#### DTU Compute

Department of Applied Mathematics and Computer Science



02616

Large-scale Modelling

## Recap from Week 01

- parallel architectures:
  - □ UMA, NUMA, cc-NUMA
- ☐ first steps in MPI:
  - "Hello World" (no communication)
  - "Hello Neighbour" (communication)
  - Ring (communication)
- everything on a single node



# Topics for Week 02

- Memory bandwidth and performance
  - "NUMA in action"
- Networks
  - cluster setup
  - Infiniband and Ethernet
  - bandwidth and latency
- MPI jobs on multiple nodes
  - multi-node batch jobs
  - process placement and binding



Single-core peak performance:

- The TPP is easy to calculate: let us assume
  - □ 2 GHz CPU/core
  - 4 Flops per clock cycle
  - □ => TPP: 8 GFlop/s (per core!)
- □ To obtain that peak performance, we need to be able to feed the core with the right amount of data!



How much data is that?

- 4 floating point operations (add, mult) need 8 floating numbers => 64 bytes (double precision)
- □ That is 64 bytes / clock cycle or 128 GB/s
  - □ 128 GB is the content of more than 27 DVDs!!!
- But what is the memory bandwidth in modern machines?

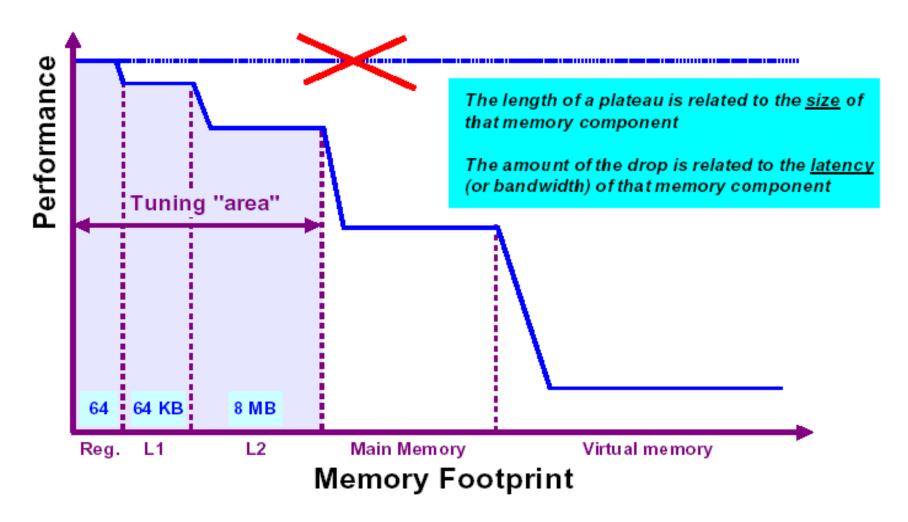


Memory bandwidth of the Xeon E5-2650 v4 family

- equipped with DDR4-2400 DIMMS:
  - □ 2400 MT/s => 19.2 GB/s per memory channel
  - □ 76.8 GB/s maximum (all 4 channels equipped)
- ■with slower DDR4-1600 DIMMS:
  - □ max. 51.2 GB/s
- ■that is the bandwidth per CPU socket
  - ... but each CPU has 12 cores!
  - □ => the memory bandwidth per core is less!!!!

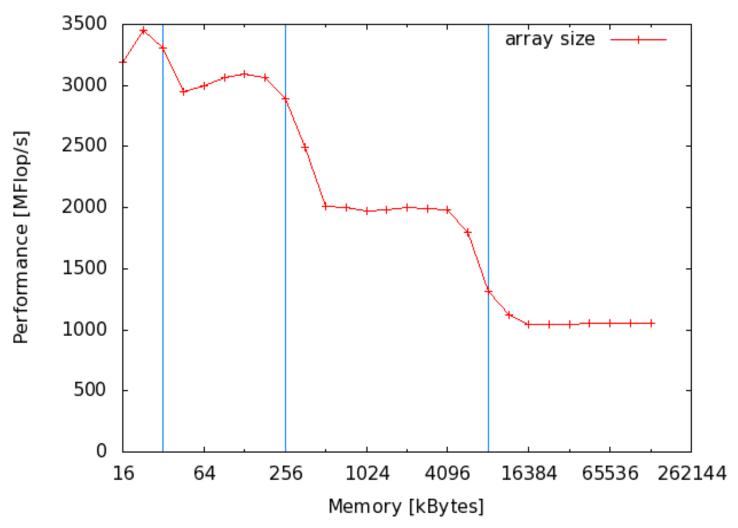


Performance staircase (single core):





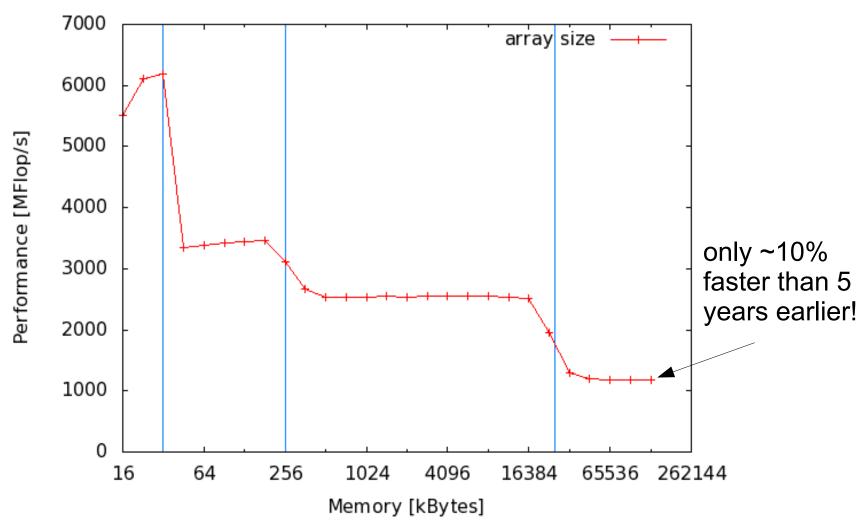
#### Performance matrix times vector





Intel Xeon X5550, 2.67 GHz, 8 MB L3 cache (release: Q1/2009)

