Read, filter and transform spectra and metadata

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For a html version of this tutorial, see here. You can also download a pdf.

1 Getting started

1.1 Prerequisites

- First, you need to be familiar how to work into R. Here I give some recommendations to start mastering spectroscopy analysis taks.
- You need to need to now that there are R basic data structures used for analysis. Have a first read here in the $Advanced\ R$ book of Hadley Wickham.

1.2 Topics and goals of this section

- You will learn how to use different R base data structures and basic operations such as subsetting to explore and transform spectral data.
- This hands-on tutorial teaches you the technical skills how to work with data structures in R by the example of manipulating spectral data.

1.3 How to interactively go throught the tutorial

- 1. Use the Clone or Download button and clone/download this tutorial repository from github to your computer.
- 2. Unzip the folder



Figure 1: Bruker ALPHA mid-IR spectrometer (diffuse reflectance Fourier transform infrared) of the Sustainable Agroecosystems group at ETH Zürich with a sample cup filled with soil.

- 3. Double-click the .RProj file and the tutorial is loaded as R project (no need to use setwd() and yourverylonganduniquedirectoryonyourpc or other nasty hard-coded approaches to set the working directory)
- 4. For working with this R markdown notebooks for reproducible and interactive analysis, see here
- 5. Have fun reproducing

2 Reading spectra from OPUS spectrometer files: prerequisites

Spectroscopy modeling requires that we first organize our spectra well. In particular, a proper and reproducible data management of spectral data, metadata, and data from reference chemical analyses is key for all the subsequent data processing and modeling workflow.

The Sustainable Agroecosystems group at ETH relies on Diffuse Reflectance Fourier Transform (DRIFT) infrared spectrometers manufactured by the company Bruker (see Figure 1). The manufacturer relies on a proprietary binary format called OPUS to store an extensive amount of data that includes different types of intermediary spectra. For each sample that was measured a single OPUS file is produced.

3 Reading spectrometer data into the R environment

First, we load the set of packages of tidyverse (see here for details) and the simplerspec package (see here). Simplerspec contains a universal file reader that allows to read selected parameters (e.g. instrument, optic and acquisition parameters) and all types of spectra from a single *OPUS* binary file or a list of files.

```
# Load collection of packages that work together seamlessly for efficient
# analysis workflows
library("tidyverse")
```

-- Attaching packages ------ tidyverse 1.2.1 --

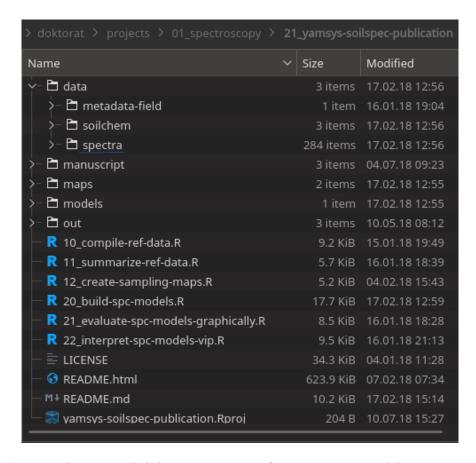


Figure 2: Recommended directory structure for spectroscopy modeling projects

```
## √ ggplot2 3.0.0
                               0.2.5
                      √ purrr
## \sqrt{\text{tibble } 1.4.2}
                      √ dplyr
                               0.7.6
## √ tidyr
            0.8.1
                      √ stringr 1.3.1
## √ readr
            1.1.1
                      √ forcats 0.3.0
## -- Conflicts ------ tidyverse conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                    masks stats::lag()
# Package that facilitates spectral data handling, processing and modeling
library("simplerspec")
## Loading required package: foreach
##
## Attaching package: 'foreach'
## The following objects are masked from 'package:purrr':
##
##
      accumulate, when
```

I recommended that you set up a self-contained directory where all R scripts, data (spectra and chemical reference data), models, outputs (figures and text files of data and model summaries), and predictions live. Further, you can use the folder structure depicted in figure 2 to organize your spectroscopy-related research projects.

When you have spectra that cover separate experiments and/or different locations and times, you might

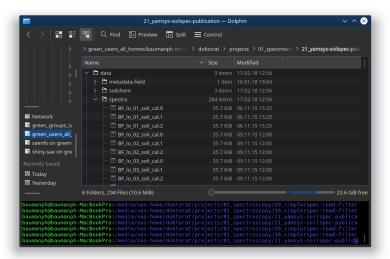


Figure 3: Screenshot showing replicate scans of first three samples reading example.

prefer to organize your spectra as sub-folders within data/spectra. This hands-on is based on spectral data that were used to build and evaluate the YAMSYS spectroscopy reference models. Besides these reference spectra measured with a Bruker ALPHA mid-IR spectrometer at the Sustainable Agroecosystems group at ETH Zürich, there are other spectra that have been acquired to test different questions such as spectrometer cross-comparisons. Therefore, other comparison spectra are in separate paths, e.g. data/spectra/soilspec_eth_bin.

In the Figure below you can see a file explorer screenshot showing OPUS files of three replicate scans for each of the first three reference soil samples. OPUS have the extension .n where n represents an integer of repeated sample measurements starting from 0.

We aim to read all the reference spectra contained within this folder. First, we get the full path names of the file names, which we subsequently assign to the object files:

```
# Extract data from OPUS binary files; list of file paths
files <- list.files("data/spectra", full.names = TRUE)</pre>
```

Note that you need to set the full.names argument to TRUE (default is FALSE to get the path of all *OPUS* spectra files contained within the target directory, otherwise R will not be able to find the files when using the universal simplerspec *OPUS* reader.

You can compactly display the internal structure of the files object:

```
str(files)
```

```
## chr [1:284] "data/spectra/BF_lo_01_soil_cal.0" ...
```

The object files has the data structure atomic vector. Atomic vectors have six possible basic (atomic) vector types. These are logical, integer, real, complex, string (or character) and raw. Vector types can be returned by the R base function typeof(x), which returns the type or internal storage mode an object x. For the files object it is

```
# Check type of files object
typeof(files)
```

[1] "character"

We get the length of the vector or the number of elements by

```
# How many files are listed to read? length of vector
length(files)
```

[1] 284

Base R has subsetting operations that allow you to extract pieces of data structures you are interested in. One of the three base subsetting operators is [.

We subset the character vector files as follows:

```
# Use character subsetting to return the first element
# Subsetting can be seen as complement to str()
# (1) Subsetting with positive integers (position)
files[1:3]

## [1] "data/spectra/BF_lo_01_soil_cal.0" "data/spectra/BF_lo_01_soil_cal.1"
## [3] "data/spectra/BF_lo_01_soil_cal.2"

# (2) Subsetting with negative integers (remove values)
head(files[-c(1:3)], n = 5L) # show only first 5 values

## [1] "data/spectra/BF_lo_02_soil_cal.0" "data/spectra/BF_lo_02_soil_cal.1"
## [3] "data/spectra/BF_lo_02_soil_cal.2" "data/spectra/BF_lo_03_soil_cal.0"
## [5] "data/spectra/BF_lo_03_soil_cal.1"

# The first three elements of the character vector are removed
```

3.1 Spectral measurement data

Bruker FTIR spectrometers produce binary files in the OPUS format that can contain different types of spectra and many parameters such as instrument type and settings that were used at the time of data acquisition and internal processing (e.g. Fourier transform operations). Basically, the entire set of *Setup Measurement Parameters*, selected spectra, supplementary metadata such as the time of measurement are written into *OPUS* binary files. In contrast to simple text files that contain only plain text with a defined character encoding, binary files can contain any type of data represented as sequences of bytes (a single byte is sequence of 8 bits and 1 bit either represents 0 or 1).

Figure 4 shows graphical representation from the OPUS viewer software to get familiarize with types of parameters OPUS files may contain.

You can download the *OPUS viewer* software from **this Bruker webpage** for free. However, Bruker only provides a Windows version and the free version is limited to visualize only final spectra. The remaining spectral blocks can be checked choosing the menu Window > New Report Window and opening OPUS by the menu File > Load File.

The types of spectra and associated data parameters that are saved after a single measurement depend on the options that are selected in the *OPUS* software. For data acquisition, the values under the tab *Advanced* of the *Setup Measurement Parameters* menu window in the *OPUS* software.

Depending on the standard of a binary file, different regions in a file can be interpreted differently by a program. For example, some information at some block positions need to be interpreted as a certain type of number representation whereas others are text. Hence, the interpretation of different bit positions in the file requires either a priori knowledge provided by some file specifications or extensive reverse-engineering.

Instead of sharing the full binary file specification, Bruker ships the *OPUS* macro programming language or Microsoft Visual Basic scripts for automated data acquisition and processing. However, this approaches are very inflexible and not transparent, and therefore not reproducible. Hence, the idea of implementing a file reader that is integrated in the R statistical programming environment was targeted first in the soil.spec

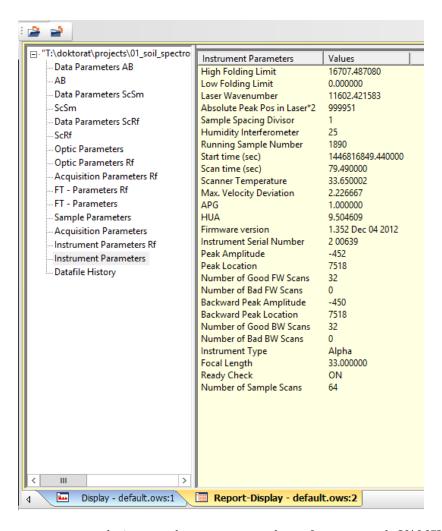


Figure 4: Instrument parameters during sample measurement shown for an example YAMSYS soil reference spectroscopy sample. Spectra and parameters can be shown by the dialogue Window > New Report Window within the OPUS viewer software.

R package created by Andrew Sila (ICRAF, Nairobi), Tomislav Hengl (ISRIC – World Soil Information) and Thomas Terhoeven-Urselmans (former member of ICRAF, Nairobi). soil.spec was created based on the African Soil Information Services (AfSIS) project (see here for more information). Because this reader worked only when applying a restricted set of settings and procedures in OPUS, the idea came up to modify and extend the previously mentioned soil.spec::read.opus() function. This restriction is mainly due to the fact that positions where spectra occur are not fixed and there is no evident accessible information about the sequence of spectra and data parameters and the type of present spectra. Therefore, I have been working extensively on a universal Bruker OPUS format file reader that can correctly assign and read out different spectra types from any type of Bruker FTIR spectrometer with different blocks saved and with and without atmospheric compensation.

Simplerspec comes with reader function written in R, that is intended to be a universal Bruker OPUS file reader that extract spectra and key metadata from files. Usually, one is mostly interested to extract the final absorbance spectra (shown as AB in the *OPUS viewer* software).

3.2 Read the spectral data (OPUS files) as list into R

```
## Register parallel backend for using multiple cores

# Allows to tune the models using parallel processing (e.g. use all available
# cores of a CPU); caret package automatically detects the registered backend
library("doParallel")

# Make a cluster with all possible threads (more than physical cores)
cl <- makeCluster(detectCores())

# Register backend
registerDoParallel(cl)

# Return number of parallel workers
getDoParWorkers() # 8 threads on MacBook Pro (Retina, 15-inch, Mid 2015);

## [1] 8

# Quadcore processor

# Read spectra and metadata of all binary OPUS files into a list
spc_list <- read_opus_univ(fnames = files, extract = c("spc"), parallel = TRUE)</pre>
```

3.3 Use R functions to gain an overview of the spectral data

The extracted spectra and metadata data are within a list. A list is a very flexible R data structure that can contain any other type of R objects. You can think of lists as containers that help to save and transform objects. Lists can contain hierarchically nested elements, e.g. a list can contain lists. In this case, the list contains the following elements:

```
# Return the names of a list; names() returns a character vector
# of the elemelement names and `[` extracts the first 10 names
names(spc_list)[1:10]

## [1] "BF_lo_01_soil_cal.0" "BF_lo_01_soil_cal.1" "BF_lo_01_soil_cal.2"
## [4] "BF_lo_02_soil_cal.0" "BF_lo_02_soil_cal.1" "BF_lo_02_soil_cal.2"
## [7] "BF_lo_03_soil_cal.0" "BF_lo_03_soil_cal.1" "BF_lo_03_soil_cal.2"
## [10] "BF_lo_04_soil_cal.0"

# The names from the spectral data list are identical to the
# files that were read (file names without path of folder where data
```

```
# are contained)
files[1:10]
```

```
## [1] "data/spectra/BF_lo_01_soil_cal.0" "data/spectra/BF_lo_01_soil_cal.1"
## [3] "data/spectra/BF_lo_01_soil_cal.2" "data/spectra/BF_lo_02_soil_cal.0"
## [5] "data/spectra/BF_lo_02_soil_cal.1" "data/spectra/BF_lo_02_soil_cal.2"
## [7] "data/spectra/BF_lo_03_soil_cal.0" "data/spectra/BF_lo_03_soil_cal.1"
## [9] "data/spectra/BF_lo_03_soil_cal.2" "data/spectra/BF_lo_04_soil_cal.0"
```

