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Automatic Graph Tracking in Dynamic Probabilistic Programs via Source Transformations

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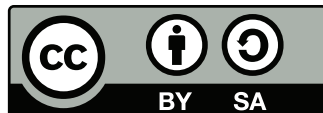
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The \LaTeX source of this document is available at
<https://github.com/philpsgabler/master-thesis>
or upon request from the author.¹

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ABSTRACT

Probabilistic programming is a means of describing stochastic models through the syntax of a programming language. These models describe probability distributions as stochastic function. Probabilistic programmes distinguish themselves from normal programs by the possibility of being sampled from conditionally, with some of the internally variables fixed to observed values. While probabilistic programming systems are often implemented as separate, domain-specific languages, they can also be embedded into “host” programming languages with sufficient syntactic flexibility. The latter is advantageous if one wants to use regular general-purpose programming constructs or interact with other functionalities of the host language.

This thesis first presents a general system for extracting rich computation graphs in the Julia programming language. These graphs contain the whole recursive structure of a program in terms of executed instructions of the intermediate representation used by the compiler. The system is flexible enough to be used for multiple purposes that require dynamic program analysis or abstract interpretation, such as automatic differentiation or dependency analysis.

The second contribution is the application of the described graph tracking system to programs written for Turing, a probabilistic programming system implemented as an embedded language within Julia. The functions describing a Turing model can be analyzed, and from them the dependency structure of involved random variables be extracted. Given this structure, analytical Gibbs conditionals can be calculated and passed to Turing’s inference mechanism, where they are used in Markov-Chain Monte Carlo samplers approximating the modelled distribution.

Contents

1	Introduction	1
1.1	Problem Description	1
1.2	Related Work	1
2	Background	3
2.1	Bayesian Inference and Probabilistic Programming	3
2.2	Computation Graphs and Automatic Differentiation	3
2.3	Metaprogramming and Compilation in Julia	3
3	Implementation of Dynamic Graph Tracking in Julia	5
3.1	Automatic Graph Tracking and Extended Wengert Lists	5
4	Graph Tracking in Probabilistic Models	7
4.1	Dependency Analysis in Dynamic Models	7
4.2	JAGS-Style Automatic Calculation of Gibbs Conditionals	7
4.3	Evaluation	7
5	Discussion	9
5.1	Future Work	9
	Bibliography	11

1 Introduction

1.1 PROBLEM DESCRIPTION

1.2 RELATED WORK

2 Background

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2.1 BAYESIAN INFERENCE AND PROBABILISTIC PROGRAMMING

2.2 COMPUTATION GRAPHS AND AUTOMATIC DIFFERENTIATION

2.3 METAPROGRAMMING AND COMPILATION IN JULIA

3 Implementation of Dynamic Graph Tracking in Julia

3.1 AUTOMATIC GRAPH TRACKING AND EXTENDED WENGERT LISTS

4 Graph Tracking in Probabilistic Models

4.1 DEPENDENCY ANALYSIS IN DYNAMIC MODELS

4.2 JAGS-STYLE AUTOMATIC CALCULATION OF GIBBS CONDITIONALS

4.3 EVALUATION

5 Discussion

5.1 FUTURE WORK

COLOPHON

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