#### Performance matrix times vector





Intel Xeon E5-2660v3, 2.66 GHz, 25 MB L3 (release: Q3/2014)

Compute-bound vs memory-bound

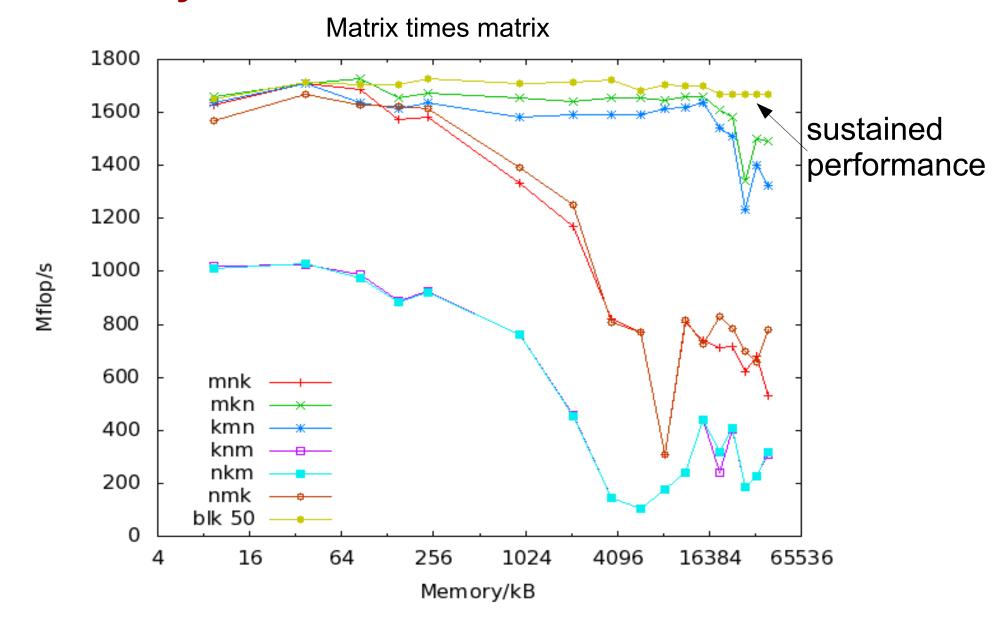
- □ Compute-bound:
  - the number of flops is higher than the number of memops (load/store)
  - example: matrix times matrix
- Memory bound:
  - □ the number of mem-ops is dominating the flops
  - example: matrix times vector



Compute-bound vs memory-bound

- □but ...
- for large problems, even matrix times matrix gets dominated by the memory operations, it turns into a memory bound problem
- ■we know how to solve that e.g. by blocking algorithms, to keep the problem compute bound







Scaling of memory-bound applications

- What happens with memory bound applications on multi-core systems?
- $\square$ N cores one CPU, e.g. N = 4
- N threads execute a memory-bound kernel
  - => all N threads fight for the same mem-bw
  - □ => this is a performance bottleneck
  - => this has a negative effect on scaling (speed-up)



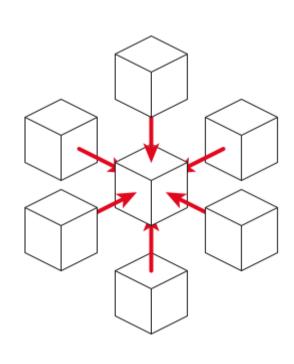
Scaling of memory-bound applications (cont'd)

- □ this effect is visible for all parallel applications, regardless of the programming model, i.e.
  - distributed applications (e.g. MPI)
  - shared-memory applications (e.g. OpenMP)
- adding more cores to the CPU makes the situation even worse!
- adding more sockets helps:
  - increased memory bandwidth
  - the overall performance is bounded by the max. memory bandwidth (saturation)



Example (from the 02614 course):

- □3D Poisson problem: N³ grid points
- 7 point stencil
- ■8 mem-ops per stencil update
- memory bound problem
- data: double precision (64 bit)
- $\square$ N = 1000
- □memory usage: 22.5 GB
- OpenMP parallel implementation





Example (from the 02614 course):

□3D Poisson problem: 1000³ grid points

- Hardware:
  - □ 2x Intel XeonE5-2650 v4, 2.2 GHz
  - □ L3 size: 30MB
  - □ 256 GB RAM (128 GB per socket)
  - □ single core TPP: 35.2 Gflop/s
  - □ 12 cores per socket
  - memory bandwidth per socket: 76.8 GB/s

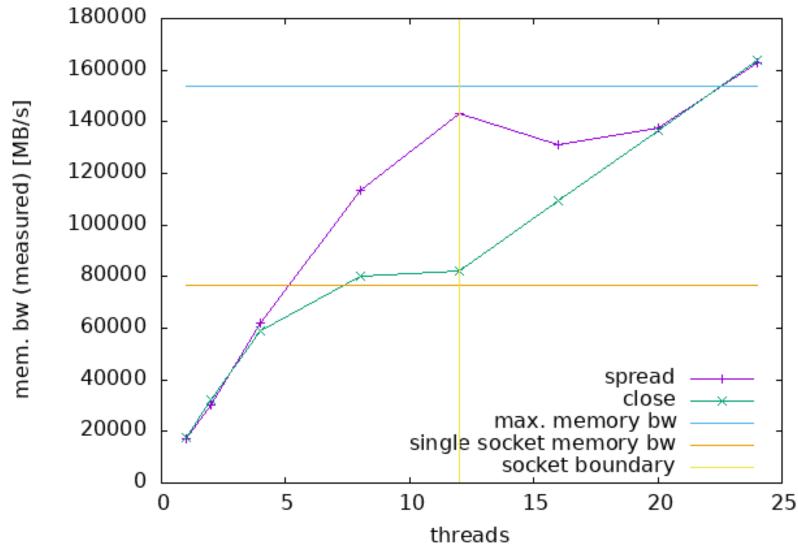


How did we do?

