# NTUT\_Kn1ghts ICPC Team Notebook

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# 1 Dynamic programming algorithms

# 1.1 Longest common subsequence (LCS)

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;

struct LCS{
   int step , max_len ;
}Dp[5000][5000];

int main()
```

```
#ifdef LOCAL
    freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
    int intX , intY , Min_step , Max_len ;
    while(cin >> intX >> strX >> intY >> strY ) {
         for(int i = 0 ; i <= intY ; i++) {</pre>
             Dp[0][i].max_len = 0 ;
             Dp[0][i].step = i ;
        for(int i = 0 ; i <= intX ; i++) {
             Dp[i][0].max\_len = 0 ;
             Dp[i][0].step = i;
        Min_step = 0;
        for(int i = 1 ; i <= intX ; i++) {</pre>
             for(int j = 1 ; j <= intY ; j++) {</pre>
                 if(strX[i-1] == strY[j-1]){
                      Dp[i][j].max_len = Dp[i-1][j-1].max_len +1;
                      Dp[i][j].step = Dp[i-1][j-1].step;
                      //cout << strX[i-1] << ' ' << strY[j-1] << ' ' << Dp[i][j].max_len << '\n'; //cout << strX[i-1] << ' ' << strY[j-1] << ' ' << Dp[i][j].step << '\n';
                      Dp[i][j].max_len = max(Dp[i-1][j].max_len , Dp[i][j-1].max_len );
                      Dp[i][j].step = min( min(Dp[i-1][j-1].step , Dp[i][j-1].step ) , Dp[i-1][j].step )
        cout << Dp[intX][intY].step << '\n';</pre>
    return 0;
```

## 1.2 Max 2D range sum

```
// Max 2D Range Sum - UVa 108 - solved with DP O(n^4).
// Abridged problem statement: Given an n x n square matrix of integers A where
// each integer ranges from [-127..127], find a sub-matrix of A with the maximum
#include <bits/stdc++.h>
using namespace std;
int A[200][200];
int main() {
  int n; scanf("%d", &n);
                                                       // square matrix size
  for (int i = 0; i < n; ++i)
for (int j = 0; j < n; ++j) {</pre>
       scanf("%d", &A[i][j]);
      if (i > 0) A[i][j] += A[i-1][j];
if (j > 0) A[i][j] += A[i][j-1];
                                                       // add from top
                                                       // add from left
      if (i > 0 && j > 0) A[i][j] -= A[i-1][j-1];// avoid double count
                                                       // inclusion-exclusion
  int maxSubRect = -127*100*100;
                                                       // the lowest possible val
  for (int i = 0; i < n; ++i)
  for (int j = 0; j < n; ++j)</pre>
                                                       // start coordinate
       for (int k = i; k < n; ++k)
        for (int 1 = j; 1 < n; ++1) {
  int subRect = A[k][1];</pre>
                                                        // end coord
                                                       // from (0, 0) to (k, 1)
           if (i > 0) subRect -= A[i-1][1];
           if (j > 0) subRect -= A[k][j-1];
           if (i > 0 && j > 0) subRect += A[i-1][j-1]; // O(1)
           maxSubRect = max(maxSubRect, subRect); // the answer is here
  printf("%d\n", maxSubRect);
  return 0;
```

# 1.3 Traveling salesman problem (TSP)

```
// This is a solution for UVa 10496 - Collecting Beepers. The problem is a // variant of the Traveling Salesman Problem (TSP): Given n cities and their // pairwise distances in the form of a matrix 'dist' of size n * n, compute the // minimum cost of making a tour that starts from any city s, goes through all // the other n - 1 cities exactly once, and finally returns to the city s. In // this case, the salesman is Karel in a 2D world who can only move along the // x and y axis. The cities are beepers whose coordinates are given, from which
```

```
// pairwise distances can be calculated. Algorithm takes time O(2^n * n^2).
// INPUT: The first line is the number of test cases. The first line of each
// test case is world's size (x-size and y-size). Next is the starting position
// of Karel. Next is the number of beepers. Next are the beepers' x- and y-
// OUTPUT: For each test case, output the minimum distance to move from Karel's
// starting position to each of the beepers and back to the starting position.
#include <bits/stdc++.h>
using namespace std;
#define LSOne(S) ((S) & -(S))
const int MAX n = 11;
int dist[MAX_n][MAX_n], memo[MAX_n][1<<(MAX_n-1)]; // Karel + max 10 beepers</pre>
int dp(int u, int mask) {
  if (mask == 0) return dist[u][0];
  int &ans = memo[u][mask];
  if (ans != -1) return ans;
                                                    // computed before
  ans = 2000000000;
  int m = mask:
  while (m) {
                                                    // up to O(n)
    int two_pow_v = LSOne(m);
                                                    // but this is fast
    int v = __builtin_ctz(two_pow_v)+1;
                                                    // offset v by +1
    ans = min(ans, dist[u][v] + dp(v, mask^two_pow_v)); // keep the min
    m -= two pow v:
  return ans:
  int TC; scanf("%d", &TC);
  while (TC--) {
    int xsize, ysize; scanf("%d %d", &xsize, &ysize); // these two values are not used
    int x[MAX_n], y[MAX_n];
    scanf("%d %d", &x[0], &y[0]);
int n; scanf("%d", &n); ++n;
                                                    // include Karel
    for (int i = 1; i < n; ++i)
  scanf("%d %d", &x[i], &y[i]);</pre>
                                                    // Karel is at index 0
   for (int i = 0; i < n; ++i)
for (int j = i; j < n; ++j)</pre>
                                                    // build distance table
        dist[i][j] = dist[j][i] = abs(x[i]-x[j]) + abs(y[i]-y[j]); // Manhattan distance
    memset (memo, -1, sizeof memo);
    printf("The shortest path has length %d\n", dp(0, (1 << (n-1))-1)); // DP-TSP
  return 0;
```

# 2 Graph algorithms

# 2.1 All-pairs shortest paths (APSP)

