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ICA-16

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Problem 1. Suppose you are given the hash and probe decrement functions below:

$$\text{hash}(\text{key}) = \text{key} \% 11$$

$$\text{probe}(\text{key}) = \max(1, \text{key} // 11)$$

- a) Fill out the columns in the table below for the **Hash value** and **Probe decrement** based on the functions defined above.

Key	Hash value	Probe decrement
19		
22		
25		
33		
36		
42		

- b) Give the final configuration of a hash table below that results from inserting the keys listed above into an empty table using double hashing. The order of insertion of the keys is: 33, 25, 36, 19, 22, 42.

0	1	2	3	4	5	6	7	8	9	10

Problem 2. We have 42,000 student names to enter as keys into a hash table. If we want a load factor of .70, what should the table size be?

Problem 3. Recall the following definition of a dictionary from lecture.

- A dictionary is an ADT that holds key/value pairs and provides the following operations:
 - `put(key, value)`
 - makes an entry for a key/value pair
 - assumes key is not already in the dictionary
 - `get(key)` looks up key in the dictionary
 - returns the value associated with key (and None if not found)
 - Note: a dictionary is of fixed sized and is set to its capacity when created
 - Usage:

```
>>> d = Dictionary(7)
>>> d.put('five', 5)
>>> d.put('three', 3)
>>> d._pairs
[['five', 5], ['three', 3], None, None, None, None, None]
```

The code below implements the dictionary ADT:

```
class Dictionary:
    def __init__(self, capacity):
        # each element will be a key/value
        self._pairs = [None] * capacity

    def _hash(self, k):
        return len(k) % len(self._pairs)

    def put(self, k, v):
        self._pairs[self._hash(k)] = [k,v]

    def get(self, k):
        return self._pairs[self._hash(k)][1]
```

a) What is the complexity of the `put()` and `get()` in this implementation?

- b) Modify the implementation to use open addressing with double hashing. The hash function is given in the code above. Use the following for the probe decrement function:

```
probe(key) = max(1, len(key) // 7)
```

Assume that there is always room in the hash table for a new entry and that the value being stored is always a new value. That is, you do not have to handle the following:

```
>>> d.put('three', 3)
>>> d.put('three', 48)
```

Also, assume that `get()` will always find a value in the dictionary.

Problem 4. Modify the dictionary class in Problem 3 with *chaining* to resolve collision.