

# MiniGraph: Querying Big Graphs with a Single Machine

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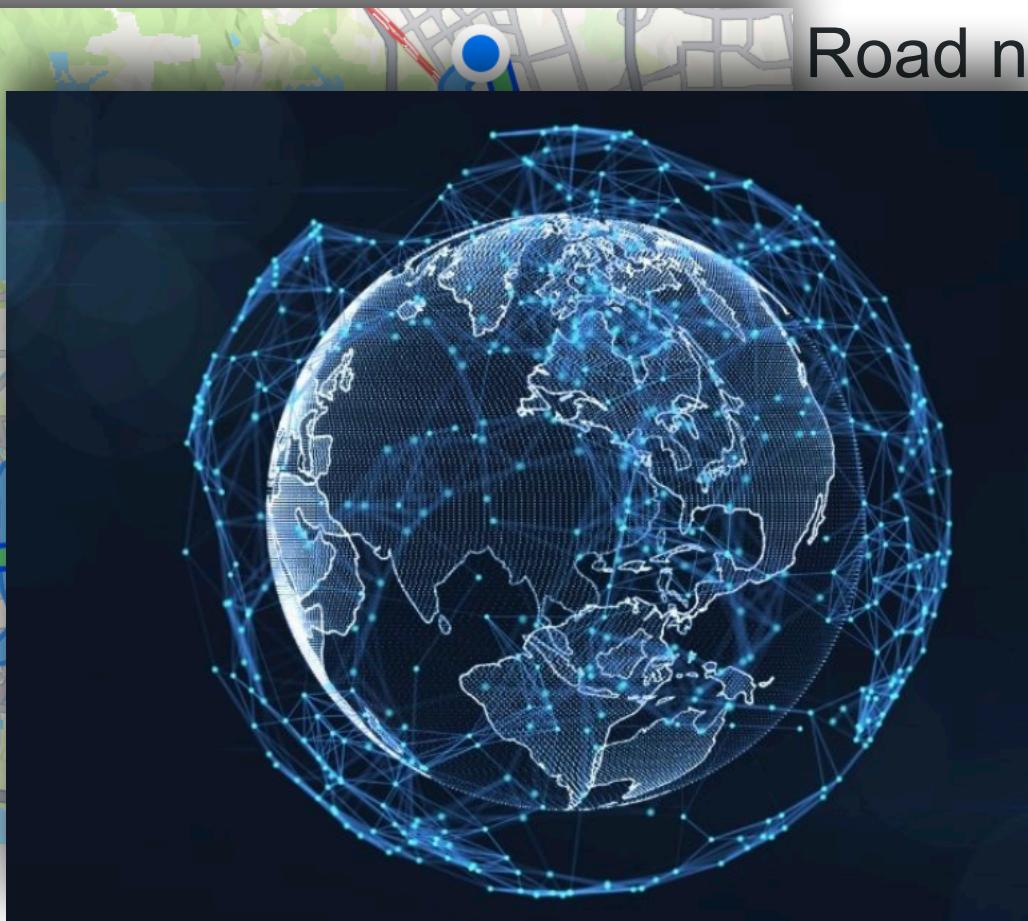
# *Graphs: Everything is Naturally Connected*

Road networks



We use *Graphs* everyday and everywhere.

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Road networks

Network topology

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Social networks

## **Michelle Royle**

CEO Mobile Outfitters Australia

Talks about #tech, #innovation, #entrepreneur, #sustainability, and #i

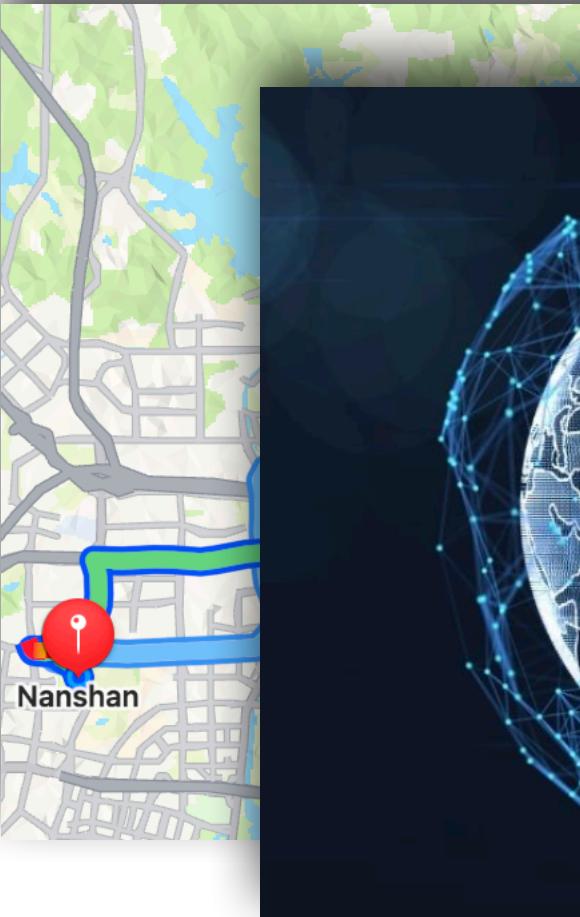
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创始人: 羅蘭·哈賽·梅西

