

Data Quality: Lecture 6

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Task 01

A data set *learning* is given. The dataset *learning* shows the relationship between learning effort in self-study [hours per week] and success on the final exam [index 0 to 10] in a master's program.

Run a “Cluster Based” outlier detection applying k-means clustering after Barai & Dey (2017). Calculate solutions with two different numbers of clusters. $x = 3$ and $x = 4$ in `kmeans(datas, centers = x, nstart = 10)`

How can the solutions be interpreted?

Load & Explore

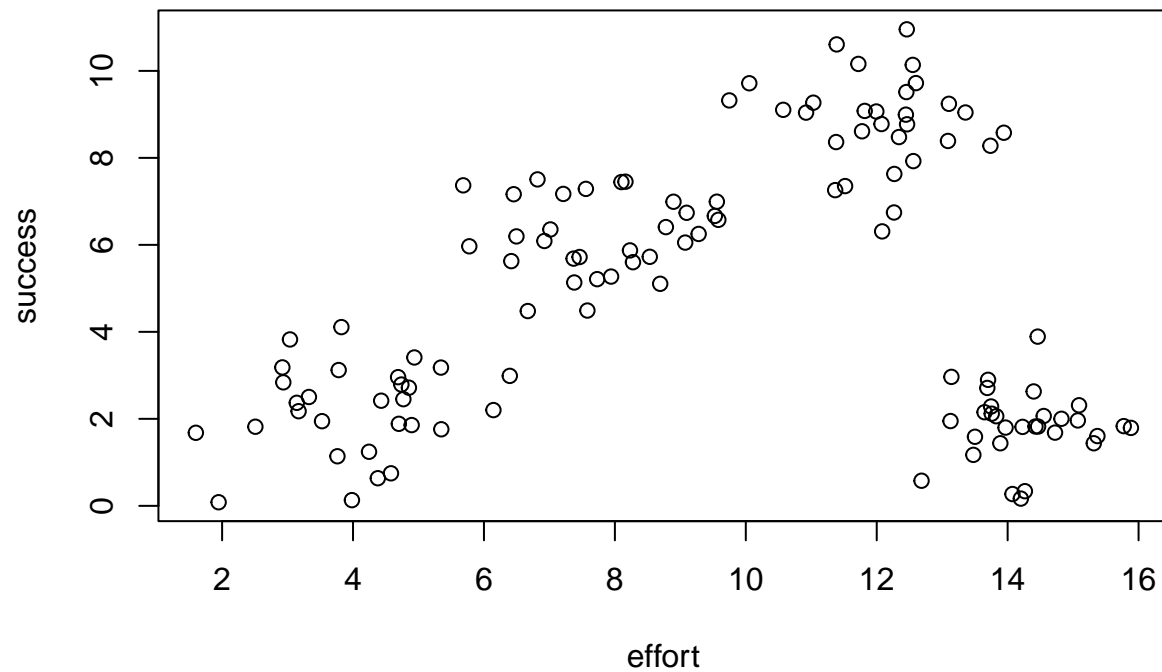
```
library(readxl)
library(MVA)
library(cluster)

data <- read_excel("data/learning.xlsx")
any(is.na(data))
## [1] FALSE

summary(data)

##      effort      success
## Min.   : 1.599   Min.    : 0.08273
## 1st Qu.: 6.332   1st Qu.: 1.99214
## Median : 9.664   Median : 4.48437
## Mean   : 9.571   Mean    : 4.80295
## 3rd Qu.:13.194   3rd Qu.: 7.35565
## Max.   :15.884   Max.    :10.95476

plot(data)
```

