# Ch. 3: Fixed Income Securities

IME 611



- Financial Instruments Bonds, annuities, futures, mortgages etc.
  - Traded as a piece of paper or entry in a database
  - Value derived from their promises
- If there is a well-developed market for an instrument, for its trading, then that instrument is termed a **security**
- **Fixed income securities** are financial instruments that are traded in market
  - Promise a fixed income to the holder over a span of time and the eventual return of principal at maturity



#### Savings Deposits

- Demand deposits depositors can withdraw any or all of funds without penalty or prior notice. Interest rate depends on market conditions – regular checking, and savings account
- Term (time) deposits deposit is maintained for a given length of time and the interest is guaranteed
  - Certificate of deposits (CD) like term deposits, offered by banks that offer an interest premium for a fixed deposit for a given time period

- Money Market Instruments Money market refers to the market for short-term (1 year or less) loans by corporations and financial intermediaries
  - Commercial papers unsecured loans to corporations
- Government Securities means to obtain loan
  - Treasury bills short-term fixed maturity, can be redeemed easily prior to the maturity
  - Treasury notes maturities of 1 to 10 years, a coupon payment every 6 months until maturity
  - Treasury bonds maturities of more than 10 years, similar to treasury notes



- Other Bonds
  - Zero-coupon bonds Gives face value of the bond upon reaching maturity
  - Municipal bonds Issued by state and local governments - NHAI
  - Corporate bonds Issued by corporations



#### Mortgages

- A future homeowner sells a home mortgage to generate immediate cash to pay for a home. It is structured so that equal monthly payments are made throughout its term.
- Allows for early repayment the income stream is not completely fixed
- Usually a contract between two parties
- Mortgages can be bundled into large packages and traded among financial institutions – called Mortgage-Backed Securities



#### Annuities

- A contract that pays the holder (the annuitant) money periodically (usually annually hence the term annuity), for a fixed period
- Many variations, for example pension benefits
  - Periodically pay a fixed amount until a random time,
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## Value Formulas: Perpetual Annuities

- Fixed income instrument which pays a fixed sum periodically *forever* (perpetuity)
- The present value P of a perpetual annuity that pays an amount A every period, beginning one period from the present, where r is the one-period interest rate is,

$$P = \frac{A}{r}$$

$$P = \sum_{k=1}^{\infty} \frac{A}{(1+r)^k} = \frac{A}{r}$$

## Finite-life Streams

• If the stream consists of *n* periodic payments of amount *A*, then

$$P = \sum_{k=1}^{n} \frac{A}{(1+r)^k} = \frac{A}{r} \left[ 1 - \frac{1}{(1+r)^n} \right]$$

- Professional tables as a function of  $\frac{P}{A}$ , r and n
- **Amortization:** the process of substituting periodic payments (A) for a current obligation (P)



## Loan Calculation

- Suppose you borrow ₹100,000 from the local bank. You repay it monthly at the yearly interest rate of 12% compounded monthly over 5 years. How much are the monthly payments?
- n = 60, r = 1%, P = ₹100,000 therefore A = ₹2224.5



#### Purchase of a New Machine

- The purchase of new machine for ₹100,000 (at t = 0) is expected to generate revenues of ₹25,000 for the next 10 years starting at year 1. Is this a profitable investment at discount rate of 16%
  - NPV of the project ₹ 1,20,830.69
  - Annuity for the project ₹ 20690.11 < ₹25,000</li>



# Annual Percentage Rate (APR)

	Pts	Term	Max amt	APR
Rate			\$203,150	7.883
7.625	1.00	30 yr	\$203,150	8.083
7.875	.50	30 yr		8.399
8.125	2.25	30 yr	\$600,000	
7.000	1.00	15 yr	\$203,150	7.429
7.500	1.00	15 yr	\$600,000	7.859

- APR describes fee and expenses
- **Points** is the % of the loan amount that is charged for providing the mortgage
- Example: consider the first entry, it has monthly payment *A* = ₹1474
  - □ Using  $r = \frac{0.07625}{12}$ , and A = ₹1474, total payment is, ₹208,267
  - Total fee and expenses are 208,267 203,150 = 5,117
  - The loan fee is 1 point, i.e., 2032
  - Hence, other expenses are: 5117-2032=3085

