# NTUT\_Kn1ghts ICPC Team Notebook

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# 1 Advanced algorithms

# 1.1 Iterative deepening A\* (IDA\*)

```
// UVa 10181 - 15-Puzzle Problem solved with Iterative Deepening A* (IDA*).
using namespace std;
//#define LOCAL
#define N 4
                        // #rows/columns
#define B 15
                       // [B]lank tile id
#define PUZZLE (N*N)
#define MAX_STEPS 45 // given by the problem description
                      // 4 [DIR]ections
#define DIR 4
int dr[DIR] = {0, -1, 0, 1}; // must be right, up, left, down
int dc[DIR] = {1, 0, -1, 0}; // for the XOR operation to work
char dm[] = "RULD"; // [d]irection [m]ove
int p[PUZZLE];
int b_init_pos;
                        // [b]lank [init]ial [pos]ition
                        // current [lim]it of the Iterative Deepening Search (IDS)
int pred[MAX_STEPS]; // [pre]viously used [d]irection to go to the current state
bool isViable()
    int sum:
    for (int i = 0; i < PUZZLE; ++i)
    for (int j = 0; j < i; ++j)</pre>
    if (p[j] > p[i]) ++sum;

sum += b_init_pos / N + b_init_pos % N;

sum -= B / N + B % N;
    return sum % 2 == 0;
int H()
    int h = 0;
    for (int pos = 0; pos < PUZZLE; ++pos) // for all tile 'p[pos]'</pre>
                                                    // compute Manhattan distance to goal state
         if (p[pos] == B) continue;
        h += abs( p[pos] / N - pos / N )
+ abs( p[pos] % N - pos % N );
                                                 // position of 'p[pos]' in goal state is 'p[pos]'
// position of 'p[pos]' in current state is 'pos'
    return h;
bool isValid(int r, int c)
    return 0 <= r && r < N && 0 <= c && c < N;
int Delta_H(int cur_r, int cur_c, int next_r, int next_c)
     \textbf{int val} = p[\text{cur}\_\text{r} \star \text{N} + \text{cur}\_\text{c}]; \text{ // [val]} \\ \text{ue of the tile being moved into the blank tile position } 
                                     // position of 'val' in goal state is 'val'
    int goal_r = val / N;
int goal_c = val % N;
    bool dfs(int g, int h, int b_pos)
    if (g + h > lim) return false;
                                    // found a solution!
    if (h == 0) return true;
    int r = b_pos / N;
int c = b_pos % N;
    for (int d = 0; d < DIR; ++d)</pre>
         if ( q != 0 && d == (pred[q] ^ 2) ) continue; // this direction gets us back to parent state
         int next_r = r + dr[d];
         int next_c = c + dc[d];
         if (!isValid(next_r, next_c)) continue;
         int next_h = h + Delta_H(next_r, next_c, r, c); // O(1)
         int b_next_pos = next_r * N + next_c;
         swap(p[b_pos], p[b_next_pos]);
         pred[g+1] = d;
         if ( dfs(g + 1, next_h, b_next_pos) ) return true;
         swap(p[b_pos], p[b_next_pos]);
    return false:
int ida_star()
```

```
int init_h = H();
    lim = init_h;
    while (lim <= MAX_STEPS)
        if ( dfs(0, init_h, b_init_pos) ) return lim;
    return -1;
void output(int steps)
   for (int i = 1; i <= steps; ++i)
    printf("%c", dm[ pred[i] ]);</pre>
    #ifdef LOCAL
    freopen("in.txt", "r", stdin);
    #endif // LOCAL
   int T;
scanf("%d", &T);
    while (T--)
        for (int i = 0; i < N; ++i)
            for (int j = 0; j < N; ++j)
            int pos = i * N + j:
            scanf("%d", &p[pos]);
            if (p[pos] == 0) p[pos] = B, b_init_pos = pos; // goal state 'p' is 0, 1, 2..14, 15
            else --p[pos];
                                                              // blank tile as 15
        if (!isViable()) // must-consider condition otherwise TLE
            printf("This puzzle is not solvable.\n");
            continue;
        int ret = ida_star();
        if (ret == -1)
            printf("This puzzle is not solvable.\n");
            continue:
        output(ret), printf("\n");
    return 0;
```

