Analysis and Graphical Representation of Health and Labour Force Participation among the Elderly in Europe

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1 Introduction

- relevance of exploring relationship between health and labour force participation due to changing demographic in Europe
- cite relevant study about ageing
- few sentences about relevant papers exploring relationship -> use paper from DIW
- very short literature overview on relationship between health and labour force participation
- share data set as rich data set for this purpose: 2 sentences about it
- introduction of journal article
- our approach: replicate results an enrich analysis
- especially: introduce graphical visualization tools for descriptive statistics -> ease interpretation of variables
- our aim: write code in a way that allows the user to work with easySHARE data set, even when working on different question

2 Panel data cleaning and subsetting

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2.1 Theory and Design

2.2 Implementation

2.3 Empirical Results

The easySHARE dataset released in spring 2017 is a panel dataset of 108 variables of more than 100.000 individuals covering data from six survey waves carried out between 2004 and 2005. As we are only concerned with a small subset of observations, an important task was to define appropriate functions for subsetting. In oder to make our subsetting process understandable to readers, we decided on using pipe-operator. This allows us to apply the filter and select option in a clever way, where we can select different criteria at once.

-> code sniplet here

In this example, we first filter for participation in wave 1 and the age group between 50 and 64 and the select the desired variables as described in Kalwij and Vermeulen (2005).

Although the overall response rate in the SHARE are comparably high, the data set still has numerous missing values. The reason for this is due to the fact that the study was carried out on a crossnational scale, with some national survey institutions deciding not to participate in all survey modules. This means that the majority of missing values are to be found within observations that have missing values for entire survey modules or waves. The reason for the missing values are documented well in the "Guide to easySHARE release 6.0.0" and specifically coded. For example, the numbers -13 and -14 refer to "not asked in this wave" and "not asked in this country". Since this coding scheme is not useful for the purpose of our analysis, we decided on recoding all of the missing values as "NA". To this end, we defined a function based on the missing codes provided by SHARE that finds the NAs in the data and declares them as such.

-> code snipet here

Since the study carried out by Kalwij and Vermeulen (2005) is based on the use of mostly binary data, we needed to construct numerous dummies based on the original data.

-> code snipet here

The resulting dataframe containes XXX observations of YYY variables.

- coded countries in more readable manner
- use packe ddd -> match offical ISO code with country name
- create country list with all countries in study (not Israel)
- defined dummies

3 Multidisciplinary and crossnational summary statistics

JULIAN

- 3.1 Theory and Design
- 3.2 Implementation
- 3.3 Empirical Results

4 Crosssectional probit regression

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- 4.1 Theory and Design
- 4.2 Implementation
- 4.3 Empirical Results

5 Wald Test

In the context of probit regression, the Wald test can be used to test multiple hypothesis regarding the model specifications and significance of coefficients. For example, it can be used to test whether the fit of the model is improved if a subset of regression coefficients are all set equal to zero, an exclusion restriction. Kalwij and Vermeulen (2005) conduct a Wald test to check the null hypothesis that none of the included health variables has an impact on labour participation in order to investigate the joint impact of health on participation.

5.1 Theory and Design

Depending on the estimation method and distributional assumptions, the Wald statistic can be formulated in different ways. The general form of the Wald statistic after MLE for testing hypothesis regarding our $k \times 1$ parameter vector θ is given by

$$W = c(\hat{\theta})' [\nabla_{\theta} c(\hat{\theta}) \hat{V} \nabla_{\theta} c(\hat{\theta})]^{-1} c(\hat{\theta})$$

where $c(\hat{\theta})$ is a $m \times 1$ vector of linear or nonlinear restrictions, $\nabla_{\theta} c(\hat{\theta})$ is the $m \times k$ Jacobian of $c(\hat{\theta})$ evaluated at $\hat{\theta}$ and \hat{V} is the estimated asymtotic covariance matrix (Wooldridge 2010, 463). Under H0, the Wald test statistic is asymptotically $\chi 2_m$ distributed, with m being the number of specified restrictions. In order to assure the test statistic W has the assumed limiting distribution, we need to impose some practical restrictions. Under H0, θ must lie within parameter space and R must be of rank m (Wooldridge 2010, 362). We limit our attention to testing a set of general linear restrictions since the Wald test is not invariant to the re-formulation of non-linear hypothesis (Wooldridge 2010, 362). We thus formulate our nullhypothesis in accordance with the common linear restriction structure of H0: $R\hat{\beta} = r$ againsts the alternative H1: $R\hat{\beta} \neq r$ to facilitate the derivation of our test statistics where R is a $m \times k$ matrix of rank m (equivalent to the Jacobian), whereas the restriction function r is a $m \times 1$ vector. Given the above technical conditions are satisfied, the Wald statistic can then be rewritten as