- we can measure the number of stencil updates (lup) per second: Mlup/s
- each lup involves 8 memory operations:
  - 7 loads and 1 store
  - uncertainty: loads and stores can overlap
- our data type is double: 8 bytes
  - □ => 64 bytes per lup
- measured memory bandwidth:
  - MB/s = Mlup/s \* 64 bytes



3d Poisson problem - 1000 x 1000 x 1000 grid
Xeon E5-2650 v4, 2.2 GHz, 12c/socket





02614 - High-Performance Computing

- Lessons learned:
  - using a single socket (close distribution), we are already limited by the socket memory bandwidth when using 8 threads on the 12 cores
  - spreading the threads over both sockets is beneficial for up to 12 threads, i.e. 6 threads per socket
  - □ for larger number of threads, e.g. 20 and 24 threads (the full node), the two distributions approach each other.
  - similar behaviour can be observed when using an MPI implementation of the problem.

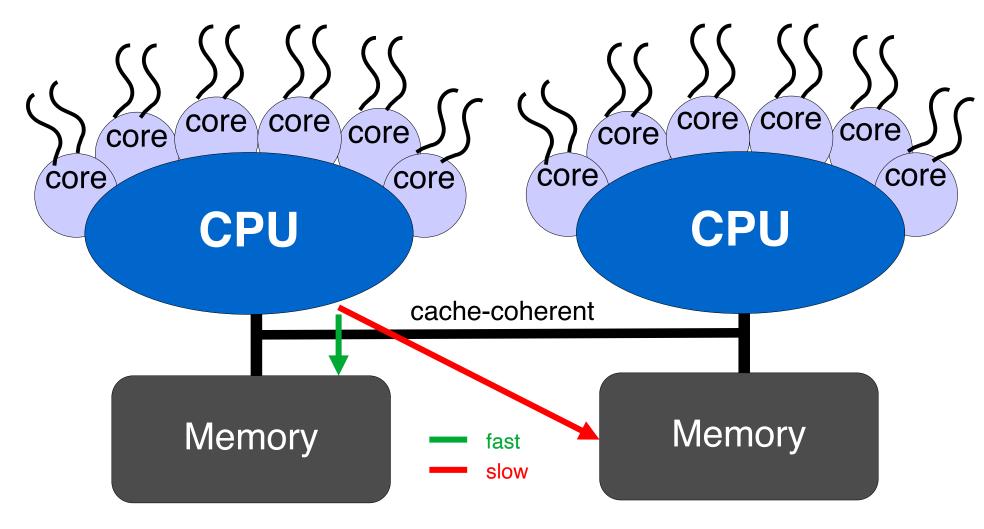


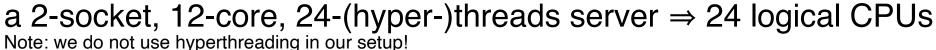
### **Networks**

Cluster of multi-socket machines



## A typical multi-core server

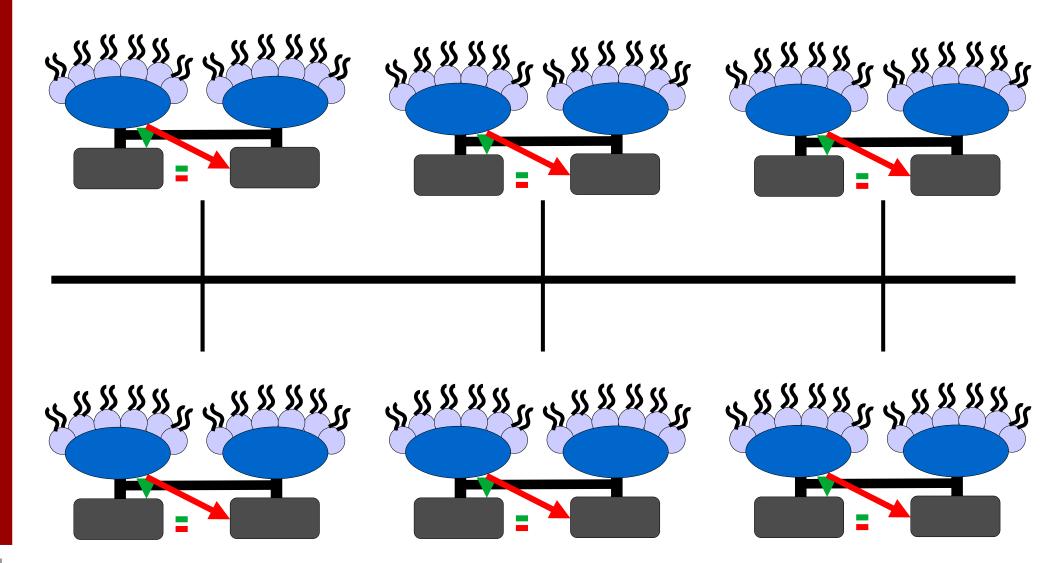






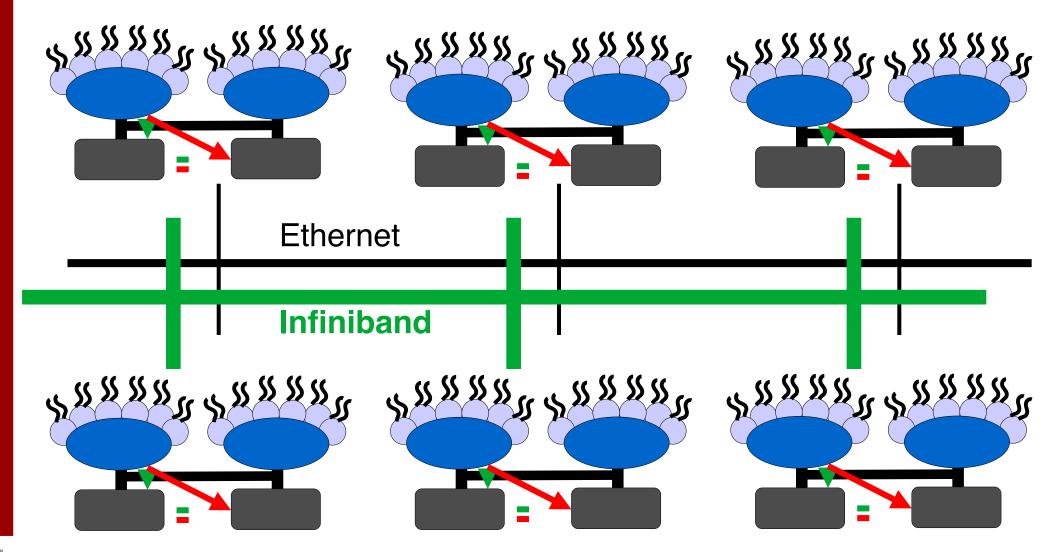
Fall 2025

# Cluster with a single network





## Cluster with two networks





# Why a fast network?

- □ for HPC applications, we want to have
  - a high network bandwidth
  - low latency
  - => minimizing the communication overhead
- this can be achieved by networks like Infiniband (IB), OmniPath (OPA), etc