创立于: 1858 年, 纽约纽约

总部: 纽约纽约

KG

*We use Graphs everyday and everywhere.*

# *Applications on Graph Data*

Map Navigation

Fraud Detection

Recommendation

Protein Interaction

*SSSP*

*PageRank*

*SubIso*

*WCC*

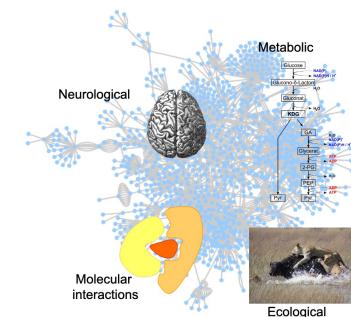
*Simulation*



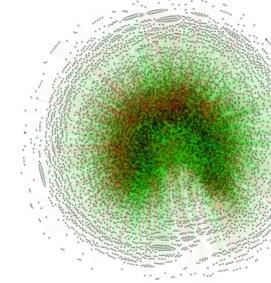
Road Network



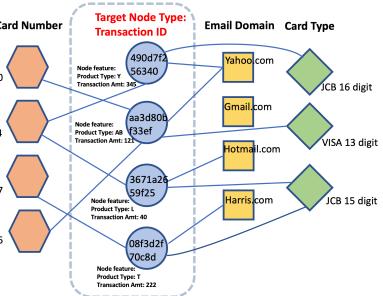
Social Media



Biological Network



Web Graph



Transaction Network

*What is graph computing and why is it important?*

# *Existing Solutions*

## *Shared memory*

- ✓ Single-node and in-memory
  - ✓ Ligra[PPoPP'13], Galois[SOSP'13]
- Limited capacity to big graphs

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## *Distributed*

- ✓ Multi-node and in-memory
  - ✓ GraphScope<sup>[VLDB'21, SIGMOD'17]</sup>, Pregel<sup>[SIGMOD'10]</sup>, Gluon<sup>[PLDI'18]</sup>
- Irregular structure, scalability problem  
Beyond the reach of small companies

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Beyond the reach of small companies

To compute connected components of a graph with billions of vertices and trillions of edges, Yahoo! employs a 1000-node cluster with 12000 processors and 128 TB of aggregated memory.

# *Existing Solutions*

## *Shared memory*

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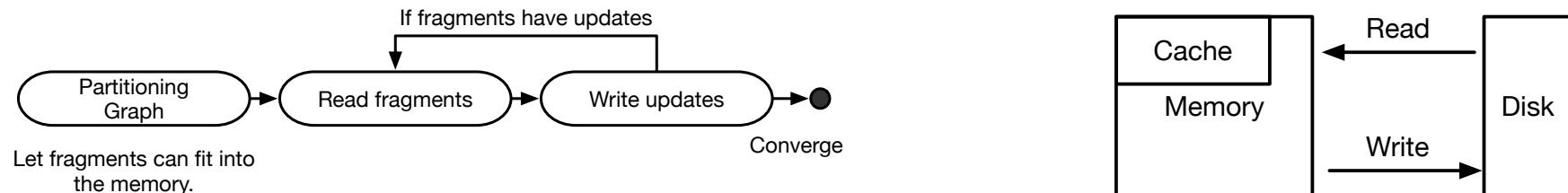
## *Out-of-core* The scope of this work

- ✓ Single-node and disk-based
  - ✓ GraphChi[OSDI'12], GridGraph[ATC'15],  
Mosaic[EuroSys'17]
- It is feasible due to promise performance of SSD, NVMe et al.  
I/O will become the bottleneck

*How to improve the performance of out-of-core system?*

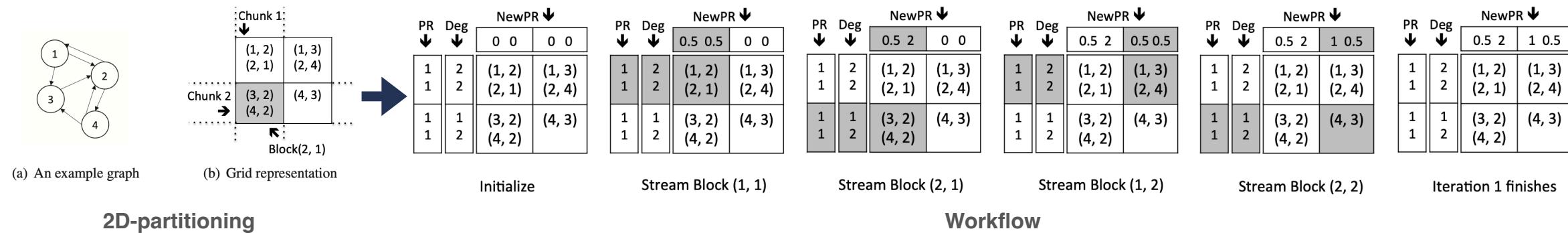
# *A review of out-of-core system*

# *Basic idea*



# *The-state-of-art: GridGraph*

- ✓ Vertex-centric model and BSP model.
  - ✓ ***Read*** from source vertices, ***Write*** to destination vertices.
  - ✓ 2-level hierarchy partitioning and skip block with no active edges.



