NTUT_Kn1ghts ICPC Team Notebook

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1 Dynamic programming algorithms

1.1 Longest common subsequence (LCS)

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
struct LCS{
   int step . max len :
}Dp[5000][5000];
int main()
    freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
    int intX , intY , Min_step , Max_len ;
    string strX , strY ;
    while(cin >> intX >> strX >> intY >> strY ) {
        for (int i = 0 ; i <= intY ; i++) {
           Dp[0][i].max_len = 0;
            Dp[0][i].step = i;
        for (int i = 0 ; i <= intX ; i++) {
            Dp[i][0].max_len = 0;
```

2 Graph algorithms

2.1 All-pairs shortest paths (APSP)

```
// All-Pairs Shortest Paths (APSP) solved with Floyd Warshall O(V^3).
// inside int main()
   // precondition: AdjMat[i][j] contains the weight of edge (i, j)
   // or INF (1B) if there is no such edge
   // AdjMat is a 32-bit signed integer array
   for (int k = 0; k < V; ++k)
                              // remember that loop order is k->i->j
      for (int i = 0; i < V; ++i)
          for (int j = 0; j < V; ++j)
              if (AdjMat[i][k] + AdjMat[k][j] < AdjMat[i][j])</pre>
                 AdjMat[i][j] = AdjMat[i][k] + AdjMat[k][j];
                 p[i][j] = p[k][j];
// print shortest paths
void printPath(int i, int j)
   if (i != j) printPath(i, p[i][j]);
   printf(" %d", j);
```

2.2 Centroid decomposition

```
#include<iostream>
#include <bits/stdc++.h>
#define LOCAL
#define MAXN 50005
using namespace std;
int n , k , a , b ;
int ans , cnt ;
int Max[MAXN] , sz[MAXN] , rt ;
int head[MAXN], dis[MAXN];
bool vis[MAXN];
struct node{
    int v , nx ;
}Edge[MAXN*2];
void init(int n ) {
   Max[0] = n;
ans = cnt = 0;
    for(int i = 0; i <= n; i++) {
        head[i] = -1;
        vis[i] = 0 ;
```