- other advantages of IB
  - □ RDMA: remote direct memory access doesn't involve the CPU when accessing memory on a remote node
  - GPU Direct: RDMA between a local and remote GPU



# Why a fast network?

Infiniband specifications:

- there are several generations of IB
- the latest generations provide
  - up to 400 Gb/s
  - 3-5 microseconds latency
- □in our setup:
  - □ FDR IB: up 56 Gb/s
  - compare to Ethernet: either 1 Gb/s or 10 Gb/s
  - today's lab: measure the difference in bandwidth and latency between IB and Ethernet



#### Fun fact

What is the memory bandwidth of our brain?

- □ It's really slow: 10 bit/s!
- Read more about it
  - □ "The unbearable slowness of being: Why do we live at 10 bits/s?"



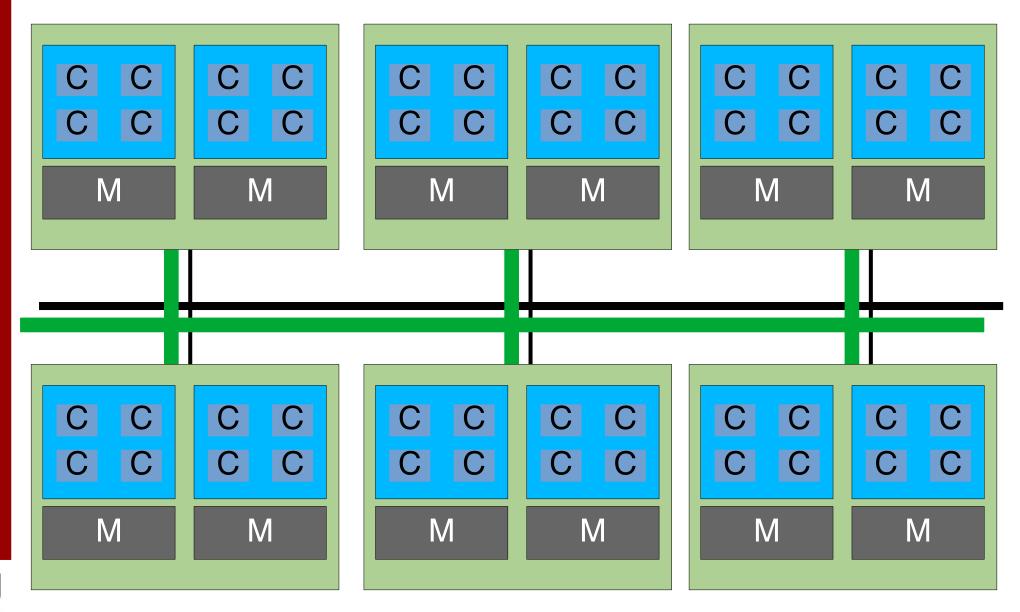
Putting it all together



What we have learned so far:

- The limiting factor in many applications is bandwidth:
  - memory bandwidth in a single node
  - network bandwidth on a network of nodes
- Now let us put those pieces together:
  - □ a cluster of multi-socket (cc-NUMA) systems,
  - connected by both Infiniband and Ethernet





- run an MPI application
  - with N ranks (single-threaded)
  - on M nodes (dual-socket)
  - each node has 2\*P cores (P cores/socket)
- we will have 2\*P\*M locations to place our N ranks on  $(N \le 2*P*M)$
- How does the placement influence the performance of our application?
- How can we control it?
  - interplay between MPI and scheduler (LSF)