```
// All-Pairs Shortest Paths (APSP) solved with Floyd Warshall O(V^3).
   // precondition: AdjMat[i][j] contains the weight of edge (i, j)
    // or INF (1B) if there is no such edge
   // AdjMat is a 32-bit signed integer array
   // let p be a 2D parent matrix, where p[i][j] is the last vertex before j
    // on a shortest path from i to j, i.e. i \rightarrow ... \rightarrow p[i][j] \rightarrow j
   for (int k = 0; k < V; ++k) // remember that loop order is k->i->j
       for (int i = 0; i < V; ++i)
           for (int j = 0; j < V; ++j)
               if (AdjMat[i][k] + AdjMat[k][j] < AdjMat[i][j])</pre>
                   AdjMat[i][j] = AdjMat[i][k] + AdjMat[k][j];
                   p[i][j] = p[k][j];
// print shortest paths
void printPath(int i, int j)
   if (i != j) printPath(i, p[i][j]);
   printf(" %d", j);
```

# 2.2 Bipartite matching BFS by David

```
#include <iostream>
#include <cstring>
#include <cstdio>
#include <vector>
#define LOCAL
using namespace std;
int fp[100010] ,fq[100010] ;
int vfp[100010] ,vfq[100010] ;
int turn = 0;
vector<int> cp[100010] , cq[100010];
int BFSBMfp(int n) {
    vfp[n] = turn ;
for(int i = 0 ; i < cp[n].size() ; i++ ) {
    if(vfq[cp[n][i]] != turn) {</pre>
             vfg[cp[n][i]] = turn;
             if(fq[cp[n][i]] == -1 || BFSBMfp(fq[cp[n][i]])){
                 fp[n] = cp[n][i];
                  fq[cp[n][i]] = n;
                  return 1 ;
    return 0 :
int main()
    ios::sync_with_stdio(false);
    cin.tie(0);
    cout.tie(0);
    int n ,p ,q ,k ,x, y ;
    while (n--) {
        cin >> p >> q >> k;
        int MaxnPQ = max(p,q);
for(int i = 1; i <= MaxnPQ; i++) {</pre>
             cp[i].clear();
             fp[i] = -1;
            cq[i].clear();
fq[i] = -1;
        for(int i = 0 ; i < k ; i++) {
             cin >> x >> y ;
             cp[x].push_back(y);
             cq[y].push_back(x);
             if(fp[x] == -1 && fq[y] == -1){
                  fp[x] = y;
                  fq[y] = x;
                 cnt++;
        for(int i = 1 ; i <= p ; i++) {
             if(fp[i] == -1){
                  turn++:
                 if(BFSBMfp(i))
                    cnt++;
        cout << cnt << '\n';
    return 0;
```

## 2.3 Centroid decomposition

```
#include<iostream>
#include <bits/stdc++.h>
#define LOCAL
#define MAXN 50005
using namespace std;
int n , k , a , b ;
int ans , cnt ;
int Max[MAXN] , sz[MAXN] , rt ;
int head[MAXN], dis[MAXN];
bool vis[MAXN] ;
struct node{
    int v . nx :
}Edge[MAXN*2];
void init(int n ){
   Max[0] = n;
ans = cnt = 0;
    for (int i = 0; i \le n; i++) {
```

```
head[i] = -1;
        vis[i] = 0 ;
void add(int u , int v) {
    Edge[cnt].v = v ;
Edge[cnt].nx = head[u] ;
    head[u] = cnt++;
void get_rt(int u , int fa ){
    sz[u] = 1 ; Max[u] = 0 ;
for(int i = head[u] ; ~i ; i=Edge[i].nx) {
        int v = Edge[i].v ;
        if(vis[v] | v == fa ) continue;
        get_rt(v,u);
        sz[u] += sz[v];
        Max[u] = max(Max[u], sz[v]);
    Max[u] = max(Max[u], n - sz[u]);
    if(Max[rt] > Max[u])
        rt = u;
void get_dis(int u , int fa , int d){
    for(int i = head[u]; i = Edge[i].nx){
        int v = Edge[i].v ;
        if(vis[v] || v == fa ) continue;
dis[++cnt] = d + 1;
        get_dis(v,u,dis[cnt]);
int get_ans(int u , int d ) {
    dis[cnt=1] = d;
    get_dis(u,0,d);
    sort(dis+1 , dis+cnt+1) ;
    int 1 = 1 , ans = 0 ;
    while(1 < cnt && dis[1] + dis[cnt] < k ) 1++ ;
while(1 < cnt && dis[1] <= k - dis[1]){</pre>
        ans += upper_bound(dis + 1 + 1 , dis + cnt + 1 , k - dis[1]) - lower_bound(dis+1+1 , dis+cnt+1
               , k-dis[1]);
    return ans ;
void dfs(int u ){
    vis[u] = 1;
    //cout << rt << ' ' << u << '\n';
    ans += get_ans(u , 0);
for(int i = head[u] ; ~i ; i = Edge[i].nx){
        int v = Edge[i].v ;
        if(vis[v]) continue;
        ans -= get_ans(v, 1);
        n = sz[v] , rt = 0 , get_rt(v,u);
        dfs(rt);
int main(){
//#ifdef LOCAL
// freopen("in1.txt" , "r" , stdin);
//#endif // LOCAL
    cin >> n >> k;
    init(n):
    for (int i =1; i < n ; i++) {</pre>
        cin >> a >> b ;
        add(a,b);
        add(b,a);
    rt = 0 ; get_rt(1,0);
    dfs(rt);
    cout << ans << '\n' ;
```

# 2.4 Detect negative weight cycle