```
void add(int u , int v) {
     Edge[cnt].v = v;
     Edge[cnt].nx = head[u] ;
     head[u] = cnt++;
void get_rt(int u , int fa ){
    sz[u] = 1 ; Max[u] = 0 ;
for(int i = head[u] ; ~i ; i=Edge[i].nx) {
         int v = Edge[i].v ;
          if(vis[v] | | v == fa ) continue;
         get_rt(v,u);
sz[u] += sz[v];
          Max[u] = max(Max[u], sz[v]);
     Max[u] = max(Max[u], n - sz[u]);
     if(Max[rt] > Max[u])
\label{point} \mbox{ \ensuremath{\mbox{void}} get\_dis(int \ u \ , \ \mbox{ int } fa \ , \ \mbox{ int } d) \ \{}
     for(int i = head[u] ; ~i ; i= Edge[i].nx){
         int v = Edge[i].v;
if(vis[v] || v == fa ) continue;
dis[++cnt] = d + 1;
          get_dis(v,u,dis[cnt]);
int get_ans(int u , int d ){
     dis[cnt=1] = d;
     get_dis(u,0,d) ;
     sort(dis+1 , dis+cnt+1) ;
     int 1 = 1 , ans = 0 ;
     while(1 < cnt && dis[1] + dis[cnt] < k ) 1++ ;
while(1 < cnt && dis[1] <= k - dis[1]){</pre>
          ans \ += \ upper\_bound(dis \ + \ 1 \ + \ 1 \ , \ dis \ + \ cnt \ + \ 1 \ , \ k \ - \ dis[1]) \ - \ lower\_bound(dis + l + l \ , \ dis + cnt + l \ )
                 , k-dis[1]);
     return ans ;
void dfs(int u ) {
     vis[u] = 1;
     //cout << rt << ' ' << u << '\n';
    ans += get_ans(u , 0);
for(int i = head[u] ; ~i ; i = Edge[i].nx){
         int v = Edge[i].v ;
          if(vis[v]) continue;
         ans -= get_ans(v , 1) ;
n = sz[v] , rt = 0 , get_rt(v,u);
          dfs(rt);
int main(){
      freopen("in1.txt" , "r" , stdin);
//#endif // LOCAL
     cin >> n >> k ;
     init(n);
     for (int i =1; i < n ; i++) {</pre>
         cin >> a >> b;
         add (a, b):
         add(b,a);
     rt = 0 ; get_rt(1,0);
     dfs(rt);
     cout << ans << '\n' ;
```

2.3 Detect negative weight cycle

ii vw = AL[u][j]; dist[vw.first] = min(dist[vw.first], dist[u] + vw.second); // relax

2.4 DFS

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
int m , n , flag=1;
int Maxn_city = 0 , Maxn_path = 0 ;
vector<int>tree[200020];
int city[200020] = {};
int visit[200020] = {};
vector<int> travel ;
void BFS_to_large_path(int root ){
    visit[root] = 1;
    travel push_back(root);
    for(int i = 0 ; i < tree[root].size() ; i++){</pre>
        int node = tree[root][i];
        if(!visit[node]){
            BFS_to_large_path(node);
            travel.pop_back();
            visit[root] = 0;
    //debug to check large path
    //if (root == 1)
// cout << "1=" << travel.size() << ' ' << Maxn_path << ' ' << city[root] << '\n';
    if(city[root] && travel.size() > Maxn_path){
        Maxn_city = travel[travel.size()/2];
        Maxn_path = travel.size();
void BFS_to_other_path(int root ,int path) {
    visit[root] = 1;
    for(int i = 0 ; i < tree[root].size() ; i++){</pre>
        int node = tree[root][i];
        if(!visit[node]){
            BFS_to_other_path(node , path+1);
            visit[root] = 0;
    //debug
    if(root == 1 )
        cout << "city=" << root << " path= " << path << '\n' ;
    if(city[root] && path != Maxn_path)
        flag = 0;
int main(){
#ifdef LOCAL
freopen("in1.txt" , "r" , stdin);
#endif // LOCAL
    cin >> n >> m;
    int a , b ;
    for(int i = 0 ; i < n-1 ; i++) {
        cin >> a >> b;
        tree[a] push back(b);
        tree[b].push_back(a);
    for (int i = 0; i < m; i++) {
        cin >> a ;
        city[a] = 1;
    BFS_to_large_path(a);
    //visit[a] = 0;
    BFS_to_other_path(Maxn_city , 1 );
    if(flag)
        cout << "YES\n" << Maxn_city ;
    else
        cout << "NO" ;
    cout << "Maxn_path= " << Maxn_path << " Maxn_city= " << Maxn_city << '\n';</pre>
```

2.5 Dijkstra by Bill

```
// Dijkstra implementation for negative weight edges O((V + E) \log V)
    vi dist(V, INF); dist[s] = 0;
    priority_queue< ii, vii, greater<ii>> pq;
pq.push( ii(0, s) );
     while (!pq.empty())
         ii front = pq.top(); pq.pop();
         int d = front.first;
         int u = front.second;
         if (d > dist[u]) continue;
         for (int i = 0; i < (int)AL[u].size(); ++i) // [A]djacency [L]ist</pre>
              ii vw = AL[u][i];
              int v = vw.first;
              int w = vw.second;
              \textbf{if} \ (\texttt{dist}[\texttt{u}] \ + \ \texttt{w} \ \leq \ \texttt{dist}[\texttt{v}])
                   dist[v] = dist[u] + w;
pq.push( ii(dist[v], v) );
                                                 // relax operation
    } // this variant can cause duplicate items in the priority queue
```