Specific example:

- $\square N = 8 \text{ ranks}$
- $\square$ M = 4 nodes
- □P = 4 cores/socket (8 cores per node)
- □32 possible locations for the 8 ranks



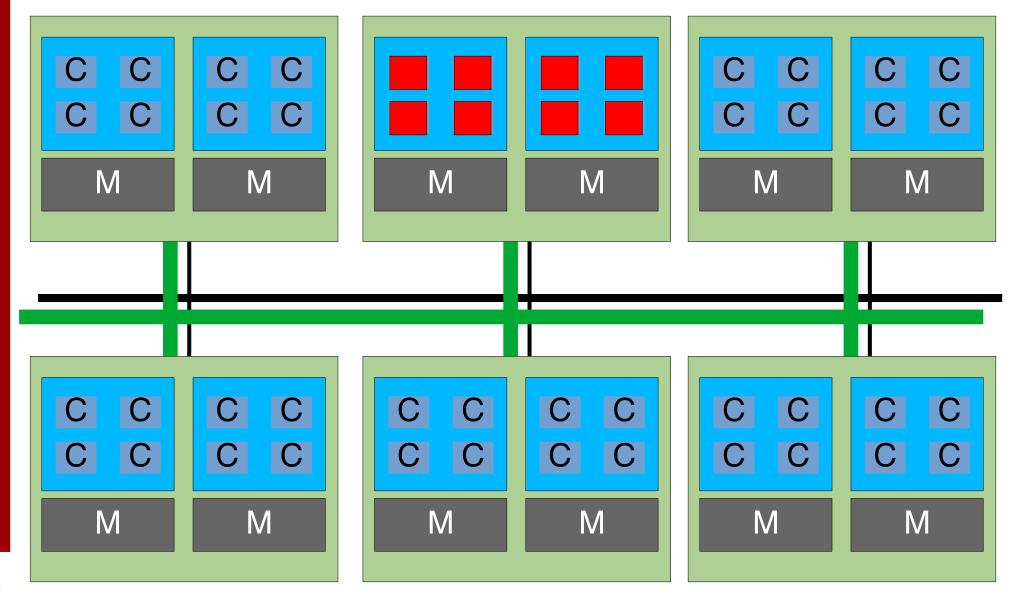
#### Scenario 1:

□all 8 ranks on a single node

```
#BSUB -J MPIapp
#BSUB -o MPIapp_%J.out
#BSUB -n 8
#BSUB -R "span[hosts=1]"

module load mpi/<version>
mpirun ./myapp
```







#### Scenario 2:

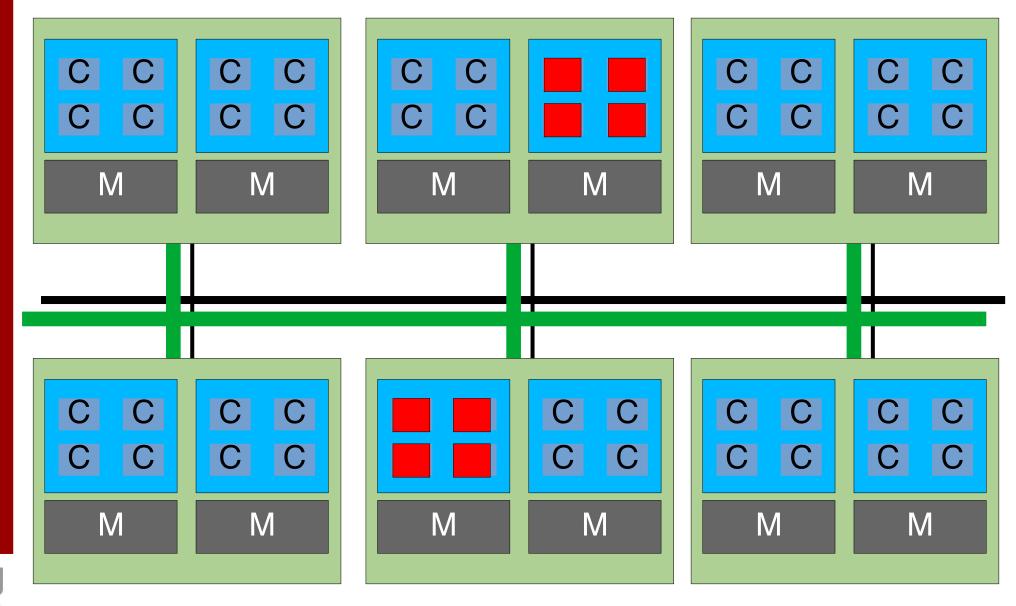
use two nodes, 4 ranks per node

```
#BSUB -J MPIapp
#BSUB -o MPIapp_%J.out
#BSUB -n 8
#BSUB -R "span[ptile=4]"

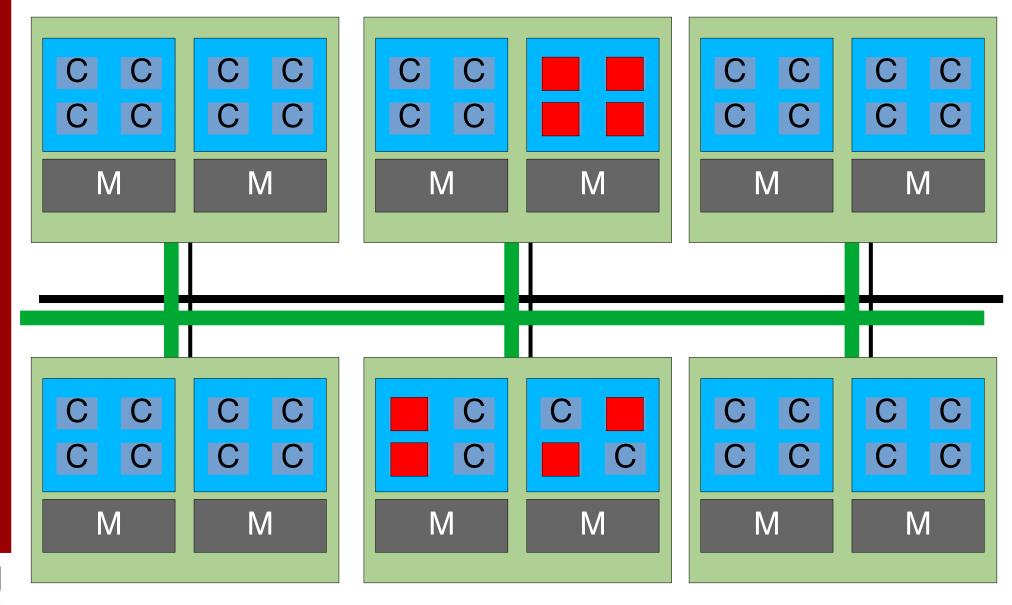
module load mpi/<version>
mpirun ./myapp
```

