

## Problem Set 1

$\frac{1.1}{n}$	X	$P(X)$
2	(1, 1)	$\frac{1}{9}$
3	(1, 2) (2, 1)	$\frac{2}{9}$
4	(1, 3) (3, 1) (2, 2)	$\frac{1}{3}$
5	(2, 3) (3, 2)	$\frac{2}{9}$
6	(3, 3)	$\frac{1}{9}$

$$b) L(C^2) = \frac{1}{9} \cdot 1 + \frac{2}{9} \cdot 1 + \frac{3}{9} \cdot 2 + \frac{2}{9} \cdot 2 + \frac{1}{9} \cdot 3$$

$$= \frac{1}{9} + \frac{2}{9} + \frac{6}{9} + \frac{4}{9} + \frac{3}{9}$$

$$= \frac{16}{9} = 1 \frac{7}{9}$$

...

c) Because  $C^2$  is not prefix-free.

d)  $C^3, C^4$

code word  
✓ in the

e) Assume being at the start of a sequence. Then find the longer code which is a prefix from this sequence. Then we decode this part and are at the start of the next code word.

Proof by contradiction.

- Assume the "true" code word was longer

↳ Since we chose longer

thus not prefix-free  $\underline{\underline{4}}$

- Store different part,  $\hookrightarrow$  by assumption
- different codebook is unique

11 It is  $n$ -suffix-free, could just start from back?

$\Gamma$   $\underbrace{010010}_{\text{1}}, \underbrace{01}_{\text{1}} \underbrace{00}_{\text{1}} \underbrace{01}_{\text{1}}$