```
for (int j = 0; j < (int)AL[u].size(); ++j) // [A]djacency [L]ist
{
    ii vw = AL[u][j];
    dist[vw.first] = min( dist[vw.first], dist[u] + vw.second ); // relax</pre>
```

#### 2.5 DFS

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
int m , n , flag=1;
int Maxn_city = 0 , Maxn_path = 0 ;
vector<int>tree[200020] ;
int city[200020] = {};
int visit[200020] = {};
vector<int> travel ;
void BFS_to_large_path(int root ) {
    visit[root] = 1;
    travel.push_back(root);
    int node = tree[root][i] ;
        if(!visit[node]){
            BFS_to_large_path(node);
            travel.pop_back();
            visit[root] = 0 ;
    //debug to check large path
    //if (root == 1)
         cout << "1=" << travel.size() << ' ' << Maxn_path << ' ' << city[root] << '\n';
    if(city[root] && travel.size() > Maxn_path){
        Maxn_city = travel[travel.size()/2];
Maxn_path = travel.size();
void BFS_to_other_path(int root ,int path) {
    visit[root] = 1;
for(int i = 0; i < tree[root].size(); i++){
   int node = tree[root][i];</pre>
        if(!visit[node]){
            BFS_to_other_path(node , path+1);
            visit[root] = 0;
     //debug
    if(root == 1)
        cout << "city=" << root << " path= " << path << '\n' ;
    if(city[root] && path != Maxn_path)
        flag = 0;
int main(){
#ifdef LOCAL
    freopen("in1.txt" , "r" , stdin);
#endif // LOCAL
    cin >> n >> m;
    int a , b ;
    for (int i = 0; i < n-1; i++) {
        cin >> a >> b ;
        tree[a].push_back(b) ;
        tree[b].push_back(a) ;
    for (int i = 0; i < m; i++) {
        cin >> a :
        city[a] = 1;
    BFS_to_large_path(a);
    //visit[a] = 0;
    BFS_to_other_path(Maxn_city , 1 );
    if(flag)
        cout << "YES\n" << Maxn_city ;</pre>
    else
        cout << "NO" ;
    cout << "Maxn_path= " << Maxn_path << " Maxn_city= " << Maxn_city << '\n' ;
```

### 2.6 Dijkstra by Bill

```
// Dijkstra implementation for negative weight edges O((V + E) log V)
    vi dist(V, INF); dist[s] = 0;
    priority_queue< ii, vii, greater<ii>> pq;
    pq.push(ii(O, s));
    while (!pq.empty())
{
        if front = pq.top(); pq.pop();
        int d = front.first;
        int u = front.second;
        if (d > dist[u]) continue;
        for (int i = 0; i < (int)AL[u].size(); ++i) // [A]djacency [L]ist
        {
            ii vw = AL[u][i];
            int v = vw.first;
            int w = vw.second;
            if (dist[u] + w < dist[v])
            {
                 dist[v] = dist[u] + w; // relax operation
                  pq.push(ii(dist[v], v));
            }
        }
} // this variant can cause duplicate items in the priority queue</pre>
```

# 2.7 Dijkstra by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define INF 99999999
using namespace std;
int intMap[1010][1010] = {} , intValue[1010][1010] = {};
int m , n ;
struct Node (
    int x , y , v ;
void read( int _x , int _y , int _v) {
        x = _x ; y = _y ; v = _v ;
    bool operator < (const Node &a) const{</pre>
         return v > a.v ;
} nodNode;
void print_map(){
    for(int i = 1; i <= n; i++) {
    for(int j = 1; j <= m; j++) {
             if (intValue[i][j] == 99999999)
    cout << 'r' << ' ';</pre>
             else
                 cout << intValue[i][i] << ' ';</pre>
         cout << '\n' ;
    cout << '\n' ;
void bfs() {
    int x , y , intDirection[4][2] = {-1,0 ,0,1 ,1,0 ,0,-1};
    int intDx , intDy ;
    Node nodTemp ;
    priority_queue<Node> deqNode ;
    nodTemp.read(1,1,0);
    degNode.push(nodTemp);
    while(deqNode.size()){
        x = deqNode.top().x;
         y = deqNode.top().y;
         deqNode.pop();
         for (int i = 0; i < 4; i++) {
             intDx = intDirection[i][0] + x ;
             intDy = intDirection[i][1] + y ;
             //cout << intDx << ' ' << intDy << ' ' << intValue[x][y] + intMap[intDx][intDy] << ' ' <<
                   i << '\n';
             if(intValue[x][y] + intMap[intDx][intDy] < intValue[intDx][intDy] ) {</pre>
                 intValue[intDx][intDy] = intValue[x][y] + intMap[intDx][intDy];
nodTemp.read(intDx , intDy , intValue[intDx][intDy]);
```

```
deqNode.push(nodTemp) ;
        //print_map();
int main() {
#ifdef LOCAL
    freopen("in1.txt" , "r" , stdin );
    freopen("out.txt" , "w" , stdout) ;
#endif
ios::sync with stdio(false);
    int intCase ;
    cin >> intCase ;
    while(intCase --) {
        cin >> n >> m;
        for(int i = 1 ; i <= n ; i++) {</pre>
            for(int j = 1; j \le m; j++) {
                 cin >> intMap[i][j];
                intValue[i][j] = INF ;
        for(int i = 1 ; i <= n ; i++) {
            intValue[i][0] = 0;
intValue[i][m+1] = 0;
            intMap[i][0] = INF +1;
            intMap[i][m+1] = INF +1;
        for(int i = 1; i <= m; i++) {
            intValue[0][i] = 0;
            intValue[n+1][i] = 0;
            intMap[0][i] = INF +1;
            intMap[n+1][i] = INF +1;
        intValue[1][1] = intMap[1][1];
        //debug
        //cout << intValue[1][1] << '\n';
        cout << intValue[n][m] << '\n';</pre>
        return 0;
```

#### 2.8 Euler tour

```
list<int> cyc; // we need list for fast insertion in the middle
void EulerTour(list<int>::iterator i, int u)
    for (int j = 0; j < (int)AL[u].size(); ++j) // [A]djacency [L]ist</pre>
        int v = vw.first;
        if (vw.second)
                          // if this edge can still be used
            vw.second = 0;  // remove this edge
            // remove bi-directional edge
for (int k = 0; k < (int) AL[v].size(); ++k)</pre>
                 ii& uw = AL[v][k];
                 if (uw.first == u && uw.second)
                     uw.second = 0;
                     break;
            // continue the tour
            EulerTour(cyc.insert(i, u), v);
   }
// inside int main()
    cvc.clear();
    EulerTour(cyc.end(), A); // 'cyc' contains an Euler tour starting at 'A'
    for (list<int>::iterator i = cyc.begin(); i != cyc.end(); ++i)
        printf("%d\n", *i);
```

# 2.9 Find articulation points and bridges

