Data Quality: Lecture 6

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Task 01

A data set *learning* is given. The dataset *learning* shows the relationship between learning effort in self-study [hours per week] and success on the final exam [index 0 to 10] in a master's program.

Run a "Cluster Based" outlier detection applying k-means clustering after Barai & Dey (2017). Calculate solutions with two different numbers of clusters. x = 3 and x = 4 in kmeans(datas, centers = x, nstart = 10)

How can the solutions be interpreted?

Load & Explore

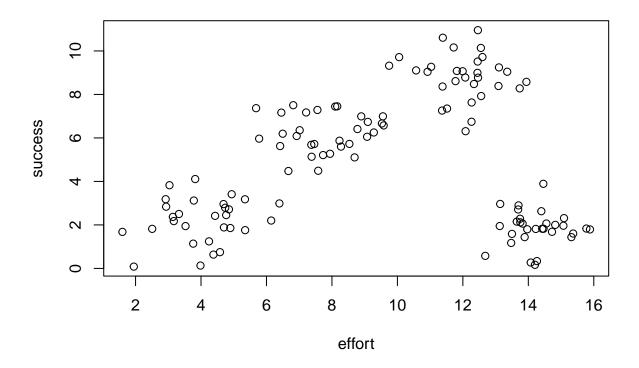
```
library(readxl)
library(MVA)
library(cluster)

data <- read_excel("data/learning.xlsx")
any(is.na(data))</pre>
```

[1] FALSE

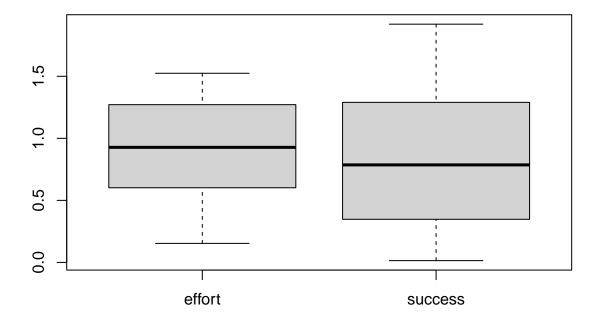
summary(data)

```
effort
                        success
##
   Min.
          : 1.599
                           : 0.08273
   1st Qu.: 6.332
                    1st Qu.: 1.99214
   Median : 9.664
                    Median: 4.48437
   Mean
         : 9.571
                           : 4.80295
##
                     Mean
    3rd Qu.:13.194
                     3rd Qu.: 7.35565
##
   Max.
           :15.884
                            :10.95476
                     Max.
plot(data)
```

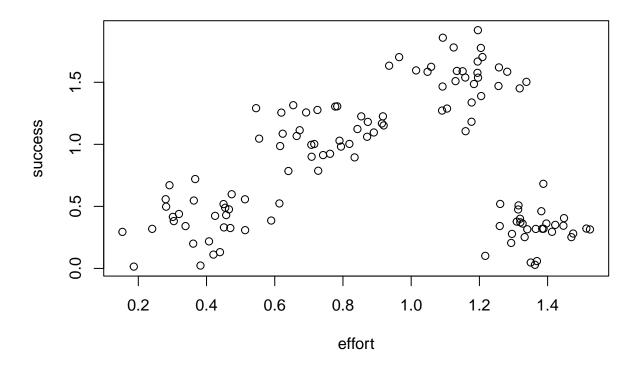


Preparation

```
data.scaled <- scale(data, center = FALSE, scale = TRUE)</pre>
dists <- dist(data.scaled)</pre>
summary(data.scaled)
##
        effort
                          success
           :0.1534
                              :0.0145
##
    Min.
                      Min.
##
    1st Qu.:0.6076
                      1st Qu.:0.3491
    Median :0.9274
                      Median :0.7859
##
            :0.9184
    Mean
                      Mean
                              :0.8418
    3rd Qu.:1.2662
##
                      3rd Qu.:1.2891
            :1.5242
                              :1.9199
    Max.
                      Max.
boxplot(data.scaled)
```

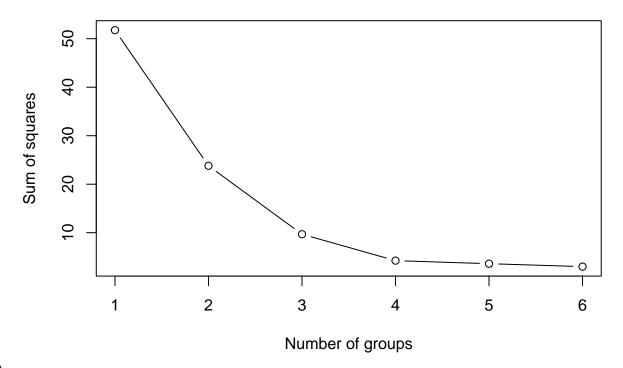


plot(data.scaled)



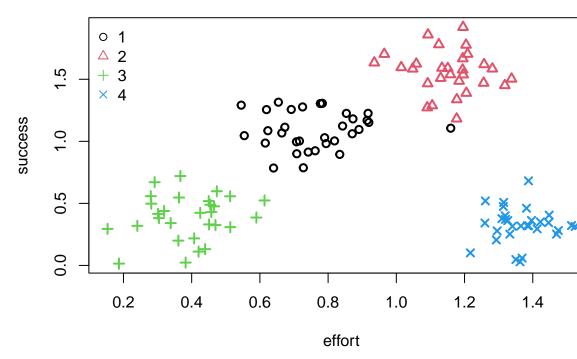
${\bf Clustering}$

```
reps <- rep(0, 6)
for (i in 1:6) reps[i] <- sum(kmeans(data.scaled, centers = i, nstart = 20)$withinss)
par(mfrow = c(1,1))
plot(1:6, reps, type = "b", xlab = "Number of groups", ylab = "Sum of squares")</pre>
```



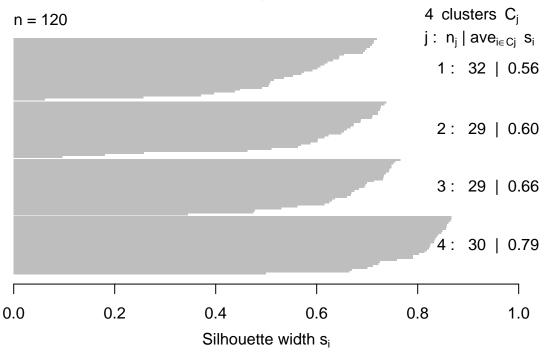
Scree plot

```
km.4 <- kmeans(data.scaled, centers = 4, nstart = 10)
km.4.groups <- km.4$cluster
km.4.groups
4 Clusters
   ## [112] 4 4 4 4 4 4 4 4 4
cluster.size.4 <- cbind(sum(km.4.groups == 1), sum(km.4.groups == 2),</pre>
               sum(km.4.groups == 3), sum(km.4.groups == 4))
cluster.size.4
     [,1] [,2] [,3] [,4]
## [1,]
      32
          29
plot(data.scaled, pch = km.4.groups, col=km.4.groups, lwd=2)
legend("topleft", legend = 1:4, pch = 1:4, col=1:4, bty="n")
```



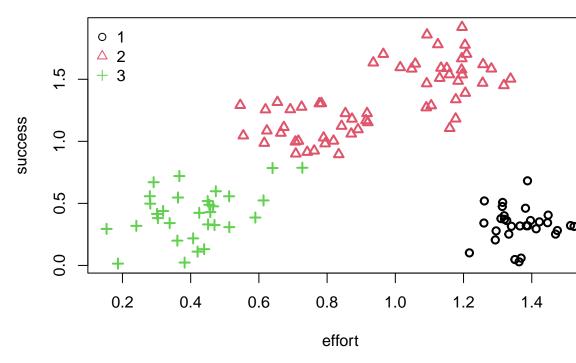
Plot / Silhouette plot
plot(silhouette(km.4.groups, dists))

Silhouette plot of (x = km.4.groups, dist = dists)



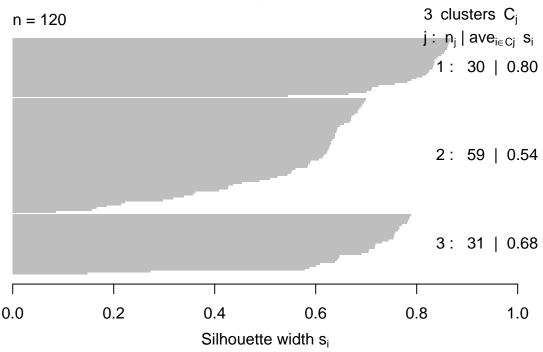
Average silhouette width: 0.66

```
km.3 <- kmeans(data.scaled, centers = 3, nstart = 10)
km.3.groups <- km.3$cluster
km.3.groups
3 Clusters
   ## [112] 1 1 1 1 1 1 1 1 1
cluster.size.3 <- cbind(sum(km.3.groups == 1), sum(km.3.groups == 2),</pre>
               sum(km.3.groups == 3))
cluster.size.3
     [,1] [,2] [,3]
## [1,]
      30
         59
plot(data.scaled, pch = km.3.groups, col=km.3.groups, lwd=2)
legend("topleft", legend = 1:3, pch = 1:3, col=1:3, bty="n")
```