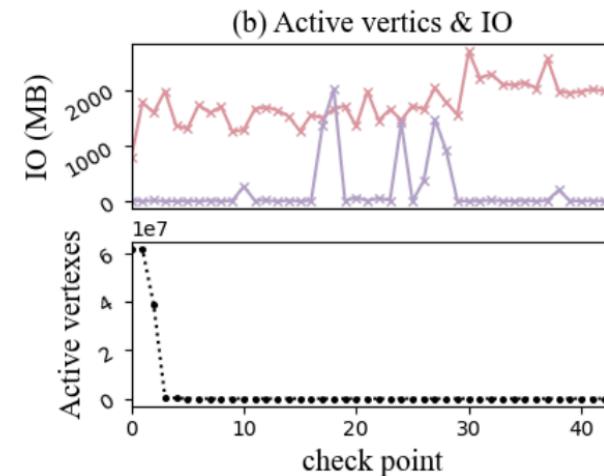
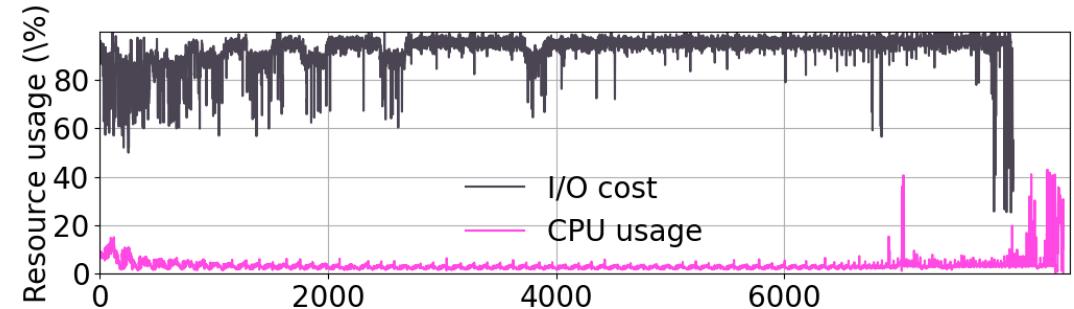
# *Why out-of-core graph system?*

# *A review of out-of-core system*

## *Findings after Profiling GridGraph*

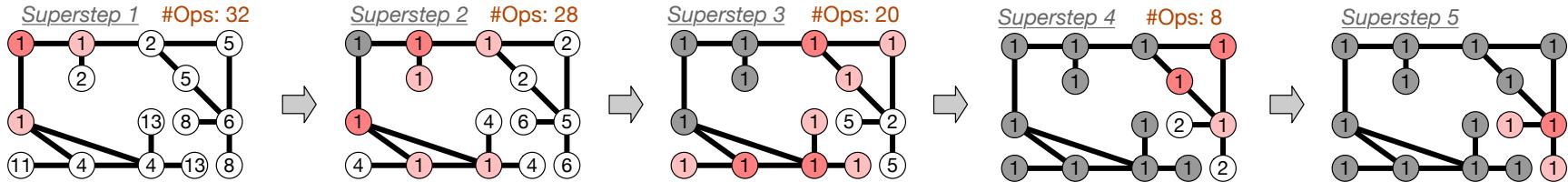
- ✓ **Setting:**
- ✓ WCC task.
- ✓ A machine powered with 20 cores and SSD.
- ✓ A graph with over 50 Millions edges (50% data out of memory).

- ✓ **Findings:**
- ✓ The rate at which a task is limited by the speed of the I/O.
- ✓ Unnecessary I/O caused by less and scattered active vertices.

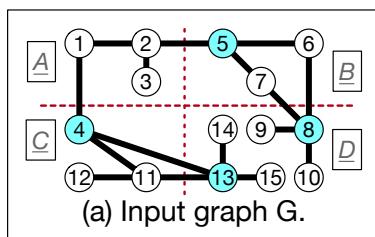


# Motivation

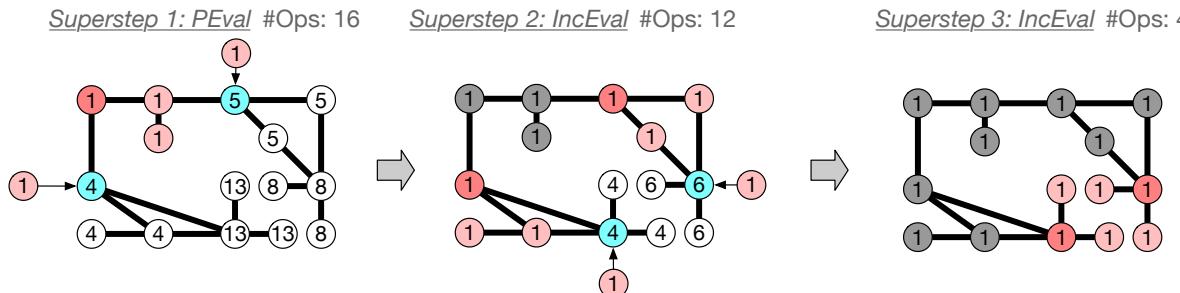
## Graph-centric (GC) vs Vertex-centric (VC)



(b) VC execution in 5 supersteps.



(a) Input graph  $G$ .



(c) GC execution in 3 supersteps.

