**Philip Mortimer ML**

1a + b)

A graph of a graph

Description automatically generated with medium confidence

Figure - Validation and training loss of neural network.

I trained a neural network to classify activity type. My model achieves a validation accuracy of 84%. The model’s training loss flatlines after about 5 epochs, demonstrating quick convergence. The validation loss follows a similar trend initially. However, the validation loss is much less smooth and only really settles after about 40 epochs. The final validation loss is about 30% larger than the training loss, which indicates that the model is overfitting to the training set slightly. However, given that both training and validation loss follow similar trends and achieve similar loss, I would say the model has trained effectively.

When training the model, I noticed that the neural network will often get stuck at a local minimum of about 60% classification accuracy. Thus, it typically requires multiple training attempts with different weight initialisations to avoid this local optimum and achieve a higher classification accuracy.

On the test dataset, the neural network achieves a loss of 0.319 and an accuracy of 89.9%. This would indicate that the model generalises well as this is marginally higher than both the training and validation classification accuracies.

1c)

There are wide variety of model hyperparameters to tune when training a neural network. I have decided to analyse the learning rate, neural network architecture, activation function and batch size. For each feature, I have selected a small number of values which are commonly used and cover a broad range of options. To compare them, I define a base neural network architecture and then investigate the relative performance as each variable is changed individually. Each model is trained for the same number of epochs to ensure effective comparison. For the number of training epochs, we can see from *Figure 1* that 5 epochs tends to be sufficient for a model to achieve strong classification. To select the best overall parameters, a randomised grid search would be a suitable search strategy.

A graph of a graph showing the impact of learning rate on model training

Description automatically generated

Figure - Impact of learning rate on ANN performance

*Figure 2* depicts the impact learning rate has on performance. From this graph, we can see that the model fails to learn for learning rates of 1e-5 and 0.1, whilst it converges for a learning rate of 0.001. This suggests that that 1e-3 is a stronger choice of learning rate. Indeed, this is conclusion is widely adopted as this is typically the default learning rate for the ADAM optimiser [1] and is viewed to be a value that yields effective performance [2]. A larger learning rate means that step sizes are larger, leading to faster initial convergence but also typically struggling to converge at the exact optimum point. Conversely, smaller step sizes converge more slowly but more accurately, even if they are more prone to getting stuck at local optima. However, in the case of ADAM, an adaptive learning rate algorithm, these problems are typically less apparent. A graph of a model