# 2 Dynamic programming algorithms

# 2.1 0-1 knapsack

```
#define W 1000 // Knapsack weight
#define N 100 // n item
int weight[N]; //item weight
int value[N]; //item value
int bag[W][2];
// 0/1 Knapsack
void ZeroOne() {
   memset(bag, 0, sizeof(bag));
  for(int i = 0 ; i < N ; i++ ) {
  for(int j = 0 ; j < W ; j++ )
    if( j >= weight[i] )
         bag[j][1] = max( bag[j][0] ,bag[j-weight[i]][0] + value[i] );
    for (int j = 0; j < W; j++)
      bag[j][0] = bag[j][1];
// group knapsack
int group; // hou much groups?
int how_many; // one group has many items?
int WEIGHT, VALUE;
void Grouping() {
  memset(bag,0,sizeof(bag));
for(int i = 0; i < group; i++){
  for(int j = 0; j < how_many; j++){</pre>
      scanf("%d %d", &WEIGHT, &VALUE);
       for (int k = 0; k < W; k++) {
```

```
if( j >= WEIGHT ) {
          bag[j][1] = max(bag[j][1], bag[j][0]);
          bag[j][1] = max(bag[j][1],bag[j-WEIGHT][0] + VALUE);
    for (int j = 0; j < W; j++)
      bag[j][0] = bag[j][1];
// mulipte knapsack
int limit[N]; // item limit
void Multiple() {
  for(int i = 0; i < N; i++) {</pre>
    int tmp = 1;
    while( tmp <= weight[i] ) {</pre>
      for (int j = 0; j < W; j++)
        if( j >= weight[i] *tmp )
          bag[j][1] = max(bag[j-weight[i]*tmp][0] + value[i]*tmp
                         , bag[j][0]);
      for(int j = 0; j < W; j++)
        bag[j][0] = bag[j][1];
      weight[i] = weight[i]-tmp;
      tmp = tmp*2;
    if( weight[i] > 0 ){
      for(int j = 0 ; j < W ; j++)
  if( j >= weight[i]*tmp )
          bag[j][1] = max(bag[j-weight[i]*tmp][0] + value[i]*tmp, bag[j][0]);
      for(int j = 0; j < W; j++)
        bag[j][0] = bag[j][1];
// inf
void Unlimited(){
  memset (bag, 0, sizeof (bag));
  for(int i = 0 ; i < N ; i++ ) {
  for(int j = 0 ; j < W ; j++ )</pre>
      if( j >= weight[i] )
        bag[j][1] = max( bag[j][0] ,bag[j-weight[i]][1] + value[i] );
    for (int j = 0; j < W; j++)
      bag[j][0] = bag[j][1];
```

# 2.2 Longest common subsequence (LCS)

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
struct LCS{
    int step , max_len ;
}Dp[5000][5000];
int main()
#ifdef LOCAL
freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
    int intX , intY , Min_step , Max_len ;
    string strX , strY ;
    while(cin >> intX >> strX >> intY >> strY ) {
        for(int i = 0 ; i <= intY ; i++) {</pre>
            Dp[0][i].max\_len = 0 ;
            Dp[0][i].step = i ;
        for(int i = 0 ; i <= intX ; i++) {
            Dp[i][0].max\_len = 0 ;
            Dp[i][0].step = i ;
        Max len = 0;
        Min step = 0;
```

# 2.3 Max 2D range sum