- ✓ **VC** takes many computations steps to propagate a piece of information from a source to a destination, even if both appear in the same partition.
- ✓ **GC** allows information to flow freely inside a partition.

# *Challenges & Opportunities*

## *Parallelism*

- ✓ GC exploits data-partitioned parallelism only. With limited memory capacity, it would result in either **underutilization of the CPU** or **graph fragmentation**.

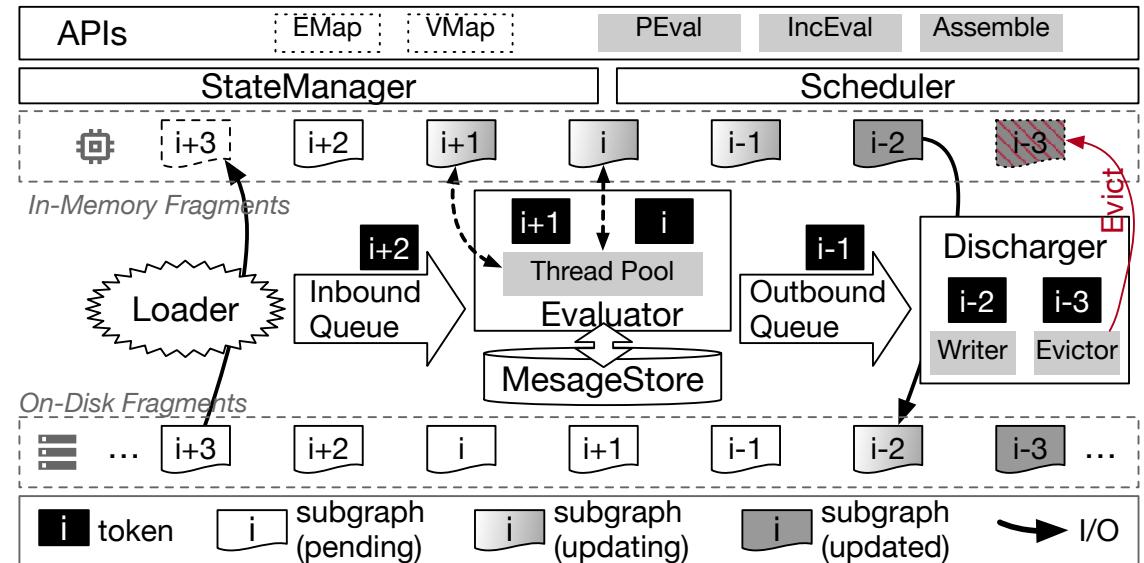
## *Out-of-core computation*

- ✓ A out-of-core system has to resort to secondary storage. Managing the in-memory and the on-disk parts of an input graph is crucial to performance.

# MiniGraph Architecture

## The characters of MiniGraph

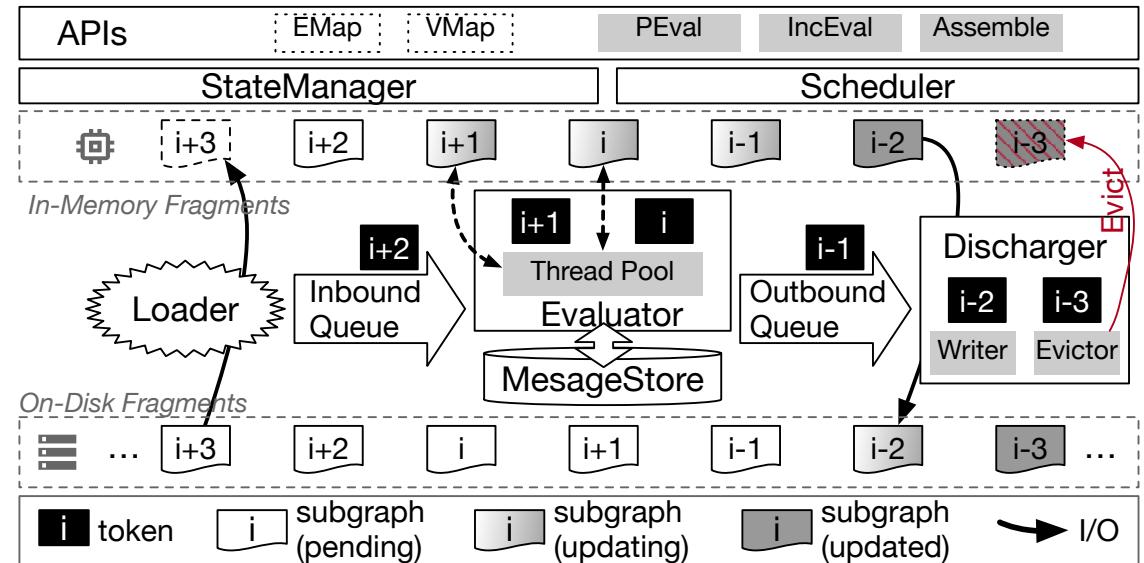
- ✓ A **pipelined architecture** to overlap I/O and CPU operations.



# MiniGraph Architecture

## The characters of MiniGraph

- ✓ A **pipelined architecture** to overlap I/O and CPU operations.
  - **Loader** continuous reads a memory absent subgraphs from disk.
  - **Evaluator** is responsible for execution of an application.
  - **Discharger** writes the data back to the disk.