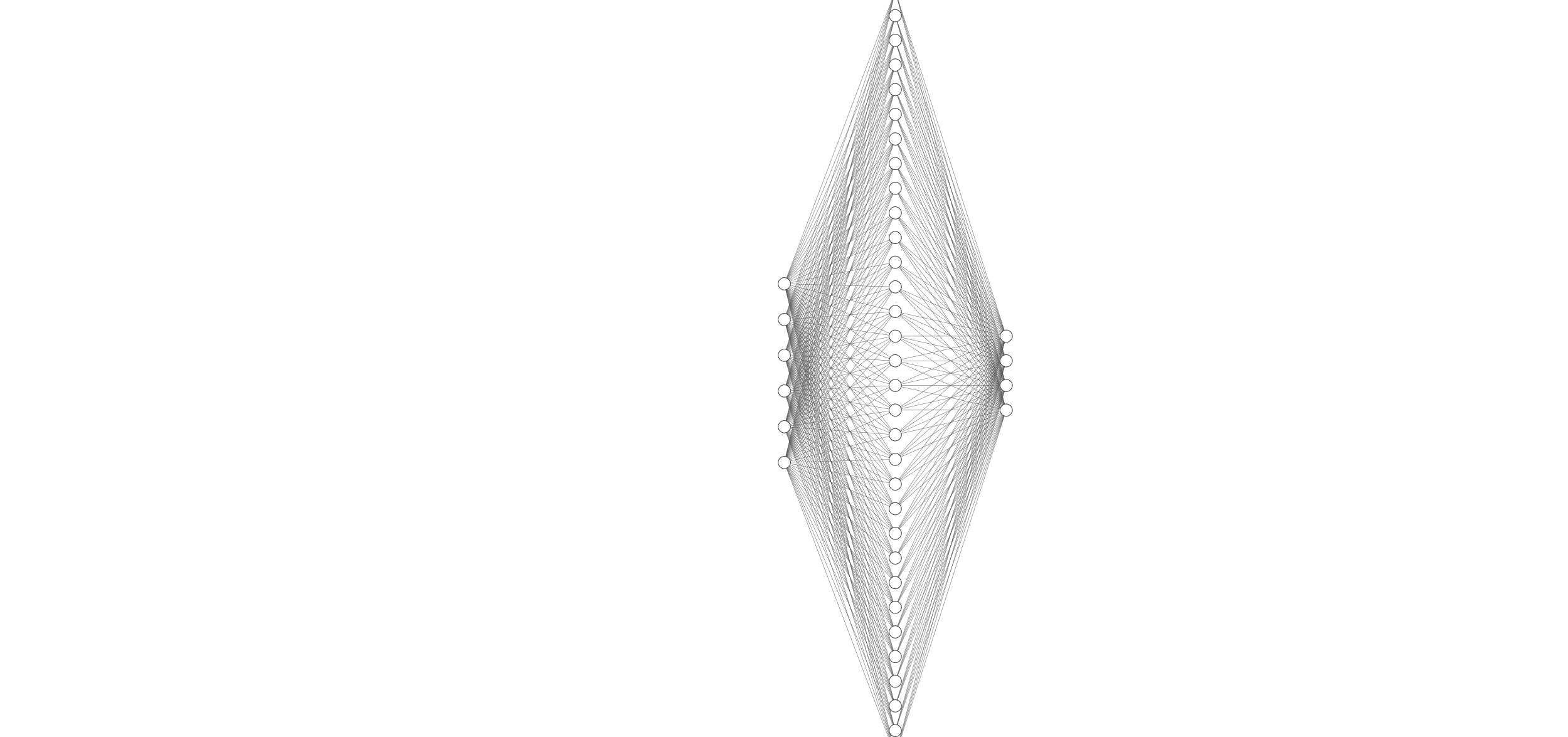
Description automatically generated

Figure 3 – Impact of model architecture on training performance.

Figure 4 – Neural network architecture with one hidden layer.

In order to assess the impact of the number of hidden layers, I created three networks with differing numbers of hidden layers. Each hidden layer has 32 neurons. It appears that larger networks converge more slowly initially but end up achieving a lower loss. This makes sense as larger networks have more capacity to model complex data relationships. However, they also have more tuneable parameters which means that they will likely learn more slowly. In the case of this instance, the difference in performance between 2 and 3 hidden layers was negligible, suggesting that both have learned the same function. Thus in this case, I would suggest that 2 hidden layers is the optimal configuration. Particularly as larger networks tend to have the capacity to overfit to training data as they can almost memorise specific training examples with their surplus power.

A graph of a function

Description automatically generated

Figure 5 - Impact of activation function on ANN training.

I experimented with three commonly used activation functions for neural networks: ReLu, hyperbolic tangent (tanh) and the sigmoid function. These functions have shown to perform well on a number of tasks. Both the sigmoid and hyperbolic tangent functions perform similarly and better than ReLu. This makes sense as the sigmoid function and tanh are fundamentally similar functions, involving exponential functions, and are commonly used for classification tasks.

A graph of a graph showing the impact of optimiser on model training

Description automatically generated

Figure 6 - Impact of model optimiser on training.

I experimented with 3 commonly used optimisers for training artificial neural networks: ADAM, stochastic gradient descent (SGD) and RMSprop. Both ADAM and RMSprop are adaptive learning functions where each weights value is altered by a different rate that decays over time. These approaches are considered state-of-the-art and are widely used. Stochastic gradient descent simply updates each weight by its error gradient multiplied by the learning rate. This approach performs noticeably worse than the adaptive optimisers.

A graph of a graph

Description automatically generated with medium confidence

Figure 7 - Impact of batch size on training.

It is clear that the model struggles to train when the batch size is too small. Batch sizes of 1 and 2 prove too small for the model to converge, whilst batch sizes greater than 16 do appear to work. This is likely because smaller batch sizes make the overall step direction too inaccurate.

