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Automatic Graph Tracking in Dynamic Probabilistic Programs via Source Transformations

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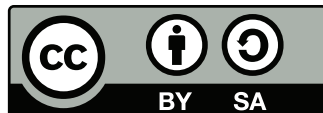
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The \LaTeX source of this document is available at
<https://github.com/philpsgabler/master-thesis>
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ABSTRACT

This thesis proposes a novel approach for the implementation of a tracking system to facilitate program analysis, based on program transformations. The system is then applied to a specific problem in the field of probabilistic programming.

The main contribution is a general system for the extraction of rich computation graphs in the Julia programming language, based on a transformation of the intermediate representation (IR) used by the compiler. These graphs contain the whole recursive structure of any Julia program in terms of executed IR instructions. The system is flexible enough to be used for multiple purposes that require dynamic program analysis or abstract interpretation, such as automatic differentiation or dependency analysis.

The second part of the thesis describes the application of this graph tracking system to probabilistic programs written for Turing, a probabilistic programming system implemented as an embedded language within Julia. Through this, an executed Turing model can be analyzed, and the dependency structure of involved random variables be extracted from it. Given this structure, analytical Gibbs conditionals can be calculated and passed to Turing's inference mechanism, where they are used in Markov-Chain Monte Carlo samplers approximating the modelled distribution.

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1 Introduction

1.1 PROBLEM DESCRIPTION

1.2 RELATED WORK

2 Background

This section provides the background for the concepts used later in chapters 3 and 4. On the one hand, it gives a quick overview of Bayesian inference and probabilistic programming in general, necessary to understand the requirements and usual approaches of probabilistic programming systems.

On the other hand, the machinery and language used to develop the graph tracking system forming the main part of the work are described. This consists firstly of a short introduction to graph tracking and source-to-source automatic differentiation, which contain many ideas and terminology that will be used later, and often provided inspiration. Second, the basic notions and techniques of the Julia compilation process, as well as the language’s metaprogramming capabilities are described, which form the basis of the implementation.

2.1 BAYESIAN INFERENCE AND PROBABILISTIC PROGRAMMING

Probabilistic programming is a means of describing stochastic models through the syntax of a programming language. These models describe probability distributions as stochastic functions. Probabilistic programmes distinguish themselves from normal programs by the possibility of being sampled from conditionally, with some of the internal variables fixed to observed values. While probabilistic programming systems are often implemented as separate, domain-specific languages, they can also be embedded into “host” programming languages with sufficient syntactic flexibility. The latter is advantageous if one wants to use regular general-purpose programming constructs or interact with other functionalities of the host language.

2.2 COMPUTATION GRAPHS AND AUTOMATIC DIFFERENTIATION

2.3 METAPROGRAMMING AND COMPILATION IN JULIA

3 Implementation of Dynamic Graph Tracking in Julia

3.1 AUTOMATIC GRAPH TRACKING AND EXTENDED WENGERT LISTS

4 Graph Tracking in Probabilistic Models

4.1 DEPENDENCY ANALYSIS IN DYNAMIC MODELS

4.2 JAGS-STYLE AUTOMATIC CALCULATION OF GIBBS CONDITIONALS

4.3 EVALUATION

5 Discussion

5.1 FUTURE WORK

COLOPHON

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