```
// Find articulation points & bridges solved with DFS O(V + E).
void articulationPointAndBridge(int u)
    for (int i = 0; i < (int)AL[u].size(); ++i) // [A]djacency [L]ist</pre>
       int v = AL[u][i].first;
       if (dfs_num[v] == UNVISITED)
                                     // a tree edge
           dfs_parent[v] = u;
           if (u == dfsRoot) ++rootChildren; // special case if 'u' is a root
           articulationPointAndBridge(v);
           if (dfs_low[v] >= dfs_num[u]) articulation_vertex[u] = true;
           if (dfs_low[v] > dfs_num[u]) printf("Edge (%d, %d) is a bridge\n", u, v);
           dfs_low[u] = min( dfs_low[u], dfs_low[v] );  // update dfs_low[u]
       else if (v != dfs_parent[u]) dfs_low[u] = min( dfs_low[u], dfs_num[v] ); // update dfs_low[u]
// inside int main()
   dfsNumberCounter = 0;
   dfs_num.assign(V, UNVISITED);
   dfs_low.assign(v, 0);
   dfs_parent.assign(V, 0);
   articulation_vertex.assign(V, 0);
   printf("Bridges:\n");
   for (int u = 0; u < V; ++u)
   if (dfs_num[u] == UNVISITED)</pre>
           dfsRoot = u;
           rootChildren = 0;
           articulationPointAndBridge(u);
           articulation_vertex[dfsRoot] = (rootChildren > 1);
    printf("Articulation Points:\n");
   for (int u = 0; u < V; ++u)
       if (articulation_vertex[u]) printf(" Vertex %d\n", u);
```

### 2.10 Floyd Warshall by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
char before[520][520] = {};
int after[520][520] = {};
int main()
     freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
     for(int i = 0 ; i < n ; i++) {
   for(int j = 0 ; j < n ; j++)
      cin >> before[i][j] ;
     for (int i = 0; i < n; i++) {
         for (int j = i+1; j < n; j++) {
              int sum = 0 ;
              for (int k = i + 1 ; k < j ; k++) {
                   if(after[i][k])
                       sum += before[k][j]-'0';
              if( (sum +1) % 10 == before[i][j] - '0'){
                   after[i][j] = 1;
     for (int i = 0; i < n; i++) {
         for (int j = 0; j < n; j++)
              cout << after[i][j];</pre>
```

```
cout << '\n';
}
return 0;</pre>
```

#### 2.11 Graph edges property check

```
// Graph Edges Property Check solved with DFS O\left(V + E\right).
void graphCheck(int u) // DFS for checking graph edge properties
    dfs num[u] = EXPLORED;
   for (int i = 0; i < (int)AL[u].size; ++i) // [Aldjancency [L]ist
       int v = AL[u][i].first;
       if (dfs_num[v] == UNVISITED) // Tree Edge, EXPLORED->UNVISITED
            dfs_parent[v] = u;
                                // parent of this child is me
           graphCheck(v);
       else if (dfs_num[v] == EXPLORED) // EXPLORED->EXPLORED
           if (v == dfs_parent[u]) printf(" Two ways (%d, %d)-(%d, %d)\n", u, v, v, u);
           else printf(" Back Edge (%d, %d) (Cycle)\n", u, v); // can check if graph is cyclic
       else if (dfs_num[v] == VISITED)
                                          // EXPLORED->VISITED
           printf(" Forward/Cross Edge (%d, %d)\n", u, v);
   dfs_num[u] = VISITED;
// inside int main()
    dfs_num.assign(V, UNVISITED);
    dfs_parent.assign(V, 0);
   for (int u = 0; u < V; ++u)
       if (dfs_num[u] == UNVISITED)
           printf("Component %d:\n", ++numComp), graphCheck(u);
```

### 2.12 Kruskal by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define 11 long long
using namespace std;
int parent[1020];
struct edge{
    11 n1, n2, w;
}node[25020];
int compare(edge A , edge B ){
    return A.w < B.w ;
int find_root(int a) {
    if(a != parent[a] )
        return parent[a] = find_root(parent[a]);
    return a ;
int main()
#ifdef LOCAL
    freopen("in1.txt" , "r" , stdin );
freopen("out.txt" , "w" , stdout );
    int n , m , p_n1 , p_n2 ; // parent_n1 , parent_n2
    vector<int> hce ; //heavy edge circle
    while (cin >> n >> m && n + m != 0 ) {
        for(int i = 0; i < m; i++) {
             cin >> node[i].n1 >> node[i].n2 >> node[i].w ;
        for(int i = 0 ; i < n ; i++)
    parent[i] = i ;</pre>
         sort(node , node + m , compare ) ;
        hce.clear();
         //kruskal
```

```
for (int i = 0; i < m; i++) {
        p_n1 = find_root(node[i].n1);
        p_n2 = find_root(node[i].n2);
        if (p_n1 != p_n2 )
            parent[p_n2] = p_n1;
            hce.push_back(node[i].w);
        //debug
        for(int i = 0 ; i < n ; i++)
        cout << parent[i] << ' ';
cout << '\n';</pre>
    sort(hce.begin() , hce.end());
    if(hce.size()){
        for(int i = 0 ; i < hce.size()-1 ; i++)</pre>
            cout << hce[i] << ' ';
        cout << hce[hce.size()-1];
    else
        cout << "forest";
    cout << '\n' ;
return 0:
```

#### 2.13 Max flow

```
int res[MAX_V][MAX_V], mf, f, s, t;
vi p; // p stores the BFS spanning tree from s
void augment(int v, int minEdge)
    if (v == s) { f = minEdge; return; }
    else if (p[v] != -1)
        augment( p[v], min(minEdge, res[ p[v] ][ v ]) );
res[ p[v] ][ v ] -= f;
        res[v][p[v]] += f;
// inside int main(): set up 'res', 's', and 't' with appropriate values
    while (true) // O(V^3 * E) Edmonds Karp's algorithm
        vi dist(MAX_V, INF); dist[s] = 0;
        queue<int> q; q.push(s);
        p.assign(MAX_V, -1);
        while (!q.empty())
            int u = q.front(); q.pop();
if (u == t) break; // immediately stop BFS if we already reach sink t
            for (int v = 0; v < MAX_V; ++v)
                if (res[u][v] > 0 && dist[v] == INF)
                    dist[v] = dist[u] + 1, q.push(v), p[v] = u;
        augment(t, INF); // find the min edge weight 'f' in this path, if any
        if (f == 0) break; // we cannot send any more flow ('f' = 0), terminate
        mf += f;
                            // we can still send a flow, increase the max flow!
    printf("%d\n", mf);
```

### 2.14 Max cardinality bipartite matching (MCBM)

### 2.15 Minimum spanning tree (MST)

# 2.16 Strongly connected component (SCC)