List subsetting/extraction of components: Lists can be subsetted similar to atomic vectors by the [and [[operators. The most important difference is that [returns a list (sub-list of list) and [[returns the content of a single component of the list (note that a single components can still contain sub-lists). Based on the [operator we can extract spectra and metadata from a single replicate measurement of a sample:

```
# Display structure
str(spc_list["BF_lo_01_soil_cal.0"])
```

```
## List of 1
##
   $ BF_lo_01_soil_cal.0:List of 10
                       :Classes 'tbl_df', 'tbl' and 'data.frame':
##
    ..$ metadata
                                                                    1 obs. of 20 variables:
     .. ..$ unique_id
##
                            : chr "BF_lo_01_soil_cal.0_2015-11-06 14:34:10"
                            : chr "BF_lo_01_soil_cal.0"
##
     .. ..$ file_id
##
     .. ..$ sample_id
                            : chr "BF_lo_01_soil_cal"
##
     .. ..$ rep_no
                            : num 0
##
     .. ..$ date_time_sm
                            : POSIXct[1:1], format: "2015-11-06 14:34:10"
##
     .. ..$ date_time_rf
                            : POSIXct[1:1], format: "2015-11-06 14:30:10"
##
     ....$ sample_name
                            : chr "BF_lo_01_soil_cal"
     ....$ instr_name_range: chr "alpha-mir"
##
##
     ...$ resolution_wn
                            : int 4
##
     .. ..$ result spc
                            : chr "AB"
##
                            : chr "ZnS"
     ....$ beamspl
##
     .. ..$ laser wn
                            : num 11602
##
     .. ..$ spc_in_file
                            : chr "ScSm; ScRf; spc nocomp; spc"
##
     ....$ zero_filling
                            : int 2
##
     ....$ temp_scanner_sm : num 33.7
##
     ....$ temp_scanner_rf : num 33.6
##
     ...$ hum_rel_sm
                            : int 25
##
     ...$ hum_rel_rf
                            : int 25
##
     ....$ hum_abs_sm
                             : num 9.5
     .. ..$ hum_abs_rf
##
                             : num 9.49
##
     ..$ spc
                        :Classes 'data.table' and 'data.frame':
                                                                 1 obs. of 1716 variables:
##
     .. ..$ 3997.4: num 0.112
##
     ....$ 3995.4: num 0.111
     .. ..$ 3993.3: num 0.11
##
##
     ...$ 3991.3: num 0.111
##
     ...$ 3989.2: num 0.111
##
     ...$ 3987.2: num 0.112
##
     .. ..$ 3985.2: num 0.112
     ...$ 3983.1: num 0.112
##
##
     ...$ 3981.1: num 0.111
##
     ....$ 3979 : num 0.111
##
     .. ..$ 3977
                  : num 0.111
                  : num 0.11
##
     .. ..$ 3975
##
     ....$ 3972.9: num 0.109
     ....$ 3970.9: num 0.109
```

```
##
     ....$ 3968.8: num 0.11
##
     .. ..$ 3966.8: num 0.111
##
     .. ..$ 3964.8: num 0.111
     .. ..$ 3962.7: num 0.111
##
##
     .. ..$ 3960.7: num 0.111
##
     .. ..$ 3958.6: num 0.11
     ....$ 3956.6: num 0.11
     ...$ 3954.6: num 0.109
##
##
     .. ..$ 3952.5: num 0.108
##
     .. ..$ 3950.5: num 0.107
     .. ..$ 3948.4: num 0.107
     ....$ 3946.4: num 0.106
##
##
     .. ..$ 3944.4: num 0.106
##
     .. ..$ 3942.3: num 0.108
##
     .. ..$ 3940.3: num 0.108
##
     .. ..$ 3938.3: num 0.11
##
     .. ..$ 3936.2: num 0.11
##
     .. ..$ 3934.2: num 0.109
##
     ...$ 3932.1: num 0.107
##
     ...$ 3930.1: num 0.103
     .. ..$ 3928.1: num 0.102
##
##
     ...$ 3926 : num 0.104
     ....$ 3924 : num 0.104
##
##
     .. ..$ 3921.9: num 0.104
##
     ...$ 3919.9: num 0.106
     ....$ 3917.9: num 0.108
##
     .. ..$ 3915.8: num 0.109
     .. ..$ 3913.8: num 0.11
##
##
     .. ..$ 3911.7: num 0.113
     .. ..$ 3909.7: num 0.112
##
##
     .. ..$ 3907.7: num 0.107
     .. ..$ 3905.6: num 0.102
##
##
     ....$ 3903.6: num 0.0946
     ....$ 3901.5: num 0.0903
##
##
     .. ..$ 3899.5: num 0.093
     ....$ 3897.5: num 0.0965
##
##
     ....$ 3895.4: num 0.1
     .. ..$ 3893.4: num 0.107
##
##
     ...$ 3891.3: num 0.108
##
     .. ..$ 3889.3: num 0.104
     .. ..$ 3887.3: num 0.105
##
     ...$ 3885.2: num 0.105
     .. ..$ 3883.2: num 0.101
##
##
     .. ..$ 3881.1: num 0.103
     .. ..$ 3879.1: num 0.104
     .. ..$ 3877.1: num 0.103
##
     ....$ 3875 : num 0.103
##
##
     ....$ 3873 : num 0.0997
##
     ....$ 3870.9: num 0.0971
##
     ....$ 3868.9: num 0.0937
##
     ....$ 3866.9: num 0.0923
##
     .. ..$ 3864.8: num 0.0978
##
     .. ..$ 3862.8: num 0.102
##
     ....$ 3860.8: num 0.101
```

```
##
     ...$ 3858.7: num 0.1
##
     ...$ 3856.7: num 0.103
##
     ...$ 3854.6: num 0.107
##
     ....$ 3852.6: num 0.0999
##
     ....$ 3850.6: num 0.0927
     ....$ 3848.5: num 0.0989
##
     .. ..$ 3846.5: num 0.109
##
     ....$ 3844.4: num 0.11
##
##
     ....$ 3842.4: num 0.101
##
     ....$ 3840.4: num 0.0939
##
     ....$ 3838.3: num 0.093
##
     ....$ 3836.3: num 0.0941
##
     ....$ 3834.2: num 0.0988
##
     ....$ 3832.2: num 0.106
##
     ....$ 3830.2: num 0.11
##
     ....$ 3828.1: num 0.11
##
     .. ..$ 3826.1: num 0.108
##
     ....$ 3824 : num 0.105
##
     ....$ 3822 : num 0.103
##
     .. ..$ 3820
                  : num 0.0964
##
     ....$ 3817.9: num 0.0978
##
     ...$ 3815.9: num 0.11
##
     ....$ 3813.8: num 0.116
     .. ..$ 3811.8: num 0.118
##
##
     ...$ 3809.8: num 0.122
##
     .. ..$ 3807.7: num 0.122
##
     .. ..$ 3805.7: num 0.111
     .. ..$ 3803.6: num 0.105
##
##
     ....$ 3801.6: num 0.107
##
     .. ..$ 3799.6: num 0.105
##
     ....$ 3797.5: num 0.11
##
     .. .. [list output truncated]
     .. ..- attr(*, ".internal.selfref")=<externalptr>
##
##
                          : NULL
     ..$ spc_nocomp
##
     ..$ sc sm
                          : NULL
##
     ..$ sc_rf
                          : NULL
##
     ..$ ig_sm
                          : NULL
##
     ..$ ig_rf
                          : NULL
##
     ..$ wavenumbers
                          : num [1:1716] 3997 3995 3993 3991 3989 ...
##
     ..$ wavenumbers_sc_sm: NULL
     ..$ wavenumbers_sc_rf: NULL
```

The above code extracts a list with one element that is named BF_lo_01_soil_cal.0, whereas using [[shows the content of the subsetted list and the name is not shown anymore. The content contains again 9 elements, as str() reveals:

```
str(spc_list[["BF_lo_01_soil_cal.0"]])
## List of 10
                      :Classes 'tbl_df', 'tbl' and 'data.frame':
##
   $ metadata
                                                                   1 obs. of 20 variables:
##
     ..$ unique_id
                         : chr "BF_lo_01_soil_cal.0_2015-11-06 14:34:10"
##
     ..$ file_id
                         : chr "BF_lo_01_soil_cal.0"
##
     ..$ sample_id
                         : chr "BF_lo_01_soil_cal"
##
     ..$ rep_no
                         : num 0
                         : POSIXct[1:1], format: "2015-11-06 14:34:10"
##
     ..$ date_time_sm
```

```
: POSIXct[1:1], format: "2015-11-06 14:30:10"
##
     ..$ date time rf
##
     ..$ sample_name
                      : chr "BF_lo_01_soil_cal"
     ..$ instr_name_range: chr "alpha-mir"
##
##
     ..$ resolution_wn : int 4
                        : chr "AB"
##
     ..$ result spc
##
     ..$ beamspl
                        : chr "ZnS"
##
     ..$ laser wn
                        : num 11602
##
     ..$ spc_in_file
                        : chr "ScSm; ScRf; spc_nocomp; spc"
     ..$ zero_filling
##
                         : int 2
##
     ..$ temp_scanner_sm : num 33.7
##
     ..$ temp_scanner_rf : num 33.6
##
     ..$ hum_rel_sm
                        : int 25
                         : int 25
##
     ..$ hum_rel_rf
                        : num 9.5
##
     ..$ hum_abs_sm
##
     ..$ hum_abs_rf
                        : num 9.49
##
    $ spc
                       :Classes 'data.table' and 'data.frame': 1 obs. of 1716 variables:
##
     ..$ 3997.4: num 0.112
##
     ..$ 3995.4: num 0.111
##
     ..$ 3993.3: num 0.11
     ..$ 3991.3: num 0.111
##
##
     ..$ 3989.2: num 0.111
##
     ..$ 3987.2: num 0.112
     ..$ 3985.2: num 0.112
##
##
     ..$ 3983.1: num 0.112
##
     ..$ 3981.1: num 0.111
##
     ..$ 3979 : num 0.111
##
     ..$ 3977 : num 0.111
##
     ..$ 3975 : num 0.11
##
     ..$ 3972.9: num 0.109
     ..$ 3970.9: num 0.109
##
     ..$ 3968.8: num 0.11
##
##
     ..$ 3966.8: num 0.111
##
     ..$ 3964.8: num 0.111
##
     ..$ 3962.7: num 0.111
     ..$ 3960.7: num 0.111
##
##
     ..$ 3958.6: num 0.11
##
     ..$ 3956.6: num 0.11
##
     ..$ 3954.6: num 0.109
##
     ..$ 3952.5: num 0.108
     ..$ 3950.5: num 0.107
##
##
     ..$ 3948.4: num 0.107
     ..$ 3946.4: num 0.106
##
     ..$ 3944.4: num 0.106
##
##
     ..$ 3942.3: num 0.108
##
     ..$ 3940.3: num 0.108
##
     ..$ 3938.3: num 0.11
     ..$ 3936.2: num 0.11
##
##
     ..$ 3934.2: num 0.109
##
     ..$ 3932.1: num 0.107
     ..$ 3930.1: num 0.103
##
##
     ..$ 3928.1: num 0.102
##
     ..$ 3926 : num 0.104
##
     ..$ 3924 : num 0.104
     ..$ 3921.9: num 0.104
##
```

```
##
     ..$ 3919.9: num 0.106
##
     ..$ 3917.9: num 0.108
##
     ..$ 3915.8: num 0.109
     ..$ 3913.8: num 0.11
##
##
     ..$ 3911.7: num 0.113
##
     ..$ 3909.7: num 0.112
     ..$ 3907.7: num 0.107
     ..$ 3905.6: num 0.102
##
##
     ..$ 3903.6: num 0.0946
##
     ..$ 3901.5: num 0.0903
     ..$ 3899.5: num 0.093
     ..$ 3897.5: num 0.0965
##
     ..$ 3895.4: num 0.1
##
     ..$ 3893.4: num 0.107
##
##
     ..$ 3891.3: num 0.108
##
     ..$ 3889.3: num 0.104
##
     ..$ 3887.3: num 0.105
##
     ..$ 3885.2: num 0.105
##
     ..$ 3883.2: num 0.101
##
     ..$ 3881.1: num 0.103
##
     ..$ 3879.1: num 0.104
##
     ..$ 3877.1: num 0.103
     ..$ 3875 : num 0.103
##
##
     ..$ 3873 : num 0.0997
##
     ..$ 3870.9: num 0.0971
     ..$ 3868.9: num 0.0937
##
     ..$ 3866.9: num 0.0923
     ..$ 3864.8: num 0.0978
##
##
     ..$ 3862.8: num 0.102
##
     ..$ 3860.8: num 0.101
##
     ..$ 3858.7: num 0.1
##
     ..$ 3856.7: num 0.103
##
     ..$ 3854.6: num 0.107
##
     ..$ 3852.6: num 0.0999
##
     ..$ 3850.6: num 0.0927
##
     ..$ 3848.5: num 0.0989
##
     ..$ 3846.5: num 0.109
##
     ..$ 3844.4: num 0.11
##
     ..$ 3842.4: num 0.101
##
     ..$ 3840.4: num 0.0939
##
     ..$ 3838.3: num 0.093
##
     ..$ 3836.3: num 0.0941
     ..$ 3834.2: num 0.0988
##
##
     ..$ 3832.2: num 0.106
     ..$ 3830.2: num 0.11
     ..$ 3828.1: num 0.11
##
##
     ..$ 3826.1: num 0.108
##
     ..$ 3824 : num 0.105
##
     ..$ 3822 : num 0.103
##
     ..$ 3820 : num 0.0964
##
     ..$ 3817.9: num 0.0978
##
     ..$ 3815.9: num 0.11
##
     ..$ 3813.8: num 0.116
##
     ..$ 3811.8: num 0.118
```

```
##
     ..$ 3809.8: num 0.122
##
     ..$ 3807.7: num 0.122
##
     ..$ 3805.7: num 0.111
##
     ..$ 3803.6: num 0.105
##
     ..$ 3801.6: num 0.107
     ..$ 3799.6: num 0.105
##
     ..$ 3797.5: num 0.11
##
##
     .. [list output truncated]
##
     ..- attr(*, ".internal.selfref")=<externalptr>
##
    $ spc_nocomp
                       : NULL
##
    $ sc_sm
                       : NULL
                       : NULL
##
    $ sc_rf
##
                       : NULL
    $ ig_sm
                       : NULL
##
  $ ig_rf
                       : num [1:1716] 3997 3995 3993 3991 3989 ...
##
  $ wavenumbers
##
    $ wavenumbers_sc_sm: NULL
## $ wavenumbers_sc_rf: NULL
head(spc_list[["BF_lo_01_soil_cal.0"]][["wavenumbers"]])
```