2.6 Dijkstra by David

```
#include <iostream>
 #include <bits/stdc++.h>
#define LOCAL
#define INF 99999999
using namespace std:
int intMap[1010][1010] = {} , intValue[1010][1010] = {};
int m , n ;
struct Node {
     int x . v . v :
     void read( int _x , int _y , int _v) {
         x = _x ; y = _y ; v = _v ;
     bool operator < (const Node &a) const{
 | nodNode;
void print_map() {
  for(int i = 1 ; i <= n ; i++) {
    for(int j = 1 ; j <= m ; j++) {
      if(intValue[i][j] == 99999999)
}</pre>
                 cout << 'r' << ' ';
             else
                 cout << intValue[i][j] << ' ';
         cout << '\n' ;
     cout << '\n' ;
void bfs() {
    int x , y , intDirection[4][2] = {-1,0 ,0,1 ,1,0 ,0,-1};
     int intDx , intDy ;
    Node nodTemp ;
    priority_queue<Node> deqNode ;
     nodTemp.read(1,1,0);
     degNode.push (nodTemp);
     while (deqNode.size()) {
         x = degNode.top().x;
         y = deqNode.top().y;
         deqNode.pop();
         for (int i = 0; i < 4; i++) {
              intDx = intDirection[i][0] + x ;
             intDy = intDirection[i][1] + y ;
             //debug
              //cout << intDx << ' ' << intDy << ' ' << intValue[x][y] + intMap[intDx][intDy] << ' ' <<
                    i << '\n';
             if(intValue[x][y] + intMap[intDx][intDy] < intValue[intDx][intDy] ){</pre>
                  intValue[intDx][intDy] = intValue[x][y] + intMap[intDx][intDy];
```

```
nodTemp.read(intDx , intDy , intValue[intDx][intDy]);
                 deqNode push (nodTemp) ;
         //print_map();
int main() {
#ifdef LOCAL
    freopen("in1.txt" , "r" , stdin );
freopen("out.txt" , "w" , stdout) ;
#endif
ios::sync_with_stdio(false);
   int intCase;
    cin >> intCase ;
    while(intCase --) {
         cin >> n >> m;
        for(int i = 1 ; i <= n ; i++) {</pre>
             for(int j = 1; j \le m; j++) {
                  cin >> intMap[i][j];
                 intValue[i][j] = INF ;
        for(int i = 1 ; i <= n ; i++) {</pre>
             intValue[i][0] = 0 ;
             intValue[i][m+1] = 0;
             intMap[i][0] = INF +1;
             intMap[i][m+1] = INF +1;
        for(int i = 1; i <= m; i++)
             intValue[0][i] = 0;
             intValue[n+1][i] = 0;
             intMap[0][i] = INF +1;
             intMap[n+1][i] = INF +1;
        intValue[1][1] = intMap[1][1];
        //cout << intValue[1][1] << '\n';
        bfs();
        cout << intValue[n][m] << '\n';</pre>
        return 0;
```

2.7 Euler tour

```
list<int> cyc; // we need list for fast insertion in the middle
void EulerTour(list<int>::iterator i, int u)
    for (int j = 0; j < (int)AL[u].size(); ++j) // [A]djacency [L]ist</pre>
        ii& vw = AL[u][j];
       int v = vw.first;
        if (vw.second)
                         // if this edge can still be used
            vw.second = 0; // remove this edge
            // remove bi-directional edge
            for (int k = 0; k < (int) AL[v].size(); ++k)</pre>
                ii\& uw = AL[v][k];
                if (uw.first == u && uw.second)
                    uw.second = 0;
                    break;
            // continue the tour
            EulerTour(cyc.insert(i, u), v);
    EulerTour(cyc.end(), A); // 'cyc' contains an Euler tour starting at 'A'
    for (list<int>::iterator i = cyc.begin(); i != cyc.end(); ++i)
        printf("%d\n", *i);
```

2.8 Find articulation points and bridges

```
// Find articulation points & bridges solved with DFS O(V + E).
void articulationPointAndBridge(int u)
   for (int i = 0; i < (int)AL[u].size(); ++i) // [A]djacency [L]ist</pre>
       int v = AL[u][i].first;
       if (dfs_num[v] == UNVISITED)
                                   // a tree edge
           dfs_parent[v] = u;
          if (u == dfsRoot) ++rootChildren; // special case if 'u' is a root
          articulationPointAndBridge(v);
          if (dfs_low[v] >= dfs_num[u]) articulation_vertex[u] = true;
          dfs_low[u] = min( dfs_low[u], dfs_low[v] );  // update dfs_low[u]
       else if (v != dfs_parent[u]) dfs_low[u] = min( dfs_low[u], dfs_num[v] ); // update dfs_low[u]
// inside int main()
   dfsNumberCounter = 0;
   dfs_num.assign(V, UNVISITED);
   dfs_low.assign(v, 0);
   dfs_parent.assign(V, 0);
   articulation_vertex.assign(V, 0);
   printf("Bridges:\n");
   for (int u = 0; u < V; ++u)
   if (dfs_num[u] == UNVISITED)</pre>
          dfsRoot = u;
          rootChildren = 0;
          articulationPointAndBridge(u);
          articulation_vertex[dfsRoot] = (rootChildren > 1);
   printf("Articulation Points:\n");
   for (int u = 0; u < V; ++u)
       if (articulation_vertex[u]) printf(" Vertex %d\n", u);
```