■What do we get?

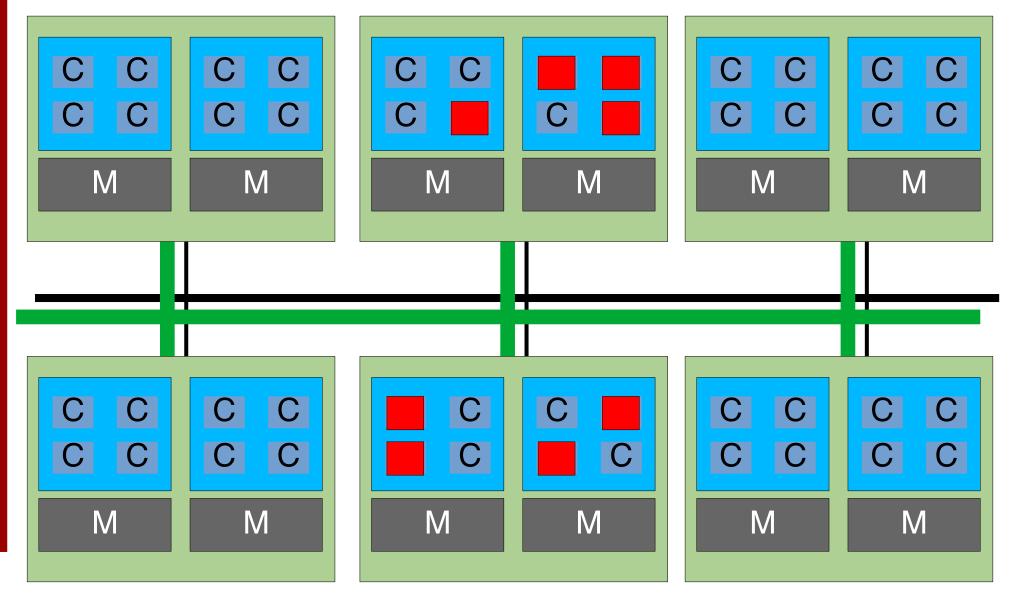




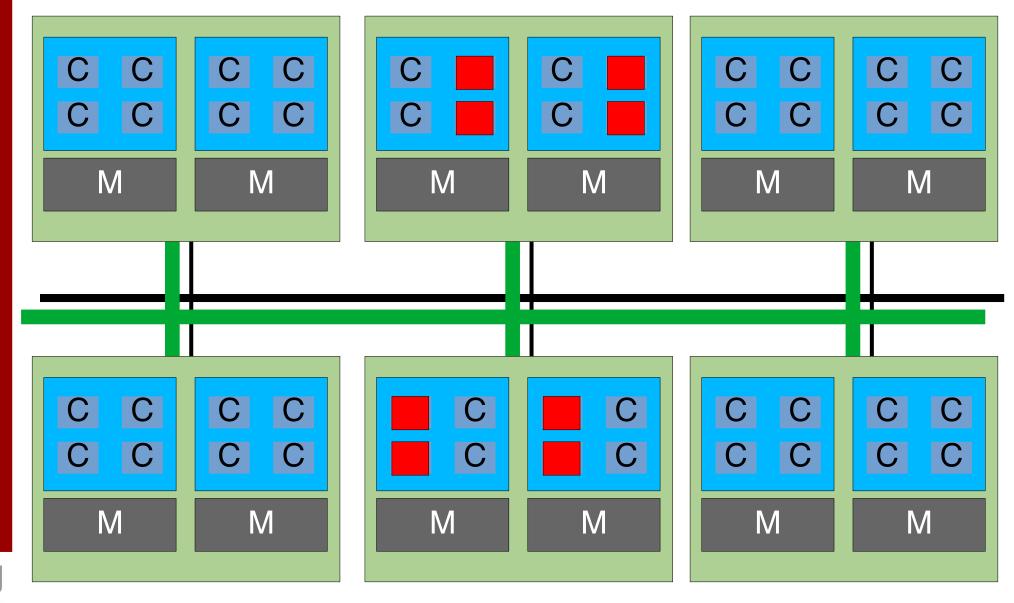














#### Scenario 3:

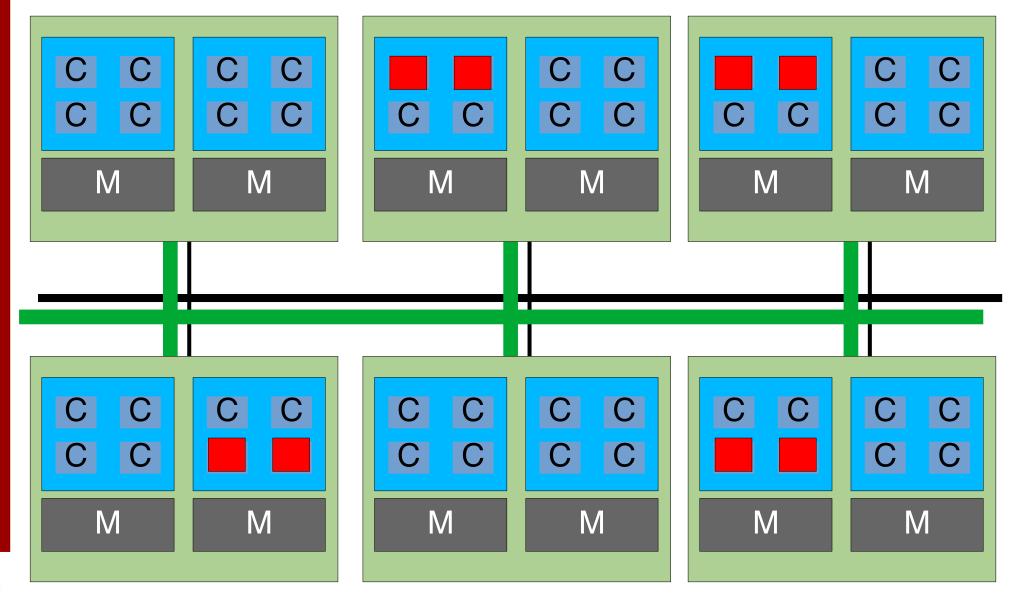
□use 4 nodes, 2 ranks per node

```