[1] 3997.397 3995.357 3993.318 3991.278 3989.239 3987.199

[1] TRUE

Using the function ls() returns a vector of character strings giving the names of the list:

To extract nested elements from a list, you can repeatedly apply subsetting operators. Besides using name subsetting for named data structures that contain a name attribute you can also use integers as index or logical vectors (TRUE and FALSE).

```
names(spc_list["BF_lo_01_soil_cal.0"]) # subset by name of first element

## [1] "BF_lo_01_soil_cal.0"

# subset by integer index, result is identical
names(spc_list[1]) == names(spc_list["BF_lo_01_soil_cal.0"])
```

For logical subsetting we create a new vector containing TRUE or FALSE that is of same length as the spectra list spc_list. Usually logical type vectors are returned when testing conditions using binary operators that allow the comparison of values in atomic vectors (see R help for relational operators by entering ?Comparision in the R console; e.g. <, >, ==). Here, we create a logical vector logical_subset manually in order to illustrate that subsetting also works with vectors of type logical:

```
# repeat FALSE length(spc_list) times
logical_subset <- rep(FALSE, length(spc_list))

# Print subsetting vector
logical_subset</pre>
```

[1] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE

```
[12] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
##
   [23] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [34] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [45] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
   [56] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [67] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [78] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [89] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [100] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [111] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [122] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [133] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [144] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [155] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [166] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [177] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [188] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [199] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [210] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [221] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [232] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [243] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [254] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [265] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
## [276] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
# Check type
typeof(logical_subset)
## [1] "logical"
Subsetting and assignment can be combined to replace the third element with FALSE:
# Replace the 3rd element with TRUE; use subsetting and assignment
logical_subset[3] <- TRUE</pre>
Subsequently, we can use the newly created logical vector for subsetting the spectral data list
# Extract list with `[`; use str() to show a compact output that
# is nicely printed
str(spc_list[logical_subset]) # Returns positions that are TRUE, element 3
## List of 1
##
   $ BF lo 01 soil cal.2:List of 10
##
    ..$ metadata
                      :Classes 'tbl_df', 'tbl' and 'data.frame':
                                                                1 obs. of 20 variables:
                           : chr "BF_lo_01_soil_cal.2_2015-11-06 14:40:55"
##
    .. ..$ unique_id
                           : chr "BF_lo_01_soil_cal.2"
##
     .. ..$ file_id
##
                           : chr "BF_lo_01_soil_cal"
     .. ..$ sample_id
##
     .. ..$ rep_no
                           : num 2
##
     .. ..$ date_time_sm
                           : POSIXct[1:1], format: "2015-11-06 14:40:55"
                           : POSIXct[1:1], format: "2015-11-06 14:30:10"
##
     .. ..$ date_time_rf
##
     .. ..$ sample_name
                           : chr "BF_lo_01_soil_cal"
##
     ....$ instr_name_range: chr "alpha-mir"
##
     .. ..$ resolution_wn
                          : int 4
##
     ....$ result_spc
                           : chr "AB"
##
    ....$ beamspl
                           : chr "ZnS"
```

: num 11602

##

.. ..\$ laser_wn

```
.. ..$ spc_in_file
                           : chr "ScSm; ScRf; spc_nocomp; spc"
                            : int 2
##
     ...$ zero_filling
##
     ....$ temp_scanner_sm : num 33.7
     ....$ temp_scanner_rf : num 33.6
##
##
     ....$ hum_rel_sm
                            : int 25
##
     ....$ hum rel rf
                            : int 25
     .. ..$ hum_abs_sm
                           : num 9.51
##
                            : num 9.49
     .. ..$ hum_abs_rf
##
    ..$ spc
                        :Classes 'data.table' and 'data.frame': 1 obs. of 1716 variables:
##
     .. ..$ 3997.4: num 0.136
     .. ..$ 3995.4: num 0.135
     .. ..$ 3993.3: num 0.135
##
     .. ..$ 3991.3: num 0.135
##
##
     .. ..$ 3989.2: num 0.135
     ....$ 3987.2: num 0.136
##
##
     .. ..$ 3985.2: num 0.136
##
     .. ..$ 3983.1: num 0.136
##
     .. ..$ 3981.1: num 0.136
##
     ...$ 3979 : num 0.135
     ....$ 3977 : num 0.135
##
##
     ....$ 3975 : num 0.134
##
     .. ..$ 3972.9: num 0.133
     .. ..$ 3970.9: num 0.134
##
##
     .. ..$ 3968.8: num 0.135
##
     .. ..$ 3966.8: num 0.135
     .. ..$ 3964.8: num 0.135
##
     .. ..$ 3962.7: num 0.136
     .. ..$ 3960.7: num 0.135
##
     .. ..$ 3958.6: num 0.134
     .. ..$ 3956.6: num 0.133
##
     .. ..$ 3954.6: num 0.133
##
     .. ..$ 3952.5: num 0.131
##
     .. ..$ 3950.5: num 0.132
##
     .. ..$ 3948.4: num 0.131
##
     .. ..$ 3946.4: num 0.13
     .. ..$ 3944.4: num 0.131
##
##
     .. ..$ 3942.3: num 0.132
##
     ...$ 3940.3: num 0.132
##
     .. ..$ 3938.3: num 0.133
     .. ..$ 3936.2: num 0.134
##
##
     .. ..$ 3934.2: num 0.134
     .. ..$ 3932.1: num 0.132
##
     .. ..$ 3930.1: num 0.128
##
     .. ..$ 3928.1: num 0.126
     ....$ 3926 : num 0.129
     ....$ 3924 : num 0.129
##
     .. ..$ 3921.9: num 0.127
##
##
     .. ..$ 3919.9: num 0.13
##
     .. ..$ 3917.9: num 0.133
     .. ..$ 3915.8: num 0.134
##
##
     .. ..$ 3913.8: num 0.135
##
     .. ..$ 3911.7: num 0.137
##
     .. ..$ 3909.7: num 0.135
     .. ..$ 3907.7: num 0.131
##
```

```
##
     .. ..$ 3905.6: num 0.126
##
     .. ..$ 3903.6: num 0.12
##
     ...$ 3901.5: num 0.116
     .. ..$ 3899.5: num 0.118
##
##
     .. ..$ 3897.5: num 0.119
##
     .. ..$ 3895.4: num 0.122
     .. ..$ 3893.4: num 0.131
     ...$ 3891.3: num 0.133
##
##
     .. ..$ 3889.3: num 0.128
##
     .. ..$ 3887.3: num 0.13
     .. ..$ 3885.2: num 0.13
     .. ..$ 3883.2: num 0.125
##
##
     .. ..$ 3881.1: num 0.128
##
     .. ..$ 3879.1: num 0.128
##
     .. ..$ 3877.1: num 0.126
##
     ....$ 3875 : num 0.127
##
     ....$ 3873 : num 0.126
##
     .. ..$ 3870.9: num 0.124
##
     ...$ 3868.9: num 0.119
##
     ...$ 3866.9: num 0.116
     .. ..$ 3864.8: num 0.122
##
##
     .. ..$ 3862.8: num 0.126
     .. ..$ 3860.8: num 0.124
##
##
     ....$ 3858.7: num 0.122
##
     .. ..$ 3856.7: num 0.128
     .. ..$ 3854.6: num 0.138
##
     .. ..$ 3852.6: num 0.131
     ....$ 3850.6: num 0.117
##
##
     .. ..$ 3848.5: num 0.12
##
     .. ..$ 3846.5: num 0.131
##
     .. ..$ 3844.4: num 0.133
     .. ..$ 3842.4: num 0.126
##
##
     .. ..$ 3840.4: num 0.119
##
     .. ..$ 3838.3: num 0.119
##
     .. ..$ 3836.3: num 0.119
##
     ...$ 3834.2: num 0.122
##
     ....$ 3832.2: num 0.13
##
     .. ..$ 3830.2: num 0.134
##
     .. ..$ 3828.1: num 0.135
##
     .. ..$ 3826.1: num 0.131
     ...$ 3824 : num 0.128
##
     ...$ 3822 : num 0.129
     ...$ 3820 : num 0.121
##
##
     .. ..$ 3817.9: num 0.122
     .. ..$ 3815.9: num 0.135
     ....$ 3813.8: num 0.139
##
##
     .. ..$ 3811.8: num 0.139
##
     .. ..$ 3809.8: num 0.145
##
     .. ..$ 3807.7: num 0.147
     .. ..$ 3805.7: num 0.135
##
##
     .. ..$ 3803.6: num 0.128
##
     ...$ 3801.6: num 0.132
##
     .. ..$ 3799.6: num 0.13
     .. ..$ 3797.5: num 0.134
##
```

```
##
     .. .. [list output truncated]
##
     .. ..- attr(*, ".internal.selfref")=<externalptr>
##
     ..$ spc nocomp
                           : NULL
##
     ..$ sc_sm
                           : NULL
##
     ..$ sc_rf
                           : NULL
##
     ..$ ig_sm
                           : NULL
##
     ..$ ig_rf
                           : NULL
                           : num [1:1716] 3997 3995 3993 3991 3989 ...
##
     ..$ wavenumbers
##
     ..$ wavenumbers_sc_sm: NULL
     ..$ wavenumbers_sc_rf: NULL
```

Samples from site abbreviation "tb" (Tieningboué)

We can also test if the spectral list contains certain characters in the file name by using pattern matching functions. If one has used the string "_tb_" as part of the sample identifier to specify the sampling region in the file names, we might be interested in selecting only spectra and metadata of these region ("_tb_" stands for the site Tieningboué in Côte d'Ivoire for YAMSYS spectroscopy reference samples).

```
contains_tb <- grepl(pattern = "tb", x = names(spc_list))</pre>
# Show names of spectral data list elements that are returned by
# looking for "CI"
names(spc_list[contains_tb])
    [1] "CI_tb_01_soil_cal.0" "CI_tb_01_soil_cal.1" "CI_tb_01_soil_cal.2"
   [4] "CI_tb_02_soil_cal.0" "CI_tb_02_soil_cal.1" "CI_tb_02_soil_cal.2"
##
  [7] "CI_tb_02_soil_cal.3" "CI_tb_02_soil_cal.4" "CI_tb_02_soil_cal.5"
## [10] "CI_tb_03_soil_cal.0" "CI_tb_03_soil_cal.1" "CI_tb_03_soil_cal.2"
## [13] "CI tb 04 soil cal.0" "CI tb 04 soil cal.1" "CI tb 04 soil cal.2"
## [16] "CI_tb_05_soil_cal.0" "CI_tb_05_soil_cal.1" "CI_tb_05_soil_cal.2"
## [19] "CI_tb_06_soil_cal.0" "CI_tb_06_soil_cal.1" "CI_tb_06_soil_cal.2"
## [22] "CI_tb_07_soil_cal.0" "CI_tb_07_soil_cal.1" "CI_tb_07_soil_cal.2"
## [25] "CI_tb_08_soil_cal.0" "CI_tb_08_soil_cal.1" "CI_tb_08_soil_cal.2"
## [28] "CI_tb_09_soil_cal.0" "CI_tb_09_soil_cal.1" "CI_tb_09_soil_cal.2"
## [31] "CI_tb_10_soil_cal.0" "CI_tb_10_soil_cal.1" "CI_tb_10_soil_cal.2"
## [34] "CI_tb_11_soil_cal.0" "CI_tb_11_soil_cal.1" "CI_tb_11_soil_cal.2"
## [37] "CI_tb_12_soil_cal.0" "CI_tb_12_soil_cal.1" "CI_tb_12_soil_cal.2"
## [40] "CI_tb_13_soil_cal.0" "CI_tb_13_soil_cal.1" "CI_tb_13_soil_cal.2"
## [43] "CI_tb_14_soil_cal.0" "CI_tb_14_soil_cal.1" "CI_tb_14_soil_cal.2"
## [46] "CI_tb_15_soil_cal.0" "CI_tb_15_soil_cal.1" "CI_tb_15_soil_cal.2"
## [49] "CI_tb_16_soil_cal.0" "CI_tb_16_soil_cal.1" "CI_tb_16_soil_cal.2"
## [52] "CI_tb_17_soil_cal.0" "CI_tb_17_soil_cal.1" "CI_tb_17_soil_cal.2"
## [55] "CI_tb_18_soil_cal.0" "CI_tb_18_soil_cal.1" "CI_tb_18_soil_cal.2"
## [58] "CI_tb_19_soil_cal.0" "CI_tb_19_soil_cal.1" "CI_tb_19_soil_cal.2"
## [61] "CI_tb_20_soil_cal.0" "CI_tb_20_soil_cal.1" "CI_tb_20_soil_cal.2"
```

As the above example illustrates, only spectral data from files containing the string "tb" are selected.

3.4 data.table data frames for storing spectral data

Data frames are one of the basic R data structures.