Plot / Silhouette plot
plot(silhouette(km.3.groups, dists))

Silhouette plot of (x = km.3.groups, dist = dists)



Average silhouette width: 0.64

```
dc <- dist(data.scaled, method = "euclidean")
dc</pre>
```

Hierarchical cluster analysis

```
2
##
                                        3
                                                                5
                                                                           6
## 2
      0.238418601
## 3
      0.169587844 0.218150335
      0.410365817 0.611284076 0.408331610
      0.399048295 0.593652338 0.387629295 0.027606096
## 5
## 6
      0.333039453 0.315530308 0.163808883 0.455515780 0.429534851
      0.185388502 0.263490110 0.045361307 0.367582688 0.345987447 0.155364889
## 7
## 8
      0.306637961 0.504021221 0.303699765 0.107334145 0.092570511 0.368947783
## 9
      0.216730524 0.162569955 0.082790889 0.489468227 0.468025532 0.158297333
      0.069935120 0.285691711 0.153276127 0.342495918 0.330193249 0.306536777
      0.173180716\ 0.090339269\ 0.219544121\ 0.573804204\ 0.559356818\ 0.354073197
      0.459394256 0.280802851 0.327270234 0.708586463 0.683928742 0.262545772
      0.173292148 \ 0.247628505 \ 0.030188007 \ 0.379015614 \ 0.358005801 \ 0.162743616
      0.183361226\ 0.420763030\ 0.289249154\ 0.274401096\ 0.273455072\ 0.425523902
  14
      0.161419744 0.302276969 0.098078874 0.312390987 0.292943092 0.213412401
      0.237887258 0.398703055 0.188011280 0.221397234 0.199814642 0.252498625
      0.084721583 0.312001316 0.180948933 0.326276621 0.315894830 0.330565597
      0.240260788 \ \ 0.476345694 \ \ 0.371706597 \ \ 0.323553037 \ \ 0.329392617 \ \ 0.514196675
      0.255039471 0.408054838 0.194165502 0.219773646 0.196694743 0.244975852
```

```
0.188629758 0.304358331 0.089120922 0.320659853 0.299257187 0.182088129
       0.095097882 0.173185065 0.091675319 0.439572413 0.423055148 0.251930798
       0.492247536 0.728305817 0.568552099 0.252644581 0.278233168 0.664401482
       0.308173686 \ \ 0.520504607 \ \ 0.330950453 \ \ 0.106473424 \ \ 0.104335346 \ \ 0.410819765
       0.118361571 0.344663773 0.200250868 0.293962151 0.284572691 0.340749712
       0.298961897 0.437005706 0.219381916 0.218036702 0.192151805 0.237480053
## 28
       0.166426623 0.380181358 0.209542976 0.243941237 0.233108078 0.330268492
  29
       0.327668764 0.401863344 0.192721164 0.322631805 0.295752585 0.139929375
       0.060359491 \ 0.183967338 \ 0.174155960 \ 0.468016300 \ 0.455572770 \ 0.335128532
   31
       0.914009105 0.701437229 0.788697072 1.154498756 1.128380426 0.699010405
       0.903560246 0.684287585 0.785808771 1.161362935 1.135695604 0.706392670
##
   32
##
       0.735471112 0.523850786 0.613438112 0.989517859 0.964043637 0.535310465
   33
       0.966376471 0.747158127 0.847451051 1.220043775 1.194182573 0.764659506
##
   34
       0.642308135 \ \ 0.444660230 \ \ 0.511568486 \ \ 0.881505631 \ \ 0.855874236 \ \ 0.426751659
##
  35
##
   36
       0.829838797 0.591905070 0.756240787 1.161463608 1.138797033 0.731878444
       0.680201468\ 0.446511607\ 0.593060412\ 0.995330377\ 0.972163957\ 0.562051451
##
  37
       0.620165378 0.421757843 0.490968972 0.864123088 0.838674662 0.410185886
##
       0.840204960 0.623394820 0.720886098 1.096448425 1.070836229 0.641660154
##
  39
       0.951520357 0.718798518 0.855216657 1.248772911 1.224327962 0.800608121
##
       0.586346955 0.385736197 0.460569694 0.839542157 0.814447564 0.387905188
       0.896939365 0.662255167 0.806993614 1.205070955 1.181153511 0.761644977
       0.655606795 \ \ 0.438245134 \ \ 0.542598675 \ \ 0.930343953 \ \ 0.905683205 \ \ 0.481739991
##
       0.815079749 0.608267212 0.686421688 1.050986941 1.024908788 0.595479358
##
       0.925610766 0.701466395 0.813912936 1.195329737 1.169974041 0.741489917
       0.737912049 0.533429258 0.609281756 0.977143694 0.951285539 0.521771368
       0.853409004 0.644288522 0.725974565 1.090832216 1.064728398 0.635336527
##
##
       0.686218390 0.457020962 0.589015517 0.986533967 0.962716374 0.545805846
       0.531492209 0.366739182 0.386078321 0.742228685 0.716322509 0.286795476
##
       0.705069482 0.501031955 0.577097433 0.947344744 0.921632055 0.492298808
  50
##
  51
       0.863061775 0.627428744 0.776934850 1.177303416 1.153712873 0.737264759
##
  52
       0.591898167 0.364261289 0.496094344 0.896380858 0.873009713 0.462371385
       0.729959534 0.498607397 0.635578113 1.033754644 1.009972661 0.592917921
       0.836471349 0.598383463 0.778690731 1.186686751 1.165128651 0.770695810
##
  54
       0.898730807 0.660940358 0.822631796 1.226632550 1.203651855 0.792729622
       0.680438602 0.498840394 0.537707160 0.886048397 0.859606518 0.431588788
##
  56
       0.947137472 0.714161698 0.851541246 1.245624515 1.221234086 0.797901824
       0.921878248\ 0.707309525\ 0.798471256\ 1.166605650\ 1.140577227\ 0.711090505
  58
       0.612309048 0.375692047 0.537491083 0.944078580 0.921924001 0.525465004
       0.666061402 0.448990079 0.552289930 0.939031984 0.914285580 0.489648845
##
  60
  61
       1.535238148 1.303361878 1.431125687 1.811880296 1.786207941 1.356833269
       1.310762285 1.075917876 1.216189659 1.607148068 1.582295370 1.155624559
##
  62
##
   63
       1.141785742 0.931670501 1.010967944 1.361901299 1.335143305 0.909056165
       1.584969554 1.350685208 1.486842452 1.872857139 1.847523671 1.418866471
##
   64
  65
       1.386592528 1.160684781 1.272251560 1.643085176 1.616936293 1.187606039
       1.690716783 1.458146659 1.587434008 1.967842232 1.942109620 1.512659739
##
  66
##
  67
       1.126915541 0.932443586 0.984201791 1.311092188 1.283836442 0.866369795
##
       1.408354707 1.199634579 1.274093651 1.612782235 1.585642365 1.164560052
  69
       1.262581082 1.040052377 1.144323109 1.511901955 1.485657728 1.056542125
##
       1.283607850 1.072448162 1.152451437 1.499579773 1.472664312 1.048180377
  70
       1.521170281 1.294528536 1.407116453 1.776748227 1.750504145 1.321373113
##
  71
       1.458515552 1.247492243 1.326011699 1.667308783 1.640208773 1.218285374
       1.385316212 1.150142651 1.291259375 1.682019797 1.657124783 1.230198241
       1.413000762 1.190598021 1.293395184 1.656906340 1.630447378 1.202100108
```

```
1.395298099 1.170276391 1.279533913 1.648459772 1.622223586 1.193078932
      1.361042238 1.138563009 1.241913366 1.606821581 1.580432985 1.151786194
      1.320223481 1.088995930 1.216142620 1.598947109 1.573472845 1.144494077
      1.338442207 1.119973556 1.214468768 1.572648061 1.546028213 1.118642733
##
  78
   79
       1.068042372  0.881536967  0.921121013  1.239233103  1.211879179  0.798042486
      1.320297817 1.097707325 1.201635717 1.567781395 1.541456155 1.112579915
##
  80
      1.329856094 1.100349620 1.222179793 1.601289272 1.575584698 1.146179623
## 81
       1.577213457 1.348176196 1.467003408 1.840761714 1.814694113 1.385246610
## 82
## 83
       1.477300207 1.258818087 1.352390911 1.706955180 1.680180303 1.253974092
       1.487161010 1.265872650 1.365611289 1.725292444 1.698675707 1.271208101
  84
## 85
       1.368826928 1.138539076 1.262391051 1.642352866 1.616684325 1.187324672
       1.227718094 1.018626104 1.095145271 1.440869387 1.413940093 0.989718760
##
  86
       1.119955024 0.910173555 0.989066293 1.340425288 1.313689626 0.887411079
   87
      1.384697672 1.164198925 1.262827545 1.623464633 1.596911655 1.169075440
## 88
       1.484073185 1.258082818 1.369203991 1.738205816 1.711945039 1.282859392
## 89
       1.376763772 1.163250587 1.247180469 1.595372266 1.568452950 1.143904315
       1.121125701 1.021421575 0.951706290 1.123038069 1.096418294 0.789858383
       1.159762215 1.191728799 1.016334774 0.932515156 0.914874708 0.877330874
       1.170147783 1.126281151 1.004627228 1.069120337 1.045242941 0.842856131
       1.100604646 1.047437320 0.933491710 1.023009109 0.998211284 0.770545781
