Bellwork 1/12

Find the general indefinite integral:

$$\int (2+\tan^2\theta)d\theta$$

Bellwork 1/12 - Solution

$$\int_{0}^{4} (4-t)\sqrt{t}dt = 4 \int_{0}^{4} \sqrt{t}dt - \int_{0}^{4} t^{\frac{3}{2}}dt$$

$$= \frac{8}{3} \left[t^{\frac{3}{2}}\right]_{0}^{4} - \frac{2}{5} \left[t^{\frac{5}{2}}\right]_{0}^{4}$$

$$= \frac{8}{3} \left(4^{\frac{3}{2}}\right) - \frac{2}{5} \left(4^{\frac{5}{2}}\right)$$

$$= \frac{128}{15}$$

Exercise 1

Find the general indefinite integral:

$$\int \sqrt[4]{x^5} dx$$

Exercise 1 - Solution

$$\int \sqrt[4]{x^5} dx = \int x^{\frac{5}{4}} dx$$
$$= \left[\frac{4}{9} x^{\frac{9}{4}} + C \right] \text{ (Power Rule)}$$

Exercise 2

Find the general indefinite integral:

$$\int \left(\frac{1+r}{r}\right)^2 dr$$

Exercise 2 - Solution

$$\int \left(\frac{1+r}{r}\right)^2 dr = \int \frac{(1+r)^2}{r^2} dr$$

$$= \int \frac{r^2 + 2r + 1}{r^2} dr$$

$$= \int 1 + \frac{2}{r} + r^{-2} dr$$

$$= \left[r + 2\ln|r| - r^{-1} + C\right]$$