#BSUB -J MPIapp
#BSUB -o MPIapp_%J.out
#BSUB -n 8
#BSUB -R "span[ptile=2]"

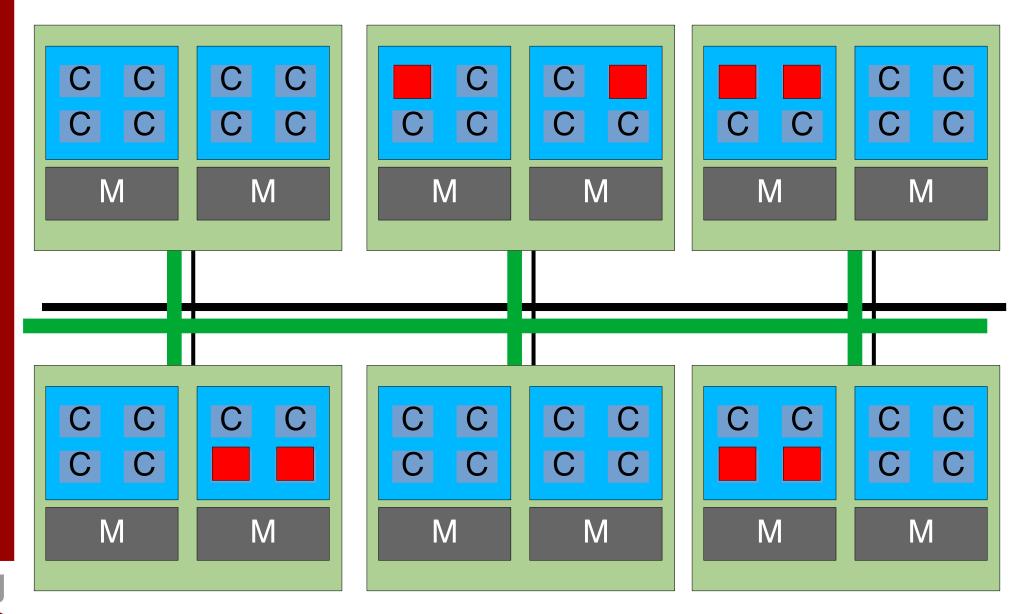
module load mpi/<version>
mpirun ./myapp
```

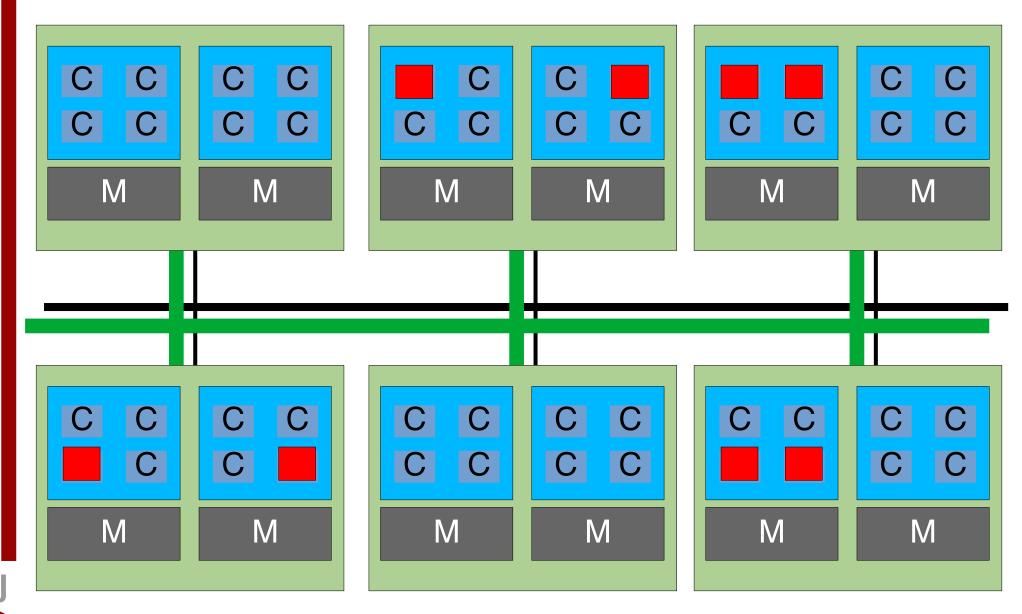
■What do we get?