## 95
      1.037399356 1.028585090 0.879145896 0.891163286 0.868668585 0.724767239
      1.046139705 1.015170379 0.882577296 0.936735764 0.912832406 0.722729455
       1.174776603 1.143186919 1.011580582 1.052222422 1.029159739 0.851845066
## 97
       1.149251535 1.129205688 0.988579791 1.009561422 0.987137582 0.831319295
## 99 1.053974022 1.024922875 0.890844397 0.940305053 0.916577031 0.731397556
## 100 1.042102212 1.004678300 0.877273889 0.944306587 0.919996552 0.716249220
## 101 1.120672544 1.097078886 0.959036472 0.990000070 0.967118599 0.800895297
## 102 1.212874446 1.192052833 1.052255780 1.068432344 1.046387530 0.894895173
## 103 1.172232646 1.200453640 1.027329497 0.949987360 0.932057829 0.886620914
## 104 1.034989211 1.003251741 0.871222767 0.928315447 0.904284113 0.711202103
## 105 1.016105190 1.051896153 0.873486214 0.797085318 0.778317844 0.736786046
## 106 1.098446336 1.076458334 0.937093712 0.967467899 0.944534394 0.779288954
## 107 1.178270487 1.212270844 1.035787030 0.946169725 0.928925790 0.897664775
## 108 1.122930550 1.090112605 0.959297676 1.007792267 0.984310930 0.799242277
## 109 1.074346579 1.054463022 0.913391538 0.942532869 0.919560087 0.756054316
## 110 1.150113818 1.118323668 0.986789733 1.030364872 1.007129851 0.826975690
## 111 1.033175308 0.971466672 0.864907315 0.978485432 0.952909443 0.701293063
## 112 1.213206144 1.198174514 1.054061544 1.058960377 1.037365544 0.898149375
## 113 1.116869096 1.093442043 0.955256157 0.986321749 0.963424358 0.797146893
## 114 0.979632509 0.916441806 0.811100738 0.934713169 0.908788284 0.647385107
## 115 0.990430075 0.969859965 0.828894721 0.870532232 0.846828279 0.671231111
## 116 1.032267504 0.978093142 0.864833892 0.964639901 0.939399496 0.701701032
## 117 1.052897272 1.059836872 0.899535282 0.878026333 0.856922859 0.750396263
## 118 1.079370139 1.073367196 0.922133595 0.923346559 0.901432376 0.768650349
## 119 1.256075986 1.226637276 1.093605338 1.122482250 1.100068500 0.934411365
## 120 1.244595639 1.214301348 1.081903503 1.113434049 1.090890756 0.922523549
##
                             8
                                         9
                                                    10
                                                                11
                                                                             12
## 2
## 3
## 4
## 5
## 6
## 7
## 8
       0.264731210
```

```
## 9
       0.122042961 0.385744595
## 10
      0.151316202 0.237643197 0.221969340
       0.261142646 0.467207817 0.196289281 0.233565047
       0.354650652\ 0.612974239\ 0.250305220\ 0.472161065\ 0.366945321
       0.016842389 0.275004124 0.110740472 0.144523337 0.244302013 0.349395190
       ##
       0.066303690 0.206569012 0.180839181 0.107009599 0.280708307 0.420360865
       0.146251430 0.120874505 0.268252910 0.170449500 0.375530060 0.492127808
       0.175276543 0.223942412 0.251144900 0.029363806 0.255481969 0.501394208
  17
       0.361341112 0.265152136 0.441263436 0.219686641 0.400614995 0.690979889
       0.150697287 0.124393489 0.272452382 0.188393730 0.388441034 0.490039937
       0.460690030 0.196464867 0.582076288 0.420314180 0.653804817 0.804363826
##
  20
       0.046988045 0.217812365 0.168833837 0.138765403 0.292526017 0.399252773
  21
       0.125105727 0.332245941 0.122013066 0.116994456 0.142521793 0.365272255
##
       0.539265226\ 0.299912050\ 0.650058142\ 0.444198117\ 0.664222254\ 0.893820264
## 23
##
       0.295481177 0.049728182 0.413727809 0.242410331 0.475800642 0.648290504
       0.187401939\ 0.193356272\ 0.275081196\ 0.059173876\ 0.289397837\ 0.525136936
##
       0.093701902 0.355286608 0.056315563 0.226983172 0.248620959 0.260956449
       0.174138618 \ 0.139416500 \ 0.292004972 \ 0.233602864 \ 0.424517766 \ 0.493011371
  27
       0.185523677 0.141203210 0.290196656 0.099313527 0.332677054 0.536591358
##
  29
       0.153258045 0.247950413 0.241596630 0.275585048 0.412264174 0.402242420
       0.202760679 0.363002470 0.197584428 0.125531651 0.113111222 0.425424258
       0.814302025 \ 1.065564447 \ 0.711343479 \ 0.932572644 \ 0.791520657 \ 0.461513578
## 31
       0.813901181 1.069604006 0.706513866 0.926040587 0.773673590 0.459282747
##
       0.641085558 0.896996198 0.534767062 0.755241190 0.614104645 0.286539958
       0.874934881 1.129339017 0.768527091 0.988416485 0.836479481 0.520524414
       0.536942173 0.790097001 0.435207250 0.657019575 0.534560325 0.184903582
##
  35
##
   36
       0.794501710 1.059154273 0.673654228 0.870413799 0.670739291 0.471096644
       0.629670601 \ 0.894316184 \ 0.510270513 \ 0.715060100 \ 0.531604316 \ 0.301214584
##
   37
  38
       0.517123702 0.771752378 0.413977845 0.635628051 0.511663474 0.163833360
##
  39
       0.748787281 1.004481837 0.641819475 0.861717753 0.713174568 0.394197525
##
       0.888726423 1.151387182 0.772959666 0.983894948 0.803709147 0.540531686
       0.488275680 0.745467975 0.382345083 0.603454003 0.475716238 0.133645913
##
       0.842050789 1.105957348 0.724346398 0.931712021 0.745806553 0.499527307
       0.573516902 0.834190802 0.461784183 0.679422604 0.528226993 0.221762743
       0.711322933 0.961968062 0.609892909 0.831553185 0.698602077 0.359654238
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##
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##
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##
  86
##
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                                               14
                                                                   15
                                                                                        16
                                                                                                            17
## 2
## 3
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##
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##
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##
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##
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##
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##
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##
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##
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##
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       0.927344317 1.149750906 0.957213267 0.939684124 1.081192443 1.239441344
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## 109 0.902528860 1.099721622 0.921658164 0.889505373 1.043792968 1.187163075
## 110 0.977426570 1.182092379 0.999864589 0.971529657 1.122791343 1.270177494
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## 112 1.042266301 1.230878909 1.058604837 1.021741690 1.179676379 1.317011256
## 113 0.944793341 1.143567348 0.964729069 0.933288134 1.087050887 1.231091303
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## 118 0.909349568 1.094086704 0.923658699 0.885188431 1.044140867 1.180072147
## 119 1.083703836 1.283550966 1.104543368 1.073327478 1.227003312 1.370946084
## 120 1.072140841 1.272988246 1.093343269 1.062685401 1.215907089 1.360514050
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      0.105064665 0.413704045
      0.246172721 0.524471437 0.150886729
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      0.166212631\ 0.178051595\ 0.249486900\ 0.347337920\ 0.254247174
## 24
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##
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  27
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##
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      0.299966660 0.544538854 0.218832775 0.083240636 0.551351005 0.367110820
## 30
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##
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##
  35
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## 37
```

