

Lecture # 27 CHE331A

Non-ideal Reactors

- ❑ Non-isothermal reactors
- ❑ Energy balance for ideal reactors
- ❑ Non-adiabatic PFR
- ❑ Reversible reactions in adiabatic reactors
- ❑ CSTR with heat effects
- ❑ Batch reactors

Goutam Deo

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Principles behind Non-ideal reactors and their analysis

- ▶ Residence time distribution
- ▶ Tank-in-series model
- ▶ Dispersion model (will not include)
- ▶ Applications to design



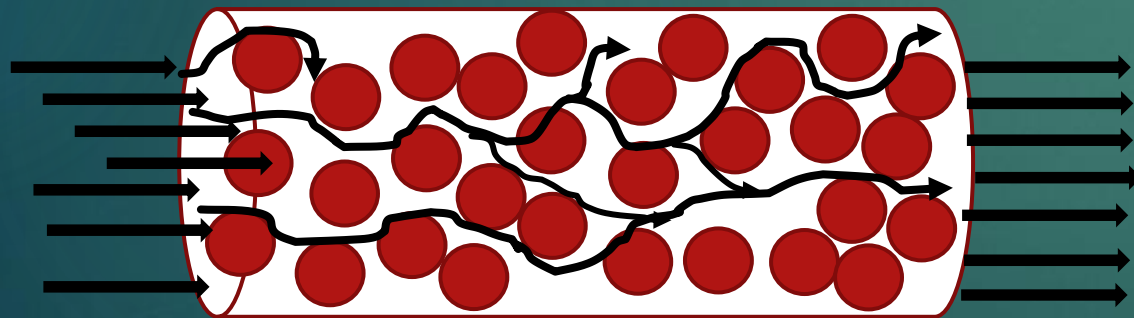
Industrial Reactors are rarely ideal

- ▶ Ideal reactors: Batch, CSTR, PFR and PBR
- ▶ Flow in these reactors are idealized and are rarely experienced
- ▶ Real flow-reactors lie between the extremes of
 - Completely mixed (no spatial variation) for CSTR (for example, no dead-zone)
 - No radial variation or axial mixing for PFR (entering fluid moves as a plug from entry to exit)

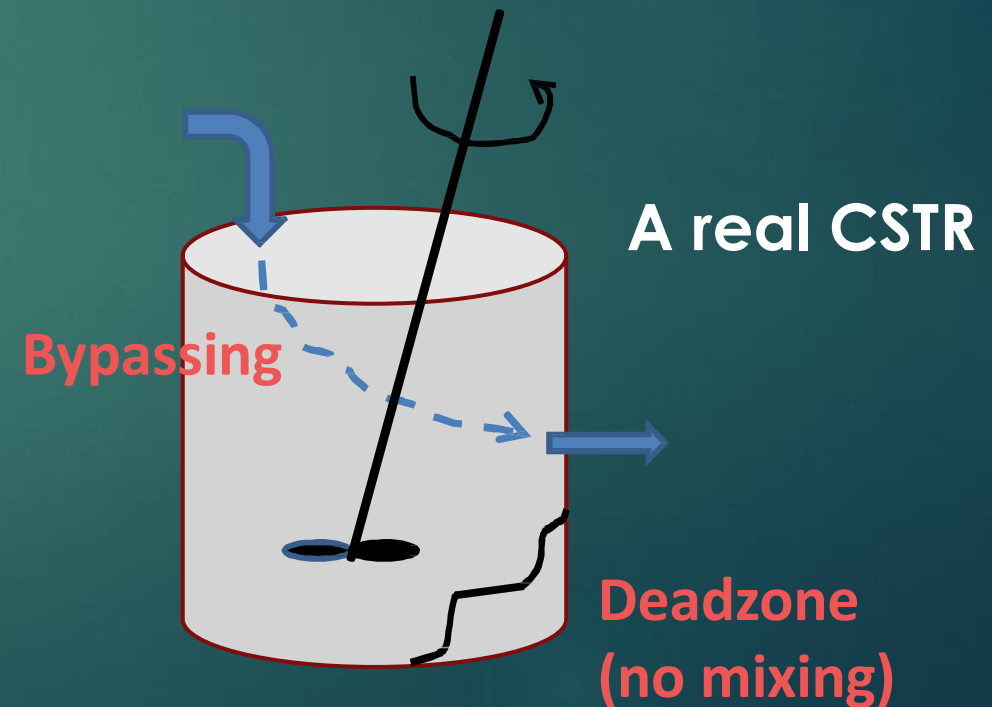


In non-ideal reactors the flows between these two extremes characterize the system

- ▶ Reasons for non-ideality in real reactors
 - Channelling, Recycle of fluid, stagnant regions, axial mixing, and velocity profile
- ▶ Time spent by fluid elements are different → *residence time distribution*

