

Selection Sort

Selection sort is a simple sorting algorithm. This sorting algorithm is an in-place comparison-based algorithm in which the list is divided into two parts, the sorted part at the left end and the unsorted part at the right end. Initially, the sorted part is empty and the unsorted part is the entire list.

The smallest element is selected from the unsorted array and swapped with the leftmost element, and that element becomes a part of the sorted array. This process continues moving unsorted array boundary by one element to the right.

This algorithm is not suitable for large data sets as its average and worst case complexities are of $O(n^2)$, where n is the number of items.

How Selection Sort Works?

Consider the following depicted array as an example.



For the first position in the sorted list, the whole list is scanned sequentially. The first position where 14 is stored presently, we search the whole list and find that 10 is the lowest value.



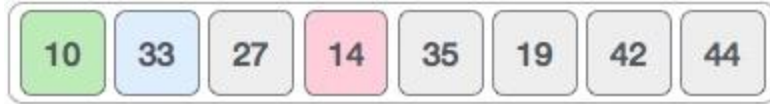
So we replace 14 with 10. After one iteration 10, which happens to be the minimum value in the list, appears in the first position of the sorted list.



For the second position, where 33 is residing, we start scanning the rest of the list in a linear manner.



We find that 14 is the second lowest value in the list and it should appear at the second place. We swap these values.



After two iterations, two least values are positioned at the beginning in a sorted manner.



The same process is applied to the rest of the items in the array.

Merge Sort

Merge sort is a sorting technique based on divide and conquer technique. With worst-case time complexity being $O(n \log n)$, it is one of the most respected algorithms.

Merge sort first divides the array into equal halves and then combines them in a sorted manner.

How Merge Sort Works?

To understand merge sort, we take an unsorted array as the following –



We know that merge sort first divides the whole array iteratively into equal halves unless the atomic values are achieved. We see here that an array of 8 items is divided into two arrays of size 4.



This does not change the sequence of appearance of items in the original. Now we divide these two arrays into halves.



We further divide these arrays and we achieve atomic value which can no more be divided.



Now, we combine them in exactly the same manner as they were broken down. Please note the color codes given to these lists.

We first compare the element for each list and then combine them into another list in a sorted manner. We see that 14 and 33 are in sorted positions. We compare 27 and 10 and in the target list of 2 values we put 10 first, followed by 27. We change the order of 19 and 35 whereas 42 and 44 are placed sequentially.



In the next iteration of the combining phase, we compare lists of two data values, and merge them into a list of found data values placing all in a sorted order.



After the final merging, the list should look like this –



Now we should learn some programming aspects of merge sorting.

Algorithm

Merge sort keeps on dividing the list into equal halves until it can no more be divided. By definition, if it is only one element in the list, it is sorted. Then, merge sort combines the smaller sorted lists keeping the new list sorted too.

Step 1 – if it is only one element in the list it is already sorted, return.

Step 2 – divide the list recursively into two halves until it can no more be divided.

Step 3 – merge the smaller lists into new list in sorted order.

Pseudocode

We shall now see the pseudocodes for merge sort functions. As our algorithms point out two main functions – divide & merge.

Merge sort works with recursion and we shall see our implementation in the same way.

```
procedure mergesort( var a as array )
    if ( n == 1 ) return a

    var l1 as array = a[0] ... a[n/2]
    var l2 as array = a[n/2+1] ... a[n]

    l1 = mergesort( l1 )
    l2 = mergesort( l2 )

    return merge( l1, l2 )
end procedure

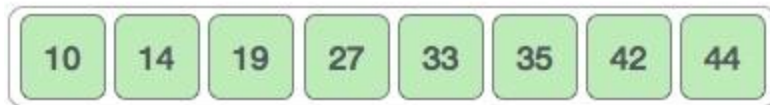
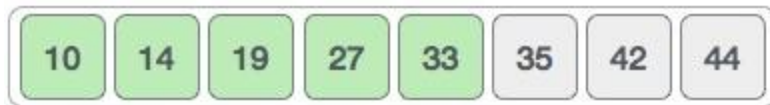
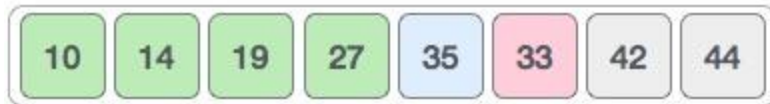
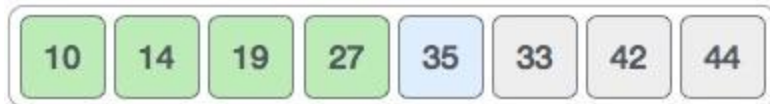
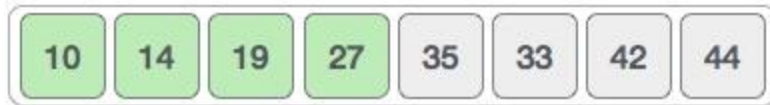
procedure merge( var a as array, var b as array )

    var c as array
    while ( a and b have elements )
        if ( a[0] > b[0] )
            add b[0] to the end of c
            remove b[0] from b
        else
            add a[0] to the end of c
            remove a[0] from a
        end if
    end while

    while ( a has elements )
        add a[0] to the end of c
        remove a[0] from a
    end while

    while ( b has elements )
        add b[0] to the end of c
        remove b[0] from b
    end while

    return c
end procedure
```



Now, let us learn some programming aspects of selection sort.

