§1 SAT-COMMAFREE INTRO 1

1. Intro. Find a comma-free block code of length n, having one code in each cyclic equivalence class, if one exists.

Codewords are represented as hexadecimal numbers.

```
#define maxn = 25
                             /* must be at most 32, to keep the variable names small */
#include <stdio.h>
#include <stdlib.h>
              /* command-line parameter */
  int n;
  char a[maxn + 1];
   main(\mathbf{int} \ argc, \mathbf{char} * argv[])
   {
     register int i, j, k;
     register unsigned int x, y, z;
     register unsigned long long m, acc, xy;
     \langle \text{Process the command line 2} \rangle;
      (Generate the positive clauses 3);
     ⟨ Generate the negative clauses 5⟩;
   }
      \langle \text{Process the command line } 2 \rangle \equiv
  if (argc \neq 2 \lor sscanf(argv[1], "%d", \&n) \neq 1) {
     fprintf(stderr, "Usage: \_\%s \_n \n", argv[0]);
     exit(-1);
  if (n < 2 \lor n > maxn) {
     fprintf(stderr, "n_b should_b be_b etween_2_and_%d,_not_%d! n", maxn, n);
  printf("~_{\sqcup}sat-commafree_{\sqcup}%d\n",n);
This code is used in section 1.
      Here I use Algorithm 7.2.1.1F to find the prime binary strings.
\langle Generate the positive clauses _3\rangle \equiv
f1: a[0] = -1, j = 1;
f2: \mathbf{if} \ (j \equiv n) \ \langle \text{ Visit the prime string } a_1 \dots a_n \ 4 \rangle;
f3: for (j = n; a[j] \equiv 1; j--);
f<sub>4</sub>: if (j) {
     a[j] = 1;
  f5: for (k = j + 1; k \le n; k++) a[k] = a[k - j];
     goto f2:
This code is used in section 1.
      \langle \text{ Visit the prime string } a_1 \dots a_n \rangle \equiv
  {
     for (i = 0; i < n; i ++) {
        for (x = 0, k = 0; k < n; k++) x = (x \ll 1) + a[1 + ((i + k) \% n)];
        printf(" " " x", x);
     printf("\n");
This code is used in section 3.
```

```
ξ5
```

```
\langle Generate the negative clauses 5\rangle \equiv
  m = (1_{\rm LL} \ll n) - 1;
   for (x = 0; x < (1 \ll n); x \leftrightarrow) {
      \langle \text{ If } x \text{ is cyclic, continue } 6 \rangle;
      for (y = 0; y < (1 \ll n); y ++) {
         \langle \text{ If } y \text{ is cyclic, continue } 7 \rangle;
         \langle Generate the clauses for x followed by y \mid 9 \rangle;
   }
This code is used in section 1.
      \langle \text{ If } x \text{ is cyclic, continue } 6 \rangle \equiv
   acc = (((\mathbf{unsigned\ long\ long})\ x) \ll n) + x;
   for (k = 1; k < n; k++)
      if (((acc \gg k) \& m) \equiv x) break;
   if (k < n) continue;
This code is used in section 5.
     \langle \text{ If } y \text{ is cyclic, } \mathbf{continue } 7 \rangle \equiv
   acc = (((\mathbf{unsigned\ long\ long})\ y) \ll n) + y;
   for (k = 1; k < n; k++)
      if (((acc \gg k) \& m) \equiv y) break;
   if (k < n) continue;
This code is used in section 5.
      \langle \text{ If } z \text{ is cyclic, continue } 8 \rangle \equiv
   acc = (((\mathbf{unsigned\ long\ long})\ z) \ll n) + z;
   for (k = 1; k < n; k++)
      if (((acc \gg k) \& m) \equiv z) break;
   if (k < n) continue;
This code is used in section 9.
      \langle Generate the clauses for x followed by y \mid 9 \rangle \equiv
   xy = (((\mathbf{unsigned\ long\ long})\ x) \ll n) + y;
   for (j = 1; j < n; j ++) {
      z = (xy \gg j) \& m;
      \langle \text{ If } z \text{ is cyclic, continue } 8 \rangle;
      printf("~%x_{\sqcup}~%x_{\sqcup}~%x \setminus n", x, y, z);
This code is used in section 5.
```

 $\S10$ Sat-commafree index 3

10. Index.

```
a: \underline{1}.
 acc: \underline{1}, 6, 7, 8.
 argc: \underline{1}, \underline{2}.
 argv: \quad \underline{1}, \quad 2. exit: \quad 2.
 fprintf: 2.

f1: \underline{3}.

f2: \underline{3}.

f3: \underline{3}.

f_4: \underline{3}.
f5: \underline{3}.
i: \underline{1}.
 j: \underline{1}.
 k: \underline{1}.
 m: \underline{1}.
 main: \underline{1}.
 maxn: \underline{1}, \underline{2}.
 n: \underline{1}.
 \begin{array}{ll} \overline{printf}\colon & 2, \ 4, \ 9. \\ sscanf\colon & 2. \end{array}
 stderr: 2.
 x: \underline{1}.
xy: \underline{1}, \underline{9}.
 y: <u>1</u>.
 z: \underline{1}.
```

4 NAMES OF THE SECTIONS

SAT-COMMAFREE

SAT-COMMAFREE

	Sect	ion	Page
Intro		. 1	1
Indev		10	•