

SOLUTIONS

Problem 1.

```
def reverse(a):  
    if a == []:  
        return []  
    if len(a) == 1:  
        return a  
    else:  
        return [a[-1]] + reverse(a[0:-1])
```

Problem 2.

```
def make_tuples(a, b):  
    if a == [] or b == []:  
        return []  
    else:  
        return [(a[0], b[0])] + make_tuples(a[1:], b[1:])
```

Problem 3.

```
def sum_leaves(t):  
    if t == None:  
        return 0  
    if t._left == None and t._right == None:  
        return t._value  
    else:  
        return sum_leaves(t._left) + sum_leaves(t._right)
```

Problem 4.

- a) An invariant is *something that is true* about the state of a program *at some point* in the code during execution.
- b) y is even
 $y \leq x + 1$

Problem 5.

```
# add a node to the head of the list
def add(self, node):
    node._next = self._head
    self._head = node

def remove(self):
    if self._head == None:
        return None
    else:
        prev = self._head
        cur = prev._next
        if cur == None:
            self._head == None
            return prev
        else:
            while (cur._next != None):
                prev = cur
                cur = cur._next

            prev._next = None
            return cur

class Queue:
    def __init__(self):
        self._items = LinkedList()

    def enqueue(self, item):
        self._items.add(Node(item))

    def dequeue(self):
        n = self._items.remove()
        return n._value
```

Note: `dequeue ()` as shown above returns the value of the node. You may have written this initially:

```
def dequeue (self):
    return self._items.remove()
```

However, this returns an object of type `Node`, which is not what the user expected. Even though we are using linked lists as the underlying representation, the user is pushing and popping elements of a given type and `dequeue ()` must return the element as it was when pushed on to the queue.

Problem 6.

0	1	2	3	4	5	6
14	2	23	10	24	19	

Problem 7.

a)

AAA

AB

BA

b) 1011111 (represents CABA)

Problem 8.

Various solutions, but the bug is exposed when `wordlist` is an empty list.

value for wordlist	value for tail
<code>[]</code>	<code>'anything'</code>
<code>['this', 'is', 'it']</code>	<code>'is'</code>
<code>['a', 'field', 'of', 'hay']</code>	<code>'go'</code>
<code>['a', 'field', 'of', 'hay']</code>	<code>'as'</code>