STIR and Tensorflow

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The big picture

► STIR

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- ▶ iterative reconstruction algorithms
- ▶ find the optimum of a cost function

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- ▶ STIR
- iterative reconstruction algorithms
- find the optimum of a cost function

$$P(\text{global LOR response}|\text{image}) = \prod_{\text{all LORs}} P(\text{LOR response}|\text{image})$$

$$P(LOR response|image) = \int_{LOR} image density$$

► Image (estimate) \(\sim \) LOR response: forward projection

Ray tracing

- ▶ in the following: how to compute / approximate this integral?
- represent image as a discretized array of voxels

$$\int_{\mathsf{LOR}}\mathsf{image}\;\mathsf{density} \leadsto \sum_{\mathsf{traversed}\;\mathsf{voxels}}\mathsf{LOI} \cdot \mathsf{voxel}\;\mathsf{brightness}$$

► LOI = <u>length of intersection</u> of the LOR through a specific voxel

(Standard) STIR spends > 90% of the reconstruction time for forward projection

is there a way to make it faster?

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The big picture

Tensorflow - what is it?

How to do ray tracing on a CPU?

How to do ray tracing on a GPU?

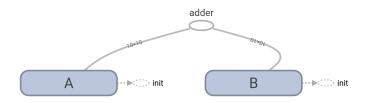
Combining STIR and Tensorflow

Results

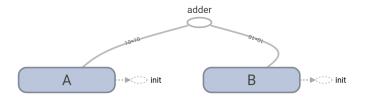
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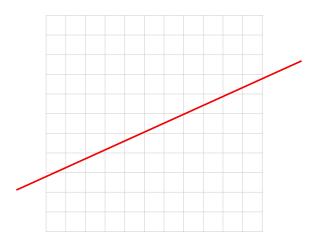


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 - heavily used in the machine-learning community
- Much more than that:
 - a software package for numerical calculations using data-flow graphs



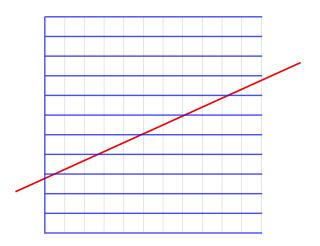
- Design the graph now, save it to a file, run it later...
- ▶ Can run it (almost) everywhere: CPU, GPU, a cluster, ...

Siddon's algorithm (2D)



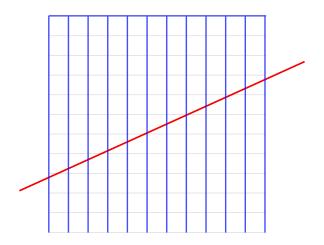
► a (very) sequential algorithm

Siddon's algorithm (2D)



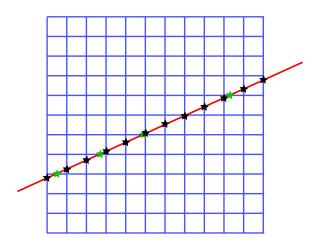
get intersections of LOI with all horizontal planes

Siddon's algorithm (2D)



get intersections of LOI with all vertical planes

Siddon's algorithm (2D)



combine them and get the individual LOIs

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 - especially problematic when trying to trace multiple LORs "in parallel"

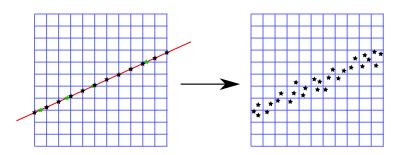
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- ▶ for Tensorflow: need an algorithm that ...
 - uses the same algorithmic steps on all voxels of the LOR
 - uses the same algorithmic steps on all LORs

Alternatives to Siddon

- naïve approach: for every LOR, compute the LOI through every voxel, then add them all up
 - works fine with Tensorflow, but scales as $\mathcal{O}(N^3)$
 - ► CPU & Siddon beat it again for real-world array sizes

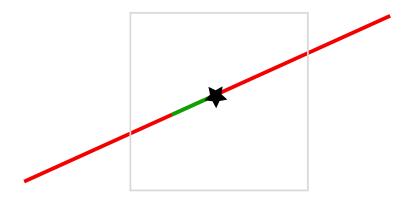
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 - works fine with Tensorflow, but scales as $\mathcal{O}(N^3)$
 - ► CPU & Siddon beat it again for real-world array sizes
- ► alternative approach: think of (intersection) points *without* the notion of an LOR