```
// Tarjan O(V + E)
vi dfs_num, dfs_low, visited;
int dfsNumberCounter, numSCC;
vi S:
void tarjanSCC(int u)
    dfs_low[u] = dfs_num[u] = dfsNumberCounter++;  // dfs_low[u] <= dfs_num[u]</pre>
                      // stores 'u' in a vector baesd on order of visitation
    S.push back(u);
    visited[u] = 1;
    for (int i = 0; i < (int)AL[u].size(); ++i) // [A]djacency [L]ist</pre>
        int v = AL[u][i].first;
        if (dfs_num[v] == UNVISITED) tarjanSCC(v);
        if (visited[v]) dfs_low[u] = min( dfs_low[u], dfs_low[v] ); // condition for update
    if (dfs_low[u] == dfs_num[u])
                                     // if this is a root (start) of an SCC
                                     // this part is done after recursion
        printf("SCC %d:", ++numSCC);
        while (true)
            int v = S.back(); S.pop_back();
            visited[v] = 0;
            printf(" %d", v);
            if (u == v) break;
       printf("\n");
// inside int main()
    dfs_num.assign(V, UNVISITED);
    dfs_low.assign(V, 0);
    visited.assign(V, 0);
    dfsNumberCounter = numSCC = 0;
    for (int u = 0; u < V; ++u)
        if (dfs_num[u] == UNVISITED)
            tarjanSCC(u);
```

# 3 Greedy algorithms

#### 3.1 Interval covering

```
// This is a solution for UVa 10382 - Watering Grass. The problem is a variant
// of Interval Covering problem, which is solved by O(n) Greedy algorithm.
#include <bits/stdc++.h>
#define pb push back
#define not set -1
using namespace std:
typedef pair<double, double> dd;
typedef vector<dd> vdd;
typedef enum { STOP = 0,
               CONTINUE | status;
int n, 1, w;
vdd spinklers;
int answer;
double pivot;
struct sort compare t {
    bool operator()(dd a, dd b) const {
        return a.first < b.first || (a.first == b.first && a.second > b.second);
} sort_compare;
void InputSpinklers() {
    for (int i = 0; i < n; i++) {
   double x, r; // must be double otherwise WA.
   scanf("%lf %lf", &x, &r);</pre>
        if (w > 2 * r) // ignore spinklers that cannot cover the width of the strip.
            continue:
        if (w == 2 * r) // ignore spinklers that produce no intervals.
            continue:
        double dx = sqrt(r * r - w * w / 4.0);
        spinklers.pb(dd(x - dx, x + dx));
status Check(int& j) {
    if (j == not_set) // there is an interval after pivot that cannot be covered.
        return STOP:
    // record j.
    answer++;
    pivot = spinklers[j].second;
    if (pivot >= 1) // solution found!
void SolveIntervalCovering() {
    sort(spinklers.begin(), spinklers.end(), sort_compare);
    answer = 0:
    pivot = 0.0;
    int j = not_set;
    int iter = 0;
    while (true) {
        if (iter == spinklers.size()) // iterated through all spinklers/intervals.
            Check(j);
            break;
        if (spinklers[iter].first <= pivot) {</pre>
            if (pivot < spinklers[iter].second) // note the next candidate down!</pre>
                if (j == not_set || spinklers[iter].second > spinklers[j].second) // note down the
                      most right candidate.
                     j = iter;
                iter++;
            } else // skip intervals that are completely covered by the previously selected ones.
```

```
{
    iter++;
    }
} else // out bound.
{
    if (Check(j) == STOP) {
        break;
    }
}

if (pivot >= 1) {
        printf("%d\n", answer);
} else {
            printf("-1\n");
}
}

int main() {
    while (scanf("%d %d %d", &n, &1, &w) != EOF) {
            spinklers.clear();
            InputSpinklers();
            SolveIntervalCovering();
}
```

#### 3.2 Longest increasing subsequence (LIS)

```
#include <bits/stdc++.h>
using namespace std;
typedef vector<int> vi;
int n;
vi A;
void print_array(const char *s, vi &L, int n) {
 for (int i = 0; i < n; ++i) {
    if (i) printf(", ");
    else printf("%s: [", s);
    printf("%d", L[i]);
 printf("]\n");
                                                    // predecessor array
vi p;
void print_LIS(int i) {
                                                    // backtracking routine
 if (p[i] == -1) { printf("%d", A[i]); return; }// base case
print_LIS(p[i]);
printf(" %d", A[i]);
int memo[10010];
                                                    // old limit: up to 10^4
int LIS(int i) {
                                                    // O(n^2) overall
 if (i == 0) return 1;
  int &ans = memo[i];
  if (ans != -1) return ans;
                                                    // was computed before
                                                    // LIS can start anywhere
  for (int j = 0; j < i; ++j)
    if (A[j] < A[i])
                                                    // increasing condition
      ans = max(ans, LIS(j)+1);
                                                    // pick the max
  return ans;
int main() {
 // note: A[n-1] must be set as the largest value ("INF")
  // so that all LIS (that can start anywhere) will end at n-1
  srand(time(NULL));
  int n = 10+rand()%11;
  A.assign(n, 0);
  A[n-1] = 99;
                                                    // set A[n-1] = INF
  for (int i = 0; i < n-1; ++i)
    A[i] = rand() %101-50;
                                                    // [-50..50]
  vi sample({-7, 10, 9, 2, 3, 8, 8, 1, 2, 3, 4, 99});
  A = sample;
  printf("n = %d:", n);
  for (int i = 0; i < n; ++i)
  printf(" %d", A[i]);</pre>
  printf("\n");
  // early 2000 problems usually accept O(n^2) solution
  memset (memo, -1, sizeof memo);
```