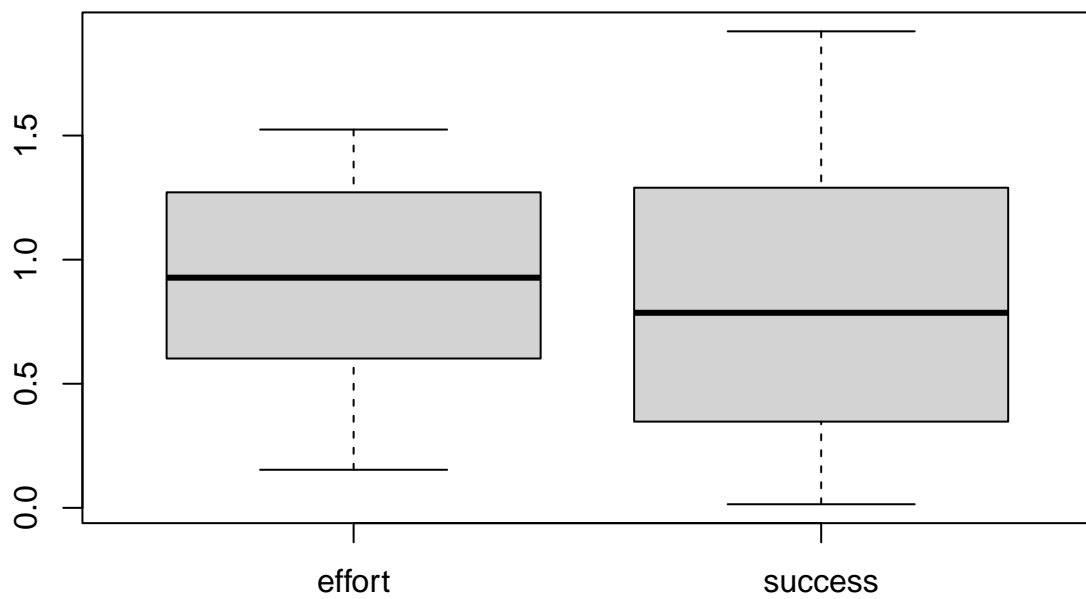


Preparation

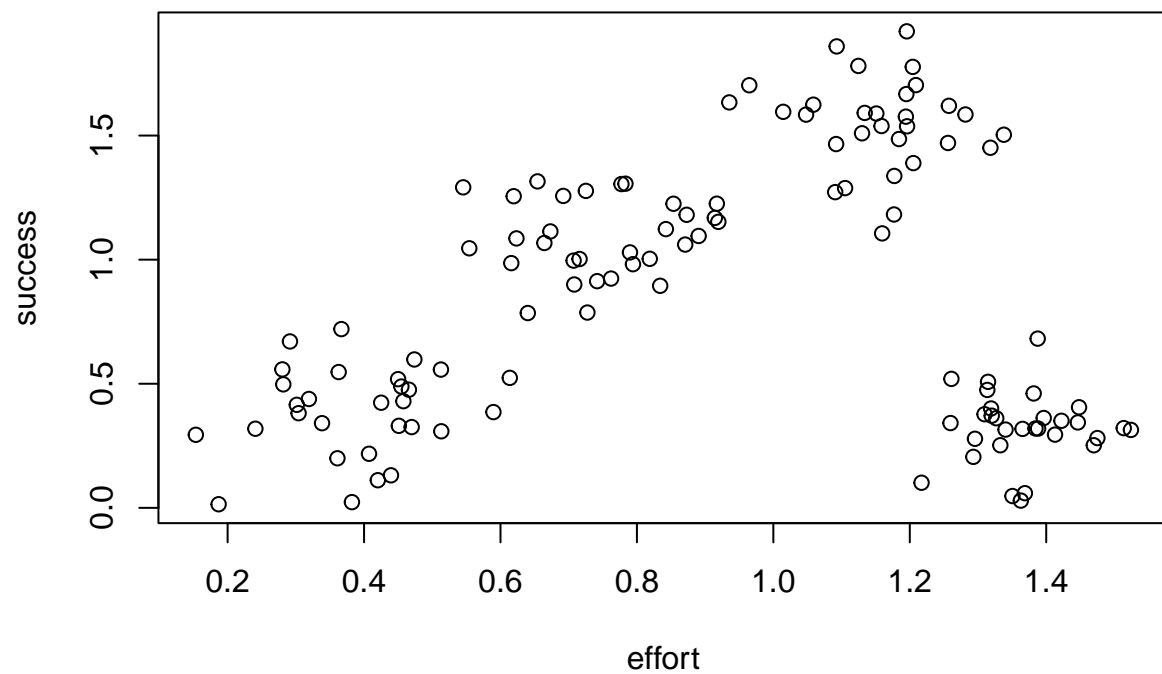
```
data.scaled <- scale(data, center = FALSE, scale = TRUE)
dists <- dist(data.scaled)
summary(data.scaled)

##      effort      success
## Min.   :0.1534  Min.   :0.0145
## 1st Qu.:0.6076  1st Qu.:0.3491
## Median :0.9274  Median :0.7859
## Mean   :0.9184  Mean   :0.8418
## 3rd Qu.:1.2662  3rd Qu.:1.2891
## Max.   :1.5242  Max.   :1.9199

boxplot(data.scaled)
```