Whilst the hyperparameters are interdependent (e.g., the optimal activation function may differ depending on the network architecture), it is clear that some parameters are more important than others. For instance, for this task, the network architecture seems to yield similar results regardless of size. However, using an adaptive optimiser and using either the sigmoid function or tanh as an activation function do seem to impact network performance significantly.

2a + b)

A single decision tree achieves a test accuracy of 83%. Training an ensemble of 200 trees using Adaboost achieves an accuracy of 92%, which is a significant improvement. The ensemble improves performance as each model is trained on more data samples that previous models got wrong. This means that models address the flaws in prior models and means that each model error is related less closely. The models are also weighted according to their classification strength. Thus, the ensemble improves performance over a single tree.

2c)

A graph with a blue line

Description automatically generatedA graph of different colored bars

Description automatically generated

Figure 9 – Individual model errors.

Figure 8 - Error rate of ensemble with different number of models.

The ensemble error rate decreases with the number of models until it plateaus at a final error rate. Twenty individual models appear to be the optimum amount with a low error rate and reduced inference/training time. The individual model error rate appears to be randomly distributed. The ensemble does outperform the average error of individual models. This is expected as we know from the application of Jensen’s inequality that ensemble error will always be at most the average error of individual base models. The ensemble error is bound as follows: where , and .

2c)

A graph of a tree

Description automatically generatedA graph of a tree depth

Description automatically generated

Figure 11 – Training runtime with as max depth varies.

Figure 10 - Impact of tree depth on performance.

The ensemble accuracy increases with maximum tree depth. This is likely because each tree is capable of making more complex splits on the data, leading to better classification. This holds till about a depth of 10. This is because whilst the trees could become deeper, it doesn’t as the data is already sufficiently classified with respect to the training set. As the maximum tree depth increases, so does the runtime. Similar to *Figure 10*, *Figure 11* plateaus at a depth of around 10, indicating that model complexity stagnates at this depth. As decision trees become larger, they are capable of making more advanced (and more accurate classifications). However, they risk overfitting to the training set. Additionally, such trees quickly become hard to interpret as depth grows – a key advantage over other classification techniques. Altering the splitter and criterion hyperparameters seems to have very little impact, suggesting that the model is robust and not overly sensitive to these parameters.

3a + b)

I trained a Gaussian Hidden Markov Model to label sequences of observation data. On the test set, it achieves an accuracy of 87%. That is to say that for each of the test sequences, when predicting the states given the sequence of observations using the Viterbi algorithm, 87% of the states are correctly labelled. This shows the HMM’s are a strong choice for this task and can accurately predict state sequences given corresponding observation sequences.

A black and white squares with white text

Description automatically generatedA red and black squares with white text

Description automatically generated  
The transition matrix shows that people are most likely to continue doing whatever activity they are doing. This makes sense and represents people doing an activity over a period of time. Those who are ambulating are less likely to remain so compared to the other 3 states, which makes sense as it is a more strenuous task. Those who are ambulating will likely sit on the bed or on the chair once they have finished but are unlikely to lie down on the bed immediately. People who are sitting on the bed are relatively likely to ambulate or lie down as their next different state but are unlikely to sit down on the chair. This makes sense as they are already sitting in a comfortable environment and would be unlikely to simply sit on a different object. Similarly, those who are lying down may sit back up on the bed or start ambulating but are unlikely to sit down on the chair immediately afterwards. Finally, those sitting on a chair may lie down or start ambulating but are unlikely to sit on the bed as their next state, as they are already sitting down.

Figure 12 - Transition matrix visualised.

Figure 13 – Logarithm of transition matrix visualised.

3c)

Analysing the distributions for the HMM model, we can see that frequency, phase and RSSI are unimportant features. This is because they have similar mean values and high variances for all emission distributions. Lateral accuracy is also a relatively poor feature as the values all have similar and small means for their emissions distributions. Additionally, their variances are relatively high (in comparison to their means), and thus it is hard to determine which label is most likely given this observed feature.

