is based on the original Breiman and Cutler's Fortran code for random forest regression. To reproduce the results, the further data preparation steps are described here. These steps are based on the cleaned ikea data set which is described in section 3.1. This data set is then transformed further allowing it to be used with the randomForest package. To learn more about how random forests work see chapter 2, to learn more about the randomForest package see Liaw and Wiener.<sup>6</sup>

First, the variable old\_price\_eur is removed from the cleaned ikea data set, due to a very high correlation and relationship to the response variable price\_eur (price) analyzed in section 3.2.5 and section 3.2.6. Then, the designers and names, which are not part of the 50 designers and 49 names with the highest number of occurences, are grouped in the other value. This is because the randomForest method does not allow categorical variables with more than 53 predictors. The

<sup>&</sup>lt;sup>5</sup>"Random Forests," 29.

<sup>&</sup>lt;sup>6</sup>"Classification and Regression by randomForest."

last step deals with the missing values in the data. As described in section 3.2.4, there are many missing values in the size\_m3 and designer variables. To apply the randomForest method of the randomForest package on the data, those missing values are treated using three different approaches. In the first approach the rows with missing values are deleted, reducing the total number of rows by aproximately 50%. In the second approach the missing values are dummy coded with a value of -1000. The third approach uses the na.roughfix = na.omit argument, which is the built-in way of the randomForest package to deal with missing values. After preparing the data, the randomForest method of the randomForest package is applied to the data with the number of trees set to 2000 and importance set to TRUE, training the random forest model with the prepared ikea data set.

randomForest(price\_eur ~ ., rf\_ikea, ntree=2000, importance=TRUE)

Then the importance method of the randomForest package is used to calculate the feature importances, which are computed by permuting feature importance, which was introduced in section 2.2.3. The three different approaches of dealing with the missing values in the data set lead to different results, so the authors chose to calculate the mean result of the three approaches. The result of this analysis is presented in the following chapter.

4

### Results

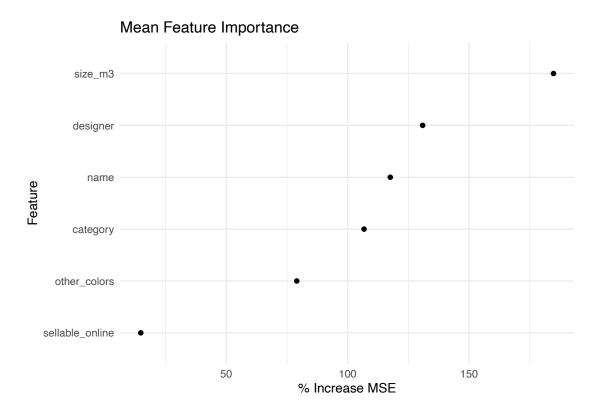
by J. Pein

In this chapter, the result of the analysis of the feature importance of different features on the response variable price of Ikea products are presented.

As described in section 3.3, the feature importance was calculated using permuting feature importance of the randomForest R package. In this analysis, feature importance is derived from the percentage increase of the mean squared error (MSE) of the overall random forest regression model in regard to the response variable price\_eur. A larger percentage increase of the MSE implies greater feature importance. Conversely, a lower percentage increase of the MSE translates to less feature importance.

Thus, as can be seen in figure 4.1, the most important feature is size\_m3 with an increase of the MSE of 182%. The second, third and fourth most important features are designer with an MSE increase of 120%, name with an increase of 114% and category with an increase of 105%. The fifth most important feature

4. Results



**Figure 4.1:** Mean Feature Importance of the Predictor Variables on the Response Variable

is other\_colors with a MSE increase of 78% and the least important feature is sellable\_online with a 9% increase.

These results are further discussed in the following chapter.

5

### Discussion

by J. Pein

In this chapter, the results are discussed in connection with the research question.

The question that the results were supposed to answer is the following:

How important are the different features of Ikea products in regard to their price?

#### 5.1 Feature Importance

The size\_m3 variable is the most important feature. Probably the main reason for this is the size of a product being closely linked to its material cost. Big items are generally more costly to produce, thus leading to a higher selling price and vice versa. Due to the high correlation to the price variable described in section 3.2.5 and section 3.2.6, it is worth discussing in future research whether or not to include this variable in a possible predictive analysis model.

The designer variable is the second most important feature. When looking at the price distribution per designer, in can be clearly seen that the interquartile 5. Discussion 20

range (IQR) of price varies for each designer. In addition, the IQR often is smaller than 300€, thus showing a tendency towards a certain price range, which might be the reason for the relatively high feature importance of the designer variable. For the plot, see figure A.1.