2.9 Floyd Warshall by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
char before[520][520] = {};
int after[520][520] = {};
int main()
     freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
    cin >> n ;
    for(int i = 0 ; i < n ; i++) {
    for(int j = 0 ; j < n ; j++)</pre>
             cin >> before[i][j];
    for (int i = 0; i < n; i++) {
         for(int j = i+1 ; j < n ; j++) {</pre>
             int sum = 0 ;
              for (int k = i + 1; k < j; k++) {
                  if(after[i][k])
                      sum += before[k][j]-'0';
             if( (sum +1) % 10 == before[i][j] - '0'){
                  after[i][j] = 1;
    for (int i = 0; i < n; i++) {
         for (int j = 0; j < n; j++)
```

```
cout << after[i][j];
cout << '\n';
}
return 0;</pre>
```

2.10 Graph edges property check

```
// Graph Edges Property Check solved with DFS O\left(V + E\right).
void graphCheck(int u) // DFS for checking graph edge properties
    dfs num[u] = EXPLORED;
    for (int i = 0; i < (int) AL[u].size; ++i) // [A]djancency [L]ist
        int v = AL[u][i].first;
        if (dfs_num[v] == UNVISITED) // Tree Edge, EXPLORED->UNVISITED
            dfs_parent[v] = u; // parent of this child is me
            graphCheck(v);
        else if (dfs_num[v] == EXPLORED) // EXPLORED->EXPLORED
            if (v == dfs_parent[u]) printf(" Two ways (%d, %d)-(%d, %d)\n", u, v, v, u);
            else printf(" Back Edge (%d, %d) (Cycle)\n", u, v); // can check if graph is cyclic
        else if (dfs_num[v] == VISITED)
                                          // EXPLORED->VISITED
           printf(" Forward/Cross Edge (%d, %d)\n", u, v);
    dfs_num[u] = VISITED;
// inside int main()
    dfs_num.assign(V, UNVISITED);
    dfs_parent.assign(V, 0);
    for (int u = 0; u < V; ++u)
        if (dfs num[u] == UNVISITED)
            printf("Component %d:\n", ++numComp), graphCheck(u);
```

2.11 Kruskal by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define 11 long long
using namespace std;
int parent[1020] ;
struct edge{
   ll n1 , n2 , w ;
}node[25020];
int compare(edge A , edge B ){
    return A.w < B.w ;
int find_root(int a) {
    if(a != parent[a] )
        return parent[a] = find_root(parent[a]);
    return a ;
int main()
    freopen("in1.txt" , "r" , stdin );
    freopen("out.txt" , "w" , stdout );
#endif // LOCAL
    int n , m , p_n1 , p_n2 ; // parent_n1 , parent_n2
vector<int> hee ; //heavy edge circle
    while (cin >> n >> m && n + m != 0 ) {
        for(int i = 0 ; i < m ; i++ ) {</pre>
            cin >> node[i].n1 >> node[i].n2 >> node[i].w ;
        for (int i = 0; i < n; i++)
            parent[i] = i ;
        sort(node , node + m , compare ) ;
        hce.clear();
```

```
//kruskal
    for (int i = 0; i < m; i++) {
        p_n1 = find_root(node[i].n1);
        p_n2 = find_root(node[i].n2);
        if (p_n1 != p_n2 )
            parent[p_n2] = p_n1 ;
            hce.push_back(node[i].w);
        //debug
        for(int i = 0 ; i < n ; i++)
        cout << parent[i] << ' ';
cout << '\n';</pre>
    sort(hce.begin() , hce.end()) ;
    if(hce.size()){
        for(int i = 0; i < hce.size()-1; i++)
            cout << hce[i] << ' ';
        cout << hce[hce.size()-1];</pre>
        cout << "forest" ;
    cout << '\n' ;
return 0:
```