```
printf("LIS length is %d\n\n", LIS(n-1));
                                              // with O(n^2) DP
// 2020s problems will likely only accept O(n log k) solution
// new limit: n can be up to 200K
int k = 0, lis_end = 0;
vi L(n, 0), L_id(n, 0);
p.assign(n, -1);
for (int i = 0; i < n; ++i) {
  int pos = lower_bound(L.begin(), L.begin()+k, A[i]) - L.begin();
  L[pos] = A[i];
                                                // greedily overwrite this
  L_id[pos] = i;
                                                // remember the index too
 p[i] = pos ? L_id[pos-1] : -1;
if (pos == k) {
                                                // predecessor info
                                                // can extend LTS?
                                                // k = longer LIS by +1
// keep best ending i
   k = pos+1:
    lis_end = i;
  printf("Considering element A[%d] = %d\n", i, A[i]);
  printf("LIS ending at A[%d] is of length %d: ", i, pos+1);
  printf("[");
  print_LIS(i);
  printf("]\n");
  print_array("L is now", L, k);
 printf("\n");
printf("Final LIS is of length %d: ", k);
print_LIS(lis_end); printf("\n");
assert (LIS (n-1) == k);
                                                // both must be identical
return 0;
```

### 3.3 Max 1D range sum

```
// Max 1D Range Sum solved with Jay Kadane O(n).
// inside int main()
int n = 9;
int A[] = { 4, -5, 4, -3, 4, 4, -4, 4, -5 }; // a sample array A
int sum = 0;
int ans = 0; // important, 'ans' must be initialized to 0
for (int i = 0; i < n; ++i)
{
    sum += A[i];
    ans = max(ans, sum);
    if (sum < 0) sum = 0;
}
printf("Max 1D Range Sum = %d\n", ans);</pre>
```

# 4 String algorithms

### 4.1 Z-algorithm

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define MAXN 1000020
using namespace std;
int z[MAXN] = {};
int x=0 , y=0 , maxn = 0;
string s ;
int main()
#ifdef LOCAL
    freopen("in1.txt","r",stdin);
#endif // LOCAL
    cin >> s ;
    for(int i = 1 ; i < s.length() ; i++ ){</pre>
        z[i] = max(0, min(z[i-x], y - i + 1));
        while (i + z[i] < s.length() && s[z[i]] == s[i+z[i]] ) {
            x = i ;
y = i + z[i] ;
            z[i]++;
```

```
for(int i = 0 ; i < s.length() ; i++)
    if(z[i] == s.length() - i && maxn >= s.length()-i ){
        cout << s.substr(0,z[i]);
        return 0 ;
    }
    maxn = max(maxn , z[i]);
}
cout << "Just a legend" ;
return 0;</pre>
```

### 5 Data structures

# 5.1 Union-find disjoint sets (UFDS) by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
int intSum[200080] , intParent[200080] , intSet[200080] ;
int find_root(int intA){
    if(intParent[intA] == intA)
        return intA ;
     intParent[intA] = find_root(intParent[intA]);
    return intParent[intA];
int each_debug(int n ){
    system("Pause") ;
int main()
#ifdef LOCAL
    freopen("in1.txt","r", stdin);
freopen("out.txt","w", stdout);
#endif // LOCAL
    int n, m , operation , p , q ;
    while(cin >> n >> m) {
   for(int i = 1 ; i <= n ; i++) {</pre>
             intParent[i] = i+n ;
              intParent[i+n] = i+n ;
              intSum[i+n] = i;
              intSet[i+n] = 1;
         while (m--) {
              cin >> operation ;
              if(operation == 1){
                   cin >> p >> q;
                   int intRoot_p , intRoot_q ;
                  intRoot_p = find_root(intParent[p]);
intRoot_q = find_root(intParent[q]);
if(intRoot_p != intRoot_q){
                       intNoot_g! = IntRoot_g;
intParent[intRoot_q] = intRoot_p;
intSum[intRoot_p] += intSum[intRoot_q];
intSet[intRoot_p] += intSet[intRoot_q];
                   //debug
                   //each_debug(n);
              else if (operation == 2 ) {
                   cin >> p >> q;
                   int intRoot_p , intRoot_q ;
                   intRoot_p = find_root(intParent[p]);
                   intRoot_q = find_root(intParent[q]);
                   if(intRoot_p != intRoot_q){
                       intParent[p] = intRoot_q;
                       intSum[intRoot_q] += p;
intSum[intRoot_p] -= p;
intSet[intRoot_q] ++;
                       intSet[intRoot_p] -- ;
                   //debug
```

# 5.2 Binary indexed/fenwick tree (BIT)

```
#include <iostream>
using namespace std;
#define LOGSZ 17
int tree[(1<<LOGSZ)+1];</pre>
int N = (1 << LOGSZ);
// add v to value at x
void set(int x, int v) {
  while (x \le N) {
    tree[x] += v;
    x += (x & -x);
// get cumulative sum up to and including x
int get(int x) {
 int res = 0;
  while(x) {
   res += tree[x];
    x -= (x & -x);
  return res;
// get largest value with cumulative sum less than or equal to x;
// for smallest, pass x-1 and add 1 to result
int getind(int x) {
  int idx = 0, mask = N;
  while(mask && idx < N) {</pre>
    int t = idx + mask;
    if(x >= tree[t]) {
     idx = t:
     x -= tree[t];
    mask >>= 1;
  return idx;
```

### 5.3 Rope

```
#include <iostream>
#include <bits/stdc++.h>
#include <ext/rope>
#define LOCAL
#define MAXN 50020
using namespace std;
using namespace __gnu_cxx ;
int main()
    freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
   int n , t , a , b , c , d=0 ;
    int v = 0;
    string strA ;
    rope<char> r[MAXN] , rtmp ;
    cin >> n ;
    while (n--) {
        cin >> t ;
        if(t==1){
           cin >> a ;
            cin >> strA :
            a -= d ;
            r[++v] = r[v] ;
```