The name variable includes around 50 different product names with partly small numbers of occurences. But, as can be seen in figure 3.2, certain product lines (names) tend to be more expensive than others. *LIDTHULT*, for example, is the most expensive product line in each of the categories *beds*, *chairs* and *sofas* & armchairs while *HEMNES* is on the lower end of the price scale. This behavior explains a relatively high feature importance of the name variable.

Category is another feature with a relatively high importance. One reason for this is the different category's price distributions showing a clear tendency towards certain price segments (see figure A.2), i.e. wardrobes and beds are generally more expensive than chairs.

The feature importance of other\_colors is the second lowest, but still considerable. This still relatively high feature importance might be due to the difference of the mean price and the relatively small IQR (see: figure A.3). On the other hand, there is a large overlapping area within the IQR in the two expressions of other\_colors possibly reducing the feature importance.

The very low feature importance of the sellable\_online variable is probably because the low number of occurences of a product being sellable online. Only around 0.6% of the products are sellable online.

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#### 5.2 Conclusion

The data used in this paper was scraped from the Saudi Arabian Ikea website, thus this analysis mainly focusses on Ikea products in the Saudi Arabian market. To analyze the geographically independent feature importances, more data should be scraped from other international Ikea websites. The research question of this paper, How important are the different features of Ikea products in regard to their price?, could thus not be answered for the global Ikea product market, but for the Saudi Arabian market only.

Also, in further research, the results presented on the feature importance of the predictor variables on the response variable price should be validated by other techniques than the random forest model used in this analysis to achieve unbiased results.

Furthermore, based on this analysis a predictive model could be developed which predicts the price of Ikea products in the Saudi Arabian Market based on the features analyzed. This could be used by Ikea internally to analyze if the price of their new product aligns with the prices of the currently available product or by market researchers.

Lastly, the authors were surprised by the high feature importances of the variables designer and name computed by the random forest model. Both variables have lots different values, suggesting an overfitting of the random forest model. This, however, is objected by scientific research. Exploring what the reason behind the high feature importances of the variables designer and name and if they are due

<sup>&</sup>lt;sup>1</sup>Breiman, "Random Forests," 29.

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to overfitting of a random forest model should be analyzed in future research. If the high feature importance of the variables truly is not due to overfitting, this example backs up the thesis of Grömping<sup>2</sup> that random forests are able to discover deeper patterns in the data. These patterns are beyond the discussion applied here, showing the power of random forests models.

 $<sup>^2\</sup>mbox{``Variable Importance Assessment in Regression: Linear Regression versus Random Forest," 317.$ 