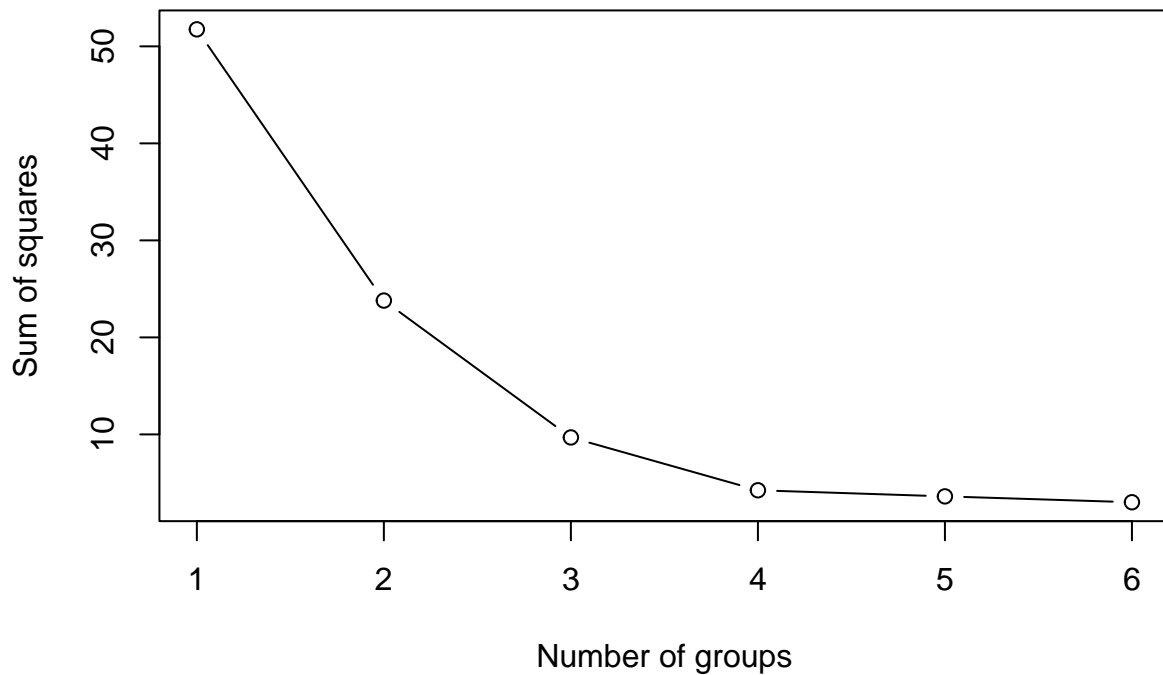
```
plot(data.scaled)
```



Clustering

Scree plot

```
reps <- rep(0, 6)
for (i in 1:6) reps[i] <- sum(kmeans(data.scaled, centers = i, nstart = 20)$withinss)
plot(1:6, reps, type = "b", xlab = "Number of groups", ylab = "Sum of squares")
```



4 Clusters

```
km.4 <- kmeans(data.scaled, centers = 4, nstart = 10)
km.4.groups <- km.4$cluster
km.4.groups

##      [1] 2 2 2 2 2 2 2 2 2 2 2 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 1 1 1 1 1 1 1
##     [38] 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 4 4 4 4 4 4 4 4 4 4 4 4 4 4
##     [75] 4 4 4 4 1 4 4 4 4 4 4 4 4 4 4 4 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
##    [112] 3 3 3 3 3 3 3 3 3
```