When first reading spectral data from binary OPUS files, simplerspec returns data.tables of final spectra (AB block in OPUS viewer software).

```
# Extract spectrum from file "BF_lo_01_soil_cal.0"
# and get overview of the data structure
str(spc_list[["BF_lo_01_soil_cal.0"]][["spc"]])
```

```
## Classes 'data.table' and 'data.frame': 1 obs. of 1716 variables:
   $ 3997.4: num 0.112
   $ 3995.4: num 0.111
  $ 3993.3: num 0.11
##
   $ 3991.3: num 0.111
##
  $ 3989.2: num 0.111
   $ 3987.2: num 0.112
##
   $ 3985.2: num 0.112
##
   $ 3983.1: num 0.112
##
   $ 3981.1: num 0.111
   $ 3979 : num 0.111
##
   $ 3977 : num 0.111
##
   $ 3975 : num 0.11
##
  $ 3972.9: num 0.109
##
   $ 3970.9: num 0.109
##
   $ 3968.8: num 0.11
##
   $ 3966.8: num 0.111
##
   $ 3964.8: num 0.111
##
  $ 3962.7: num 0.111
##
   $ 3960.7: num 0.111
##
   $ 3958.6: num 0.11
## $ 3956.6: num 0.11
   $ 3954.6: num 0.109
##
##
   $ 3952.5: num 0.108
##
   $ 3950.5: num 0.107
   $ 3948.4: num 0.107
##
   $ 3946.4: num 0.106
##
   $ 3944.4: num 0.106
## $ 3942.3: num 0.108
   $ 3940.3: num 0.108
##
   $ 3938.3: num 0.11
##
   $ 3936.2: num 0.11
##
   $ 3934.2: num 0.109
##
   $ 3932.1: num 0.107
##
   $ 3930.1: num 0.103
##
   $ 3928.1: num 0.102
##
  $ 3926 : num 0.104
##
   $ 3924 : num 0.104
##
   $ 3921.9: num 0.104
##
   $ 3919.9: num 0.106
   $ 3917.9: num 0.108
##
   $ 3915.8: num 0.109
   $ 3913.8: num 0.11
## $ 3911.7: num 0.113
   $ 3909.7: num 0.112
##
   $ 3907.7: num 0.107
##
   $ 3905.6: num 0.102
##
   $ 3903.6: num 0.0946
##
   $ 3901.5: num 0.0903
##
   $ 3899.5: num 0.093
##
   $ 3897.5: num 0.0965
## $ 3895.4: num 0.1
## $ 3893.4: num 0.107
## $ 3891.3: num 0.108
```

```
$ 3889.3: num 0.104
##
    $ 3887.3: num 0.105
##
    $ 3885.2: num 0.105
##
    $ 3883.2: num 0.101
##
      3881.1: num 0.103
##
    $ 3879.1: num 0.104
    $ 3877.1: num 0.103
##
##
    $
     3875
            : num 0.103
##
    $ 3873
            : num 0.0997
##
    $ 3870.9: num 0.0971
    $ 3868.9: num 0.0937
##
    $ 3866.9: num 0.0923
##
    $ 3864.8: num 0.0978
    $ 3862.8: num 0.102
##
##
    $ 3860.8: num 0.101
##
    $ 3858.7: num 0.1
##
    $ 3856.7: num 0.103
##
    $ 3854.6: num 0.107
##
    $ 3852.6: num 0.0999
##
    $ 3850.6: num 0.0927
##
    $ 3848.5: num 0.0989
##
    $ 3846.5: num 0.109
##
    $ 3844.4: num 0.11
    $ 3842.4: num 0.101
##
##
    $ 3840.4: num 0.0939
    $ 3838.3: num 0.093
##
    $ 3836.3: num 0.0941
##
    $ 3834.2: num 0.0988
##
    $ 3832.2: num 0.106
##
    $ 3830.2: num 0.11
##
    $ 3828.1: num 0.11
##
    $ 3826.1: num 0.108
##
    $ 3824
            : num 0.105
##
    $ 3822
            : num 0.103
##
    $
      3820
            : num 0.0964
##
    $ 3817.9: num 0.0978
##
    $ 3815.9: num 0.11
##
    $ 3813.8: num 0.116
##
    $ 3811.8: num 0.118
##
    $ 3809.8: num 0.122
    $ 3807.7: num 0.122
##
    $ 3805.7: num 0.111
    $ 3803.6: num 0.105
##
##
    $ 3801.6: num 0.107
    $ 3799.6: num 0.105
##
##
    $ 3797.5: num 0.11
##
     [list output truncated]
    - attr(*, ".internal.selfref")=<externalptr>
You can test if the above output has the class data.frame with
is.data.frame(spc_list[["BF_lo_01_soil_cal.0"]][["spc"]])
```

[1] TRUE

As the output TRUE indicates, the selected spectrum from the list is a data frame.

You can get the number of rows and columns of a data.table by

```
# Assign data.table to object
spc_dt <- spc_list[["BF_lo_01_soil_cal.0"]][["spc"]]
nrow(spc_dt)
## [1] 1
ncol(spc_dt)</pre>
```

[1] 1716

The spectral data.table within the file "BF_lo_01_soil_cal.0" has 1 rows and 1716 columns. The columns correspond to wavenumber variables.

Data frames have a dimnames attribute that names columns and rows:

```
# Show row name and only first and last 10 column names
rownames(spc_dt)
## [1] "1"
idx_firstandlast10 <- c(1:10, seq(from = ncol(spc_dt) - 10, ncol(spc_dt), 1))
colnames(spc_dt)[idx_firstandlast10]
    [1] "3997.4" "3995.4" "3993.3" "3991.3" "3989.2" "3987.2"
                                                                "3985.2"
  [8] "3983.1" "3981.1" "3979"
                                    "520.1"
                                             "518"
                                                       "516"
                                                                "514"
## [15] "511.9" "509.9" "507.8" "505.8"
                                             "503.8"
                                                       "501.7"
                                                                "499.7"
You can also get dimension names in list form
# Show row and column names as list
str(dimnames(spc dt))
## List of 2
```

```
## $ : NULL
## $ : chr [1:1716] "3997.4" "3995.4" "3993.3" "3991.3" ...
```

Subsetting data frames: Data frame subsetting operations allow you to extract parts of values stored within a data frame that you are interested in. The basic syntax is that you can use [and supply a 1D index for both rows and columns, separated by a comma. Blank subsetting without an index value keeps all rows or columns:

```
# Show columns 2, 3 and 6

spc_dt[, c(2, 3, 6)]

## 3995.4 3993.3 3987.2

## 1: 0.1110472 0.1104522 0.1115582
```

The first index before the comma is the row index and the second the column index. Omitting the row index shows all rows. In the case of data.table spc_dt there is only one row. For exemplifying the subsetting behavior of matrices we can duplicate the data.table spc_dt and copy the same content into a second row using rbind(), which is a generic function to combine objects by rows (equivalent for columns is cbind()):

```
spc_dt2 <- rbind(spc_dt, spc_dt)
# Check dimensions
dim(spc_dt2)</pre>
```

```
## [1] 2 1716
```

Now we can e.g. replace the first value in the second row by first selecting the value in the second row of the first column by 1 and then assigning the number 1 to it. This will modify the value at the selection position

in the previous data frame in place.

```
spc_dt2[2, 1] # extract 2nd row and first column

## 3997.4

## 1: 0.1116138

# Subset and modify by assignment

spc_dt2[2, 1] <- 1

# Check if value at selected position has been replaced

spc_dt2[2, 1]

## 3997.4

## 1: 1</pre>
```