Algorithm

- Step 1** - Set MIN to location 0
- Step 2** - Search the minimum element in the list
- Step 3** - Swap with value at location MIN
- Step 4** - Increment MIN to point to next element
- Step 5** - Repeat until list is sorted

Pseudocode

```

procedure selection sort
    list  : array of items
    n      : size of list

    for i = 1 to n - 1
        /* set current element as minimum */
        min = i

        /* check the element to be minimum */

        for j = i+1 to n
            if list[j] < list[min] then
                min = j;
            end if
        end for

        /* swap the minimum element with the current element */
        if indexMin != i then
            swap list[min] and list[i]
        end if
    end for
end procedure

```

Shell Sort

Shell sort is a highly efficient sorting algorithm and is based on insertion sort algorithm. This algorithm avoids large shifts as in case of insertion sort, if the smaller value is to the far right and has to be moved to the far left.

This algorithm uses insertion sort on a widely spread elements, first to sort them and then sorts the less widely spaced elements. This spacing is termed as **interval**. This interval is calculated based on Knuth's formula as –

Knuth's Formula

```

h = h * 3 + 1
where -
    h is interval with initial value 1

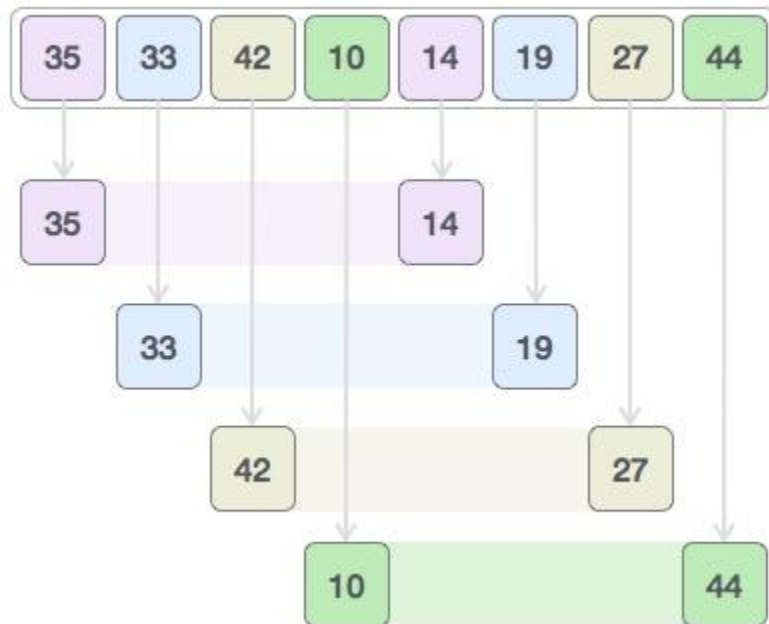
```

This algorithm is quite efficient for medium-sized data sets as its average and worst-case complexity of this algorithm depends on the gap sequence the best known is $O(n)$, where n is the number of items. And the worst case space complexity is $O(n)$.

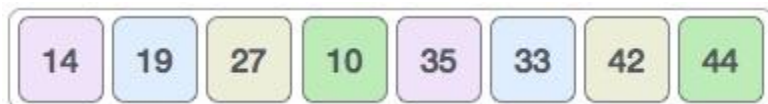
How Shell Sort Works?

Let us consider the following example to have an idea of how shell sort works. We take the same array we have used in our previous examples. For our example and ease of understanding, we

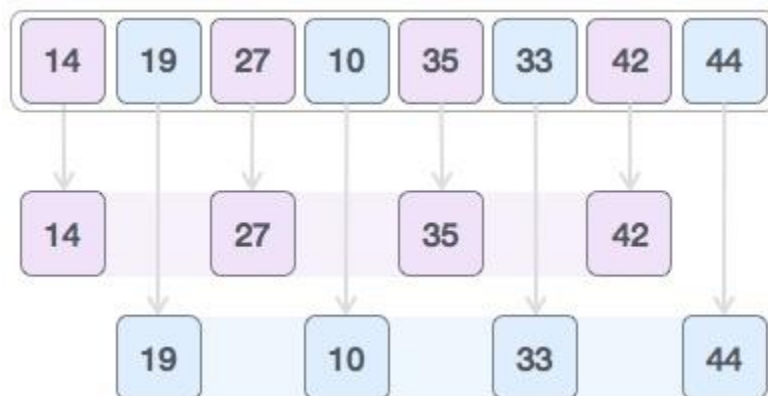
take the interval of 4. Make a virtual sub-list of all values located at the interval of 4 positions. Here these values are {35, 14}, {33, 19}, {42, 27} and {10, 44}