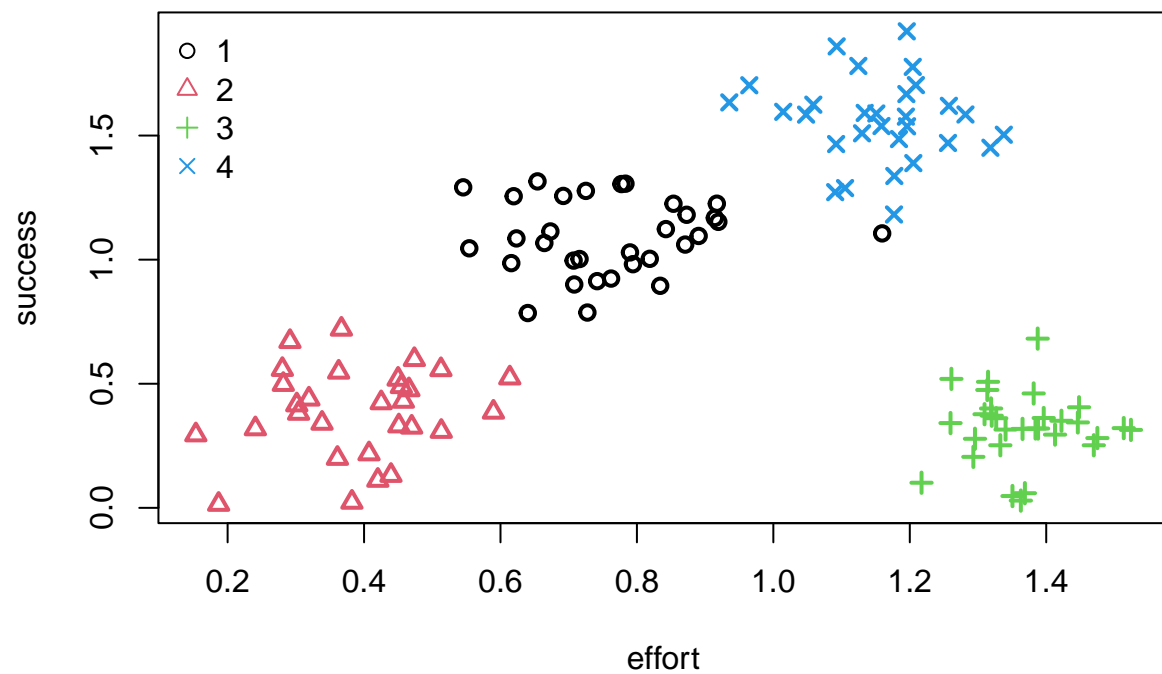
```
cluster.size.4 <- cbind(sum(km.4.groups == 1), sum(km.4.groups == 2),
                        sum(km.4.groups == 3), sum(km.4.groups == 4))

cluster.size.4

##      [,1] [,2] [,3] [,4]
## [1,]   32   29   30   29
```

Plot / Silhouette plot

```
plot(data.scaled, pch = km.4.groups, col=km.4.groups, lwd=2)
legend("topleft", legend = 1:4, pch = 1:4, col=1:4, bty="n")
```



```
plot(silhouette(km.4.groups, dists))
```