The above code shows that the selected value has been correctly replaced. It is also possible to only show the first row of spc_dt2, by leaving the column index empty:

```
head(spc_dt[1, ]) # Show only first 10 values (default of head())
```

```
3997.4
                    3995.4
                              3993.3
                                         3991.3
                                                   3989.2
                                                              3987.2
                                                                        3985.2
## 1: 0.1116138 0.1110472 0.1104522 0.1107337 0.1113628 0.1115582 0.1116115
         3983.1
                    3981.1
                                3979
                                           3977
                                                    3975
                                                             3972.9
                                                                       3970.9
## 1: 0.1116768 0.1113948 0.1110339 0.1107579 0.109912 0.1089011 0.1090422
##
         3968.8
                    3966.8
                              3964.8
                                         3962.7
                                                   3960.7
                                                              3958.6
                                                                        3956.6
## 1: 0.1099667 0.1105003 0.1109353 0.1112978 0.1105624 0.1098195 0.1098699
         3954.6
                    3952.5
                              3950.5
                                         3948.4
                                                   3946.4
                                                              3944.4
                                                                        3942.3
   1: 0.1092134 0.1078505 0.1072382 0.1066292 0.1056538 0.1063747 0.1077091
##
##
         3940.3
                    3938.3
                              3936.2
                                         3934.2
                                                   3932.1
                                                              3930.1
                                                                        3928.1
##
  1: 0.1084273 0.1096656 0.1101731 0.1092632 0.1068086 0.1033797 0.1024289
##
                      3924
           3926
                              3921.9
                                         3919.9
                                                   3917.9
                                                              3915.8
                                                                     3913.8
## 1: 0.1039596 0.1039926 0.1035535 0.1058372 0.1082846 0.1088962 0.11031
##
         3911.7
                    3909.7
                              3907.7
                                         3905.6
                                                    3903.6
                                                                3901.5
                                                                          3899.5
   1: 0.1126094 0.1115171 0.1073066 0.1019541 0.09455585 0.09026368 0.0930251
##
          3897.5
                     3895.4
                               3893.4
                                          3891.3
                                                    3889.3
                                                               3887.3
                                                                        3885.2
##
   1: 0.09647838 0.1002236 0.1065465 0.1080022 0.1044163 0.1052921 0.104677
##
         3883.2
                  3881.1
                             3879.1
                                        3877.1
                                                    3875
                                                                3873
                                                                        3870.9
## 1: 0.1006632 0.102958 0.1044673 0.1030064 0.1025012 0.09970551 0.0971354
                                                    3860.8
##
          3868.9
                      3866.9
                               3864.8
                                          3862.8
                                                                3858.7
                                                                          3856.7
## 1: 0.09369191 0.09233829 0.097812 0.1017904 0.1012478 0.09999011 0.1029824
##
         3854.6
                     3852.6
                                3850.6
                                          3848.5
                                                    3846.5
                                                               3844.4
                                                                        3842.4
  1: 0.1070663 0.09993207 0.09267305 0.098864 0.1089062 0.1100293 0.101408
##
          3840.4
                      3838.3
                                 3836.3
                                             3834.2
                                                       3832.2
                                                                  3830.2
##
   1: 0.09394594 0.09304497 0.09413817 0.09882298 0.1061592 0.1099934
##
                                          3822
                                                     3820
                                                               3817.9
         3828.1
                   3826.1
                               3824
                                                                         3815.9
## 1: 0.1104877 0.107561 0.1046565 0.1031307 0.09639382 0.09775814 0.1102891
##
         3813.8
                    3811.8
                             3809.8
                                        3807.7
                                                  3805.7
                                                             3803.6
                                                                       3801.6
## 1: 0.1161217 0.1178017 0.122399 0.1221272 0.1113749 0.1050898 0.1065325
##
         3799.6
                    3797.5
                              3795.5
                                         3793.4
                                                   3791.4
                                                             3789.4
##
   1: 0.1051933 0.1098949 0.1206683 0.1290725 0.1349746 0.137058 0.1360136
##
        3785.3
                  3783.3
                             3781.2
                                        3779.2
                                                  3777.1
                                                             3775.1
                                                                       3773.1
## 1: 0.134024 0.1321631 0.1341237 0.1378448 0.1387957 0.1398433 0.1425246
##
           3771
                      3769
                              3766.9
                                         3764.9
                                                   3762.9
                                                              3760.8
                                                                       3758.8
## 1: 0.1438005 0.1416286 0.1409272 0.1428057 0.1447936 0.1481354 0.148438
                   3754.7
                             3752.7
                                        3750.6
                                                  3748.6
                                                             3746.5
##
         3756.7
                                                                       3744.5
## 1: 0.1438407 0.142666 0.1452873 0.1412795 0.1345256 0.1467782 0.1670109
##
         3742.5
                    3740.4
                              3738.4
                                         3736.3
                                                   3734.3
                                                              3732.3
                                                                        3730.2
```

```
## 1: 0.1698551 0.1683959 0.1752269 0.1832757 0.1916004 0.2045362 0.2196238
                  3726.1
                          3724.1
                                     3722.1
                                                 3720
                                                           3718
        3728.2
## 1: 0.2355921 0.2515314 0.2675849 0.2890549 0.3161238 0.343578 0.3706079
                           3709.8
                 3711.9
                                     3707.8
                                               3705.8
                                                         3703.7
       3713.9
## 1: 0.404244 0.4496876 0.5026801 0.5598037 0.6234682 0.6987669 0.7819785
                 3697.6
                           3695.6
                                     3693.5
                                               3691.5
                                                         3689.4
       3699.6
## 1: 0.855344 0.9035529 0.9179483 0.8980334 0.8533946 0.7960867 0.7427536
        3685.4
                 3683.3
                           3681.3
                                     3679.2
                                               3677.2
                                                         3675.2
## 1: 0.7079352 0.687908 0.6708944 0.6567918 0.6553099 0.6605251 0.6698021
        3671.1
                   3669
                             3667
                                     3665
                                            3662.9
                                                      3660.9
                                                                 3658.8
## 1: 0.6929669 0.711397 0.7123793 0.71206 0.7149729 0.7191647 0.7290136
        3656.8
                 3654.8
                           3652.7
                                      3650.7
                                                3648.6
                                                          3646.6
## 1: 0.7397532 0.7387432 0.7297438 0.7138904 0.6853508 0.6612893 0.6531969
                            3638.4
        3642.5
                  3640.5
                                      3636.4
                                                3634.4
                                                          3632.3
## 1: 0.6528124 0.6513506 0.6481165 0.6458585 0.6446651 0.6500137 0.6743921
        3628.2
                  3626.2
                           3624.2
                                      3622.1
                                                3620.1
                                                         3618.1
## 1: 0.7154637 0.7650172 0.8259271 0.8828155 0.8908083 0.8285634 0.7421793
         3614
                 3611.9
                           3609.9
                                     3607.9
                                              3605.8
                                                        3603.8
## 1: 0.673768 0.6267841 0.5968329 0.5779265 0.565888 0.5626228 0.5643913
        3599.7
                 3597.7
                           3595.6
                                      3593.6
                                                3591.5
                                                         3589.5
## 1: 0.5631593 0.5582041 0.5510668 0.5404087 0.5300417 0.5245773 0.5191186
                  3583.4
                            3581.3
                                      3579.3
        3585.4
                                                3577.3
                                                         3575.2
## 1: 0.5123681 0.5112181 0.5143472 0.5151356 0.5134943 0.511289 0.507393
        3571.1
                  3569.1
                            3567.1
                                      3565
                                                  3563
                                                          3560.9
## 1: 0.5021104 0.4969654 0.4907912 0.4861864 0.4897577 0.4987744 0.505169
       3556.9
                 3554.8
                           3552.8
                                    3550.7
                                               3548.7
                                                         3546.7
## 1: 0.506789 0.5063753 0.5048466 0.5019996 0.5005469 0.5010287 0.5011958
        3542.6
                  3540.6
                           3538.5
                                      3536.5
                                               3534.4
                                                         3532.4
                                                                   3530.4
## 1: 0.5025658 0.5061851 0.5095251 0.5102621 0.5089468 0.5078958 0.5070646
        3528.3
                 3526.3
                           3524.2
                                     3522.2
                                               3520.2 3518.1
## 1: 0.5051079 0.503341 0.5036097 0.5052959 0.5080728 0.51164 0.514064
          3514
                    3512
                              3510
                                      3507.9
                                                3505.9
                                                          3503.8
                                                                    3501.8
## 1: 0.5145297 0.5139735 0.5129235 0.5114836 0.5116599 0.5134345 0.5139225
                  3497.7
                            3495.7
                                      3493.6
                                               3491.6
        3499.8
                                                         3489.6
## 1: 0.5145717 0.5174403 0.5200608 0.5208555 0.5211441 0.5215181 0.5212984
                  3483.4
                            3481.4
                                    3479.4
                                              3477.3
        3485.5
                                                         3475.3
                                                                   3473.2
## 1: 0.5208611 0.5211357 0.5209543 0.520404 0.5219475 0.5248185 0.5266916
       3471.2
                 3469.2
                         3467.1
                                    3465.1
                                              3463.1
                                                          3461
##
## 1: 0.528021 0.5295117 0.529994 0.5294459 0.5294614 0.5295542 0.5291033
                                      3450.8 3448.8
                                                        3446.7
        3456.9
                  3454.9
                            3452.9
## 1: 0.5293549 0.5306885 0.5320562 0.5322884 0.531772 0.530844 0.5305933
                 3440.6
                           3438.6
                                     3436.5
                                              3434.5
                                                         3432.5
                                                                   3430.4
       3442.7
## 1: 0.532656 0.5355729 0.5383387 0.5407725 0.5418113 0.5417949 0.5415865
        3428.4
                  3426.3
                           3424.3
                                      3422.3
                                               3420.2
                                                         3418.2
## 1: 0.5410931 0.5400733 0.5390592 0.5386636 0.5384083 0.538309 0.5391221
                 3412.1
                             3410
                                       3408
                                               3405.9
       3414.1
                                                         3403.9
## 1: 0.540336 0.5409092 0.5404803 0.5400574 0.5406018 0.5413219 0.541763
                            3395.7
        3399.8
                  3397.8
                                      3393.7
                                               3391.7
                                                         3389.6
## 1: 0.5432697 0.5428165 0.5424205 0.5431384 0.543209 0.5422207 0.5421394
        3385.6
                3383.5
                           3381.5
                                     3379.4
                                               3377.4
                                                         3375.4
                                                                   3373.3
## 1: 0.5425027 0.542112 0.5419476 0.5423765 0.5426027 0.5426469 0.5432032
        3371.3
                  3369.2
                           3367.2
                                      3365.2
                                                3363.1
                                                         3361.1
## 1: 0.5443523 0.5452251 0.5448565 0.5431483 0.5419671 0.5421976 0.5419435
##
          3357
                    3355
                            3352.9
                                      3350.9
                                                3348.8
                                                        3346.8
```

```
## 1: 0.5409678 0.5408535 0.5415211 0.5418525 0.5416046 0.5411514 0.5408642
                  3340.7
                                                3334.6
                            3338.6
                                      3336.6
         3342.7
                                                           3332.5
## 1: 0.5410772 0.541231 0.5407252 0.5399434 0.5388844 0.5375247 0.5367965
         3328.4
                   3326.4
                             3324.4
                                       3322.3
                                                 3320.3
                                                            3318.2
## 1: 0.5370393 0.5374069 0.5375454 0.5378051 0.5380245 0.5378212 0.5372844
                   3312.1
                             3310.1
                                         3308
                                                   3306
         3314.2
                                                              3304
                                                                     3301.9
## 1: 0.5367095 0.5364211 0.5366427 0.5367549 0.5363613 0.5358801 0.535311
         3299.9
                   3297.9
                             3295.8
                                       3293.8
                                                 3291.7
                                                            3289.7
                                                                      3287.7
## 1: 0.5347087 0.5342708 0.5338174 0.5332146 0.5324051 0.5316291 0.5315127
                                                 3277.5
         3285.6
                   3283.6
                           3281.5
                                      3279.5
                                                          3275.4
                                                                    3273.4
## 1: 0.5318202 0.5315689 0.530727 0.5300602 0.5298554 0.529889 0.5297794
                 3269.3
                            3267.3
                                      3265.2
         3271.3
                                                3263.2
                                                           3261.1
                                                                     3259.1
## 1: 0.5292903 0.528484 0.5276083 0.5270485 0.5267999 0.5263633 0.5257509
         3257.1
                     3255
                               3253
                                       3250.9
                                                3248.9
                                                           3246.9
## 1: 0.5253119 0.5249451 0.5242097 0.5229785 0.521868 0.5214114 0.5207522
         3242.8
                   3240.7
                            3238.7
                                      3236.7
                                                 3234.6
                                                           3232.6
## 1: 0.5193753 0.5183725 0.518406 0.5189752 0.5192338 0.5185085 0.5168555
         3228.5
                   3226.5
                             3224.4
                                       3222.4
                                                 3220.4
                                                            3218.3
## 1: 0.5151792 0.5143575 0.5142948 0.5141286 0.5132591 0.5117249 0.510248
         3214.2
                   3212.2
                             3210.2
                                       3208.1
                                                 3206.1
                                                              3204
                                                                        3202
## 1: 0.5092981 0.5084108 0.5074376 0.5066918 0.5061628 0.5052173 0.5036492
           3200
                   3197.9
                             3195.9
                                      3193.8
                                                 3191.8
                                                           3189.8
## 1: 0.5021023 0.5007395 0.4998238 0.499485 0.4987416 0.4974239 0.4962434
         3185.7
                   3183.6
                             3181.6
                                       3179.6
                                                  3177.5
                                                            3175.5
                                                                     3173.4
## 1: 0.4952952 0.4942829 0.4929222 0.4914428 0.4897038 0.4875807 0.485836
         3171.4
                   3169.4
                             3167.3
                                       3165.3
                                                3163.2
                                                          3161.2
                                                                    3159.2
## 1: 0.4846831 0.4837314 0.4826354 0.4812084 0.479837 0.478722 0.4774536
         3157.1
                   3155.1
                               3153
                                        3151
                                                   3149
                                                           3146.9
                                                                     3144.9
## 1: 0.4762946 0.4755839 0.4744931 0.472665 0.4706939 0.4689855 0.4677578
         3142.9
                   3140.8
                             3138.8
                                       3136.7
                                                 3134.7
                                                           3132.7
## 1: 0.4668166 0.4657238 0.4642204 0.4622339 0.4601486 0.4582447 0.4567231
         3128.6
                   3126.5
                             3124.5
                                       3122.5
                                                3120.4
                                                           3118.4
                                                                     3116.3
## 1: 0.4554727 0.4539556 0.4526301 0.4517795 0.450786 0.4495825 0.4482124
                   3112.3
                             3110.2
         3114.3
                                       3108.2
                                                 3106.1
                                                           3104.1
## 1: 0.4466802 0.4455313 0.4448372 0.4437627 0.4417416 0.4393316 0.437277
                                       3093.9
           3100
                     3098
                             3095.9
                                                 3091.9
                                                            3089.8
                                                                      3087.8
## 1: 0.4355066 0.4340266 0.4327925 0.4315788 0.4306334 0.4297255 0.4283357
         3085.7
                   3083.7
                             3081.7
                                       3079.6
                                                 3077.6
                                                            3075.5
##
## 1: 0.4268396 0.4256024 0.4242012 0.4222257 0.4199938 0.4181655 0.4166711
                   3069.4
                             3067.4
                                                  3063.3
         3071.5
                                       3065.4
                                                            3061.3
                                                                     3059.2
## 1: 0.4152657 0.4141215 0.4128367 0.4110576 0.4092566 0.4076953 0.406259
         3057.2
                   3055.2 3053.1
                                     3051.1
                                                 3049
                                                            3047
                                                                      3045
## 1: 0.4047865 0.4031602 0.40165 0.4000423 0.3979223 0.3958364 0.3942071
         3042.9
                   3040.9
                            3038.8
                                      3036.8
                                                 3034.8
                                                           3032.7
                                                                     3030.7
## 1: 0.3927376 0.3911098 0.389294 0.3873783 0.3854076 0.3833377 0.3813303
                  3026.6
                                     3022.5
                                              3020.5
         3028.6
                            3024.6
                                                         3018.4
                                                                   3016.4
## 1: 0.3798245 0.378882 0.3778149 0.376241 0.374638 0.3733432 0.3721929
         3014.4
                   3012.3
                             3010.3
                                       3008.2
                                                  3006.2
                                                           3004.2
## 1: 0.3708816 0.3694541 0.3680324 0.3665663 0.3651873 0.363994 0.3629195
         3000.1
                     2998
                               2996
                                         2994
                                                 2991.9
                                                           2989.9
                                                                     2987.9
## 1: 0.3620983 0.3615842 0.3608212 0.3597927 0.3590308 0.358226 0.3573054
         2985.8
                   2983.8
                             2981.7
                                       2979.7
                                                 2977.7
                                                           2975.6
## 1: 0.3568687 0.3570132 0.3571981 0.3569482 0.3563045 0.3555854 0.3548411
##
         2971.5
                   2969.5
                             2967.5
                                       2965.4
                                                 2963.4
                                                           2961.3
                                                                     2959.3
```

```
## 1: 0.3540446 0.3533451 0.3527457 0.3523849 0.3525358 0.3527181 0.352321
                                       2951.1
                   2955.2
                             2953.2
                                                 2949.1
##
         2957.3
                                                           2947.1
## 1: 0.3516042 0.3510642 0.3508189 0.3505593 0.3503009 0.3504573 0.3507631
           2943
                   2940.9
                             2938.9
                                       2936.9
                                                 2934.8
                                                           2932.8
                                                                     2930 7
## 1: 0.3507062 0.3505201 0.3506619 0.3508518 0.3507602 0.3507479 0.3508274
                  2926.7
                             2924.6
                                       2922.6
                                                 2920.5
         2928.7
                                                           2918.5
                                                                     2916.5
