### Bellwork 9/8

If a tennis ball on Earth is launched upward with a velocity of 19.6  $\frac{m}{s}$ , the height of the ball from its initial position can be modeled by the equation:

$$h(t) = 19.6t - 4.9t^2$$

- Find its average velocity over the given time intervals:

  - **1** [0.9, 1] **2** [0.99, 1] **3** [1, 1.01] **4** [1, 1.1]
- 2 Estimate the instantaneous velocity of the ball at t=1.

# Bellwork 9/8 - Solutions

1

- **1** 0.49  $\frac{m}{s}$
- $0.049 \frac{m}{s}$

 $0 \frac{m}{s}$ 

- 3  $-0.049 \frac{m}{s}$
- $\bullet$  -0.49  $\frac{m}{s}$

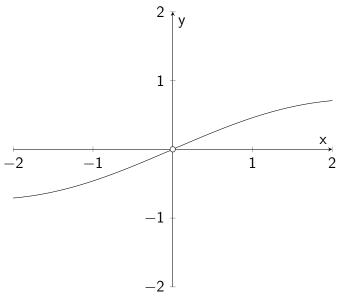
### Exercise 1

- Graph  $f(x) = \frac{1-\cos(x)}{x}$  on a calculator.
- Fill in the table:

$$\begin{array}{c|cc}
x & f(x) \\
\hline
0.5 & \\
0.1 & \\
0.01 & \\
0.001 & \\
\end{array}$$

• Estimate:  $\lim_{x \to 0} \left[ \frac{1 - \cos(x)}{x} \right]$ 

## Exercise 1 - Solutions



#### Exercise 1 - Solutions

$$\begin{array}{c|cccc} x & f(x) \\ \hline -0.1 & -0.05 \\ \hline -0.01 & -0.005 \\ \hline 0.01 & 0.005 \\ \hline 0.1 & 0.05 \\ \hline \end{array}$$

From the table,

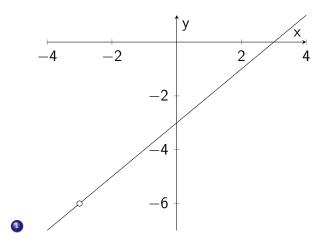
$$\lim_{x\to 0} \left[ \frac{1-\cos(x)}{x} \right] \approx \boxed{0}$$

### Exercise 2

- Graph  $f(x) = \frac{x^2-9}{x+3}$  on a calculator.
- Fill in the table:

$$\begin{array}{c|cc}
x & f(x) \\
\hline
-3.1 & \\
-3.01 & \\
-2.99 & \\
-2.9 & \\
\end{array}$$

## Exercise 2 - Solutions



#### Exercise 2 - Solutions

$$\begin{array}{c|cccc} x & f(x) \\ \hline -3.1 & -6.1 \\ \hline -3.01 & -6.01 \\ -2.99 & -5.99 \\ -2.90.1 & -5.9 \\ \end{array}$$

From the table,

$$\lim_{x \to -3} \left( \frac{x^2 - 9}{x + 3} \right) \approx \boxed{-6}$$