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##
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##
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##
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##
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       0.675912894 0.981897419 0.598262420 0.585653137 1.092584216 0.840732516
      1.026382494 1.341155987 0.931440135 0.863520323 1.418819829 1.180703520
##
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##
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      0.720491095 1.034836659 0.628323345 0.576309926 1.120777272 0.877751410
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##
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##
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##
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       1.293078982 1.594760694 1.216123847 1.190975228 1.710631057 1.458418684
##
       1.563701829 1.872741810 1.478698351 1.432816541 1.974074770 1.726240766
       1.463252873 1.762019708 1.388297296 1.365712334 1.881886552 1.629002653
##
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##
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       1.041537514 1.332944631 0.974525789 0.973119239 1.461882202 1.207743071
      1.355450842 1.663723436 1.271708884 1.230548604 1.767382817 1.518557613
##
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  81
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##
  82
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##
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       1.412912731 1.719205921 1.331178000 1.294195623 1.826911002 1.576877917
##
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##
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      0.984503155 1.201956894 0.963416406 1.033525008 1.373667572 1.134100607
      0.923520461 0.968629525 0.971239402 1.106866986 1.164181524 1.001205414
```

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## 93 0.981580437 1.132365447 0.990777268 1.094563475 1.320424402 1.106401058
## 94  0.921837270 1.091128845 0.924492797 1.022464156 1.275454762 1.053528130
## 97
      0.976724744 1.111521623 0.992390338 1.102391540 1.301928302 1.094931911
## 98  0.943589843  1.065981444  0.964695972  1.079924858  1.257757161  1.056237934
## 99 0.857672346 1.003188872 0.871784199 0.981716689 1.191414128 0.979136640
## 100 0.852687706 1.010094728 0.862034187 0.967582823 1.196281266 0.978983120
## 101 0.918285693 1.048632820 0.936921719 1.050226710 1.239344951 1.034049720
## 102 1.006219607 1.122906027 1.028184007 1.143595432 1.315524630 1.117045974
## 103 0.937584517 0.987189602 0.983630845 1.118097666 1.182763989 1.017562014
## 104 0.841405345 0.992744990 0.853565075 0.961917152 1.179917115 0.965096187
## 105 0.780340166 0.838653133 0.827602466 0.963799224 1.034032829 0.861915401
## 106 0.895546022 1.026424713 0.914504228 1.028341648 1.216954502 1.011289740
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## 108 0.927258207 1.069250343 0.941131266 1.049997844 1.258408778 1.047987323
## 109 0.870660273 1.001765298 0.890137667 1.004711622 1.192132695 0.986217923
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## 115 0.790078062 0.933551169 0.806881331 0.920143340 1.121640768 0.909868219
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## 117 0.832078565 0.929031586 0.865125159 0.991147993 1.122688826 0.932222903
## 118 0.866041287 0.977757375 0.892920136 1.013785375 1.170296450 0.973182127
## 119 1.054488809 1.178505938 1.072831086 1.184581150 1.370525133 1.168854954
## 120 1.043879880 1.170090853 1.061578392 1.172827958 1.361826727 1.159080933
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##
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       0.986410215 \ \ 0.720831280 \ \ 0.936467524 \ \ 0.997755114 \ \ 0.834370909 \ \ 0.872799804 
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##
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##
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##
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##
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##
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##
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##
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##
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##
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##
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##
   53
##
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##
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##
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##
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##
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##
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##
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##
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##
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##
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##
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##
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## 95
## 96
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## 102 1.175267062 1.001124188 0.962212937 1.138197958 0.891545473 1.226411728
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## 108 1.092455376 0.904937689 0.884730913 1.058114309 0.807026808 1.133152463
## 109 1.038448440 0.862304642 0.827207017 1.002305642 0.754043274 1.087546590
## 110 1.118705136 0.932740477 0.910107168 1.083959293 0.833414344 1.160704088
## 111 1.018579870 0.803561180 0.825940207 0.990451763 0.735273738 1.035704124
## 112 1.172837803 1.004468903 0.958193206 1.134821399 0.890186595 1.228160741
## 113 1.081951637 0.903298694 0.871102750 1.046042237 0.797330976 1.129387496
## 114 0.966897912 0.749244420 0.777024698 0.939694924 0.684547589 0.981497862
## 115 0.956479152 0.777464450 0.747224319 0.921282325 0.671500653 1.003038774
## 116 1.013931374 0.805141883 0.817565314 0.984370176 0.729455173 1.036707720
## 117 1.004649776 0.856073930 0.786741711 0.964349300 0.726286565 1.072503568
## 118 1.036760662 0.874898714 0.821451019 0.998281430 0.754998486 1.095979342
## 119 1.222026044 1.040320571 1.011020511 1.186107867 0.937315083 1.267642142
## 120 1.211108166 1.028387311 1.000530229 1.175410970 0.926261321 1.255910744
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       0.054507066
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       0.178701763 0.172872631
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       0.073253656 0.062948585 0.234025239
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       0.277389225 0.279865077 0.108977380 0.339251399
       0.317274664 0.264328179 0.283402297 0.299335821 0.361190994
       0.303392976 \ \ 0.267034331 \ \ 0.175797854 \ \ 0.325395944 \ \ 0.213212566 \ \ 0.169936652
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       0.297728811 0.297858117 0.125403401 0.358085040 0.022902540 0.363409683
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##
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       0.082226269 0.065165462 0.107719515 0.126725806 0.214963049 0.259435750
       0.205454153 0.154144927 0.277054064 0.156381298 0.382946073 0.171462087
       0.329119998 0.325637573 0.152924774 0.386943926 0.059044267 0.366545961
##
##
       0.230822899 0.176332119 0.256244538 0.198796080 0.355272537 0.108019895
       0.263375815 0.248011053 0.088975414 0.310900055 0.090959901 0.273757648
##
   43
       0.103606635 0.120024333 0.086894919 0.171145107 0.174866029 0.318045025
##
   45
       0.098235247 0.048491239 0.206212718 0.063580582 0.315073811 0.236193490
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       0.179637694 \ 0.185425848 \ 0.038783056 \ 0.242901232 \ 0.097771370 \ 0.321510888
##
       0.063685134 0.087048409 0.120549206 0.132696988 0.214422457 0.314824477
       0.268881684\ 0.237524552\ 0.131147099\ 0.298367380\ 0.173552435\ 0.193700235
##
   48