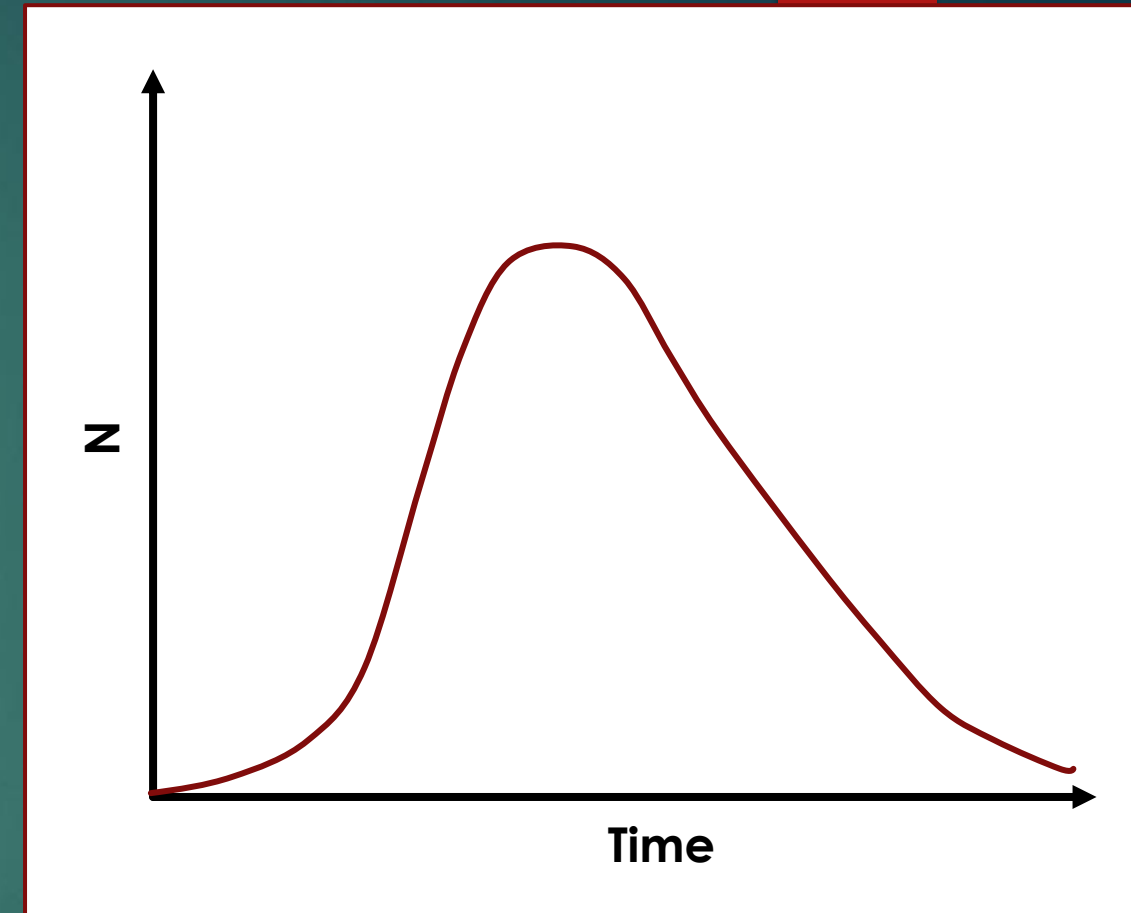


A real Packed Bed Reactor



Ways to account for non-ideality

- ▶ Three concepts used to describe non-ideal reactors:
 - Residence time distribution
 - Quality of mixing
 - Model used to describe the system
- ▶ For example, in an ideal PFR reactor all atoms of material have been in the reactor for the same “residence” time
- ▶ In real reactors some material leave quicker than the rest
 - There is a residence time distribution (RTD) or exit age distribution for a stream of fluid