2.12 Max flow

```
int res[MAX_V][MAX_V], mf, f, s, t;
vi p; // p stores the BFS spanning tree from s
void augment(int v, int minEdge)
    if (v == s) { f = minEdge; return; }
    else if (p[v] != -1)
         augment( p[v], min(minEdge, res[ p[v] ][ v ]) );
        res[ p[v] ][ v ] -= f;
res[ v ][ p[v] ] += f;
// inside int main(): set up 'res', 's', and 't' with appropriate values
    while (true)
                   // O(V^3 * E) Edmonds Karp s algorithm
         vi dist(MAX_V, INF); dist[s] = 0;
         queue<int> q; q.push(s);
         p.assign(MAX V. -1);
         while (!q.empty())
             int u = q.front(); q.pop();
if (u == t) break; // immediately stop BFS if we already reach sink t
             for (int v = 0; v < MAX_V; ++v)
                 if (res[u][v] > 0 && dist[v] == INF)
                      dist[v] = dist[u] + 1, q.push(v), p[v] = u;
        augment(t, INF); // find the min edge weight f in this path, if any if (f == 0) break; // we cannot send any more flow ( f = 0), terminate
         mf += f;
                              // we can still send a flow, increase the max flow!
    printf("%d\n", mf);
```

2.13 Max cardinality bipartite matching (MCBM)

2.14 Minimum Spanning Tree (MST)

2.15 Strongly connected component (SCC)

```
// Tarjan O(V + E)
vi dfs_num, dfs_low, visited;
int dfsNumberCounter, numSCC;
vi S:
void tarjanSCC(int u)
    dfs_low[u] = dfs_num[u] = dfsNumberCounter++;  // dfs_low[u] <= dfs_num[u]</pre>
                       // stores 'u' in a vector baesd on order of visitation
    S.push back(u);
    visited[u] = 1;
    for (int i = 0; i < (int)AL[u].size(); ++i) // [A]djacency [L]ist</pre>
        int v = AL[u][i].first;
        if (dfs_num[v] == UNVISITED) tarjanSCC(v);
        if (visited[v]) dfs_low[u] = min( dfs_low[u], dfs_low[v] ); // condition for update
    if (dfs_low[u] == dfs_num[u])
                                     // if this is a root (start) of an SCC
                                      // this part is done after recursion
        printf("SCC %d:", ++numSCC);
        while (true)
            int v = S.back(); S.pop_back();
            visited[v] = 0;
            printf(" %d", v);
            if (u == v) break;
        printf("\n");
// inside int main()
    dfs_num.assign(V, UNVISITED);
    dfs_low.assign(V, 0);
    visited.assign(V, 0);
dfsNumberCounter = numSCC = 0;
    for (int u = 0; u < V; ++u)
        if (dfs_num[u] == UNVISITED)
            tarjanSCC(u);
```

3 Greedy algorithms

#include <bits/stdc++.h>

3.1 Longest increasing subsequence (LIS)

```
using namespace std:
typedef vector<int> vi;
int n:
vi A:
void print_array(const char *s, vi &L, int n) {
 for (int i = 0; i < n; ++i) {
   if (i) printf(", ");
    else printf("%s: [", s);
    printf("%d", L[i]);
  printf("]\n");
                                                 // predecessor array
// backtracking routine
  printf(" %d", A[i]);
int memo[10010];
                                                 // old limit: up to 10^4
int LIS(int i) {
                                                 // O(n^2) overall
  if (i == 0) return 1;
  int &ans = memo[i];
                                                 // was computed before
  if (ans != -1) return ans;
  ans = 1:
                                                 // LIS can start anywhere
  for (int j = 0; j < i; ++j)
if (A[j] < A[i])</pre>
                                                 // O(n) here
                                                 // increasing condition
     ans = max(ans, LIS(j)+1);
                                                 // pick the max
  return ans:
int main() {
  // note: A[n-1] must be set as the largest value ("INF")
  // so that all LIS (that can start anywhere) will end at n-1
  srand(time(NULL));
  int n = 10 + rand() %11;
  A.assign(n, 0);
                                                 // set A[n-1] = INF
  A[n-1] = 99;
  for (int i = 0; i < n-1; ++i)
   A[i] = rand() %101-50;
                                                 // [-50..501
  vi sample({-7, 10, 9, 2, 3, 8, 8, 1, 2, 3, 4, 99});
  A = sample;
  printf("n = %d:", n);
  for (int i = 0; i < n; ++i)
  printf(" %d", A[i]);</pre>
  printf("\n");
  // early 2000 problems usually accept O(n^2) solution
 memset (memo, -1, sizeof memo);
printf("LIS length is %d\n\n", LIS(n-1));
                                              // with O(n^2) DP
  // 2020s problems will likely only accept O(n \log k) solution
  // new limit: n can be up to 200K
  int k = 0, lis_end = 0;
  vi L(n, 0), L_id(n, 0);
  p.assign(n, -1);
  for (int i = 0; i < n; ++i) {
    int pos = lower_bound(L.begin(), L.begin()+k, A[i]) - L.begin();
    L[pos] = A[i];
                                                 // greedily overwrite this
    L_id[pos] = i;
                                                 // remember the index too
    p[i] = pos ? L_id[pos-1] : -1;
                                                 // predecessor info
    if (pos == k) {
                                                 // can extend LIS?
     k = pos+1;
                                                 // k = longer LIS by +1
     lis_end = i;
                                                 // keep best ending i
    printf("Considering element A[%d] = %d\n", i, A[i]);
    printf("LIS ending at A[%d] is of length %d: ", i, pos+1);
    printf("[");
    print_LIS(i);
```

```
printf("\n");
print_array("L is now", L, k);
printf("\n");
}

printf("Final LIS is of length %d: ", k);
print_LIS(lis_end); printf("\n");

assert(LIS(n-1) == k);  // both must be identical
return 0;
```