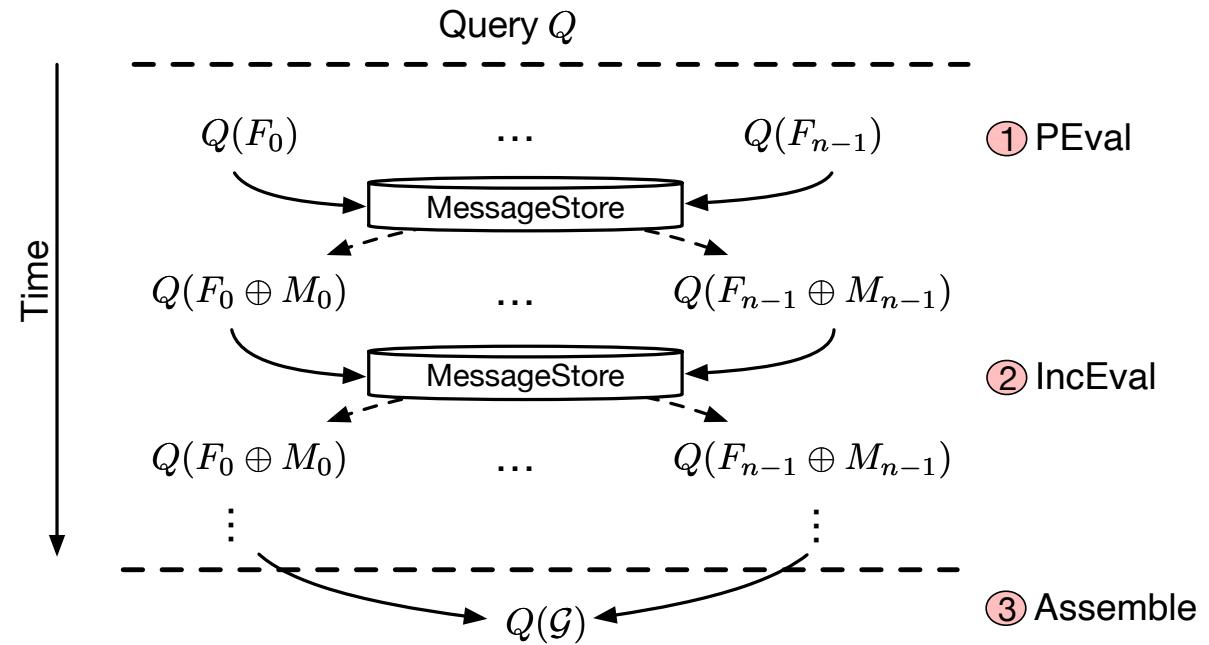


# MiniGraph Architecture

## The characters of MiniGraph

- ✓ A pipelined architecture to overlap I/O and CPU operations.
- ✓ A hybrid parallel model to support both the *data-partitioned parallelism of GC* and the *operation-level parallelism of VC*.

## PIE model



# MiniGraph Architecture

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### PEval + EMap/VMap (VC)

HashMin algorithm.

- Init: each vertex is assigned a distinct numeric label
- Run: each vertex collects the labels from its neighbors and update its own label with minimum
- Border vertices: with an edge to another fragment.

Push updates to border vertices.

### IncEval + EMap/VMap (VC)

Incremental HashMin algorithm.

- Run: each vertex collects the labels from its neighbors and update its own label
- Messages  $M_i$ : changed for border vertices of  $F_i$ .

### Assemble

The union of all partial results.

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- ✓ Two-level parallelism: inter-subgraph parallelism via high-level GC abstraction, and intra-subgraph parallelism for low-level VC operations.

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- ✓ A learned scheduler: to further improve hardware utilization.

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# Learned Scheduling

## The scheduling problem

- ✓ When to load and process a subgraph?
- ✓ How to allocate resources to maximize two-level parallelism?

## Goal

$$\arg \min_{\mathcal{S}} \max_{i \in [0, n]} \{t_i + \mathcal{C}_{\mathcal{A}}(F_i, p_i)\}$$

- ✓ It is in NPC.

## A learned model

$$\mathcal{C}_{\mathcal{A}_{PIE}}(F_i) = \sum_{u \in F_i} h_{\mathcal{A}_{PIE}}(\bar{x}_i(u))$$

- ✓ Where  $\bar{x}_i(u)$  takes into account the **average in/out-degree** of all vertices and the **number of  $u$ 's mirror** across all fragments.
- ✓ Collecting training data from log.