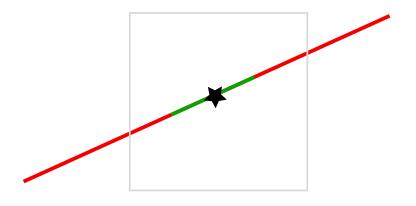


- still not much easier than the full problem!
- a cube is very discontinuous, hard to do it analytically without branches

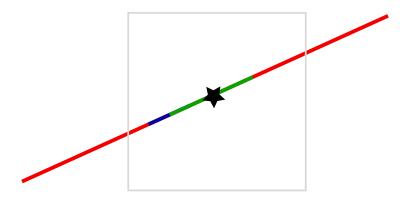
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- what if content with an approximate solution?



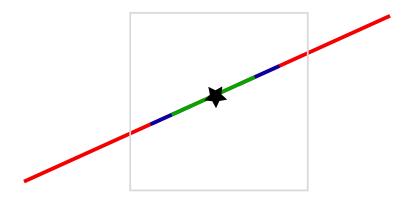
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Ray marching: an iterative algorithm

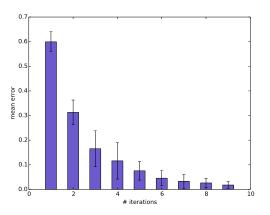
- Use signed distance function of a cube to cut down the number of iterations that are needed
 - a heuristic that produces an underestimation of the distance to the voxel boundary

need to assess the residual error that remains

Ray marching: an iterative algorithm

Accuracy

assume: have "enough" points along the LOR



ightharpoonup with 6 iterations, are already at $\sim 5\%$ level!

Bringing together STIR and Tensorflow

The infrastructure

- ▶ Build the Tensorflow graph in a Python script
 - much easier and faster to prototype
 - Python API much better documented and more stable

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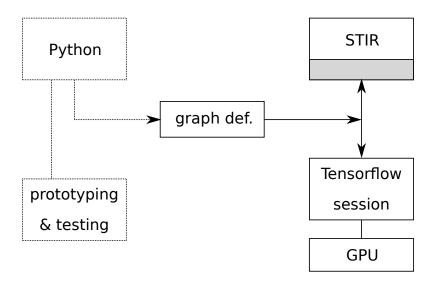
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Bringing together STIR and Tensorflow

The infrastructure

- Build the Tensorflow graph in a Python script
 - much easier and faster to prototype
 - Python API much better documented and more stable
- ► Save the complete graph into a ProtoBuf file
- ▶ Load the file using the C++ API and make use of it in STIR
 - link STIR against the Tensorflow (shared) library

The workflow



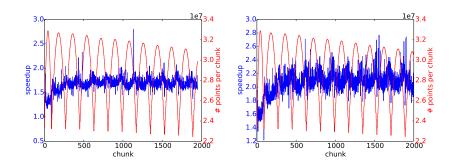
Caching in STIR

- scanners have (many) symmetries
- ProjMatrixByBin maintains a cache
 - already computed matrix elements are stored
 - new matrix elements related by symmetries to known ones "come for free"!

Caching in STIR

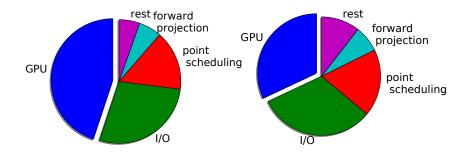
- scanners have (many) symmetries
- ProjMatrixByBin maintains a cache
 - already computed matrix elements are stored
 - new matrix elements related by symmetries to known ones "come for free"!
- but: caching most efficient if every new matrix element request is checked against cache before computing
- batching the matrix element requests makes caching (very) inefficient!