4 String algorithms

4.1 Z-algorithm

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define MAXN 1000020
using namespace std;
int z[MAXN] = \{\};
int x=0 , y=0 , maxn = 0;
string s ;
int main()
     freopen("in1.txt", "r", stdin);
#endif // LOCAL
     cin >> s,
for(int i = 1; i < s.length(); i++){
   z[i] = max(0,min(z[i-x], y - i + 1));
   while(i + z[i] < s.length() && s[z[i]] == s[i+z[i]]){</pre>
               y = i + z[i];
               z[i]++ ;
     for(int i = 0 ; i < s.length() ; i++)</pre>
          if(z[i] == s.length() - i && maxn >= s.length()-i){
    cout << s.substr(0, z[i]);</pre>
               return 0 ;
          maxn = max(maxn , z[i]);
     cout << "Just a legend" ;</pre>
     return 0;
```

5 Data structures

5.1 Rope

```
#include <iostream>
#include <bits/stdc++.h>
#include <ext/rope>
#define LOCAL
#define MAXN 50020
using namespace std;
using namespace __qnu_cxx ;
int main()
#ifdef LOCAL
   freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
    int n , t , a , b , c , d=0 ;
   int v = 0;
string strA;
    rope<char> r[MAXN] , rtmp ;
    cin >> n;
    while (n--) {
        cin >> t ;
```

```
if(t==1){
        cin >> a ;
        cin >> strA ;
        r[++v] = r[v];
        r[v].insert(a,strA.c_str());
        //cout << r[v] << '\n' ;
   else if(t==2) {
       cin >> a >> b;
a -= d; b -= d;
        r[++v] = r[v];
        r[v].erase(a-1,b);
        //debug
        //cout << r[v] << ' ' << r[v-1] << '\n';
    else if(t==3) {
       cin >> a >> b >> c ;
        a -= d; b -= d; c -= d;
        rtmp = r[a].substr(b-1,c);
        cout << rtmp << '\n' ;
       d += count(rtmp.begin() , rtmp.end() , 'c' );
return 0:
```

5.2 Union-find disjoint sets (UFDS) by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
int intSum[200080] , intParent[200080] , intSet[200080] ;
int find root(int intA){
    if(intParent[intA] == intA)
       return intA :
    intParent[intA] = find_root(intParent[intA]);
    return intParent[intA];
int each_debug(int n ) {
   system("Pause");
int main()
    freopen("in1.txt","r", stdin);
freopen("out.txt","w", stdout);
#endif // LOCAL
    int n, m , operation , p , q ;
    \textbf{while}\,(\texttt{cin} >> n >> m)\;\{
        for(int i = 1 ; i <= n ; i++) {
            intParent[i] = i+n :
            intParent[i+n] = i+n ;
            intSum[i+n] = i;
            intSet[i+n] = 1;
        while (m--) {
            cin >> operation ;
            if(operation == 1 ){
                cin >> p >> q;
                int intRoot_p , intRoot_q ;
                intRoot_p = find_root(intParent[p]);
                intRoot_q = find_root(intParent[q]);
                if(intRoot_p != intRoot_q){
                   intParent[intRoot_q] = intRoot_p;
intSum[intRoot_p] += intSum[intRoot_q];
                   intSet[intRoot_p] += intSet[intRoot_q];
                //debug
                //each_debug(n);
```

```
else if (operation == 2 ) {
            cin >> p >> q;
            int intRoot_p , intRoot_q ;
            intRoot_p = find_root(intParent[p]);
            intRoot_q = find_root(intParent[q]);
            if(intRoot_p != intRoot_q){
                intParent[p] = intRoot_q;
                intSum[intRoot_q] += p ;
               intSum[intRoot_p] -= p ;
                intSet[intRoot_q] ++ ;
               intSet[intRoot_p] -- ;
            //debug
            //each_debug(n) ;
        else if (operation == 3) {
            cout << intSet[find_root(p)] << ' ' << intSum[find_root(p)] << '\n';</pre>
return 0:
```