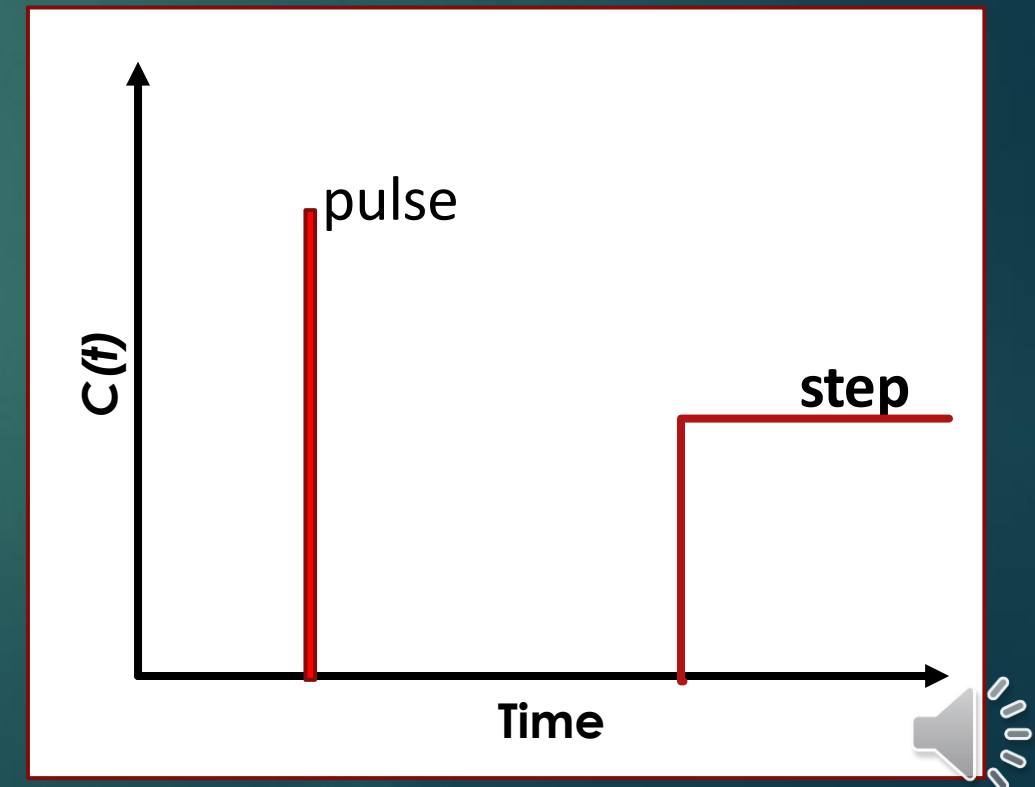
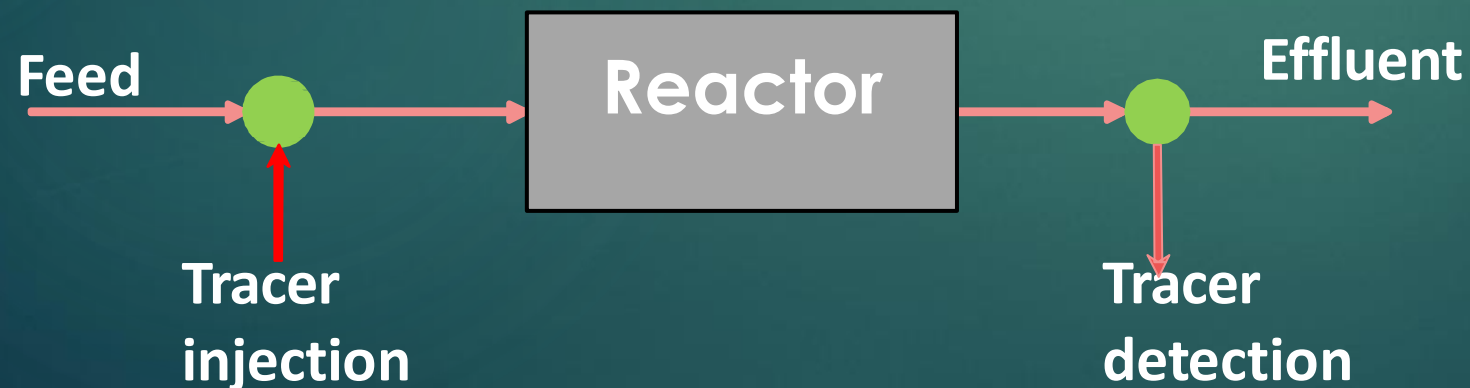


- In PFR/PBR and Batch are the only reactors in which each fluid element spends the same amount time in the reactor
- In a CSTR there is a distribution



Residence time distribution is determined experimentally

- ▶ Injecting tracer at some time and measuring outlet concentration of tracer
 - Tracer is an inert chemical molecule that can be detected in the feed
- ▶ Reactors give responses to different types of tracer input
- ▶ Tracer input primarily of two types
 - Pulse input and step input
 - Other types exist



A known amount of tracer material injected in one shot in a pulse input to determine the RTD

- ▶ Outlet concentration in a real reactor is measured as a function of time, C-curve. For example,