$$W = (R\hat{\beta} - r)'[R\hat{V}R']^{-1}(R\hat{\beta} - r)$$

which facilitates our calculations (Greene 2012, 527–29; Wooldridge 2010, 362). When we are interested in the joint significance of a subset of s coefficients, the nullhypothesis is that each of the s coefficients in the vector β_s is equal to zero. The Wald test statistic can then be even more simplified:

$$W = \hat{\beta}'_s [R\hat{V}R']^{-1} \hat{\beta}_s = \hat{\beta}'_s [\hat{V}_s]^{-1} \hat{\beta}_s$$

where the test statistic is distributed as $W \stackrel{a}{\sim} \chi 2_s$ (Wooldridge 2010, 362).

5.2 Implementation

In order to test linear hypothesis regarding the model specifications and significance of coefficients we design two versions of a Wald test. The function joint.wald.test is a simplied version to test the joint significance of a subset of model coefficients, whereas general.wald.test allows checking any linear hypothesis. The two tests are constructed in a way so they align well with the general glm estimation output, especially relevant for probit regression. An advantage over alternative Wald test functions from other packages (e.g. aod) is that it allows for empty class membership, as discussed in detail below.

We designed the joint significance test that makes it both easy to use, understand and modify to special needs. The only required input is the model summary from glm estimation, whereas the significance level and test specifications are optional.

```
joint.wald.test = function(model.summary, signf.level = NULL, spec = NULL){
    joint.wald.test = numeric(6)
    names(joint.wald.test) = c("Name","W","p-value", "df", "HO" , "Decision")
    beta = model.summary$coefficients[,1]
    Var_beta_est = vcov(model.summary)
```

In order to set up default values for both the significance level and the hypothesis specification, we make use of a local if-else statement inside the joint.wald.test function. By declaring the model specification to be null in line XXX we set the foundation for the default specification in line XXX - XXX. Here, we re-asign a sequence vector to the spec that includes the number of all model coefficients in increasing order, unless spec is specified differently by the user. In that case, the if-else statement will use the user specification assured by line XXX.

```
spec = if (is.null(spec)){
    spec = 1: length(beta) # default is joint significance test
} else {
    spec = spec}
```

This means that joint.wald.test function will conduct a joint significance test on all model coefficients by default. We setup a default significance level of 95% in the same manner. The Wald test statistic is calculated via simple matrix algebra based on the provided input by the model summary. This formula is equivalent to equation YYY.

```
W = t(beta[spec]) %*% solve(Var_beta_est[spec,spec]) %*% beta[spec]
```

As can be seen in line XXX the proper format of the specification vector spec is crucial as it is used to extract the needed estimates from the model coefficient vector and covariance matrix. In line XXX, the term $Var_beta_est[spec,spec]$ extracts all covariance matrix elements corresponding to the joint significance hypothesis of the particular specification. To assure the proper extraction of the covariance elements and determination of degrees of freedom in line XXX, spec must be a vector of integers of length $0 < m \le k$.

As a last step we set up the test ouput by assigning values to the empty vector elements of joint.wald.test. This vector will be the function output that is returned. We determine the critical value and p-value in lines XXX-XXX based on the inbuilt qchisq and display four significant decimal places. As can be seen in lines XX, we do not only list the test statistic and p-value but also the degrees of freedom, nullhypothesis and test decision as output to assure comprehensibility and correctness of the test.

The general Wald test is designed in a similar manner, except that it allows for the general formulation of linear hypothesis of the form $R\hat{\beta}=r$. The test statistic in this case is giving by equation YYY. As in the joint.wald.test function, we use local local if-else statements to setup a default settings. If only the model summary is given as an input, the general.wald.test conducts a joint significance test at a 95% significance level. The crucial part to the proper usage of this function are the correctly specified Jacobian matrix R and restriction vector r, which must be of size $m \times k$ and $m \times 1$ respectively. To assure the proper asymptotic distribution of the test statistic we additional need to assures that R is of rank m.

We therefore incorporate ...

