GEOMETRIC ALGEBRA FOR PHYSICISTS

Geometric algebra is a powerful mathematical language with applications across a range of subjects in physics and engineering. Written by two of the leading researchers in the field, this book is a complete guide to the current state of the subject.

Early chapters provide a self-contained development of geometric algebra and form the basis of an undergraduate lecture course. Topics covered include new techniques for handling rotations in arbitrary dimensions, and the links between rotations, bivectors and the structure of the Lie groups. Following chapters extend the concept of a complex analytic function theory to arbitrary dimensions. This has applications in quantum theory and electromagnetism. All four Maxwell equations are united into one single equation, and new techniques are discussed for its solution. Later chapters cover some advanced topics in physics, including non-Euclidean geometry, quantum entanglement and gauge theories. The final chapters describe the construction of a gauge theory of gravitation in Minkowski spacetime. Using the tools of geometric algebra, advanced applications such as black holes and cosmic strings are explored.

This book will be of interest to researchers working in the fields of geometry, relativity and quantum theory. It can also be used as a textbook for advanced undergraduate and graduate courses on the physical applications of geometric algebra.

CHRIS DORAN obtained his PhD from the University of Cambridge, having gained a distinction in Part III of his undergraduate degree. He was elected a Junior Research Fellow of Churchill College, Cambridge in 1993, was made a Lloyd's of London Fellow in 1996 and was the Schlumberger Interdisciplinary Research Fellow of Darwin College, Cambridge between 1997 and 2000. He is currently a Fellow of Sidney Sussex College, Cambridge and holds an EPSRC Advanced Fellowship. Dr Doran has published widely on aspects of mathematical physics and is currently researching applications of geometric algebra in engineering and computer science.

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