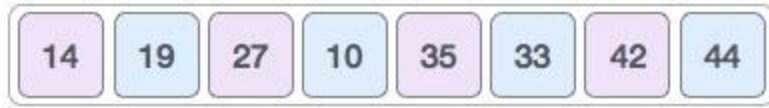
We compare values in each sub-list and swap them (if necessary) in the original array. After this step, the new array should look like this –



Then, we take interval of 1 and this gap generates two sub-lists - {14, 27, 35, 42}, {19, 10, 33, 44}



We compare and swap the values, if required, in the original array. After this step, the array should look like this –



Finally, we sort the rest of the array using interval of value 1. Shell sort uses insertion sort to sort the array.

Following is the step-by-step depiction –



We see that it required only four swaps to sort the rest of the array.

Algorithm

Following is the algorithm for shell sort.

Step 1 - Initialize the value of h

Step 2 - Divide the list into smaller sub-list of equal interval h
Step 3 - Sort these sub-lists using **insertion sort**
Step 3 - Repeat until complete list is sorted

Pseudocode

Following is the pseudocode for shell sort.

```
procedure shellSort()
    A : array of items

    /* calculate interval*/
    while interval < A.length /3 do:
        interval = interval * 3 + 1
    end while

    while interval > 0 do:

        for outer = interval; outer < A.length; outer ++ do:

            /* select value to be inserted */
            valueToInsert = A[outer]
            inner = outer;

            /*shift element towards right*/
            while inner > interval -1 && A[inner - interval] >= valueToInsert
do:
                A[inner] = A[inner - interval]
                inner = inner - interval
            end while

            /* insert the number at hole position */
            A[inner] = valueToInsert

        end for

        /* calculate interval*/
        interval = (interval -1) /3;

    end while
end procedure
```

Quick Sort

Quick sort is a highly efficient sorting algorithm and is based on partitioning of array of data into smaller arrays. A large array is partitioned into two arrays one of which holds values smaller than the specified value, say pivot, based on which the partition is made and another array holds values greater than the pivot value.

Quicksort partitions an array and then calls itself recursively twice to sort the two resulting subarrays. This algorithm is quite efficient for large-sized data sets as its average and worst-case complexity are $O(n^2)$, respectively.

Partition in Quick Sort

Following animated representation explains how to find the pivot value in an array.



The pivot value divides the list into two parts. And recursively, we find the pivot for each sub-lists until all lists contains only one element.

Quick Sort Pivot Algorithm

Based on our understanding of partitioning in quick sort, we will now try to write an algorithm for it, which is as follows.

- Step 1** - Choose the highest index value has pivot
- Step 2** - Take two variables to point left and right of the list excluding pivot
- Step 3** - left points to the low index
- Step 4** - right points to the high
- Step 5** - while value at left is less than pivot move right
- Step 6** - while value at right is greater than pivot move left
- Step 7** - if both step 5 and step 6 does not match swap left and right
- Step 8** - if $\text{left} \geq \text{right}$, the point where they met is new pivot

Quick Sort Pivot Pseudocode

The pseudocode for the above algorithm can be derived as –

```
function partitionFunc(left, right, pivot)
    leftPointer = left
    rightPointer = right - 1

    while True do
        while A[++leftPointer] < pivot do
            //do-nothing
        end while

        while rightPointer > 0 && A[--rightPointer] > pivot do
            //do-nothing
        end while

        if leftPointer >= rightPointer
            break
        else
            swap leftPointer, rightPointer
        end if

    end while

    swap leftPointer, right
    return leftPointer

end function
```

Quick Sort Algorithm

Using pivot algorithm recursively, we end up with smaller possible partitions. Each partition is then processed for quick sort. We define recursive algorithm for quicksort as follows –

Step 1 - Make the right-most index value pivot
Step 2 - partition the array using pivot value
Step 3 - quicksort left partition recursively
Step 4 - quicksort right partition recursively

Quick Sort Pseudocode

To get more into it, let see the pseudocode for quick sort algorithm –

```
procedure quickSort(left, right)

    if right-left <= 0
        return
    else
        pivot = A[right]
        partition = partitionFunc(left, right, pivot)
        quickSort(left, partition-1)
```

```
        quickSort(partition+1, right)
    end if
end procedure
```