5.3 Empirical Results

We use our designed wald test functions to carry out several hypothesis test on our model coefficients from probit estimation. Speficically, we check the null hypothesis that none of the four included health variables has an impact on labour participation for each country and for both men an women. The results for men can be seen in table XXX

Our results our in line with the findings of Kalwij and Vermeulen (2005). As expected, the null hypothesis of no impact of health on labour participation is rejected at a 95% level for most countries. A particularity is the high p-value of France, leading to the inability to reject H0, which stands in contrast to the findings of Kalwij and Vermeulen (2005). We explain this with our differing sample, which is almost 50% larger and the lower overall employmen rate of our sample. Regarding the Wald tests for women, our results are very similar to those Kalwij and Vermeulen (2005). As for men, The majority of null hypothesis can be rejected for women, with the null for German women being barely not rejected.

TEXT: 1 - 2 SENTENCES ABOUT WHY FAIL TO REJECT

The results of our joint.wald.test function are comparable those of our packages, like the wald.test from the aod packages. To check our function this we can conduct both test on all subsets. For example, for German women the aod packages gives the following output

```
Test W p-value df H0 Decision
"Wald" "9.17" "0.0569" "4" "b equal to 0" "Cannot reject H0""
```

A weakness of the aod package is, that its wald test cannot deal with empty classes. For the case of Switzerland, where our male sample does not include any 64-year-olds, the wald.test from the aod packages lead to the error messages

```
 wald.test(Sigma = vcov(allModels\$Switzerland.MALE), \ b = allModels\$Switzerland.MALE\$coefficients, \\ Error in L \%*\% V : non-conformable arguments
```

Our wald test function is robust against the presence of empty classes since we work with model summaries, meaning that the coefficients of empty classes have been dropped instead of being a missing value. Thus, our joint.wald.test function can conduct the test for Swiss men without errors:

```
joint.wald.test(allSummaries$Switzerland.MALE, spec = 16:19)
```

```
Test W p-value df H0 Decision
"Wald" "9.91" "0.042" "4" "b equal to 0" "Reject H0"
```

Both our wald test functions are sensitive to the improper formulation of tested model restrictions. For example, the spec vector must be a numerical vector specifying the coefficients to be included given their ordering in the model summary. The test also works when spec is specified as a logical vector but will return an inappropriate test distribution:

```
specification = c(rep(FALSE,15), rep(TRUE, 4), rep(FALSE,3))
```

```
joint.wald.test(allSummaries$Switzerland.MALE, spec = specification)
```

Test	W	p-value	df	НО	Decision
"Wald"	"9.91"	"0.987"	"22"	"b equal to 0"	"Cannot reject HO"

As in line XXX, our specification and Wald statistic are similar. However, the function fasely assigns 22 degrees of freedoms since this is the length of our specification vector.

6 Counterfactual exercise

Counterfactual exercises are a common tool in economic policy analysis that allow assessing and quantifying possible effects of policies. In order to evaluate the quantitative importance of a healthy population on labour participation, XXX conduct a counterfactual exercise. They compare the current national employment rate to the predicted counterfactual rate. This counterfactual employment rate is obtained by assuming that all individuals are in perfect health.

6.1 Theory and Design

Counterfactual exercises based on regression methods that can be carried out in different ways (see Chernozhukov et al 2013). The simplest method to is to replace the existing covariates values X with counterfactual values X_{cf} . For the case of probit regression with a binary response variable y for employment, we can interpret the fitted values \hat{y} and \hat{y}_{cf} as current and counterfactual employment probabilities for each individual. Based on these calculated individual employment probabilities, we can also calculate the national population employment rates by taking the mean, making use of the Law of Large Numbers.

Obtaining the counterfactual probabilities \hat{y}_{cf} requires a two-step procedure. First, the regular probit regression of y on X is tun to obtain the estimated coefficients $\hat{\beta}$. Second, the counterfactual probabilities for each individuals Π_i are calculated by predicting y based on X_{cf} and the estimated coefficients.

$$\Pi_{icf} = Pr(Yi = 1|Xi = xi_{cf}) = \Phi(xi'_{cf}\beta)$$

6.2 Implementation

6.3 Empirical Results

7 Graphical representation

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- 7.1 Theory and Design
- 7.2 Implementation
- 7.3 Empirical Results

8 Conclusion

9 References

Greene, William H. 2012. Econometric Analysis. Seventh Edition. Pearson Education.

Kalwij, Adriaan, and Frederic Vermeulen. 2005. "Labour Force Participation of the Elderly in Europe: The Importance of Being Healthy."

Wooldridge, Jeffrey M. 2010. Econometric Analysis of Cross Section and Panel Data. MIT press.

Declaration of Authorship

We hereby confirm that we have authored this Seminar paper independently and without use of others than the indicated sources. All passages which are literally or in general matter taken out of publications or other sources are marked as such.

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