Perfect set games and colorings on generalized Baire spaces

Dorottya Sziráki

The notion of perfectness can be generalized for the κ -Baire space in a number of different ways (when $\kappa = \kappa^{<\kappa} > \omega$). We discuss the connections between these different generalizations and between the games underlying some of their definitions, as well as the corresponding generalizations of scatteredness, density in itself and the Cantor-Bendixson hierarchy. For example, we show that Väänänen's generalized Cantor-Bendixson theorem is equivalent to the κ -perfect set property, and is therefore equiconsistent with the existence of an inaccessible cardinal above κ . If time permits, we will mention analogues of the above results for variants of these perfect set games associated to open colorings. As an application, we present a Cantor-Bendixson theorem for independent subsets of κ with respect to $\Pi_2^0(\kappa)$ colorings.