## Scheduling strategy

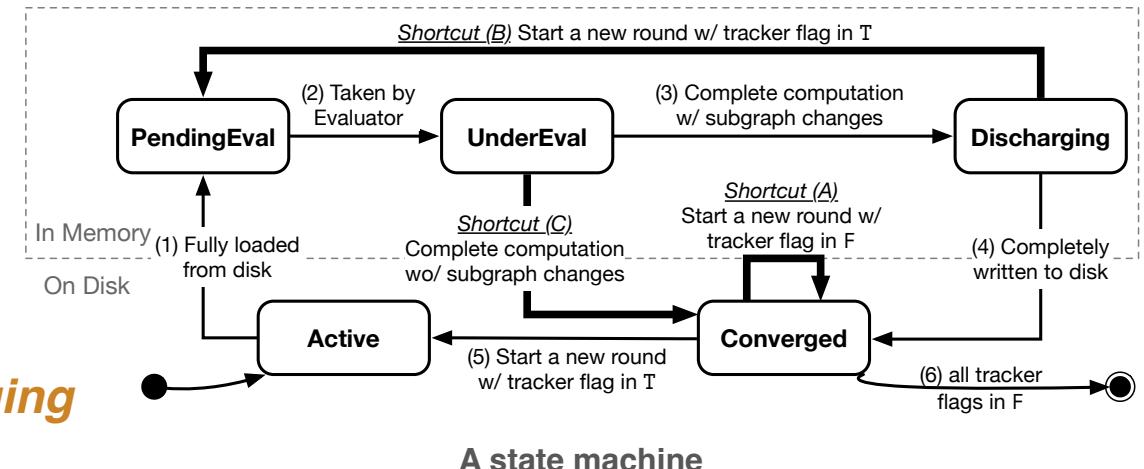
- ✓ **Tentative resource allocation:** allocates resources based on the subgraph size and the memory size.
- ✓ **Greedy subgraph processing:** Scheduler keeps track of a list of pending subgraphs, sorted by  $\mathcal{C}_{\mathcal{A}}(F_i, \hat{p}_i)$ .

# Other Optimizations

## StateManager: a light weight state machine for optimization

### Subgraphs states management

- ✓ Targets: Manage subgraphs, determine if the program is finished, and optimize I/O.
- ✓ At any point of time,  $F_i$  is in one of the five states: **Active**, **PendingEval**, **UnderEval**, **Converged**, **Discharging**.
- ✓ In-memory: **PendingEval**, **UnderEval**, **Discharging**
- ✓ On-disk: **Active**, **Converged**.



### I/O optimization

- ✓ ShortCut A: If  $F_i$  requires no further processing, we can skip handling subgraph  $F_i$  in the round. (**Avoid both Read&Write**)

- ✓ ShortCut B:  $F_i$  is set to **PendingEval** directly, such that it starts the new round without going through the disk. (**Avoid Read**)
- ✓ ShortCut C:  $\text{IncEval}(F_i)$  completes with no changes,  $F_i$  skips **Discharging** and is set to **Converged** directly. (**Avoid Write**)

# *Experimental setting*

## Datasets

Name	Type	V	E	MaxDegree	Raw Data
roadNetCA [1]	road network	2M	2.7M	23	83MB
skitter [42]	network topology	1.6M	11M	35455	142MB
twitter [8, 40]	social network	41.6M	1.5B	3M	25GB
friendster [5]	social network	65.6M	1.8B	5124	30.14GB
web-sk [55]	Web	50M	1.9B	8.5M	32GB
clueWeb [55]	Web	1.7B	7.9B	6.4M	137GB

## Testbed

- ✓ Ubuntu Server 20.04 LTS
- ✓ Intel Core i9-7900X CPU @3.30GHz
- ✓ 13.75MB LLC
- ✓ 10 cores (20 hyper threads)
- ✓ 64GB of DDR4-2666 memory
- ✓ 1TB WD blue SATA SSD, whose read throughput is 560MB/s.

## Baseline

### Out-of-core

- ✓ GridGraph[ATC'15], GraphChi[OSDI'12], XStream[SIGOPS'13]

### Distributed

- ✓ GraphScope[VLDB'21], Gluon[PLDI'18]

## Applications

- ✓ WCC
- ✓ PageRank
- ✓ SSSP
- ✓ BFS
- ✓ Random Walk
- ✓ Simulation

# Result

## Experimental results overview

Data	Memory Budget	#Partitions (PR/Others)	SSSP			WCC			PR					
			MiniGraph	GraphChi	GridGraph	XStream	MiniGraph	GraphChi	GridGraph	XStream	MiniGraph			
roadNetCA	100%	1/1	8.66	22.5 (2.6×)	10.55 (1.2×)	<b>2 (0.2×)</b>	<b>2.76</b>	17.2 (6×)	18.22 (6.6×)	2.93 (1.1×)	<b>0.25</b>	0.91 (3.5×)	0.71 (2.7×)	2.34 (2.6×)
skitter	100%	1/1	0.53	1.64 (78.5×)	<b>0.35 (0.67×)</b>	0.69 (1.3×)	<b>0.16</b>	13.43 (115.2×)	0.33 (2.1×)	0.59 (3.9×)	<b>0.27</b>	1.27 (4.7×)	0.82 (3.0×)	0.98 (3.6×)
twitter	50% (12.5GB)	4/10	<b>150.8</b>	802.8(5.3×)	195.4(1.29×)	2365(15.6×)	<b>159.5</b>	594.8(3.7×)	186(1.2×)	1983(12.4×)	<b>224.2</b>	782.1(3.5×)	371.3(1.7×)	2183(9.7×)
friendster	50% (15.07GB)	4/10	<b>201.8</b>	535(2.7×)	293.1(1.45×)	3061(15.2×)	<b>171.8</b>	1636(9.5×)	204.7(1.2×)	2037(11.8×)	<b>190.104</b>	450.7(1.9×)	485.3(1.9×)	2685(11.3×)
web-sk	50% (16GB)	4/10	<b>326.4</b>	1140(3.5×)	917.9(2.8×)	9437 (28.9×)	<b>172</b>	620.1(3.6×)	704.6(4.1×)	4056(23.5×)	<b>248.3</b>	2288(9.2×)	395(1.6×)	2903(11.7×)
clueWeb	47% (64GB)	4/10	<b>2514</b>	/	11534 (4.59×)	/	<b>2742</b>	/	11665 (4.25×)	/	<b>2022</b>	/	3803(2.1×)	/
	10% (13.7GB)	20/50	<b>5871</b>	/	/	/	<b>7486</b>	/	/	/	<b>2979</b>	/	/	/