Speedup without caching



left: 6 iterations, right: 2 iterations

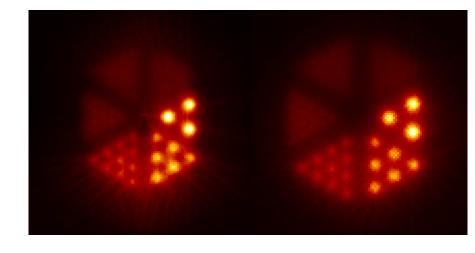
▶ average speedup is similar



left: 6 iterations, right: 2 iterations

- ► I/O: converting from ProjMatrixElemsForOneBin to Tensor and back
- point scheduling: choose points to sample the TOR / LOR

Images



left: 2 iterations, 20LORs per matrix element, right: original STIR

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- whole toolchain is in place
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Not too bad, but still some limitations:

how to improve utilization of GPU (conversion between Tensors and STIR objects)?

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- how to improve utilization of GPU (conversion between Tensors and STIR objects)?
- is there a better way to estimate the matrix elements?

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Not too bad, but still some limitations:

- how to improve utilization of GPU (conversion between Tensors and STIR objects)?
- is there a better way to estimate the matrix elements?
- so far, use only a single thread (no openMP support)
 - Tensorflow sessions tend to allocate all of the available GPU memory to avoid fragmentation...

Where to find the code?

- ► STIR-TF: https://github.com/philippwindischhofer/ STIR/tree/stir-tf
 - in particular: https://github.com/philippwindischhofer/STIR/blob/ stir-tf/documentation/statistics/doc/main.pdf
- ray tracing scripts: https://gitlab.phys.ethz.ch/luster/tf-raytracing (ask Werner for access)

Any comments and contributions are welcome!



Backup

How to do ray tracing on a CPU?

Siddon's algorithm (2D)

parametrize the LOR

$$\mathbf{x} = (\mathbf{x}_{\mathsf{end}} - \mathbf{x}_{\mathsf{start}}) \cdot \alpha + \mathbf{x}_{\mathsf{start}}$$

$$\alpha \in [0,1]$$

- \blacktriangleright get intersections with horizontal and vertical planes in terms of the line parameter α
- merge and sort them
- differences between neighbouring α values in the merged list describe the LOIs!

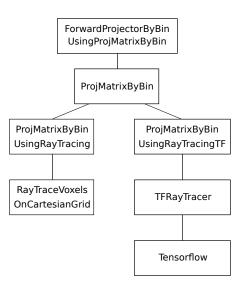
Signed Distance Functions

for a cube with side lenghts (d_x, d_y, d_z) , origin in the center:

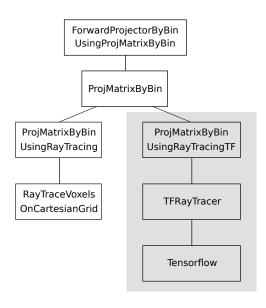
$$\mathsf{SDF}(x,y,z) = -\max\left(\left|x - \frac{d_x}{2}\right| - \frac{d_x}{2}, \left|y - \frac{d_y}{2}\right| - \frac{d_y}{2}, \left|z - \frac{d_z}{2}\right| - \frac{d_z}{2}\right)$$

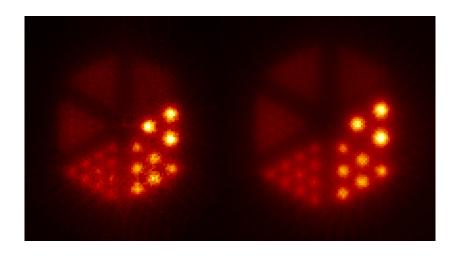
- SDF is small (by design) close to the voxel boundary
 - but must march in both directions
 - time until convergence depends on the location of the initial point

Tensorflow in STIR

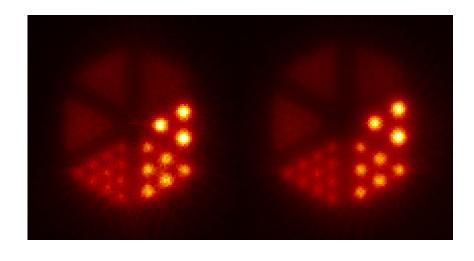


Tensorflow in STIR





left: 3 iterations, 2LORs per matrix element, right: original STIR



left: 30 iterations, 2LORs per matrix element, right: original STIR