```
r[v].insert(a,strA.c_str());
       //debug
       //cout << r[v] << '\n' ;
   else if(t==2){
       cin >> a >> b;
       a = d; b = d;
       r[++v] = r[v];
       r[v].erase(a-1,b);
       //debug
       //cout << r[v] << ' ' << r[v-1] << '\n';
   else if(t==3){
       cin >> a >> b >> c;
       a -= d; b -= d; c -= d;
       rtmp = r[a].substr(b-1,c);
       cout << rtmp << '\n' ;
       d += count(rtmp.begin() , rtmp.end() , 'c' );
return 0;
```

# 5.4 Segment tree

#include <iostream>

```
#include <bits/stdc++.h>
#include <string>
#define LOCAL
#define Lson(x) ((x << 1) +1)
#define Rson(x) ((x << 1) +2)
#define INF 99999999
using namespace std;
const int N = 100005;
int shift[35] , num[N] , len_shift ;
string strLine ;
struct Node(
   int left , right , Min_Value ;
}node[4 * N ];
void build(int left , int right , int x = 0 ){
    node[x].left = left ;
    node[x].right = right;
    if(left == right){
        node[x].Min_Value = num[left] ;
        return ;
    int mid = (left + right ) / 2;
    //cout << mid << '\n' ;
    //cout << x << ' ' << node[x].left << ' ' << node[x].right << ' ' << '\n';
    build(left , mid , Lson(x)) ;
    build(mid + 1 , right , Rson(x)) ;
    node[x].Min_Value = min(node[Lson(x)].Min_Value , node[Rson(x)].Min_Value);
void handle(){
    len_shift = 0 ;
    fell_shift | = 0;
for(int i = 6; i < strLine.length(); i++){
   if(strLine[i] >= '0' && strLine[i] <= '9') {</pre>
            shift[len_shift] = shift[len_shift] * 10 + (int) (strLine[i] - '0');
        else{
            shift[++len_shift] = 0;
    //finaly char is ')' , so len_shift is right
    sort(shift , shift + len_shift );
    //debug
    for(int i = 0 ; i < len_shift ; i++)
       cout << shift[i] << ' ';
    cout << '\n' ;
int query(int left , int right , int x = 0 ){
    if(node[x].left >= left && node[x].right <= right)</pre>
```

```
return node[x].Min_Value ;
    int mid = (node[x].left + node[x].right ) / 2;
    int ans = INF ;
    //cout << x << ' ' << node[x].left << ' ' << node[x].right << ' ' << node[x].Min_Value << '\n';
    if( left <= mid )</pre>
        ans = min(ans , query(left , right , Lson(x))) ;
    if(mid < right )</pre>
        ans = min(ans , query(left , right , Rson(x))) ;
    return ans ;
void set_num(int position , int value , int x = 0 ){
    if(node[x].left == position && node[x].right == position ) {
       node[x].Min_Value = value ;
    int mid = (node[x].left + node[x].right ) / 2;
    if(position <= mid )</pre>
        set_num(position , value , Lson(x) );
    if(mid < position )</pre>
        set_num(position , value , Rson(x)) ;
    \label{eq:node_exp} \verb|node[x].Min_Value = min(node[Lson(x)].Min_Value , node[Rson(x)].Min_Value );\\
int main()
    int n , q , intTemp ;
    ios::sync_with_stdio(0);
#ifdef LOCAL
    freopen("out.txt" , "w" , stdout ) ;
freopen("in1.txt" , "r" , stdin ) ;
#endif // LOCAL
    cin >> n >> q;
    for (int i = 1; i \le n; i++)
        cin >> num[i] ;
    build(1,n);
    //debug
    for(int i = 0; i < 13; i++){
    cout << node[i].left << ' ' << node[i].right << ' ' << node[i].Min_Value << '\n';</pre>
    return 0 ;
    while (q--) {
        cin >> strLine ;
        if(strLine[0] == 'q'){
             handle():
             cout << query(shift[0] , shift[1] ) << '\n';</pre>
        else if (strLine[0] == 's'){
             handle();
             intTemp = num[shift[0]];
             for(int i = 1 ; i < len_shift ; i++) {</pre>
                 set_num(shift[i-1] , num[shift[i]]);
                 num[shift[i-1]] = num[shift[i]] ;
             num[shift[len_shift-1]] = intTemp;
             set_num(shift[len_shift-1] , intTemp );
             //cout << intTemp << ' ' << shift[len_shift-1] << '\n' ;
             //for(int i = 1; i <= n; i++)
                  cout << num[i] << ' ';
    return 0;
```

## 5.5 Union-find disjoint sets (UFDS) by Bill

```
class UnionFind {
public:
    UnionFind(int N)
    {
       rank.assign(N, 0);
       p.assign(N, 0);
       for (int i = 0; i < N; ++i) p[i] = i;</pre>
```

#### 6 Utilities

#### 6.1 Bit manipulation

```
#define isOn(S, j) (S & (1<<j)) #define setBit(S, j) (S |= (1<<j)) #define (learBit(S, j) (S = ^{\circ} (1<<j)) #define toggleBit(S, j) (S ^{\circ} = (1<<j)) #define toggleBit(S, j) (S ^{\circ} ((-S)) #define lowBit(S) (S & (-S)) #define setAll(S, n) (S = (1<<n)-1)
```

### 6.2 C++ input output

```
#include <iostream>
#include <iomanip>
using namespace std;
    // Ouput a specific number of digits past the decimal point,
    cout.setf(ios::fixed); cout << setprecision(5);</pre>
    cout << 100.0/7.0 << endl;
    cout.unsetf(ios::fixed);
    // Output the decimal point and trailing zeros
    cout.setf(ios::showpoint);
    cout << 100.0 << endl;
    cout.unsetf(ios::showpoint);
    // Output a '+' before positive values
    cout.setf(ios::showpos);
    cout << 100 << " " << -100 << endl;
    cout.unsetf(ios::showpos);
    // Output numerical values in hexadecimal
    cout << hex << 100 << " " << 1000 << " " << 10000 << dec << endl;
```

#### 6.3 C++ STL

