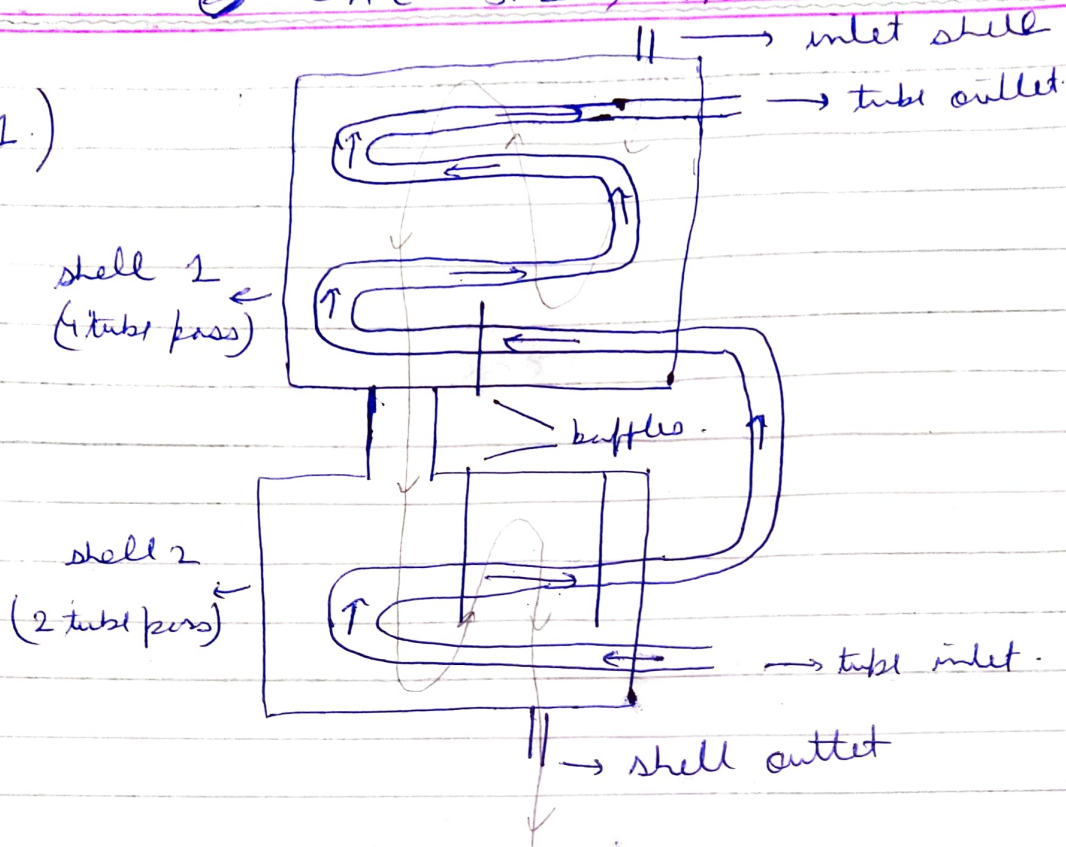


CHE-312, ASSIGNMENT-6

1.)



2.) log mean temperature diff. (LMTD)

$$\Delta T_{lm} = \frac{\Delta T_1 - \Delta T_2}{\ln(\Delta T_1 / \Delta T_2)}$$

average mean temperature diff (AMTD)

$$\Delta T_{am} = \frac{\Delta T_1 + \Delta T_2}{2}$$

ΔT_1 is temp difference b/w hot & cold fluid at inlet
 ΔT_2 is temp difference b/w hot & cold fluid at outlet

if $\Delta T_1 = \Delta T_2$, $\boxed{AMTD = \Delta T_1 = \Delta T_2}$

now, we write $\ln(\Delta T_1 / \Delta T_2)$ as $\ln\left(1 + \frac{\Delta T_1 - \Delta T_2}{\Delta T_2}\right)$

using Taylor series expansion

$$\ln(\Delta T_1 / \Delta T_2) = \left(\frac{\Delta T_1 - \Delta T_2}{\Delta T_2}\right)$$

since $\ln(1+x) \approx x$

$$\boxed{LMTD = \frac{(\Delta T_1 - \Delta T_2) \Delta T_2}{(\Delta T_1 - \Delta T_2)} = \Delta T_1 = \Delta T_2}$$

$AMTD = LMTD$ if temp. diff. b/w hot & cold fluid is constant throughout the length of heat exchanger.

also, $\Delta T_1 = \Delta T_2$ when $C_c \approx C_h$

This is also applicable when diff. b/w ΔT_1 & ΔT_2 is not very large compared to values of ΔT_1 & ΔT_2

when ΔT_1 differs from ΔT_2 by not more than 40%. Then error in using $AMTD$ is less than 1% compared to $LMTD$.