5.3 Union-find disjoint sets (UFDS) by Bill

```
class UnionFind
public:
    UnionFind(int N)
        rank.assign(N. 0);
        p.assign(N, 0);
        for (int i = 0; i < N; ++i) p[i] = i;
    int findSet(int i) { return (p[i] == i) ? i : ( p[i] = findSet(p[i]) ); }
    bool isSameSet(int i, int j) { return findSet(i) == findSet(j); }
    void unionSet(int i, int j)
        if ( !isSameSet(i, j) )
            int x = findSet(i);
            int y = findSet(j);
            if (rank[x] > rank[y]) p[y] = x; // rank keeps the tree short
                p[x] = y;
if (rank[x] == rank[y]) ++rank[y];
private:
    vi p, rank;
```

6 Utilities

6.1 Bit manipulation

```
#define isOn(S, j) (S & (1<<j)) #define setBit(S, j) (S |= (1<<j)) #define clearBit(S, j) (S &= ~(1<<j)) #define toggleBit(S, j) (S ^{*}= (1<<j)) #define lowBit(S) (S & (-S)) #define setAll(S, n) (S = (1<<n)-1)
```

6.2 Prime numbers

```
// O(sqrt(x)) Exhaustive Primality Test
#include <cmath>
#define EPS 1e-7
typedef long long LL;
bool IsPrimeSlow (LL x)
{
```

```
if(x<=1) return false;</pre>
  if(x<=3) return true;</pre>
  if (!(x%2) || !(x%3)) return false;
  LL s=(LL) (sqrt((double)(x))+EPS);
  for (LL i=5; i<=s; i+=6)
   if (!(x%i) || !(x%(i+2))) return false;
  return true;
// Primes less than 1000:
                                       13
61
113
181
251
                                 11
59
                                               17
67
                                                      19
71
                                                             23
73
                                                                    29
                                                                          31
83
                  47 53
103 107
167 173
233 239
                                                                    79
                                                                                 89
             4.3
                                             127
191
257
                                                                         149
211
277
                                109
179
                                                     131
193
                                                            137
                                                                  139
                                                                                151
223
                                                            197
                                                                   199
            163
      283
            293
                    307
                          311
                                 313
                                       317
                                              331
                                                     337
                                                            347
                                                                   349
                                                                         353
                                                                                359
             373
                    379
                          383
                                 389
                                       397
                                              401
                                                     409
                                                            419
                                                                   421
                                                                         431
                                                                                433
                                       463
557
      439
            443
                   449
                          457
                                 461
                                              467
                                                     479
                                                            487
                                                                  491
                                                                         499
                                                                                503
                                 547
      509
             521
                    523
                          541
                                              563
                                                     569
                                                            571
                                                                  577
                                                                         587
                                                                                593
                                       619
701
787
863
                   607
677
761
                                 617
                                                                  647
733
      599
            601
                          613
                                              631
                                                     641
                                                            643
                                                                         653
                                                                                659
                          683
769
857
                                691
773
859
                                              709
797
                                                     719
                                                            727
                                                                         739
      661
            673
                                                                                743
      751
             757
                                                     809
                                                           811
                                                                  821
                                                                         823
                                                                                827
                                              877
            839
                   853
                                                     881
                                                           883
                                                                  887
                                                                         907
                                                                                911
```