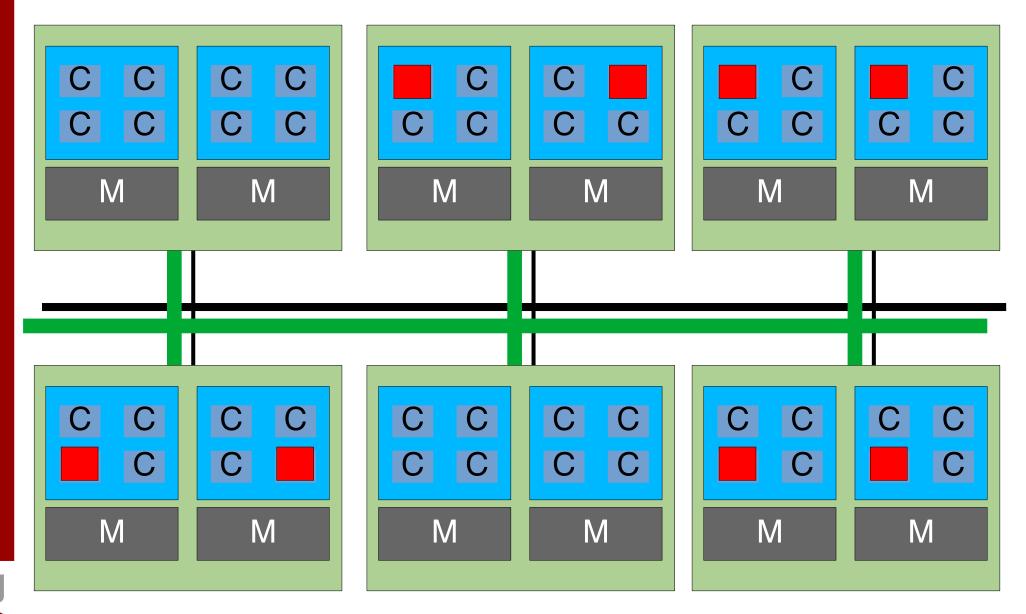












- □ If our MPI application needs a lot of memory bandwidth, then we want to distribute the ranks over as many CPU sockets as possible.
- Here, the OpenMPI runtime options for mapping can help
- □Syntax:
  - mpirun –map-by ppr:n:<resource>
  - ppr stands for "process(es) per resource"
  - <resource> can be package (a CPU socket), core, ...
  - check the documentation for more details



Scenario 3 – with mapping

use 4 (full) nodes, 2 ranks per node

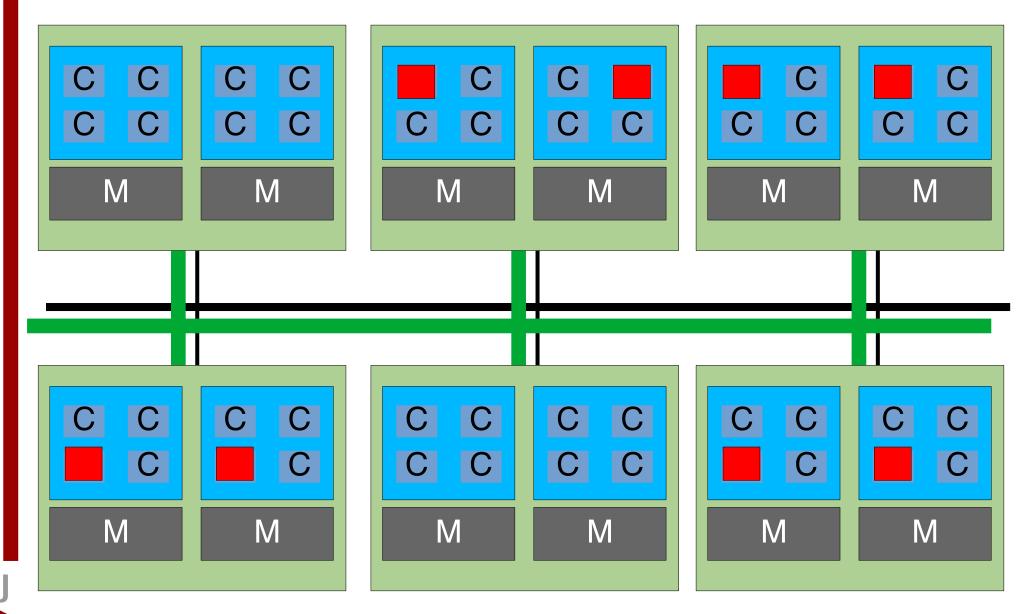
```
#BSUB -J MPIapp
#BSUB -o MPIapp_%J.out
#BSUB -n 32
#BSUB -R "span[ptile=8]"

module load mpi/<version>

mpirun -np 8 -map-by ppr:1:package ./myapp
```

☐ Then we get something like ... on the next slide





- The solution above gives us the maximum bandwidth for our problem
- in the price of allocating more resources than we need!
- There are other ways to implement this, e.g. using the affinity options of LSF, both with and without additional MPI runtime options
  - helps to save resources
  - ... but that's beyond the scope of today!



Today's lab: measure runtime of such a Falplacement scenario 02616 - Large-scale Modelling