       0.412701221 0.419846419 0.250132361 0.477864047 0.141157287 0.480891531
##
       0.211602753 0.214093915 0.047684320 0.273097198 0.066193914 0.324920283
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   50
       0.250177433 0.196164072 0.247733746 0.227298200 0.340297614 0.072697228
##
       0.346068575 \ 0.322486930 \ 0.179275245 \ 0.384904685 \ 0.159002400 \ 0.269512924
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       0.249224252 0.210728092 0.144044504 0.268460404 0.209656702 0.151788229
## 53
##
       0.399031960 0.345707547 0.358507243 0.377622657 0.426748358 0.082220507
       0.311239515 0.256732526 0.316702766 0.277847103 0.406189345 0.069271768
       0.271327000 0.288695424 0.141560501 0.341079568 0.077639033 0.419917890
##
   56
   57
       0.208303361 0.156452568 0.275750256 0.160715333 0.381158317 0.165381135
       0.016644649 0.043221385 0.186487527 0.057467612 0.287818881 0.307547509
##
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       0.252613384 0.237510803 0.078572819 0.300374359 0.091313830 0.270815876
##
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       0.661005575 0.650519297 0.822657810 0.592600656 0.930375468 0.728703330
##
       0.481580984 0.457120058 0.621726622 0.408499223 0.730683836 0.492775867
##
   63
       0.230318759 0.255989714 0.408197252 0.198219955 0.500624470 0.486916865
##
   64
       0.727864485 0.713162455 0.883591281 0.657563350 0.992151104 0.767174728
       0.488596200 \ 0.486443368 \ 0.659043542 \ 0.425141012 \ 0.764049162 \ 0.614400744
##
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       0.815812117 0.806509604 0.978813887 0.748136610 1.086372296 0.879467371
       0.259215767 0.303980522 0.416101004 0.263310455 0.488554860 0.562345060
##
  67
       0.498261253 0.520853614 0.676055751 0.460039903 0.766237845 0.725657430
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0.357837159 0.359450619 0.530931436 0.297095893 0.634458320 0.517278976
          0.371106343 0.392132208 0.549525177 0.331162921 0.642438047 0.600833618
          0.622523380 0.621309423 0.793846048 0.559881229 0.898560768 0.740396674
          0.546236098 \ 0.565895044 \ 0.724677465 \ 0.504138897 \ 0.816923538 \ 0.760033886889 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.816923538 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0.81692358 \ 0
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          0.552290872 0.529953632 0.695890054 0.479566124 0.804866969 0.565026156
##
          0.505294529 0.509596214 0.680348053 0.446992064 0.782616891 0.658331374
          0.494246169 0.493858783 0.666128978 0.432104747 0.770462253 0.627490758
##
   76
          0.454206710 0.457717216 0.628715231 0.395181406 0.731397569 0.608899282
          0.453488724 0.438400439 0.609434793 0.382751445 0.717744358 0.521348475
    77
          0.425925227 \ \ 0.435869667 \ \ 0.603398156 \ \ 0.372929242 \ \ 0.702923464 \ \ 0.609964475
          0.244622989 0.296277531 0.377539962 0.270295526 0.437108846 0.560538922
          0.414414777 \ 0.417080497 \ 0.588325594 \ 0.354630718 \ 0.691404458 \ 0.570190342
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##
          0.450825149 0.439938905 0.612288935 0.381959554 0.719803496 0.540226184
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    82
          0.686339800 0.681868329 0.854737977 0.621478963 0.960726812 0.783451862
          83
## 84
          0.576936827 0.583606735 0.753313384 0.520790559 0.854275377 0.734684205
          0.492287758 \ 0.480992671 \ 0.653168916 \ 0.423287101 \ 0.760847981 \ 0.573628312
##
    85
          0.317378470 0.342252340 0.494989035 0.283089889 0.585919951 0.563894779
          0.208968871 0.236091291 0.386583321 0.179591010 0.478730033 0.471587744
    87
          0.474161700 0.481219584 0.650582039 0.418341737 0.751514553 0.641857310
##
    89
          0.584087890 0.583440399 0.755845378 0.521835819 0.860314417 0.707712318
          0.463023080 \ 0.480140314 \ 0.641724101 \ 0.417934667 \ 0.736540834 \ 0.671861638
          0.663666183 \ 0.716753662 \ 0.691225193 \ 0.718853247 \ 0.670518395 \ 0.958719264
## 91
          1.185881805 1.229758294 1.130434134 1.255124822 1.055431867 1.412023982
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## 93
          0.915268033 0.965606853 0.906990148 0.977133516 0.859931139 1.187396825
          0.831694731 0.881500875 0.820436985 0.894621187 0.773315200 1.101140536
          0.951566620 0.996602796 0.905328022 1.020039413 0.837407922 1.188429655
## 95
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          0.877796417 0.924793260 0.844949735 0.944461023 0.785206853 1.128236956
          0.964803654 1.014318649 0.948817541 1.028036561 0.896732309 1.230685510
   97
          0.989158862 1.037361670 0.962859237 1.054271412 0.904861969 1.245890204
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## 99
          0.889936879 0.936964121 0.857079823 0.956555508 0.797119683 1.140376991
## 100 0.851646531 0.899042551 0.821959035 0.917893921 0.764388396 1.105051879
## 101 0.955638752 1.003608038 0.928165977 1.021083825 0.870024466 1.211241411
## 102 1.033266959 1.082539377 1.014386670 1.096812653 0.959778980 1.296766420
## 103 1.182010848 1.226449666 1.129715399 1.250828691 1.056285380 1.411809488
## 104 0.867737619 0.914531879 0.833737635 0.934630203 0.773560584 1.117059523
## 105 1.092528138 1.133209894 1.021687927 1.163706759 0.940108439 1.300022887
## 106 0.945931516 0.993345877 0.914763970 1.012057540 0.854801285 1.198034762
## 107 1.207499156 1.251492181 1.152502828 1.276646470 1.077551534 1.434123355
## 108 0.923151717 0.971876721 0.901690255 0.987623169 0.847287638 1.184175912
## 109 0.936949740 0.983701563 0.901519363 1.003818285 0.839438287 1.184907593
## 110 0.946235937 0.995362798 0.927470425 1.010094859 0.874159346 1.209678402
## 111 0.756115358 0.805078235 0.739824680 0.820476489 0.691678414 1.021125462
## 112 1.055082460 1.103907623 1.032482965 1.119278182 0.975605139 1.315287447
## 113 0.953566230 1.001451045 0.925530022 1.019119161 0.867118783 1.208640244
## 114 0.719030436 0.766666306 0.693992788 0.785181999 0.642041104 0.976373749
## 115 0.879208280 0.924012999 0.832742712 0.947930274 0.765808515 1.115921234
## 116 0.783700789 0.832101885 0.762532127 0.848796711 0.711027386 1.044645328
## 117 1.018033257 1.062101110 0.965379876 1.087224007 0.893361484 1.247750896
## 118 0.990498477 1.036226020 0.947854179 1.058333559 0.881262097 1.231117885
## 119 1.033702653 1.084200292 1.025042627 1.095125744 0.975992431 1.305843092
## 120 1.021707216 1.072121344 1.012468482 1.083303474 0.963260559 1.293349464
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       0.209030799
       0.222280070 0.232729486
## 40
       0.272305974 0.394959240 0.192346113
       0.204165422 0.036200090 0.260553938 0.413104326
##
       0.216854332 0.364134242 0.193537602 0.064840582 0.377594964
       0.122537706 0.089809588 0.185487926 0.319063131 0.096353052 0.281437393
##
       0.248660602 0.195930111 0.068504487 0.260529119 0.228778439 0.260766346
       0.269252518 0.331369654 0.102723088 0.107226263 0.356407548 0.138473365
##
       0.212069556 0.118558049 0.122054247 0.304821235 0.151566372 0.289286034
       0.267290343 0.235190634 0.055392860 0.236363252 0.267440261 0.245544846
       0.044937916 \ 0.172161505 \ 0.186750055 \ 0.266927260 \ 0.172867635 \ 0.218629395
## 48
       0.316303587 0.127218108 0.355349863 0.522174519 0.114594277 0.490173145
  49
       0.199979170 0.086140877 0.149486578 0.324646389 0.118723114 0.303390678
##
  51
       0.184379659 0.346988802 0.201200769 0.103651571 0.357224602 0.038901649
## 52
       0.099885940 0.145377007 0.264877897 0.361190233 0.126245701 0.310931535
       0.057092707 \ 0.211667842 \ 0.169582586 \ 0.221748238 \ 0.216543330 \ 0.171589558
##
  53
       0.220001582 0.425966849 0.341431210 0.238300549 0.423940247 0.180419519
## 55
      0.231788122 0.411421420 0.269015273 0.129247772 0.418942720 0.080592385
## 56  0.284388451  0.094256932  0.228604082  0.414574353  0.126108651  0.397623912
```