## 1: 0.3504285 0.3495554 0.3485362 0.3473839 0.3461746 0.3445974 0.3423133
         2914.4
                  2912.4
                             2910.3
                                       2908.3
                                                 2906.3
                                                           2904.2
## 1: 0.3395411 0.3362026 0.3323449 0.3288594 0.3264198 0.3245966 0.3227441
        2900.2
                  2898.1
                           2896.1
                                        2894
                                                  2892
                                                            2890
## 1: 0.320984 0.3196257 0.3183629 0.3167847 0.3150124 0.3132942 0.3117562
                  2883.8
                             2881.8
                                      2879.8
                                                          2875.7
         2885.9
                                                 2877.7
## 1: 0.3105685 0.3097504 0.3090168 0.3079851 0.3065872 0.3051333 0.3038726
        2871.6
                  2869.6
                             2867.5
                                      2865.5
                                                 2863.4
                                                          2861.4
## 1: 0.3026466 0.3012969 0.3002169 0.2995717 0.2990038 0.2985632 0.2984579
         2857.3
                   2855.3
                           2853.2
                                      2851.2
                                                2849.2
                                                         2847.1
## 1: 0.2985099 0.2985424 0.298408 0.2976204 0.2955565 0.292193 0.2883257
           2843
                     2841
                              2839
                                      2836.9
                                               2834.9
                                                         2832.8
## 1: 0.2847506 0.2818656 0.279624 0.2775547 0.275508 0.2737524 0.2724171
         2828.8
                  2826.7
                             2824.7
                                       2822.7
                                                 2820.6
                                                           2818.6
## 1: 0.2711698 0.2695814 0.2678879 0.2665878 0.2655897 0.2645297 0.2634342
                  2812.5
         2814.5
                             2810.4
                                       2808.4
                                                 2806.3
                                                           2804.3
## 1: 0.2623775 0.2612831 0.2602028 0.2591853 0.2582712 0.2573304 0.2562202
         2800.2
                  2798.2
                             2796.1
                                       2794.1
                                                 2792.1
                                                             2790
## 1: 0.2552605 0.2546754 0.2541961 0.2535369 0.2527328 0.2518808 0.2510207
         2785.9 2783.9
                          2781.9
                                    2779.8
                                              2777.8
                                                         2775.7
## 1: 0.2503209 0.24973 0.2490896 0.2483945 0.2475453 0.2465792 0.2456174
        2771.7
                  2769.6
                           2767.6
                                     2765.5
                                               2763.5
                                                          2761.5
## 1: 0.244683 0.2438409 0.2429538 0.2419268 0.2410522 0.2404164 0.2399455
        2757.4
                  2755.3
                           2753.3
                                      2751.3
                                               2749.2
                                                          2747.2
## 1: 0.239663 0.2391533 0.2381958 0.2373295 0.2368063 0.2362972 0.2356566
         2743.1
                  2741.1
                               2739
                                         2737
                                                   2735
                                                          2732.9
## 1: 0.2350737 0.2345497 0.2338663 0.2331409 0.2325692 0.231903 0.2311729
                  2726.8
                            2724.8
                                      2722.7
                                                 2720.7
                                                          2718.6
         2728.8
                                                                     2716.6
## 1: 0.2307145 0.2304081 0.2300178 0.2294743 0.2289951 0.2288389 0.2287743
                 2712.5
                           2710.5
                                      2708.4
                                               2706.4
        2714.6
                                                          2704.4
                                                                    2702.3
## 1: 0.2285083 0.228184 0.2280095 0.2278003 0.2274894 0.2272945 0.2270769
         2700.3 2698.2
                           2696.2
                                    2694.2
                                              2692.1
                                                        2690 1
##
## 1: 0.2265878 0.22594 0.2253874 0.225072 0.2247745 0.2242955 0.2238819
                    2684
                           2681.9
                                      2679.9
                                               2677.8
           2686
                                                         2675.8
                                                                   2673.8
## 1: 0.2236616 0.223544 0.2233306 0.2227497 0.221904 0.2212504 0.2210051
         2671.7
                  2669.7
                             2667.7
                                       2665.6
                                                 2663.6
                                                          2661.5
## 1: 0.2207698 0.2201602 0.2193687 0.2185495 0.2175338 0.2164703 0.2155813
                  2655.4
                             2653.4
                                       2651.3
                                               2649.3
         2657.5
                                                          2647.3
                                                                    2645.2
## 1: 0.2147695 0.2141363 0.2137252 0.2131507 0.212358 0.2117684 0.2112713
                                       2637.1
                                                   2635
         2643.2
                  2641.1
                             2639.1
                                                             2633
                                                                     2630.9
## 1: 0.2105103 0.2096616 0.2089354 0.2084005 0.2079351 0.2073775 0.2069598
         2628.9
                  2626.9
                             2624.8
                                       2622.8 2620.7
                                                          2618.7
## 1: 0.2067885 0.2065707 0.2061754 0.2057166 0.205264 0.2048489 0.2044144
        2614.6
                  2612.6
                           2610.5
                                      2608.5
                                                2606.5
                                                          2604.4
## 1: 0.203919 0.2034856 0.2032949 0.2032846 0.2031309 0.2027634 0.2023235
        2600.3
                  2598.3
                            2596.3
                                       2594.2
                                                 2592.2
                                                          2590.1
## 1: 0.2020511 0.2019674 0.2017749 0.2015207 0.2011737 0.2006037 0.2000985
##
        2586.1
                  2584
                             2582
                                        2580
                                                2577.9 2575.9
                                                                   2573.8
```

```
## 1: 0.1996744 0.199149 0.1986157 0.1979529 0.1971816 0.196717 0.1963912
                                       2565.7
                   2569.8
                             2567.7
                                                 2563.6
         2571.8
                                                           2561.6
                                                                     2559.6
## 1: 0.1958149 0.1951383 0.1944825 0.1938472 0.1933301 0.1929015 0.1924474
         2557.5
                   2555.5
                             2553.4
                                       2551.4
                                                 2549.4
                                                           2547.3
## 1: 0.1920758 0.1918961 0.1916155 0.1911568 0.1908246 0.1907399 0.1908108
                   2541.2
                           2539.2
                                    2537.1
                                                           2533
         2543.2
                                               2535.1
## 1: 0.1907593 0.1906016 0.190625 0.190644 0.1903998 0.1902221 0.1903922
           2529
                   2526.9
                             2524.9
                                       2522.8
                                                 2520.8
                                                          2518.8
                                                                    2516.7
## 1: 0.1906241 0.1907047 0.1907314 0.1909027 0.1912429 0.191473 0.1915401
         2514.7
                  2512.6
                           2510.6
                                      2508.6
                                                2506.5
                                                         2504.5
                                                                    2502.5
## 1: 0.1915556 0.191518 0.1914998 0.1914636 0.1913608 0.191323 0.1912995
         2500.4
                  2498.4
                             2496.3
                                                           2490.2
                                       2494.3
                                                 2492.3
## 1: 0.1912087 0.1911368 0.1909571 0.1905987 0.1903221 0.1901574 0.1899598
                   2484.1
                           2482.1
                                                         2475.9
         2486.1
                                       2480
                                                 2478
                                                                    2473.9
## 1: 0.1898361 0.1898071 0.189735 0.189539 0.1891058 0.1885616 0.1881597
         2471.9
                   2469.8
                             2467.8
                                       2465.7
                                                 2463.7
                                                           2461.7
                                                                     2459.6
## 1: 0.1878602 0.1876146 0.1874123 0.1871042 0.1867703 0.1867193 0.1868503
         2457.6
                  2455.5
                            2453.5
                                      2451.5
                                               2449.4
                                                         2447.4
## 1: 0.1868531 0.186872 0.1870877 0.1873379 0.187577 0.1878938 0.1882769
         2443.3
                  2441.3
                             2439.2
                                       2437.2
                                                 2435.1
                                                           2433.1
## 1: 0.1887338 0.1892045 0.1896035 0.1900466 0.1905884 0.1911163 0.1915722
           2429
                     2427
                                       2422.9
                                                 2420.9
                               2425
                                                          2418.8
## 1: 0.1919656 0.1924128 0.1929838 0.1935772 0.1941245 0.194733 0.1954936
         2414.8
                   2412.7
                             2410.7
                                       2408.6
                                                 2406.6
                                                           2404.6
## 1: 0.1961208 0.1964405 0.1968059 0.1974269 0.1980293 0.1983627 0.1985923
         2400.5
                  2398.4
                             2396.4
                                       2394.4
                                                 2392.3
                                                           2390.3
## 1: 0.1989102 0.1993953 0.2001064 0.2008504 0.2016567 0.2026635 0.203835
         2386.2
                   2384.2
                             2382.1
                                       2380.1
                                                   2378
                                                             2376
                                                                       2374
## 1: 0.2052747 0.2072179 0.2095475 0.2118544 0.2138398 0.2155401 0.2173137
         2371.9
                   2369.9
                             2367.8
                                       2365.8
                                                 2363.8
                                                           2361.7
## 1: 0.2193464 0.2212174 0.2228134 0.2245507 0.2262253 0.2270229 0.2261788
         2357.6
                  2355.6
                            2353.6
                                     2351.5
                                               2349.5
                                                         2347.5
                                                                    2345.4
## 1: 0.2231189 0.218977 0.2172361 0.220046 0.2243243 0.2256732 0.2245269
                  2341.3
                            2339.3
                                     2337.3
                                               2335.2
         2343.4
                                                         2333.2
                                                                    2331.1
## 1: 0.2245706 0.226635 0.2282614 0.228422 0.2278818 0.2270822 0.2260817
                   2327.1
                               2325
                                         2323
                                                 2320.9
                                                          2318.9
                                                                    2316.9
         2329.1
## 1: 0.2251698 0.2242131 0.2226208 0.2203192 0.2181364 0.216905 0.2164398
##
       2314.8
                  2312.8
                            2310.7
                                      2308.7
                                                2306.7
                                                          2304 6
## 1: 0.215977 0.2152278 0.2145288 0.2141319 0.2140807 0.2144012 0.2150439
                   2298.5
                             2296.5
                                       2294.4
                                                 2292.4
                                                           2290.3
         2300.5
                                                                     2288.3
## 1: 0.2159045 0.2169865 0.2184417 0.2203356 0.2224006 0.2244177 0.2266573
         2286.3
                   2284.2
                             2282.2
                                       2280.1
                                                 2278.1
                                                           2276.1
                                                                       2274
## 1: 0.2293695 0.2323925 0.2354934 0.2385634 0.2415636 0.2445503 0.2476283
                     2270
                             2267.9
                                       2265.9
                                                 2263.8
                                                           2261.8
                                                                    2259.8
           2272
## 1: 0.2508035 0.2539351 0.2568142 0.2594292 0.2619443 0.2643344 0.266483
         2257.7
                  2255.7
                            2253.6
                                      2251.6
                                               2249.6
                                                         2247.5
##
                                                                    2245.5
## 1: 0.2684737 0.270452 0.2725147 0.2746207 0.276796 0.2790623 0.2818789
        2243.4
                  2241.4
                            2239.4
                                      2237.3
                                                2235.3
                                                          2233.2
## 1: 0.285076 0.2878294 0.2894648 0.2898161 0.2890913 0.2877187 0.2861056
        2229.2
                  2227.1
                            2225.1
                                        2223
                                                  2221
                                                            2219
                                                                    2216.9
## 1: 0.284319 0.2822145 0.2797021 0.2763741 0.2719711 0.2668023 0.2612127
         2214.9
                  2212.8
                             2210.8
                                       2208.8
                                                 2206.7
                                                           2204.7
## 1: 0.2554203 0.2498267 0.2449351 0.2407101 0.2367809 0.2330648 0.2296744
##
         2200.6 2198.6
                           2196.5
                                      2194.5
                                                2192.4 2190.4
                                                                   2188.4
```

```
## 1: 0.2266406 0.224052 0.2219028 0.2201797 0.2191449 0.218623 0.2182251
                2184.3
                           2182.3
                                     2180.2
                                               2178.2
        2186.3
                                                         2176.1
                                                                   2174.1
## 1: 0.218071 0.218227 0.2185614 0.2190577 0.2195305 0.2199427 0.2207188
         2172.1
                    2170
                               2168
                                       2165.9
                                                 2163.9
                                                           2161.9
## 1: 0.2219036 0.2231934 0.2246622 0.2263748 0.2282893 0.2305868 0.2332546
                                                 2149.6
         2157.8
                  2155.7
                             2153.7
                                       2151.7
                                                          2147.6
                                                                    2145.5
## 1: 0.2361391 0.2393571 0.2428689 0.2464771 0.2502639 0.254244 0.2583639
         2143.5
                  2141.5
                             2139.4
                                       2137.4
                                                 2135.3
                                                           2133.3
                                                                     2131.3
## 1: 0.2626402 0.2669046 0.2706926 0.2733262 0.2742656 0.2732744 0.2705629
         2129.2
                  2127.2
                             2125.1
                                       2123.1
                                                2121.1
                                                           2119
                                                                     2117
## 1: 0.2666961 0.2624812 0.2587278 0.2557887 0.253774 0.252658 0.2522013
                                                           2104.8
         2114.9
                  2112.9
                             2110.9
                                       2108.8
                                                 2106.8
                                                                     2102.7
## 1: 0.2521722 0.2523921 0.2527611 0.2534698 0.2545506 0.2557837 0.2572536
                                     2094.6
       2100.7
                  2098.6
                           2096.6
                                                2092.5
                                                         2090.5
                                                                   2088.4
## 1: 0.259068 0.2610668 0.2631638 0.2649927 0.2668558 0.268945 0.2711989
         2086.4
                  2084.4
                             2082.3
                                       2080.3
                                                 2078.2
                                                           2076.2
                                                                     2074.2
## 1: 0.2737866 0.2767222 0.2798313 0.2830872 0.2863315 0.2894454 0.2928044
        2072.1
                  2070.1
                              2068
                                        2066
                                                 2064
                                                          2061.9
## 1: 0.296687 0.3006549 0.3047351 0.3094227 0.3146083 0.3205504 0.3275099
         2057.8
                  2055.8
                             2053.8
                                      2051.7
                                                 2049.7
                                                           2047.6
## 1: 0.3350146 0.3432627 0.3527284 0.3635199 0.3759581 0.3903468 0.406487
                             2039.5
                                                 2035.4
         2043.6
                  2041.5
                                       2037.4
                                                           2033.4
## 1: 0.4245726 0.4445577 0.4652808 0.4857983 0.5050242 0.5216759 0.5353383
         2029.3
                  2027.3
                             2025.2
                                       2023.2
                                                 2021.1
                                                           2019.1
                                                                     2017.1
## 1: 0.5460196 0.5542056 0.5608922 0.5668865 0.5730138 0.5810183 0.5919769
           2015
                    2013
                             2010.9
                                       2008.9
                                                 2006.9
                                                           2004.8
## 1: 0.6057075 0.6215136 0.6371487 0.6509101 0.6628121 0.6722536 0.6789364
         2000.7
                  1998.7
                            1996.7
                                       1994.6
                                                 1992.6
                                                           1990.5
                                                                     1988.5
## 1: 0.6837332 0.6870543 0.6886986 0.6896302 0.6898804 0.6885819 0.6880152
         1986.5
                  1984.4
                            1982.4
                                      1980.3
                                                1978.3
                                                           1976.3
## 1: 0.6889279 0.6897303 0.6902634 0.6903749 0.6900518 0.6894872 0.6881517
         1972.2
                  1970.1
                             1968.1
                                     1966.1
                                                  1964
                                                            1962
                                                                    1959.9
## 1: 0.6847953 0.6798356 0.6743259 0.667933 0.6619502 0.6577308 0.6540996
                  1955.9
                            1953.8
                                       1951.8
         1957.9
                                                 1949.8
                                                           1947.7
## 1: 0.6511117 0.6497398 0.6499001 0.6506879 0.6508807 0.6495761 0.6474292
                  1941.6
                            1939.6
                                       1937.5
                                                 1935.5 1933.4
         1943.6
                                                                   1931.4
## 1: 0.6455458 0.6429656 0.6416749 0.6432763 0.6444253 0.64354 0.6421303
         1929.4
                  1927.3
                             1925.3
                                       1923.2
                                                 1921.2
                                                           1919.2
##
                                                                     1917.1
## 1: 0.6408225 0.6390602 0.6378056 0.6378496 0.6404552 0.6495574 0.6627601
                     1913
                                         1909
                                                 1906.9
         1915.1
                               1911
                                                           1904.9
                                                                    1902.8
## 1: 0.6771255 0.6948482 0.7148547 0.7355357 0.7565718 0.7774422 0.796982
         1900.8
                  1898.8
                            1896.7
                                      1894.7
                                                 1892.6
                                                           1890.6
                                                                     1888.6
## 1: 0.8138902 0.8281921 0.8416411 0.8539357 0.8647389 0.8757226 0.8849502
                  1884.5
                            1882.4 1880.4
                                              1878.4
                                                                   1874.3
         1886.5
                                                         1876.3
## 1: 0.8923687 0.9008589 0.9089894 0.91483 0.9182107 0.9200395 0.9204667
                  1870.2
                            1868.2
         1872.3
                                       1866.1
                                                 1864.1
                                                           1862.1
                                                                       1860
## 1: 0.9197532 0.9181081 0.9130774 0.9067181 0.9029787 0.8968185 0.8830624
           1858
                  1855.9
                            1853.9
                                       1851.9
                                                 1849.8
                                                           1847.8
## 1: 0.8630878 0.8397918 0.8144802 0.7877668 0.7604284 0.7347587 0.7135391
         1843.7
                  1841.7
                            1839.6
                                      1837.6
                                                 1835.5
                                                           1833.5
                                                                    1831.5
## 1: 0.6938103 0.6764979 0.6681138 0.6652289 0.6613817 0.6581873 0.6583902
       1829.4
                  1827.4
                           1825.3
                                     1823.3
                                              1821.3
                                                        1819.2
## 1: 0.659372 0.6632024 0.6737301 0.6854708 0.696447 0.7088509 0.7194676
##
        1815.1 1813.1 1811.1
                                     1809
                                                 1807
                                                        1804.9
                                                                   1802.9
```

```
## 1: 0.7265387 0.733813 0.743332 0.7531476 0.7626001 0.7717848 0.7800118
                  1798.8
                            1796.8
                                    1794.7