## Findings

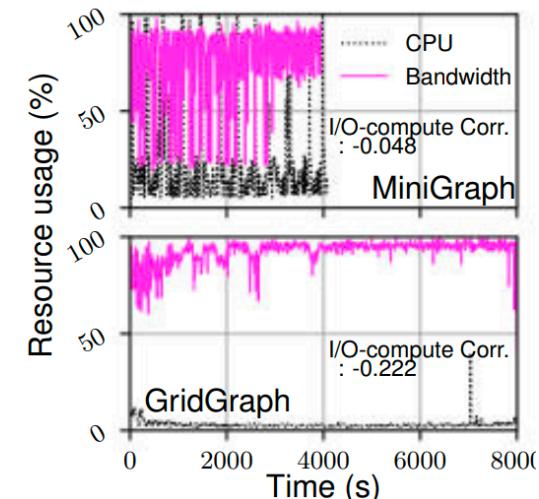
- ✓ MiniGraph consistently outperforms the prior single-machine systems under all out-of-core workloads. It is up to **4.6×**, **9.5×** and **28.9×** faster than GridGraph, GraphChi and XStream, respectively.

# Result: Runtime statistics and comparison over resource usage

## Runtime statistics for SSSP, WCC and PR

Dataset	Metric	SSSP		WCC		PR	
		MiniGraph	GridGraph	MiniGraph	GridGraph	MiniGraph	GridGraph
friendster	# Supersteps	<b>8</b>	32	<b>6</b>	21	<b>8</b>	10
	Disk Read (GB)	<b>78</b>	115.1	<b>74</b>	135	<b>107</b>	160
	Shortcut I/O (GB)	-12	N/A	-12	N/A	-10.4	N/A
	Avg. CPU Util.	<b>33.74%</b>	4.45%	<b>48.2%</b>	6.83%	<b>68.46%</b>	62.38%
	I/O-Compute Corr.	<b>0.095</b>	-0.113	<b>0.163</b>	-0.202	<b>0.185</b>	-0.156
	Cache Hits	<b>45.33%</b>	9.59%	<b>48.25%</b>	12.04%	<b>34.8%</b>	36.2%
web-sk	# Supersteps	<b>10</b>	63	<b>9</b>	120	<b>15</b>	20
	Disk Read (GB)	<b>112.5</b>	232	<b>81.9</b>	367	<b>87</b>	232
	Shortcut I/O (GB)	<b>-30.9</b>	N/A	<b>-6.1</b>	N/A	<b>-20.9</b>	N/A
	Avg. CPU Util.	<b>15.76%</b>	5.83%	<b>25.04%</b>	5.16%	<b>42%</b>	42%
	I/O-Compute Corr.	<b>0.008</b>	0.003	<b>0.013</b>	0.009	<b>0.082</b>	-0.039
	Cache Hits	<b>50.89%</b>	6.37%	<b>37.42%</b>	11.63%	<b>50.22%</b>	46.04%

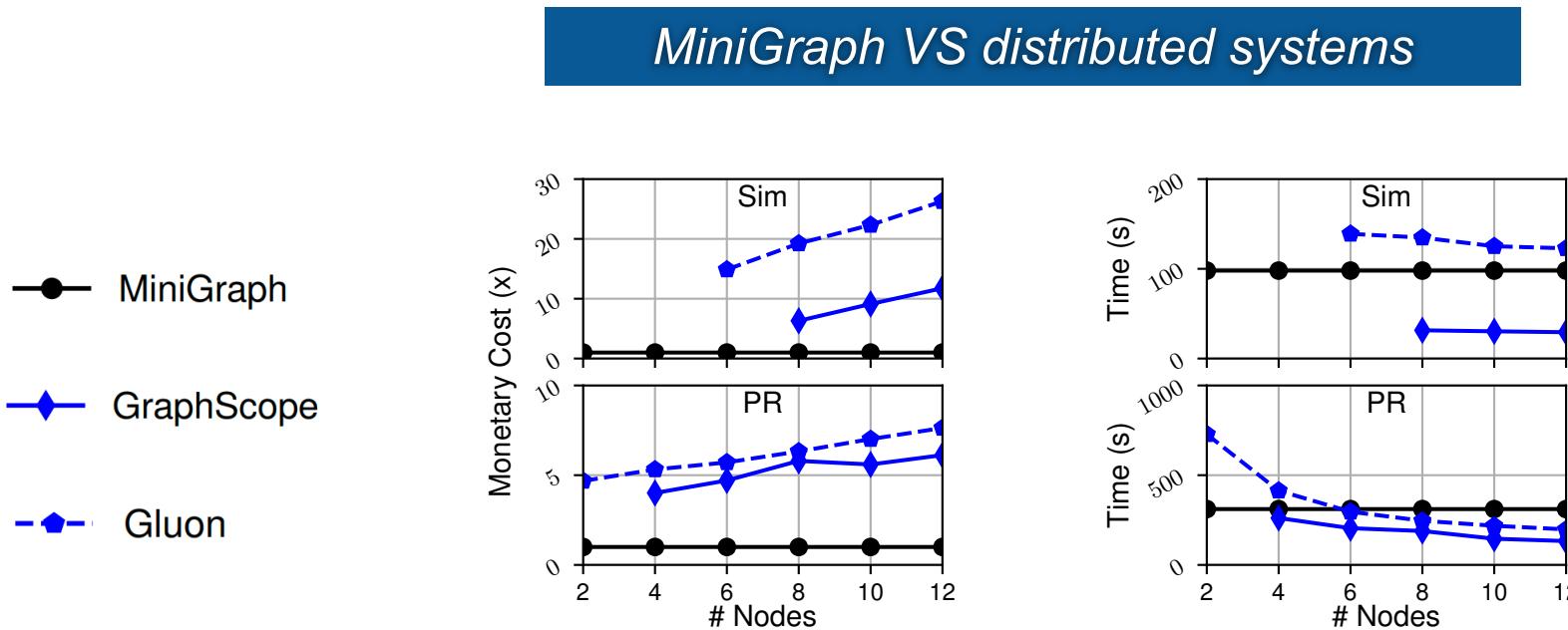
## CPU & I/O utilization: WCC over clueWeb