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0.267650110 0.392879988 0.192823420 0.006088497 0.410584926 0.058904301
          0.302307210 0.307664030 0.084675032 0.190307766 0.338252577 0.218190669
          0.079767573 0.229509367 0.298389719 0.346662537 0.212008644 0.287617805
          ##
    60
          0.856873898 0.948026382 0.715453743 0.584569004 0.974233633 0.642698048
          0.630573319 0.745837513 0.518845891 0.361127211 0.768100063 0.413856907
    62
##
          0.522707317 0.522242288 0.310342536 0.322467403 0.555486148 0.380130948
## 64
          0.904838612 1.008889241 0.777444317 0.633831110 1.033542451 0.688442346
          0.718537441 0.783174954 0.551421620 0.452012405 0.811955204 0.515502555
    65
##
          1.011653596 1.104154385 0.871510001 0.739473106 1.130509947 0.796540758
          0.561814047 \ 0.511378450 \ 0.339535423 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.412796527 \ 0.547077110 \ 0.46157909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \ 0.4127909681 \
    67
##
    68
          0.784998298 0.788231562 0.577723991 0.554276671 0.822088565 0.617962048
##
          0.603382869 0.654068165 0.423821617 0.347623092 0.683753541 0.412459089
    69
##
    70
          0.656133685 0.664088879 0.449698904 0.430055424 0.697331264 0.492848264
          0.851161330\ 0.917823216\ 0.686257572\ 0.582305467\ 0.946767109\ 0.644761143
##
    71
##
          0.827615169 0.838716584 0.624459983 0.588689258 0.872179198 0.653092485
          0.705191875 \ \ 0.820256564 \ \ 0.592319679 \ \ 0.436164313 \ \ 0.842825518 \ \ 0.488380301
##
    73
          0.752743965 0.802640164 0.573645969 0.491902706 0.832942404 0.556349568
##
          0.729123489 0.789841919 0.558660959 0.463925491 0.819048592 0.527725547
    75
##
          0.701008364 0.751291547 0.521873305 0.441430644 0.781397173 0.506041906
##
    77
          0.642716172 0.734824233 0.502868355 0.370581601 0.760238871 0.430302385
          0.688961457 0.723566567 0.498331981 0.439419345 0.754982445 0.504208840
##
   79
          0.536529409 0.459991888 0.317530460 0.426336808 0.496148338 0.466888741
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          0.902793530 0.979449836 0.747019472 0.631495045 1.007448194 0.692201037
          0.826171386 0.861679792 0.637251920 0.571105737 0.893396473 0.635884760
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    84
          0.829033930 0.874648075 0.647179951 0.568555132 0.905529021 0.632973518
          0.692641566 0.778524229 0.545929368 0.420947517 0.804884140 0.481473676
##
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          0.608372396 0.607761484 0.397408584 0.395344859 0.641376745 0.456082317
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          0.503060015 0.500360852 0.289389716 0.309363992 0.533640549 0.365493481
##
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          0.729369453\ 0.771866373\ 0.544590269\ 0.473193421\ 0.802752008\ 0.537972259
          0.815474832 0.879662572 0.648318059 0.547712468 0.908769933 0.610661956
          0.740331265\ 0.757986893\ 0.539858817\ 0.500475347\ 0.790823323\ 0.564831035
##
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          0.864245221 0.686000358 0.701275326 0.868852973 0.713502737 0.890482358
          1.267426272 1.058405962 1.189538480 1.380530122 1.067317538 1.379426783
          1.069206273 0.870170336 0.939282121 1.119732547 0.890123435 1.132620559
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          0.997858897 0.792676830 0.890731383 1.078043934 0.808668123 1.083695367
          1.107760876 0.905813907 0.985670690 1.168436032 0.924044842 1.179202497
          1.117312184 0.912556334 1.005551313 1.191142737 0.928736370 1.198903938
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## 100 0.976631201 0.772426145 0.865866061 1.052507403 0.789282599 1.059039029
## 101 1.082474607 0.877736823 0.971364154 1.157302742 0.893980966 1.164661824
## 102 1.171549852 0.968197232 1.053131611 1.236618219 0.985394216 1.246665632
## 103 1.268666007 1.059720440 1.187141494 1.377726271 1.069337964 1.377629205
## 104 0.986269253 0.780946252 0.880097904 1.067674557 0.796829374 1.072972594
## 105 1.149736367 0.941152004 1.088542622 1.280769923 0.947201524 1.274745284
## 106 1.067537742 0.862094571 0.959952397 1.146790370 0.877735686 1.153037519
## 107 1.289540131 1.080518889 1.211426151 1.402357345 1.089400622 1.401397395
## 108 1.058898305 0.855918509 0.941411879 1.125839089 0.873540890 1.134910817
## 109 1.052426999 0.846229011 0.949000579 1.136791188 0.861142410 1.141757159
## 110 1.085511126 0.882997521 0.965796063 1.149419396 0.900894725 1.159329788
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## 111 0.901063077 0.702017243 0.775701916 0.959118738 0.722319672 0.969238484
## 112 1.187892195 0.983471113 1.073377694 1.257884138 0.999837499 1.266856407
## 113 1.079614852 0.874770644 0.969029806 1.155110730 0.890928580 1.162299360
## 114 0.852626372 0.651674406 0.734460657 0.920287788 0.671045969 0.927845846
## 115 0.979020924 0.771470255 0.885924428 1.075797360 0.784802084 1.077417022
## 116 0.921611280 0.720583981 0.801317111 0.985989426 0.739731348 0.994815750
## 117 1.106127303 0.897399956 1.022473614 1.213162643 0.908107333 1.212940254
## 118 1.094473052 0.886816500 0.999479610 1.188626757 0.899830039 1.191469067
## 119 1.186137674 0.985637953 1.058047662 1.238308634 1.004623220 1.251387030
## 120 1.173446210 0.972887874 1.045755625 1.226240805 0.991856957 1.239120924
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0.271821266 0.165390764
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##
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       0.122186619 0.204572764 0.212200350 0.182675499 0.218078235 0.047307900
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      0.336561206 0.398848613 0.315261935 0.397135572 0.396822912 0.253829044
      0.323475758 0.334218283 0.218752634 0.352718217 0.322691509 0.248443932
      0.162564023 0.170074048 0.331143216 0.109773262 0.208587142 0.242003407
##
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##
      0.316237203 0.261160786 0.110095508 0.304071589 0.237769651 0.262989109
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      0.269075398 0.115798116 0.083308281 0.190332934 0.076373625 0.269531468
##
      0.160721943 0.316859782 0.349005432 0.267936608 0.339859551 0.112087277
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##
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##
      0.888531092 0.763286915 0.617953474 0.835200553 0.723995492 0.849085674
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      0.493694357 0.326713235 0.259360487 0.403974086 0.288589906 0.493253627
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##
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      0.732212360 0.592155519 0.461005771 0.666962954 0.552274176 0.703728875
       1.044845575 0.918486947 0.774270105 0.990922733 0.879035258 1.004739929
      0.505076144 \ \ 0.329206838 \ \ 0.326153013 \ \ 0.400088257 \ \ 0.299151225 \ \ 0.525259879
##
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##
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      0.607035922 0.461434082 0.338608707 0.536986954 0.421493068 0.584630253
      0.634226969 0.468553917 0.387830884 0.545828475 0.430294783 0.629383178
      0.867049110 0.726129298 0.595690441 0.801319536 0.686203392 0.837507692
##
       0.809249580 0.643439353 0.558414571 0.720626889 0.605351999 0.802451908
      0.751945514 \ 0.648778140 \ 0.490208979 \ 0.714365177 \ 0.611709436 \ 0.703005795
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      0.757404771 0.608573040 0.489133402 0.684909536 0.568669783 0.734889849
##
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       0.705460435 0.557625664 0.437100193 0.633745630 0.517694667 0.682917616
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      0.683560910 0.528139426 0.420941762 0.605187901 0.488501761 0.667527017
##
  78
       0.465422195 0.292228607 0.328421783 0.355737520 0.269239169 0.496714588
##
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      0.679727527 0.552772571 0.408338104 0.624524378 0.513594737 0.643997831
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      0.925321640 0.789785957 0.653500871 0.864027502 0.749972594 0.891669475
       0.822505553 0.665972981 0.559064069 0.743188092 0.626498590 0.805710892
      0.831604071 \ 0.679708300 \ 0.564545572 \ 0.756504021 \ 0.639931324 \ 0.810671881
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      0.719832023 0.594165667 0.448765543 0.665740938 0.555021811 0.682707809
      0.580743684 0.412754084 0.342511221 0.489810580 0.375065520 0.579735678
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       0.472310489 0.304875917 0.241613513 0.382115899 0.266841185 0.472996287
      0.729228966 \ 0.576993073 \ 0.463316409 \ 0.653743813 \ 0.537195453 \ 0.709814533
##
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      0.829575073 0.687693988 0.558474898 0.763005693 0.647760571 0.801095097
      0.725136275 0.562150248 0.471078968 0.639527648 0.523428756 0.715924562
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       0.749442032 0.640747871 0.761796428 0.653259037 0.646636330 0.819396515
      1.146254586 1.121042302 1.278247096 1.093759115 1.144491132 1.228980294
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##
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      0.928295420 0.890383731 1.045074753 0.867822367 0.912161026 1.010353227
      0.875348579 0.822950636 0.973073921 0.806726213 0.842061299 0.956152651
      0.985711968 0.919157300 1.061961481 0.910165285 0.934659546 1.065033528
      0.994843116 0.938194878 1.085409992 0.924476173 0.955863918 1.075392906
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## 99 0.887297973 0.835148544 0.985240774 0.818866115 0.854251342 0.968147918