                                              1792.7
        1800.9
                                                        1790.7
## 1: 0.7852439 0.7859122 0.7856979 0.789613 0.7944728 0.7944072 0.7950629
                  1784.6
                            1782.5
                                      1780.5
                                               1778.4
                                                         1776.4
        1786.6
## 1: 0.7996248 0.7996845 0.7933956 0.7847486 0.7737378 0.7614144 0.7487826
                  1770.3
                           1768.2
                                      1766.2
                                               1764.2
        1772.3
                                                       1762.1
## 1: 0.7308344 0.7099648 0.6950607 0.6838962 0.6742592 0.663413 0.6503311
          1758
                    1756
                              1754
                                      1751.9
                                               1749.9
                                                        1747.8
                                                                  1745.8
## 1: 0.6424942 0.6376837 0.6329696 0.6301775 0.6257612 0.622558 0.6273794
        1743.8
                  1741.7
                           1739.7
                                     1737.6
                                               1735.6
                                                         1733.6
                                                                   1731.5
## 1: 0.6379182 0.6497558 0.6574647 0.6619542 0.6728814 0.6835651 0.6884136
                1727.4
                          1725.4
                                    1723.4
                                              1721.3
        1729.5
                                                        1719.3
                                                                  1717.2
## 1: 0.7007347 0.718362 0.7327242 0.7400877 0.7430097 0.7485709 0.7548907
                           1711.1
                                                          1705
        1715.2
                 1713.2
                                     1709.1
                                               1707.1
## 1: 0.7632685 0.7793766 0.7983832 0.8142949 0.8253139 0.8301442 0.8372598
        1700.9
                  1698.9
                            1696.9
                                     1694.8
                                               1692.8
                                                         1690.7
## 1: 0.8511749 0.8630756 0.8832048 0.9099836 0.9296537 0.9451532 0.9548337
        1686.7
                  1684.6
                           1682.6
                                     1680.5
                                               1678.5
                                                         1676.5
## 1: 0.9632362 0.9720988 0.9703767 0.9695725 0.9780273 0.9838293 0.9748406
        1672.4 1670.3
                         1668.3
                                   1666.3
                                             1664.2
                                                       1662.2
## 1: 0.9609842 0.95664 0.9537789 0.9522406 0.9591398 0.9644592 0.9607282
                  1656.1
                              1654
                                      1652
                                              1649.9
                                                        1647.9
## 1: 0.9558428 0.9592143 0.9627786 0.944855 0.9308831 0.9454197 0.9661474
                                    1637.7 1635.7
                                                     1633.6
        1643.8
                  1641.8
                            1639.7
## 1: 0.9770033 0.9858872 0.9945096 1.005947 1.02103 1.032875 1.047728
       1629.6
               1627.5 1625.5
                               1623.4
                                        1621.4
                                                 1619.4
                                                          1617.3
                                                                   1615.3
## 1: 1.068045 1.085088 1.10068 1.118557 1.132558 1.148376 1.167747 1.177166
                                1607.1
       1613.2
               1611.2
                        1609.2
                                         1605.1
                                                     1603
                                                              1601
## 1: 1.181439 1.189113 1.193428 1.191191 1.186874 1.182235 1.175511 1.166149
      1596.9
              1594.9
                       1592.8 1590.8
                                        1588.8
                                                 1586.7
                                                          1584.7
                                                                    1582.6
## 1: 1.15459 1.141558 1.129143 1.118826 1.109511 1.099738 1.088334 1.073457
       1580.6
               1578.6 1576.5 1574.5
                                         1572.4
                                                    1570.4
                                                             1568.4
## 1: 1.056157 1.041774 1.027006 1.007625 0.997574 0.9953833 0.984488
                  1564.3
                            1562.2
                                      1560.2
                                               1558.2
        1566.3
                                                         1556.1
                                                                   1554.1
## 1: 0.9688963 0.9555764 0.9475166 0.9444385 0.9303682 0.9177717 0.9252619
                    1550
                              1548
                                      1545.9
                                               1543.9
        1552.1
                                                         1541.9
                                                                   1539.8
## 1: 0.9398876 0.9490331 0.9508841 0.9487134 0.9452324 0.9488472 0.9660062
##
        1537.8
                 1535.7
                         1533.7
                                  1531.7
                                           1529.6
                                                    1527.6
                                                            1525 5
## 1: 0.9849195 1.009903 1.039598 1.058371 1.068892 1.074303 1.068979
                        1519.4
                                 1517.4
                                         1515.3
                                                  1513.3
       1523.5
               1521.5
                                                           1511.3
## 1: 1.061176 1.054583 1.047749 1.048933 1.054541 1.055031 1.049165 1.045009
               1505.1
                       1503.1 1501.1
                                           1499
                                                    1497 1494.9
       1507.2
## 1: 1.048459 1.050195 1.054166 1.06538 1.078351 1.087872 1.09124 1.092707
       1490.9 1488.8 1486.8 1484.7
                                         1482.7
                                                   1480.7
                                                           1478.6
## 1: 1.094714 1.093907 1.095388 1.102632 1.109686 1.110165 1.103938 1.096193
                                                  1464.4
       1474.5
               1472.5
                        1470.5
                                1468.4
                                         1466.4
                                                           1462.3
## 1: 1.092941 1.094769 1.096534 1.101865 1.111025 1.112091 1.104619 1.101636
      1458.2
              1456.2
                       1454.2
                               1452.1
                                         1450.1
                                                    1448
                                                            1446
## 1: 1.10404 1.102548 1.104718 1.116437 1.130162 1.139601 1.14616 1.153346
       1441.9
               1439.9
                        1437.8
                                1435.8
                                         1433.8
                                                  1431.7
                                                           1429.7
## 1: 1.159197 1.163249 1.169926 1.176684 1.185152 1.200418 1.213874 1.219774
       1425.6
              1423.6
                       1421.5
                                1419.5
                                         1417.4
                                                  1415.4 1413.4
## 1: 1.224605 1.230257 1.238636 1.250732 1.258729 1.264017 1.271988 1.280354
##
       1409.3 1407.2 1405.2
                                1403.2
                                         1401.1 1399.1
                                                             1397
                                                                       1395
```

```
## 1: 1.287074 1.294225 1.301958 1.307837 1.314378 1.321572 1.327622 1.334741
       1393 1390.9 1388.9 1386.9
                                     1384.8 1382.8 1380.7 1378.7
## 1: 1.3419 1.35018 1.360281 1.36574 1.367126 1.37245 1.381116 1.386504
                1374.6
                        1372.6
                                 1370.5
                                          1368.5
                                                  1366.5
                                                           1364.4
       1376.7
## 1: 1.389725 1.395255 1.401417 1.407382 1.413147 1.416379 1.418046 1.417489
                1358.3 1356.3
                                1354.2
                                         1352.2
                                                  1350.1
       1360.3
                                                           1348.1
## 1: 1.414929 1.414946 1.416894 1.417007 1.415711 1.415545 1.416645 1.416662
                 1342 1339.9
                              1337.9
                                       1335.9
         1344
                                                1333.8
                                                         1331.8 1329.7
## 1: 1.412989 1.40474 1.39212 1.379583 1.374229 1.371929 1.363388 1.34961
       1327.7 1325.7
                       1323.6 1321.6 1319.5 1317.5
                                                          1315.5
                                                                   1313.4
## 1: 1.336855 1.32644 1.316342 1.303723 1.286369 1.266922 1.249876 1.233412
       1311.4 1309.4 1307.3 1305.3
                                         1303.2
                                                  1301.2 1299.2
## 1: 1.213433 1.189988 1.164596 1.139891 1.117976 1.097631 1.077008 1.055666
      1295.1
                1293
                                    1289
                          1291
                                            1286.9
                                                    1284.9
                                                               1282.8
## 1: 1.03449 1.014309 0.9949605 0.9765551 0.9601166 0.946182 0.9328504
        1280.8
                  1278.8
                            1276.7
                                    1274.7
                                              1272.6
                                                        1270.6
## 1: 0.9176705 0.9000382 0.8798357 0.856875 0.8318049 0.8055416 0.7789696
        1266.5
                  1264.5
                           1262.4
                                     1260.4
                                               1258.4
                                                         1256.3
## 1: 0.7522391 0.7248882 0.6974965 0.6708843 0.6453679 0.6212834 0.5991463
        1252.2
                 1250.2
                          1248.2
                                    1246.1
                                              1244.1
                                                         1242
## 1: 0.5795731 0.5623887 0.546556 0.5313795 0.5164368 0.5014066 0.4862332
          1238
                  1235.9
                           1233.9
                                     1231.9
                                               1229.8
                                                         1227.8
## 1: 0.4711551 0.4561473 0.4409237 0.4258466 0.4117343 0.3993773 0.3896341
        1223.7
                  1221.7
                            1219.6
                                     1217.6
                                               1215.5
                                                         1213.5
## 1: 0.3832918 0.3803936 0.3800659 0.3814077 0.3840582 0.3878914 0.3925252
        1209.4
                 1207.4
                           1205.3
                                     1203.3
                                               1201.3
                                                         1199.2
## 1: 0.3973109 0.4016806 0.4055205 0.4088893 0.4117463 0.4138082 0.4152618
      1195.1
                1193.1
                         1191.1
                                     1189
                                               1187
                                                       1184.9
                                                                 1182.9
## 1: 0.41641 0.4174617 0.4182681 0.4186524 0.4185354 0.4183592 0.4186199
        1180.9
                  1178.8
                           1176.8
                                     1174.7
                                               1172.7
                                                         1170.7 1168.6
## 1: 0.4193295 0.4207148 0.4230926 0.4265077 0.4314648 0.4390258 0.45081
        1166.6
                  1164.5
                            1162.5
                                      1160.5
                                               1158.4
                                                         1156.4
## 1: 0.4698372 0.4996755 0.5386854 0.5721505 0.5782802 0.5539836 0.5193987
                  1150.3
                           1148.2
                                    1146.2
                                               1144.2
        1152.3
                                                         1142.1
## 1: 0.4920336 0.4752426 0.4653306 0.4591783 0.4556306 0.4537032 0.4527488
                  1136
                           1134
                                   1131.9
                                             1129.9
                                                       1127.8
        1138
                                                                 1125.8
## 1: 0.45264 0.4530876 0.4541757 0.4564499 0.4604871 0.4667877 0.4760741
        1123.8
                  1121.7
                           1119.7
                                     1117.6
                                               1115.6
                                                         1113.6
##
                                                                   1111.5
## 1: 0.4893965 0.5067351 0.5268102 0.5472615 0.5639021 0.5730795 0.5737542
                           1105.4
                                   1103.4
        1109.5
                  1107.4
                                              1101.3
                                                      1099.3
                                                                1097.2
## 1: 0.5677071 0.5594865 0.5523421 0.545719 0.5388507 0.531889 0.524775
               1093.2
                         1091.1
                                   1089.1
                                               1087
                                                                  1083
       1095.2
                                                        1085
## 1: 0.518263 0.512896 0.5080931 0.5035716 0.4997366 0.496511 0.4937072
        1080.9
                  1078.9
                           1076.8
                                     1074.8
                                               1072.8
                                                         1070.7
## 1: 0.4921822 0.4927377 0.4956594 0.5018623 0.5128586 0.5295364 0.5517834
                  1064.6
                            1062.6
                                    1060.5
                                             1058.5
        1066.7
                                                       1056.5
                                                                1054.4
## 1: 0.5791399 0.6106418 0.6435356 0.674998 0.704585 0.7314813 0.7549881
        1052.4
                  1050.3
                            1048.3
                                     1046.3
                                               1044.2
                                                         1042.2
## 1: 0.7768853 0.7975787 0.8165885 0.8352177 0.8528181 0.8682247 0.8836612
        1038.1
                1036.1
                            1034
                                      1032
                                              1029.9
                                                        1027.9
                                                                  1025.9
## 1: 0.8995727 0.913731 0.9270241 0.9419158 0.9573241 0.9695439 0.9764957
        1023.8
                  1021.8
                           1019.7
                                     1017.7
                                               1015.7
                                                        1013.6
## 1: 0.9781508 0.9768183 0.9773781 0.9815739 0.9870954 0.9928296 0.9993315
##
       1009.5 1007.5 1005.5 1003.4 1001.4
                                               999.3
                                                          997.3
```

```
## 1: 1.006669 1.0128 1.015397 1.014144 1.00975 1.003282 0.9946108 0.9839067
                991.2
                        989.2 987.1 985.1 983
        993.2
## 1: 0.9735417 0.9645339 0.956132 0.9487029 0.9416921 0.9332432 0.9251598
                                   972.8
          979
                 976.9
                          974.9
                                            970.8
                                                      968.8
## 1: 0.9203745 0.9169893 0.9125625 0.9085623 0.9066138 0.9061237 0.9058103
                 962.6
                         960.6
                                   958.6
        964.7
                                            956.5
                                                      954.5
## 1: 0.9050562 0.9047009 0.9066653 0.9108105 0.9148113 0.9188726 0.9253743
                                 944.3
        950.4
                 948.4
                         946.3
                                            942.2
                                                     940.2
                                                              938.2
## 1: 0.9348465 0.9461966 0.958491 0.9712009 0.9823509 0.9887967 0.9911999
                                     930
        936.1
                 934.1
                        932
                                              928
                                                    925.9
## 1: 0.9923388 0.9926874 0.9926212 0.9945093 1.000194 1.008093 1.017442
              919.8 917.8 915.7 913.7 911.7 909.6 907.6
       921.8
## 1: 1.029262 1.041144 1.049601 1.054311 1.055449 1.049562 1.033203 1.009329
                         901.5 899.4
        905.5
                903.5
                                           897.4
                                                    895.3
## 1: 0.9850855 0.9638402 0.9455262 0.931088 0.9195706 0.9093636 0.9007655
        891.3
                 889.2
                         887.2
                                   885.1
                                            883.1
                                                     881.1
## 1: 0.8929474 0.8861811 0.8826476 0.8827348 0.8847384 0.8853771 0.8839515
          877
                 874.9
                           872.9
                                   870.9
                                            868.8
                                                     866.8
## 1: 0.8832534 0.8838876 0.8843753 0.884126 0.8840216 0.8848061 0.8858573
        862.7
                860.7
                        858.6
                                   856.6
                                           854.5
                                                   852.5
## 1: 0.8865796 0.8877847 0.8903769 0.8942684 0.8999804 0.9076024 0.9166541
                          844.3
                                   842.3
                 846.4
                                            840.3
                                                     838.2
## 1: 0.9267167 0.9368833 0.9476102 0.9606766 0.9775124 0.996714 1.016719
        834.2 832.1 830.1
                             828
                                      826
                                                824
                                                      821.9 819.9
## 1: 1.039647 1.06624 1.0959 1.130151 1.169797 1.216309 1.270681 1.32758
       817.8
               815.8
                      813.8 811.7 809.7 807.6
                                                         805.6 803.6
## 1: 1.382659 1.430273 1.445481 1.395426 1.286608 1.165328 1.067809 1.006209
                         797.4 795.4
        801.5
                 799.5
                                         793.4 791.3 789.3
## 1: 0.9770509 0.9705174 0.9812149 1.004687 1.027478 1.032775 1.013031
        787.2
                 785.2
                          783.2
                                   781.1
                                            779.1
                                                     777
## 1: 0.9769564 0.9404109 0.9135262 0.9012579 0.9041522 0.9197652 0.9432277
          773
                 770.9
                           768.9
                                   766.8
                                            764.8
                                                      762.8
## 1: 0.9653238 0.9799578 0.9878464 0.9923843 0.9947126 0.9927589 0.9871795
                756.7
                        754.6 752.6 750.5
                                                     748.5
        758.7
                                                              746.5
## 1: 0.9811397 0.9751622 0.9684627 0.9625272 0.9576369 0.9523183 0.9458433
                742.4
                        740.3 738.3 736.3
                                                     734.2
        744.4
## 1: 0.9388286 0.9330544 0.9298475 0.9290744 0.9274654 0.9229878 0.9185377
                 728.1
                         726.1
                                  724
                                             722
                                                     719.9
##
        730.1
## 1: 0.9174708 0.9203739 0.926225 0.9331405 0.9393432 0.9478413 0.9626306
                                709.7
                713.8
                        711.8
                                         707.7
                                                 705.7
        715.9
## 1: 0.9832187 1.006982 1.035382 1.071967 1.114598 1.159656 1.210158
               699.5
                      697.5 695.5
                                       693.4
                                               691.4
                                                       689.3
       701.6
## 1: 1.263396 1.296431 1.285549 1.240254 1.192466 1.157585 1.131266 1.108463
              683.2 681.2
       685.3
                            679.1 677.1
                                              675.1
                                                       673
## 1: 1.08635 1.063957 1.04276 1.024641 1.011362 1.002306 0.9939887 0.9817234
                666.9
                                 662.8
                                            660.8
                                                    658.8
       669
                         664.9
## 1: 0.9667233 0.961104 0.9668172 0.9707398 0.9687711 0.9661812 0.9673088
                 652.6
                          650.6
                                   648.6
                                            646.5
                                                     644.5
## 1: 0.971487 0.9748294 0.9759796 0.9778861 0.9823143 0.9851651 0.9842871
        640.4
                638.4
                        636.3 634.3 632.2
                                                      630.2
## 1: 0.9837391 0.9840354 0.9833273 0.9835184 0.9854859 0.9879117 0.9901843
       626.1
                624.1
                        622
                                 620 618
                                              615.9
                                                       613.9
## 1: 0.993646 1.001137 1.013614 1.024857 1.03083 1.035325 1.041453 1.047529
##
       609.8
               607.8 605.7
                             603.7
                                      601.6
                                              599.6 597.6
```

```
## 1: 1.058421 1.077376 1.09301 1.103226 1.118228 1.132412 1.136551 1.135012
##
         593.5
                 591.5
                           589.4
                                    587.4
                                              585.3
                                                       583.3
                                                                 581.3
                                                                          579.2
## 1: 1.140959 1.16393 1.187397 1.202764 1.222412 1.233156 1.241099 1.264126
                            573.1
                                                 569
##
         577.2
                  575.1
                                     571.1
                                                          567
                                                                  564.9
## 1: 1.286093 1.306753 1.332745 1.345832 1.355993 1.386634 1.425907 1.413305
##
         560.9
                  558.8
                            556.8
                                    554.7
                                              552.7
                                                       550.7
                                                                 548.6 546.6
## 1: 1.338575 1.273166 1.244596 1.22533 1.193218 1.153975 1.118852 1.0916
##
         544.5
                  542.5
                           540.5
                                     538.4
                                              536.4
                                                       534.3
                                                                 532.3
## 1: 1.064162 1.035039 1.02096 1.011657 1.006508 1.032715 1.081272 1.109735
##
         528.2
                  526.2
                            524.1
                                     522.1
                                              520.1
                                                           518
                                                                     516
## 1: 1.105115 1.058516 1.028691 1.040851 1.03179 0.9974678 0.9752454
                              509.9
                                         507.8
                                                   505.8
                                                              503.8
##
           514
                    511.9
## 1: 0.937062 0.8714066 0.8047704 0.7785948 0.7818117 0.7179397 0.6106296
          499.7
##
## 1: 0.5528126
The first column of the first row has still the value 0.1116138.
# Check if dimnames attribute is present
str(attributes(spc_dt))
## List of 4
                        : chr [1:1716] "3997.4" "3995.4" "3993.3" "3991.3" ...
##
    $ names
    $ row.names
                        : int 1
                        : chr [1:2] "data.table" "data.frame"
##
    $ class
```