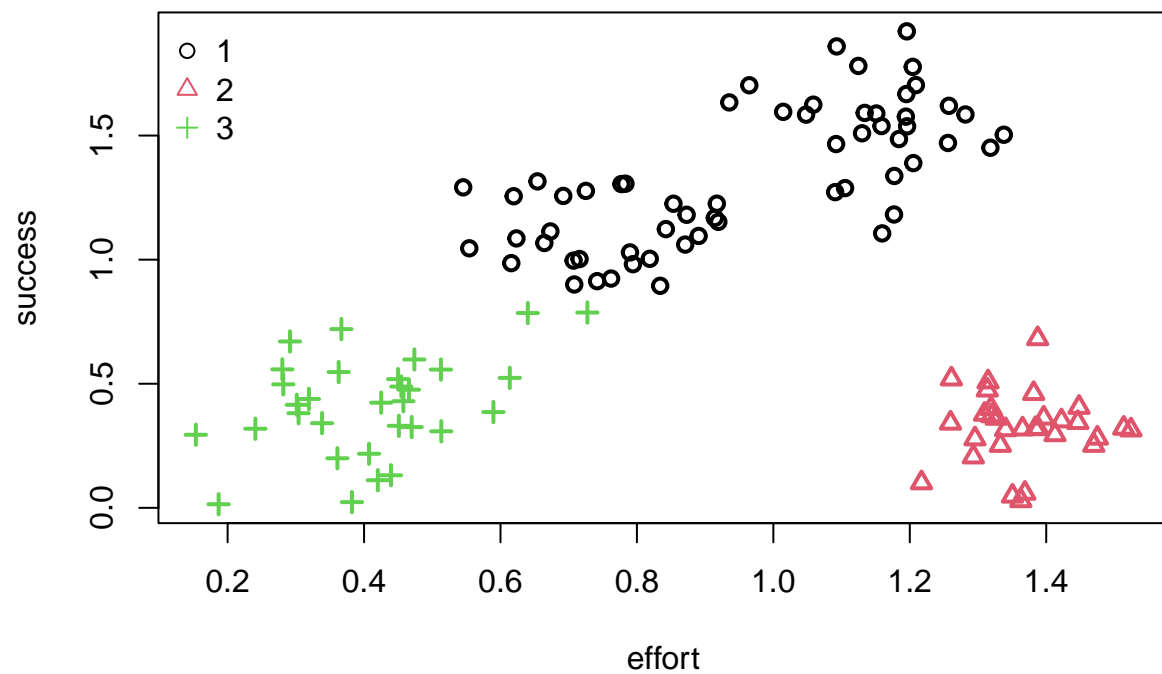
4 clusters C_j
 $j: n_j \mid \text{ave}_{i \in C_j} s_i$
 1: 32 | 0.56
 2: 29 | 0.66
 3: 30 | 0.79
 4: 29 | 0.60