## 100 0.854204771 0.798274322 0.947254003 0.783602299 0.816750770 0.934593756
## 101 0.960004574 0.903924344 1.051709359 0.889802885 0.921859757 1.040563971
## 102 1.049264540 0.986362063 1.130274446 0.975817185 1.002443865 1.129163004
## 103 1.147188342 1.118676875 1.274939731 1.092803229 1.141511103 1.229825154
## 104 0.863750288 0.812252459 0.962842042 0.795551060 0.831610139 0.944623730
## 105 1.030217855 1.020242077 1.181466995 0.986288616 1.046682930 1.113022207
## 106 0.945016198 0.892273621 1.041559991 0.876525550 0.910984363 1.025899475
## 107 1.168373661 1.142933145 1.299982307 1.115809578 1.166283340 1.251099864
## 108 0.936654405 0.874420388 1.019780533 0.863138303 0.891113200 1.016455431
## 109 0.929890188 0.881082753 1.032021504 0.863447452 0.900679466 1.011124025
## 110 0.963351846 0.899032307 1.043142366 0.888866620 0.915138209 1.042933225
## 111 0.779569566 0.709146432 0.852895537 0.701105337 0.724868173 0.857854933
## 112 1.065463368 1.006301332 1.151789598 0.994017990 1.023157704 1.145829844
## 113 0.957135079 0.901551640 1.049571039 0.887184518 0.919606036 1.037743454
## 114 0.730689333 0.667177728 0.814820197 0.655408034 0.684811291 0.809821414
## 115 0.856628772 0.817572881 0.972492257 0.795174284 0.839457127 0.938528175
## 116 0.799689181 0.734340214 0.880084557 0.723904819 0.751081668 0.878773804
## 117 0.984315378 0.954002844 1.110592227 0.928353799 0.977004081 1.066809854
## 118 0.972094313 0.931250108 1.084657791 0.910179256 0.952276604 1.054006990
## 119 1.064416282 0.992271652 1.131411685 0.986302035 1.006163627 1.143062792
## 120 1.051708011 0.979917065 1.119374642 0.973732057 0.993939603 1.130387805
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      0.205863396
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      0.471151345 0.293449699
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       0.228235804 0.178417400 0.281239054
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      0.331135808 0.179046438 0.144401213 0.139844154
      0.536256287 0.397276011 0.150720963 0.313330783 0.218926065
      0.533464284 \ \ 0.361850262 \ \ 0.069724223 \ \ 0.331556276 \ \ 0.202647348 \ \ 0.111542060 
## 55
       0.151653991 0.095699391 0.388947327 0.236632234 0.271717849 0.490637089
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      0.520074426 0.323392052 0.097757262 0.357147962 0.217554544 0.232322753
      0.424490105 0.221736648 0.239206634 0.349544889 0.247147816 0.388913557
      0.311401920 0.248333338 0.251972523 0.085772607 0.136858031 0.245724325
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      0.215888344 0.081001560 0.255358778 0.101440171 0.119028562 0.335434848
      1.070124210 0.864577782 0.679375137 0.943508558 0.805438408 0.758260711
##
      0.871836240 0.667050705 0.448595214 0.722121512 0.582390432 0.518939803
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       ##
   64
       1.132793751 0.926930839 0.723554013 0.994926919 0.855572987 0.788779121
##
       0.901202701 0.697855469 0.554205345 0.796674430 0.663668691 0.660588253
      1.225894182 1.020498077 0.832671971 1.099197653 0.960773371 0.904404286
##
  66
       0.598390508 0.431928256 0.490560424 0.594264599 0.508333025 0.640926583
##
      0.888769933 0.703409433 0.655582197 0.842283389 0.727929222 0.789174768
##
   68
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##
  70
      0.768584713 0.578630241 0.529900540 0.713925151 0.599071200 0.667024876
       1.035224597 0.832374622 0.683122220 0.930768166 0.796803674 0.781126886
##
##
      0.941202885 0.753457372 0.691286004 0.888202363 0.770531663 0.820380237
      0.946022136 0.740934610 0.522716041 0.797083095 0.657319004 0.587465619
      0.917043814 0.716649931 0.595245787 0.826400934 0.696859488 0.708730163
##
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       0.906945637 0.704287934 0.566506296 0.806105668 0.673955449 0.674775624
##
      0.866364747 0.665367407 0.544942455 0.774371815 0.645038652 0.661118616
  76
  77
      0.858179462 0.652331366 0.467780299 0.728396891 0.590670231 0.559184642
      0.834959815 0.637426119 0.542835695 0.756858738 0.632232796 0.667774336
##
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  79
       0.537029423 0.385842968 0.491253077 0.556725642 0.486432840 0.641597231
##
  80
      0.826862350 0.625322646 0.505509541 0.733516091 0.604318479 0.623945733
##
  81
      0.859455289 0.653954895 0.483749305 0.738064558 0.601757859 0.581807324
##
       1.098643503 0.894559582 0.729902863 0.985609622 0.849598546 0.818433096
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      0.971560009 0.775562496 0.674749188 0.895501345 0.769655146 0.792645300
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      0.987208567 0.788535778 0.671866440 0.901804828 0.773026774 0.784136063
##
      0.900636236 0.695056933 0.519205348 0.776935557 0.639964549 0.611888574
  85
      0.710768688 0.522660201 0.491884620 0.662237776 0.551509310 0.633624933
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0.605976104 0.414928067 0.398904414 0.554266576 0.446529418 0.545658375
      0.884723886 0.685757311 0.576836470 0.800360118 0.673030301 0.695644544
       0.996782001 0.794137039 0.649191928 0.894122424 0.760809645 0.750559243
      0.863850503 0.672245999 0.602995736 0.802627067 0.683275319 0.732821321
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      0.966933234 1.087224099 1.376868631 1.191858648 1.263041062 1.481660089
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## 94
## 95
       0.762616229 0.863817094 1.149671037 0.981339383 1.041740270 1.260640410
      0.723913550 0.805683554 1.085588048 0.934832527 0.984658936 1.202803145
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       0.843711579 0.924247730 1.201884046 1.054885274 1.103288139 1.321080753
## 98
       0.735222996 0.817765421 1.097773969 0.946557722 0.996730829 1.214902646
## 100 0.706869319 0.783304561 1.061502575 0.915293942 0.962346479 1.180143947
## 101 0.809306964 0.889474247 1.167449811 1.020117712 1.068511134 1.286348172
## 102 0.902643469 0.976860750 1.250953955 1.111348957 1.155844488 1.372883392
## 103 0.970136529 1.086904975 1.375676425 1.194248750 1.263314029 1.482088315
## 104 0.711892206 0.794329639 1.074671927 0.923006041 0.973279795 1.191493271
## 105 0.842751812 0.976866901 1.269355771 1.069912803 1.149380023 1.366745433
## 106 0.791678513 0.875516692 1.155175913 1.003943117 1.054488245 1.272637580
## 107 0.988915984 1.109316310 1.398902335 1.213914840 1.285155817 1.503778034
## 108 0.792536631 0.864103344 1.138770936 0.999364682 1.043089152 1.260176503
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## 119 0.926584311 0.989283712 1.257489031 1.129946048 1.167748361 1.383241962
## 120 0.913838989 0.976645607 1.245119375 1.117185700 1.155135842 1.370696067
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       0.287528127 0.318020891 0.341651160 0.380154259
##
       0.318862210 0.159991235 0.308262597 0.258340010 0.167331811
       0.661585763 0.932331193 0.589252788 0.647629477 0.930198809 0.878896362
##
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       0.698615419 0.998576033 0.638045332 0.713769991 0.975519612 0.935899767
##
       0.553340919 0.758331922 0.457548835 0.476773288 0.795939688 0.722024992
  65
       0.811495990 1.087070775 0.744027225 0.802723705 1.084156385 1.035221694
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##
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       0.677644499 0.737376478 0.560364607 0.493142358 0.864709864 0.750869168
##
       0.462842814 0.626556043 0.353558927 0.346665523 0.682271070 0.596645856
##
  70
       0.555812290 0.618065991 0.436134257 0.365298564 0.735836375 0.623475036
       0.676928350 0.891300235 0.587655767 0.611019867 0.927905025 0.856878017
##
  71
       0.708964756 0.790054537 0.594752841 0.540223617 0.907381561 0.798502750
## 73
       0.496414785 0.818503265 0.440017940 0.536975296 0.774614049 0.743079737
## 74 0.599732811 0.770857945 0.497665264 0.494979884 0.831259112 0.746980443
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## 75  0.567038774  0.763098747  0.469527918  0.482819875  0.806853407  0.730139285
## 76  0.551416149  0.720846571  0.447244605  0.443640283  0.779632874  0.695048137
      0.456412625 0.723820203 0.375460225 0.439168197 0.717043845 0.664051461
      0.556645249 0.687054311 0.445420380 0.416953809 0.768395727 0.672966872
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       0.476829343 0.722074532 0.389273346 0.437221955 0.730621219 0.669928611
       0.717907037 0.956519368 0.636563032 0.674168527 0.978148719 0.915339640
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      0.675587224 \ 0.839628249 \ 0.574310844 \ 0.567279732 \ 0.907665315 \ 0.821116871
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       0.523494541 \ 0.559986300 \ 0.401344923 \ 0.312737838 \ 0.687808134 \ 0.569980625
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       0.084762901 0.275068000 0.570922603
       0.189592211 0.202978728 0.304220159 0.271067113
       0.156335364 0.386877023 0.637954451 0.119393501 0.334391736
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       0.382328593 0.424155977 0.267965910 0.466350376 0.231635587 0.484742448
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       0.316577234 0.229573788 0.177816652 0.393460684 0.132342685 0.465848345
##
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       0.399824647 0.364155157 0.141855802 0.483433157 0.214445980 0.530999806
       0.114401723 0.282316298 0.427734450 0.194376574 0.134895539 0.216977618
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##
       0.244573402 0.242602360 0.255652126 0.327443401 0.058303649 0.383291316
       0.215256041 \ \ 0.087647542 \ \ 0.320415003 \ \ 0.274894814 \ \ 0.119566530 \ \ 0.371394083
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##
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       0.675706029\ 0.573402175\ 0.190504876\ 0.756319707\ 0.486114714\ 0.814891365
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       0.210676972 0.122839258 0.301464963 0.278437270 0.086237936 0.366573508
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       0.079826146 0.304622437 0.498240806 0.138746429 0.198335610 0.143508296
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       0.250864494 0.349597369 0.345066961 0.332945554 0.147817199 0.345827118
       0.208457790 0.322220067 0.364732703 0.290417962 0.126688650 0.306323664