We can e.g. also select the first column by its name, which is commonly known in R as name subsetting

```
spc_dt[, "3997.4"] # Select first column with wavenumber variable "3997.4"

## 3997.4

## 1: 0.1116138

spc_dt[, "3997.4"] == spc_dt[, 1] # both are equivalent

## 3997.4

## [1,] TRUE
```

3.5 Advantages of lists

\$.internal.selfref:<externalptr>

Applying the same function to all elements of a list: Lists are data structures that allow to store complex, hierarchical objects. Lists are fundamental units when applying functions on each elements using apply family functions. Apply family functions are a specific type of functionals that take functions and other objects as input and return lists or atomic vectors. Note that lists are also vectors. Functionals are an elegant way to solve common data manipulation tasks. A often used functional is lapply(). The functional lapply(X, FUN, ...) applies a function FUN to each of the corresponding elements of X and returns the result as a list of the same length as its input X. The argument ... can be other arguments passed to the function. Let us explore the behavior of lapply() on a simple example. A list shall contain three different the numeric vectors named "a", "b", and "c".

```
x <- list(
   "a" = 1:10,
   "b" = c(0.5, 2.3, 5),
   "c" = seq(0.1, 1, 0.1)
)
x</pre>
```

```
## $a
   [1] 1 2 3 4 5 6 7 8 9 10
##
##
## $b
## [1] 0.5 2.3 5.0
##
## $c
   [1] 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1.0
##
We can simply calculate the mean value for all the elements (vectors) in the list x by using lapply():
lapply(x, mean) # First argument is X, second is FUN;
## $a
## [1] 5.5
##
## $b
## [1] 2.6
##
## $c
## [1] 0.55
# you can also supply arguments explicitly with lapply(X = x, FUN = mean)
```

As you can see, the mean value is computed for the elements 'a, 'b', and 'c' and returned as list.

We can also remove the hierarchy from the list and returning it as named numeric vector using unlist(). unlist() concatenates all elements of all components into a single vector:

```
mean_v <- unlist(lapply(x, mean))
str(mean_v)

## Named num [1:3] 5.5 2.6 0.55

## - attr(*, "names")= chr [1:3] "a" "b" "c"
```

4 Session info

sessionInfo()

```
## R version 3.4.4 (2018-03-15)
## Platform: x86_64-pc-linux-gnu (64-bit)
## Running under: KDE neon User Edition 5.13
## Matrix products: default
## BLAS: /usr/lib/libblas/libblas.so.3.6.0
## LAPACK: /usr/lib/lapack/liblapack.so.3.6.0
##
## locale:
   [1] LC_CTYPE=en_US.UTF-8
                                   LC_NUMERIC=C
##
  [3] LC_TIME=de_CH.UTF-8
                                   LC COLLATE=en US.UTF-8
   [5] LC_MONETARY=de_CH.UTF-8
                                   LC_MESSAGES=en_US.UTF-8
##
##
   [7] LC_PAPER=de_CH.UTF-8
                                   LC NAME=C
   [9] LC_ADDRESS=C
##
                                   LC_TELEPHONE=C
## [11] LC_MEASUREMENT=de_CH.UTF-8 LC_IDENTIFICATION=C
##
```

```
## attached base packages:
## [1] stats
                 graphics grDevices utils
                                               datasets methods
                                                                    base
## other attached packages:
                                             forcats_0.3.0
##
   [1] simplerspec_0.1.0 foreach_1.4.4
   [4] stringr 1.3.1
                          dplyr 0.7.6
                                             purrr 0.2.5
##
   [7] readr 1.1.1
                          tidyr 0.8.1
                                             tibble 1.4.2
                          tidyverse_1.2.1
## [10] ggplot2_3.0.0
##
## loaded via a namespace (and not attached):
   [1] tidyselect_0.2.4
                          reshape2_1.4.3
                                             haven_1.1.1
   [4] lattice_0.20-35
                          colorspace_1.3-2
                                            htmltools_0.3.6
  [7] yaml_2.1.19
                          rlang_0.2.1
                                             pillar_1.2.2
## [10] foreign_0.8-70
                          glue_1.2.0
                                             withr_2.1.2
## [13] modelr_0.1.2
                          readxl_1.1.0
                                             bindrcpp_0.2.2
## [16] bindr_0.1.1
                          plyr_1.8.4
                                             munsell_0.4.3
## [19] gtable_0.2.0
                          cellranger_1.1.0
                                            rvest_0.3.2
## [22] codetools 0.2-15
                          psych_1.8.3.3
                                             evaluate 0.10.1
## [25] knitr_1.20
                          parallel_3.4.4
                                             broom_0.4.4
                          scales_0.5.0
## [28] Rcpp_0.12.17
                                             backports_1.1.2
## [31] jsonlite_1.5
                          mnormt_1.5-5
                                             hms_0.4.2
## [34] digest_0.6.15
                          stringi_1.2.2
                                             grid_3.4.4
                          cli_1.0.0
                                             tools_3.4.4
## [37] rprojroot_1.3-2
## [40] magrittr 1.5
                          lazyeval_0.2.1
                                             crayon 1.3.4
## [43] pkgconfig_2.0.1
                          data.table_1.11.4 xml2_1.2.0
## [46] lubridate_1.7.4
                          assertthat_0.2.0
                                            rmarkdown 1.9
## [49] httr_1.3.1
                          rstudioapi_0.7
                                             iterators_1.0.9
## [52] R6_2.2.2
                          nlme_3.1-137
                                             compiler_3.4.4
```