0.0 0.2 0.4 0.6 0.8 1.0
 Silhouette width s_i

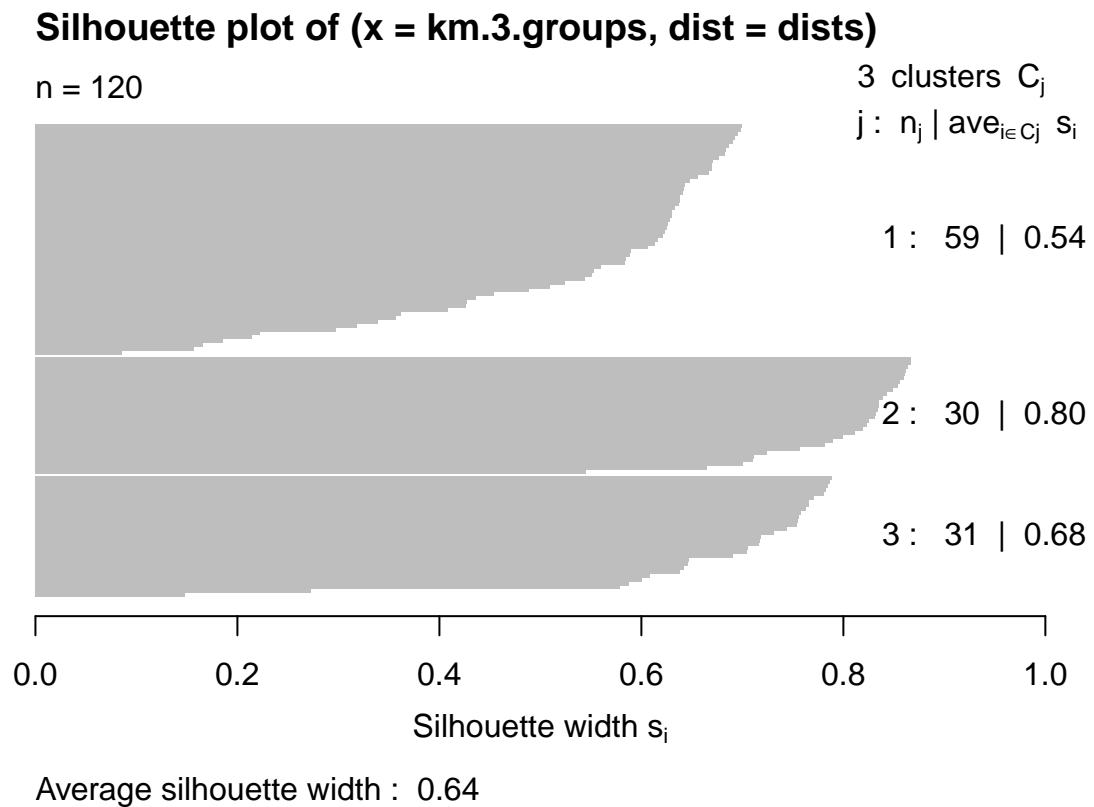
3 Clusters

Plot / Silhouette plot

7



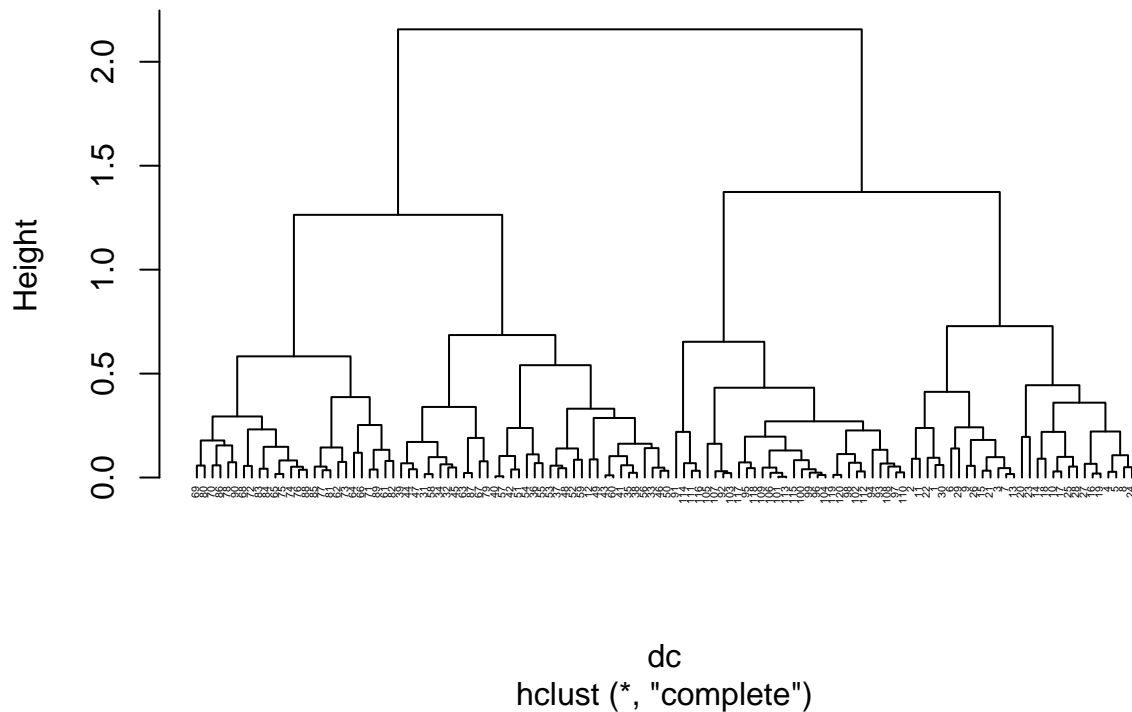
```
plot(silhouette(km.3.groups, dists))
```

Hierarchical cluster analysis

```
dc <- dist(data.scaled, method = "euclidean")
dc
cc <- hclust(dc, method = "complete")
plot(cc, cex = 0.3, hang = -1)
```

Cluster Dendrogram



Interpretation

According to the numbers you could argue for 3 and 4 clusters. However, 4 clusters seems to be more appropriate considering the domain of the data set.

1. Those who learn little and have a bad grade
2. Those who learn an average amount and have an average grade
3. Those who learn a lot and have good performance
4. Those who learn a lot and still have bad performance (maybe not an appropriate learning technique)