Appendices

A Plots

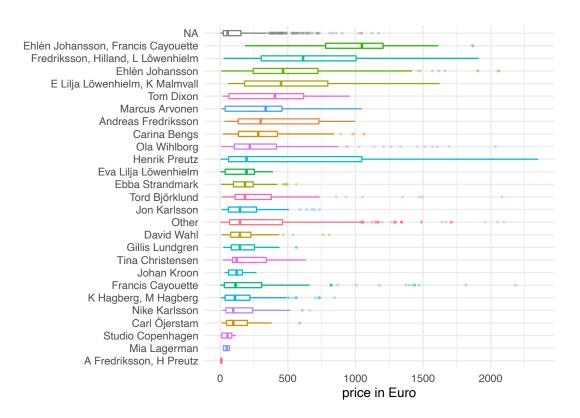


Figure A.1: Price Distribution per Designer

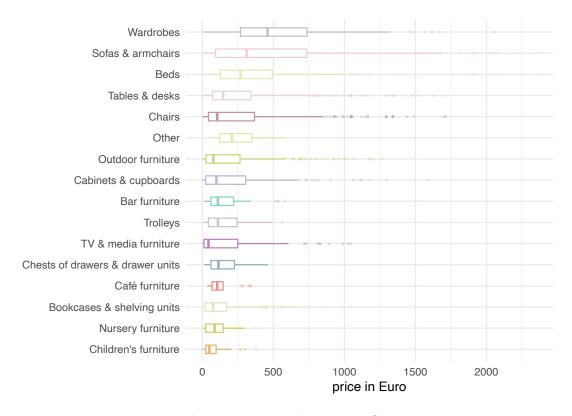


Figure A.2: Price Distribution per Category

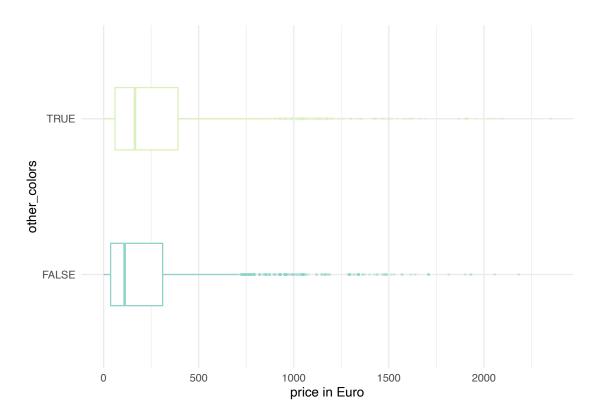


Figure A.3: Price Distribution Other Colors

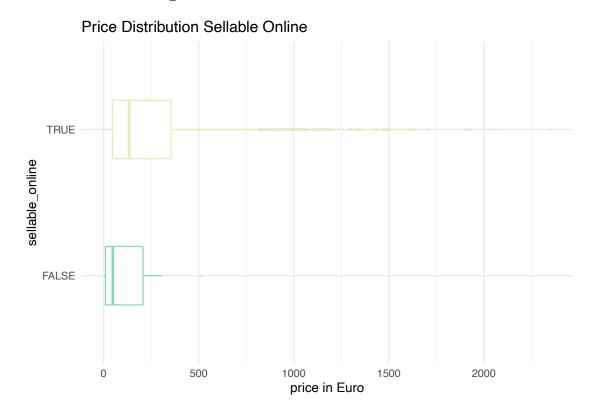


Figure A.4: Price Distribution Sellable Online

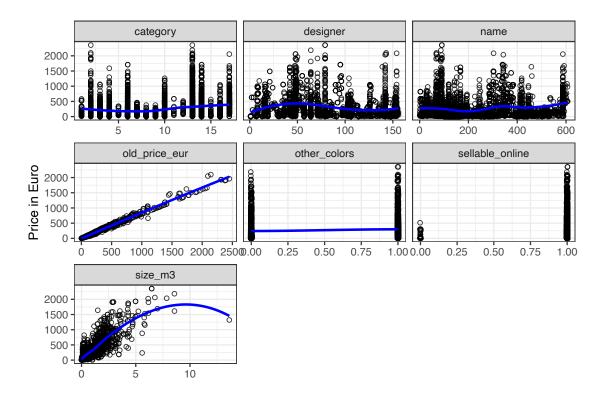
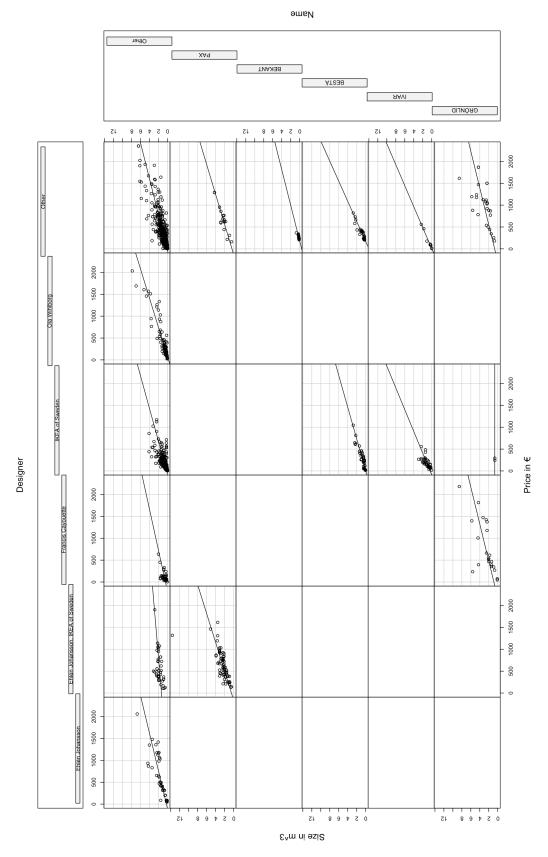


Figure A.5: Relationship between Independent Variables and Price



 $\textbf{Figure A.6:} \ \, \textbf{Coplot of Size and Price Split by Designer and Name}$ 

## B

## Code Chunks

```
fct_lump_n(category, 5), data = drop_na(tidy_ikea),
ylab = "Size in m^3",

xlab = "Price in Euro", panel = function(x, y, ...) {
   tmp <- lm(y ~ x, na.action = na.omit)
   abline(tmp)
   points(x, y)})</pre>
```

## Declaration of Honor

Declaration: We hereby declare that we

- 1. wrote this project report without the assistance of others;
- 2. have marked direct quotes used from the literature and the use of ideas of other authors at the corresponding locations in the thesis;
- 3. have not presented this thesis for any other exam. We acknowledge that a false declaration will have legal consequences.

Hamburg, 01.12.20

(Place, date) (Signatures)

Mein

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Hamburg, 01.12.20

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