## Findings

- ✓ Under BSP, MiniGraph requires only a fraction of supersteps (<29%) and disk read traffic (<53.3%) of GridGraph for SSSP and WCC.
- ✓ MiniGraph improves the CPU utilization of GridGraph, the best-performing baseline, by up to 41.4%.
- ✓ MiniGraph's shortcut optimization effectively reduces I/O cost, especially

# *Result: Runtime statistics and comparison over resource usage*



## *Findings*

- ✓ MiniGraph works better than Gluon, a distributed graph analysis system, with 12 machines on a graph simulation task, and saves the monetary cost of multi-machine systems from 3.0x to 13.9x.

## *Conclusion*

MiniGraph is an out-of-core system for graph computations. It is the first single-machine system that extends graph-centric (GC) model from multiple machines to multiple cores.

It shows that GC speeds up beyond-neighborhood and reduces I/O.



<https://github.com/SICS-Fundamental-Research-Center/MiniGraph>

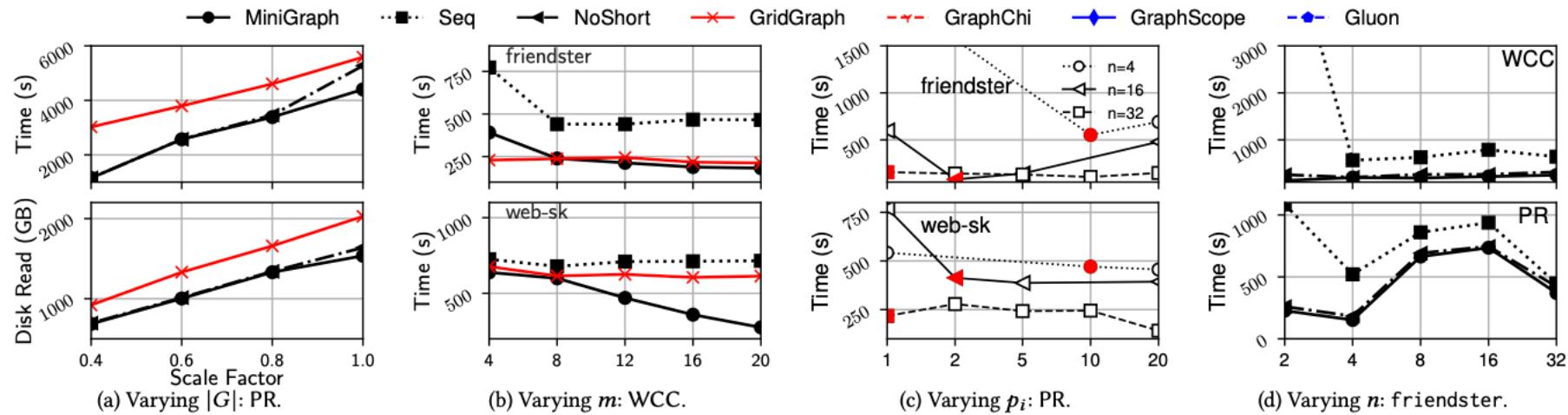
# Thanks!

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I am looking for postdoctoral position. Please contact me if you are interested.  
Email: zhuxk@buaa.edu.cn

# *Result: other results II*

## *Scalability of MiniGraph*



## *Accuracy and effectiveness of cost model formulations*

Cost model	$C_{\mathcal{A}}$	Model (a)	Model (b)
Normalized loss over $S_{\text{test}}$	0.16	0.22	0.22
Normalized loss over $S'_{\text{test}}$	0.40	0.50	0.43
Improvement web-sk (%)	39.0%	27.2%	27.3%
Improvement clueWeb (%)	30.0%	16.5%	17.1%