```
// Example for using stringstreams and next_permutation
#include <algorithm>
#include <iostream>
#include <stream>
#include <vector>

using namespace std;
int main(void) {
    vector<int> v;
    v.push_back(1);
```

```
v.push_back(2);
v.push_back(3);
v.push_back(4);
// Expected output: 1 2 3 4
                      4 3 2 1
do {
 ostringstream oss;
oss << v[0] << " " << v[1] << " " << v[2] << " " << v[3];
  // for input from a string s,
 // istringstream iss(s);
// iss >> variable;
  cout << oss.str() << endl;</pre>
} while (next_permutation (v.begin(), v.end()));
v.clear();
v.push_back(1);
v.push_back(2);
v.push back(1):
v.push_back(3);
// To use unique, first sort numbers. Then call
// unique to place all the unique elements at the beginning
// of the vector, and then use erase to remove the duplicate
// elements.
sort(v.begin(), v.end());
v.erase(unique(v.begin(), v.end()), v.end());
// Expected output: 1 2 3
for (size_t i = 0; i < v.size(); i++)
  cout << v[i] << " ";</pre>
cout << endl;
```

#### 6.4 Dates

```
// Routines for performing computations on dates. In these routines,
// months are expressed as integers from 1 to 12, days are expressed
// as integers from 1 to 31, and years are expressed as 4-digit
// integers.
#include <iostream>
#include <string>
using namespace std;
string dayOfWeek[] = {"Mon", "Tue", "Wed", "Thu", "Fri", "Sat", "Sun"};
// converts Gregorian date to integer (Julian day number)
int dateToInt (int m, int d, int y) {
  return
    1461 * (y + 4800 + (m - 14) / 12) / 4 +
    367 * (m - 2 - (m - 14) / 12 * 12) / 12 - 3 * ((y + 4900 + (m - 14) / 12) / 100) / 4 +
    d - 32075;
// converts integer (Julian day number) to Gregorian date: month/day/year
void intToDate (int jd, int &m, int &d, int &y) {
  int x, n, i, j;
  x = jd + 68569;
  n = 4 * x / 146097;
  x = (146097 * n + 3) / 4;
  i = (4000 * (x + 1)) / 1461001;
x -= 1461 * i / 4 - 31;
j = 80 * x / 2447;
  d = x - 2447 * j / 80;
 x = j / 11;

m = j + 2 - 12 * x;
  y = 100 * (n - 49) + i + x;
```

```
// converts integer (Julian day number) to day of week
string intToDay (int jd){
   return dayOfWeek[jd % 7];
}
int main (int argc, char ++argv){
   int jd = dateToInt (3, 24, 2004);
   int m, d, y;
   intToDate (jd, m, d, y);
   string day = intToDay (jd);

// expected output:
// 2453089
// 3/24/2004
// Wed
cout << jd << endl
   < m << "/" << d << ""/" << y << endl
   < day << endl;
}
</pre>
```

#### 6.5 Prime numbers

```
// O(sgrt(x)) Exhaustive Primality Test
#include <cmath>
#define EPS 1e-7
typedef long long LL;
bool IsPrimeSlow (LL x)
  if(x<=1) return false;</pre>
  if(x<=3) return true;</pre>
  if (!(x%2) || !(x%3)) return false;
  LL s=(LL) (sqrt ((double)(x))+EPS);
  for (LL i=5; i <= s; i+=6)
   if (!(x%i) || !(x%(i+2))) return false;
 return true:
// Primes less than 1000:
                                                          23
73
                                                                29
79
                                59
                                       61
                                             67
                                                   71
             43
                   47
                         53
                                                                      83
       97
                  103
                         107
                               109
                                      113
                                            127
                                                        137
                                                               139
                                                                     149
      157
            163
                  167
                         173
                               179
                                      181
                                            191
                                                  193
                                                        197
                                                               199
                                                                     211
                                                                            223
      227
            229
                  233
                         239
                               241
                                      251
                                            257
                                                  263
                                                        269
                                                               271
                                                                            281
      283
            293
                  307
                         311
                               313
                                      317
                                            331
                                                  337
                                                        347
                                                               349
                                                                            359
                                      397
      367
            373
                  379
                         383
                               389
                                            401
                                                  409
                                                        419
                                                               421
                                                                     431
                                                                            433
                                                        487
      439
            443
                         457
                               461
                                      463
                                                  479
                  449
                                            467
                                                               491
                                                                     499
                                      557
      509
                               547
                                                  569
                                                        571
                                                               577
                                                                            593
            521
                  523
                         541
                                            563
                                                                     587
      599
            601
                  607
                         613
                               617
                                      619
                                            631
                                                  641
                                                        643
                                                               647
                                                                     653
                                                                            659
      661
            673
                  677
                         683
                               691
                                            709
                                                  719
                                                         727
                                                                     739
                                                                            743
                                      787
                                                  809
      751
            757
                   761
                         769
                                773
                                            797
                                                        811
                                                               821
                                                                            827
                                                                     823
      829
            839
                  853
                         857
                                859
                                      863
                                            877
                                                  881
                                                        883
                                                               887
                                                                     907
                                                                            911
      919
            929
                  937
                         941
                               947
                                      953
                                            967
// Other primes:
      The largest prime smaller than 10 is 7.
      The largest prime smaller than 100 is 97.
      The largest prime smaller than 1000 is 997.
      The largest prime smaller than 10000 is 9973.
The largest prime smaller than 10000 is 99991.
The largest prime smaller than 100000 is 999983.
The largest prime smaller than 10000000 is 9999991.
      The largest prime smaller than 100000000 is 99999989.
The largest prime smaller than 1000000000 is 999999937.
      The largest prime smaller than 10000000000 is 9999999967.
      The largest prime smaller than 10000000000 is 99999999977.
      The largest prime smaller than 100000000000 is 99999999999999.
      The largest prime smaller than 1000000000000 is 999999999971.
      The largest prime smaller than 1000000000000 is 9999999999973.
      The largest prime smaller than 100000000000000 is 99999999999937.
      The largest prime smaller than 1000000000000000 is 99999999999997.
      The largest prime smaller than 10000000000000000 is 99999999999999999.
```