3) Given:

$$c_{p \text{ water}} = 4180 \text{ J/kg K}$$

$$c_{p \text{ geowater}} = 4310 \text{ J/kg K}$$

$$\dot{m}_{\text{water}} = 0.2 \text{ kg/s}$$

$$\dot{m}_{\text{geowater}} = 0.3 \text{ kg/s}$$

$$U = 550 \text{ W/m}^2 \text{ K}$$

$$D = 0.8 \text{ cm} = 8 \times 10^{-3} \text{ m}$$

rate of heat transfer in heat exchanger

$$\dot{Q} = [\dot{m} c_p (T_{\text{out}} - T_{\text{in}})]_{\text{water}}$$

$$\boxed{\dot{Q} = 29.26 \text{ kW}}$$

the outlet temp of geothermal water:

$$\dot{Q} = [\dot{m} c_p (T_{\text{in}} - T_{\text{out}})]_{\text{geo}}$$

$$\boxed{T_{\text{out}} = 117.4^\circ \text{C}}$$

now we will calculate ΔT_{em}

$$\Delta T_{\text{em}} = \frac{\Delta T_1 - \Delta T_2}{\ln(\Delta T_1 / \Delta T_2)}$$

$$\Delta T_1 = 140 - 28 = 112^\circ \text{C}$$

$$\Delta T_2 = 117.4 - 60 = 57.4^\circ \text{C}$$

$$\therefore \boxed{\Delta T_{\text{em}} = 82.9^\circ \text{C}}$$

for surface area of heat exchanger

$$\dot{Q} = U A_s \Delta T_{\text{em}}$$

solving for A_s ,

$$\boxed{A_s = 0.642 \text{ m}^2}$$

$$\therefore \text{length of tube} = \frac{A_s}{\pi D} \Rightarrow$$

$$\boxed{L = 25.5 \text{ m}}$$

(Ans)

4.) modifying the parallel flow heat exchanger to counter flow heat exchanger

$$\Delta T_1 = 140 - 60 = 80^\circ\text{C}$$

$$\Delta T_2 = 117.37 - 25 = 92.37^\circ\text{C}$$

$$\Delta T_{\text{em}} = 86.04^\circ\text{C}$$

$$\dot{Q} = UA_s(\Delta T_{\text{em}})$$

solving for A_s

$$A_s = 0.62$$

$$A_s = \pi D L$$

$$L = 24.6 \text{ m}$$

∴ the modification, i.e., change parallel flow heat exchanger to a counter flow heat exchanger is good.

5). Given : $T_{in H} = 95^\circ C$
 ~~$T_{out H} = 20^\circ C$~~
 $T_{in C} = 20^\circ C$
 $T_{out H} - T_{in C} = 15^\circ C$
 $\dot{m}_H = 1.5 \dot{m}_C$
 $UA = 1400 W/K$
 $c_p = 4180 J/kg \cdot K$

a) $C_h = \dot{m}_h C_{ph} = 1.5 \dot{m}_c (4.18) = 6.27 \dot{m}_c$
 $C_c = 4.18 \dot{m}_c$

$$C_{min} = C_c = 4.18 \dot{m}_c$$

$$C = \frac{C_{min}}{C_{max}} = \frac{4.18 \dot{m}_c}{6.27 \dot{m}_c}$$

$$C = 0.667$$

now the rate of heat transfer

$$\dot{Q} = C_c (T_{c out} - T_{c in})$$

$$\dot{Q} = 4.18 \dot{m}_c (T_{c out} - 20) \quad \text{--- (1)}$$

also

$$\dot{Q} = C_h (T_{h in} - T_{h out})$$

$$\dot{Q} = 6.27 \dot{m}_c (95 - (T_{c out} + 15)) \quad \text{--- (2)}$$

solving (1) & (2) to get $T_{c out}$

$$T_{c out} = 56^\circ C$$

b) effectiveness of heat exchanger

$$\varepsilon = \frac{\dot{Q}}{\dot{Q}_{max}} = \frac{C_c (T_{c out} - T_{c in})}{C_c (T_{h in} - T_{c in})}$$

$$\varepsilon = 0.48$$

c) NTU of heat exchanger

$$NTU = \frac{1}{C-1} \ln \left(\frac{\varepsilon-1}{\varepsilon C-1} \right)$$

$$NTU = 0.805$$

we will obtain \dot{m}_c from NTU definition

$$NTU = \frac{UA_s}{C_{min}} = \frac{1400 \text{ kW/}^\circ\text{C}}{4.18 \dot{m}_c}$$

$$\therefore \boxed{\dot{m}_c = 0.416 \text{ kg/s}}$$

d.)

rate of heat transfer

$$\dot{Q} = \dot{m}_c C_{pc} (T_{c \text{ out}} - T_{c \text{ in}})$$

$$\boxed{\dot{Q} = 62.6 \text{ kW}}$$

(Ans)