Frontal accuracy is the most important factor as the emission means are well separated for different labels and as the corresponding variances are low. Vertical accuracy is less important, but still a good feature. It is particularly useful for identifying lying down people, as this has a mean value that differs significantly from the other three label means.

3d)

|  |  |
| --- | --- |
| **Classification Accuracy** | |
| Neural Network | Ensemble |
| 89.9% | 92.5% |

|  |
| --- |
| **Sequence Labelling Accuracy** |
| Hidden Markov Model |
| 86.8% |

Table 1 - Classification accuracy on test set of different models.

Table 2 – HMM performance.

*Tables 1 and 2* summarises the performances of the three models. The ensemble classifier achieves the best performance on the test set, followed by the neural network. Both achieve a strong classification accuracy of around 90%. The HMM classifies 87% of labels correctly when given a sequence of observations. Given that the HMM requires a sequence of observations to make accurate label predictions but still performs marginally worse than the classification techniques (which only require a single observation), I conclude that the HMM has the worst performance of the three models. Conversely, the ensemble technique performs best.

|  |  |  |
| --- | --- | --- |
| **Model Type** | **Training Time(s)** | **Relative Speed** |
| Neural Network | 159.75 | 1x |
| Ensemble | 0.52 | 307x |
| Hidden Markov Model | 0.13 | 1229x |

Table 3 – Model training time.

In terms of training time, the HMM model is the fastest. This is because it is a simplistic model that involves a number of simple calculations on the data. The ensemble is 4 times slower to train than the HMM, but still very fast with less than a second of training time. The neural network is the slowest model to train, taking over 2 minutes to train. Both the neural network and ensemble have variable training times depending on model hyperparameters (e.g., network architecture or number of base models), whilst the HMM training time is only dependent on the size of training data. Additionally, with the neural network, given its tendency to get stuck at a local minimum for this specific task, the actual training time is even longer. As a result, training a neural network is significantly more arduous for this problem.

A diagram of a chair and bed

Description automatically generatedA diagram of a number

Description automatically generated

Figure 15 – Decision tree visualised.

Figure 14 – Transition matrix visualisation.

The HMM benefits from being easy to interpret, with its transition matrix providing a strong intuition towards model performance. Similarly, a decision tree is easy to interpret and can be visualised quite effectively. As the maximum depth of the tree increases, this interpretability is lost somewhat. And within the context of an ensemble model that has 200 trees, the model does prove to be quite difficult to interpret. A neural network is very hard to interpret as it contains lots of weights and biases that work together in an extremely complicated way to produce a classification (see *Figure 4*). Thus, within the context of this specific task, the HMM is the easiest to interpret. As the data is fundamentally sequentially, one could argue that the HMM is more suitable for modelling the task than the other two approaches.

Each approach has various merits, however I would say that the ensemble approach is the most suitable for this task as it is quick to train, achieves a strong classification accuracy and is somewhat interpretable.

4 + 5 + 6)

A diagram of red and green dots

Description automatically generatedA diagram of red and green dots

Description automatically generated

Figure 17 – Plot of responsibility composition for each data point for the GMM.

Figure 16 - PCA results.

*Figure 16* displays the results of using PCA to reduce the dataset dimensionality to 2. The first principal component accounts for 98.2% of the original data variance and 1.6% of the original data variance is explained by the second principal component, accounting for over 99.8% of the original variance in combination.

*Figure 17* depicts the results of a Gaussian Mixture Model that has two components. The redness of a point indicates the responsibility strength from the first responsibility function. The greenness of a point indicates the responsibility strength from the second responsibility function.

At a first glance, both of these scatter plots appear very similar. This demonstrates the strength of the GMM. We can intuitively think of the first responsibility as denoting the likelihood that the tumour is malignant and the second responsibility as denoting the likelihood of a benign tumour. If we use this to classify data, the model classifies 95% of the data correctly (though of course this essentially amounts to evaluation on the training set). The GMM is most uncertain at regions where the red and green dots meet in *Figure 16*, with points being some mixture of green and red (and hence the two distributions).

References

[1] <https://keras.io/api/optimizers/adam/>

[2] <https://arxiv.org/pdf/1412.6980.pdf>