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       0.446527821 0.382572343 0.087103857 0.528770830 0.257722532 0.582985149
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       0.509768805 0.393536228 0.021905531 0.587207418 0.322190381 0.656370016
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       0.253512652 0.277815194 0.265035139 0.337963219 0.082221893 0.382537671
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## 117 1.584235054 1.472357510 1.099220963 1.665903783 1.394999082 1.717304301
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## 120 1.510363587 1.434132276 1.049909939 1.594508389 1.325591574 1.630016589
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       0.359419786 0.055976053 0.248712872 0.175152738 0.237927806
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##
       0.407751149 0.216832189 0.136570240 0.207146106 0.128294444 0.205559026
       0.356890968 0.182053599 0.098551674 0.156522200 0.172465586 0.182696161
##
       0.444454644 0.336508646 0.151358879 0.281264036 0.222333721 0.336346139
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##
       0.304010879 0.138562855 0.094321712 0.099178010 0.218841570 0.154700772
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##
       0.330508956 0.196987495 0.057730331 0.141732456 0.209613961 0.207906950
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       0.595309437 0.345066997 0.330612503 0.387672510 0.073469430 0.304187181
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##
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##
   86
       0.124625786 0.289485955 0.193748294 0.163728576 0.447292597 0.338577031
##
       0.355895288 0.149673325 0.126306863 0.148658193 0.166476580 0.145854714
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       0.485610569 0.248978375 0.226317844 0.278456914 0.038701428 0.217453622
##
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       0.298871957 \ \ 0.065127560 \ \ 0.164058287 \ \ 0.095795613 \ \ 0.237839927 \ \ 0.088310541 
       0.542667858 0.772172535 0.837707521 0.730252588 1.036957117 0.822972342
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  100 0.794505628 1.050588945 1.089344704 0.995209828 1.307658353 1.103162388
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## 105 1.081588669 1.353540823 1.370306118 1.287894662 1.602207593 1.407363543
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## 120 0.924315379 1.146486332 1.219711453 1.111442277 1.415306034 1.195120782
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      0.117995792 0.180893140 0.136686322 0.155087534
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      0.308452328 0.090902230 0.108216021 0.058398478 0.202117130
      0.627881963 0.471715780 0.483178235 0.432597202 0.510919552 0.380895160
##
      0.254531318 0.092891764 0.082453583 0.040856014 0.144395420 0.058892590
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      0.144667865 0.146550374 0.103097601 0.119773253 0.035378173 0.168052912
      0.250771417\ 0.200669059\ 0.195192610\ 0.242614894\ 0.262325339\ 0.291452484
##
  82
      0.338053100 0.087753602 0.130708751 0.131551990 0.267382718 0.138946203
      0.304110119\ 0.076671283\ 0.110792063\ 0.128034164\ 0.244098474\ 0.152647901
## 84
      0.122191674 0.144007823 0.098974249 0.131911849 0.052704037 0.186982419
##
  85
      0.422825396 0.239641546 0.253082779 0.202073006 0.305519814 0.148861781
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  87
      0.448761789 0.321428675 0.322619897 0.274944777 0.332568840 0.233464959
##
  88
      0.232955689\ 0.091017182\ 0.089863954\ 0.133899193\ 0.194200333\ 0.181672364
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      0.372697378 0.122703723 0.158521052 0.118947692 0.272219621 0.073560267
## 91
      1.104927379 0.915014377 0.937386080 0.886612977 0.987049270 0.829365622
## 92 1.699509831 1.536635834 1.554207409 1.503143845 1.584188260 1.447929621
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## 93 1.384619503 1.198226789 1.220431203 1.169605011 1.267017953 1.112471182
      1.309929358 1.130976156 1.151363674 1.100362137 1.192730691 1.043868559
      1.462374074 1.301934526 1.318611866 1.267578459 1.347105539 1.212784460
      1.378009962 1.211478673 1.229289462 1.178218117 1.261960986 1.122855503
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       1.441428780 1.257640451 1.279358350 1.228469525 1.324002255 1.171507799
      1.477280401 1.299708574 1.320108353 1.269101057 1.360310654 1.212629303
## 99 1.389627195 1.222377626 1.240367339 1.189293959 1.273517264 1.133848304
## 100 1.349753488 1.182528177 1.200428433 1.149355728 1.233600944 1.093946640
## 101 1.446556235 1.271609972 1.291380839 1.240339219 1.329778530 1.184115563
## 102 1.510367467 1.325160881 1.347305440 1.296462914 1.392891707 1.239367109
## 103 1.692598948 1.527201978 1.545297559 1.494224475 1.576976099 1.438762549
## 104 1.369589170 1.204522876 1.222000513 1.170935552 1.253684527 1.115732095
## 105 1.621343402 1.475272069 1.489237721 1.438453338 1.508241941 1.385154490
## 106 1.441416814 1.269739215 1.288788017 1.237721642 1.324925825 1.181803345
## 107 1.720239809 1.556230876 1.574069445 1.523000137 1.604800460 1.467660686
## 108 1.408558789 1.231031032 1.251300055 1.200286694 1.291542143 1.143856326
## 109 1.437400655 1.269411110 1.287654310 1.236579638 1.321265679 1.181022274
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## 115 1.392680443 1.236347492 1.252016079 1.201044906 1.277828054 1.146773397
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## 119 1.497154071 1.304624627 1.328403136 1.277814959 1.379330341 1.220229488
## 120 1.486560247 1.295029186 1.318564847 1.267933682 1.368769824 1.210412906
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## 80 0.404425582
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## 81 0.491403641 0.111328753
       0.672345786 0.277634048 0.247850290
       0.494434467 0.169461915 0.233646911 0.206702681
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       0.528394474 \ 0.135650872 \ 0.041479731 \ 0.210727441 \ 0.226490614 \ 0.198799600
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       0.179875719 0.240426594 0.315306825 0.517330326 0.366613161 0.385754415
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       0.481355341 0.866435169 0.964275836 1.110011913 0.909262410 0.946987820
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       0.682090359 1.078036834 1.171990291 1.327656722 1.128486285 1.165615213
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       0.751844489 1.153610146 1.243219968 1.410102044 1.214228961 1.250120609
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## 118 0.871031560 1.273223823 1.362304588 1.529881335 1.333741626 1.369763033
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## 114 1.123252504 0.821867015 0.771412615 1.019825528 1.149544982 0.950592448
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## 100 0.289698903 0.354147746 0.129033708 0.086981318 0.124333863 0.029026904
## 101 0.362375392 0.274488329 0.104674116 0.141551940 0.101252420 0.085455078
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## 103 0.623101446 0.021522604 0.355154660 0.402055714 0.231105018 0.316042104
## 104 0.314407982 0.332212645 0.141317271 0.110370775 0.099984658 0.012080216
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## 111 0.188657847 0.461607604 0.168259990 0.081678022 0.230333545 0.136578604
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## 106 0.259057923 0.081276133 0.262651918
## 107 0.030463048 0.352132028 0.162404712 0.288922221
## 108 0.304119710 0.088080916 0.316344580 0.053699046 0.334427964
## 109 0.257793690 0.069213031 0.247018851 0.025072156 0.286981680 0.072828456
## 110 0.296647216 0.115800012 0.323111154 0.065754391 0.327107176 0.028275642
## 111 0.451988819 0.130639027 0.418171518 0.196338211 0.481033494 0.167147824
## 112 0.217919858 0.203228871 0.294226105 0.123512457 0.247300029 0.132055981
## 113 0.261142468 0.094244737 0.275082696 0.019007887 0.291348958 0.043881336
## 114 0.473006593 0.150422916 0.420745379 0.226927644 0.500900532 0.207807500
## 115 0.302898649 0.061306903 0.244201576 0.108199906 0.329033837 0.138124209
## 116 0.419591035 0.097826757 0.386080119 0.165207972 0.448534600 0.140095223
## 117 0.164697038 0.172665467 0.128958106 0.133813558 0.189465909 0.187471071
## 118 0.196464337 0.127200473 0.190135254 0.073511655 0.225028690 0.126829246
## 119 0.298646074 0.223741738 0.373583698 0.158962995 0.327419916 0.136557612
## 120 0.299558491 0.211621168 0.369196705 0.148388566 0.328714792 0.124188809
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## 111 0.194222476 0.190314938
## 112 0.143938261 0.109466666 0.298970021
## 113 0.044076565 0.049165760 0.200499091 0.108987910
## 114 0.219222037 0.233501409 0.055025320 0.339285761 0.234826976
## 115 0.084886770 0.162892478 0.175041702 0.228314823 0.126453448 0.177987759
## 116 0.161951735 0.165037656 0.032813006 0.272091787 0.170571654 0.069001642
## 117 0.119614666 0.194513796 0.303188471 0.182668636 0.146187393 0.315882417
## 118 0.063557899 0.133255721 0.256248304 0.137016442 0.084947502 0.276888880
## 119 0.183830331 0.108318334 0.285348212 0.082443169 0.140090886 0.333986169
## 120 0.173371989 0.096001677 0.272725476 0.081850447 0.129427586 0.321244233
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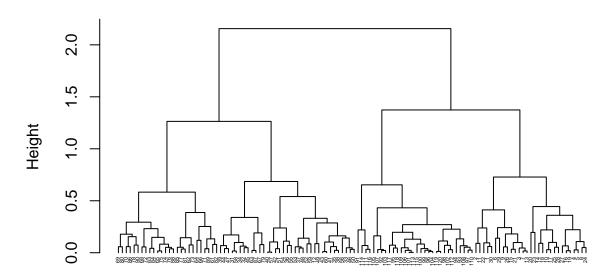
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## 118 0.115479147 0.223638058 0.061284836
## 119 0.265952730 0.265054135 0.255323495 0.201228099
## 120 0.254779679 0.252304098 0.249072211 0.193654761 0.012770276

cc <- hclust(dc, method = "complete")
plot(cc,cex = 0.3, hang = -1)</pre>
```

Cluster Dendrogram



dc hclust (*, "complete")

Interpretation

According to the numbers you could argue for 3 and 4 clusters. However, 4 clusters seems to be more appropriate considering the domain of the data set.

- 1. Those who learn little and have a bad grade
- 2. Those who learn an average amount and have an average grade
- 3. Those who learn a lot and have good performance
- 4. Those who learn a lot and still have bad performance (maybe not an appropriate learning technique)