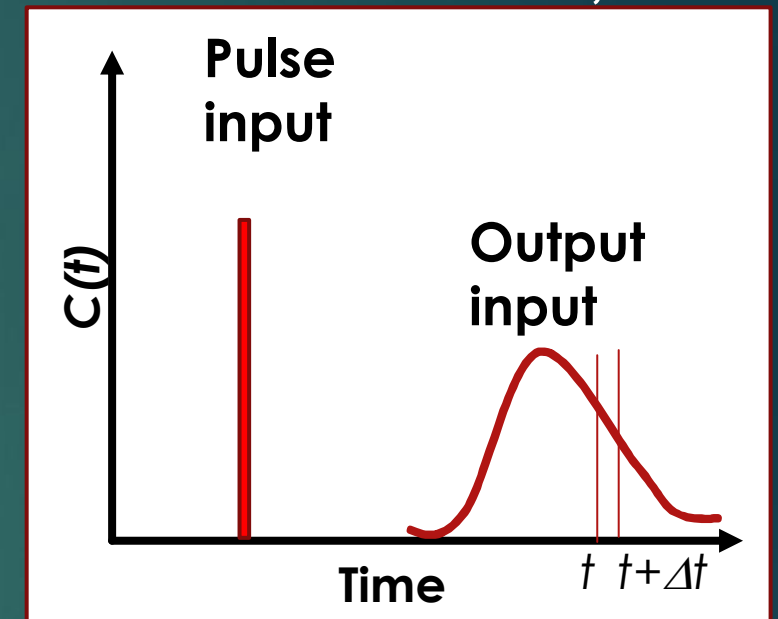
- ▶ Amount of tracer leaving between t and $t + dt$ is
$$\Delta N = C(t) \cdot v \cdot \Delta t$$

Where, v is the volumetric flowrate

- ▶ To make this independent of the amount of tracer

- ▶ Fraction of material spending between t and $t + dt$ in the reactor is $\Delta N / N_0$ where N_0 is the total amount of material injected

- ▶ For a pulse injection the residence time distribution function, $E(t)$, is defined as $E(t) = (C(t) \cdot v) / N_0$ so that $\frac{\Delta N}{N_0} = E(t) \cdot \Delta t$



The residence time distribution function, $E(t)$

- ▶ $E(t)$, is defined as $E(t) = (C(t) \cdot v) / N_0$ so that $\frac{\Delta N}{N_0} = E(t) \cdot \Delta t$
 - describes quantitatively how much time different fluid elements spend in the reactor
 - $E(t) \cdot dt$ is the fraction of fluid exiting the reactor that has spent between t and $t + dt$ time inside the reactor
- ▶ If N_0 is not known it can be determined by integrated the outlet concentration vs time curve

- $dN = C(t) \cdot v \cdot dt \rightarrow \int_0^\infty dN = N_0 = \int_0^\infty C(t) \cdot v \cdot dt$ and

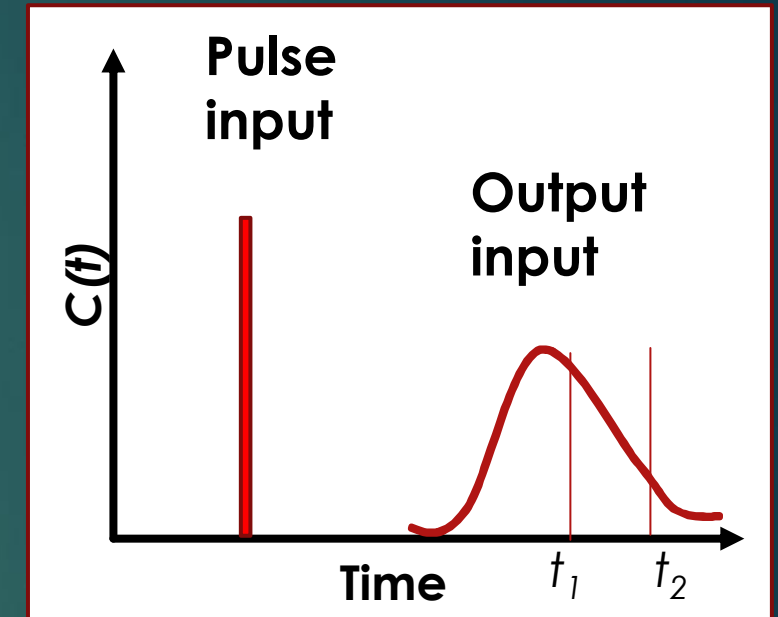
$$E(t) = \frac{C(t) \cdot v}{\int_0^\infty C(t) \cdot v \cdot dt} = \frac{C(t)}{\int_0^\infty C(t) dt}$$



Residence time distribution function is also expressed in its integral form

$$\int_{t_1}^{t_2} E(t) dt = \text{The fraction of material leaving the reactor that has resided in the reactor between } t_1 \text{ and } t_2$$

$$\text{Furthermore, } \int_0^{\infty} E(t) dt = 1$$



- Sometimes there are difficulties with the pulse technique, such as:
 - injection must take place in a short time compared to the residence time,
 - negligible dispersion between point of injection and entrance to the reactor, and
 - the $C(t)$ vs t curve has a long tail