```
// Max 2D Range Sum - UVa 108 - solved with DP O(n^4).
// Abridged problem statement: Given an n x n square matrix of integers A where
// each integer ranges from [-127...127], find a sub-matrix of A with the maximum
#include <bits/stdc++.h>
using namespace std;
int A[200][200];
int main() {
  int n; scanf("%d", &n);
                                                                 // square matrix size
   for (int i = 0; i < n; ++i)
  for (int j = 0; j < n; ++j) {</pre>
       scanf("%d", &A[i][j]);
if (i > 0) A[i][j] += A[i-1][j];
                                                                 // add from top
        if (j > 0) A[i][j] += A[i][j-1];
                                                                 // add from left
         \textbf{if} \ (\texttt{i} \ > \ 0 \ \&\& \ \texttt{j} \ > \ 0) \ A[\texttt{i}][\texttt{j}] \ -= \ A[\texttt{i}-1][\texttt{j}-1]; // \ avoid \ double \ count 
                                                                 // inclusion-exclusion
   int maxSubRect = -127+100+100
                                                                 // the lowest possible val
  int maxSubRect = -12'*100*100;
for (int i = 0; i < n; ++i)
for (int j = 0; j < n; ++j)
for (int k = i; k < n; ++k)
for (int l = j; l < n; ++l)
int subRect = A[k][1];</pre>
                                                                 // start coordinate
                                                                 // end coord
                                                                // from (0, 0) to (k, 1)
             if (i > 0) subRect -= A[i-1][1];
             if (j > 0) subRect -= A[k][j-1];
             if (i > 0 && j > 0) subRect += A[i-1][j-1]; // O(1)
             maxSubRect = max(maxSubRect, subRect); // the answer is here
   printf("%d\n", maxSubRect);
   return 0;
```

# 2.4 Traveling salesman problem (TSP)

```
// This is a solution for UVa 10496 - Collecting Beepers. The problem is a
// variant of the Traveling Salesman Problem (TSP): Given n cities and their
// pairwise distances in the form of a matrix 'dist' of size n \, * \, n, compute the
// minimum cost of making a tour that starts from any city s, goes through all
// the other n - 1 cities exactly once, and finally returns to the city s. In
// this case, the salesman is Karel in a 2D world who can only move along the
// x and y axis. The cities are beepers whose coordinates are given, from which
// pairwise distances can be calculated. Algorithm takes time O(2^n * n^2).
// INPUT: The first line is the number of test cases. The first line of each
// test case is world's size (x-size and y-size). Next is the starting position
// of Karel. Next is the number of beepers. Next are the beepers' x- and y-
// OUTPUT: For each test case, output the minimum distance to move from Karel's
// starting position to each of the beepers and back to the starting position.
#include <bits/stdc++.h>
using namespace std;
#define LSOne(S) ((S) & -(S))
const int MAX n = 11:
int dist[MAX_n] [MAX_n], memo[MAX_n] [1<<(MAX_n-1)]; // Karel + max 10 beepers</pre>
int dp(int u, int mask) {
                                                  // mask = free coordinates
  if (mask == 0) return dist[u][0];
                                                  // close the loop
```

```
int &ans = memo[u][mask];
  if (ans != -1) return ans;
                                                       // computed before
  ans = 2000000000;
                                                       // up to O(n)
    int two_pow_v = LSOne(m);
                                                       // but this is fast
    int v = __builtin_ctz(two_pow_v)+1;
                                                       // offset v by +1
    ans = min(ans, dist[u][v] + dp(v, mask^two_pow_v)); // keep the min
    m -= two_pow_v;
  return ans;
int main() {
  int TC; scanf("%d", &TC);
  while (TC--) {
    int xsize, ysize; scanf("%d %d", &xsize, &ysize); // these two values are not used
    int x[MAX_n], y[MAX_n];
scanf("%d %d", &x[0], &y[0]);
    int n; scanf("%d", &n); ++n;
                                                       // include Karel
    for (int i = 1; i < n; ++i)
  scanf("%d %d", &x[i], &y[i]);</pre>
                                                       // Karel is at index 0
    for (int i = 0; i < n; ++i)
                                                       // build distance table
      for (int j = i; j < n; ++j)
    dist[i][j] = dist[j][i] = abs(x[i]-x[j]) + abs(y[i]-y[j]); // Manhattan distance</pre>
    memset (memo, -1, sizeof memo);
    printf("The shortest path has length d^n, dp(0, (1 << (n-1))-1)); // DP-TSP
  return 0:
```

# 3 Graph algorithms

# 3.1 All-pairs shortest paths (APSP)

```
// All-Pairs Shortest Paths (APSP) solved with Floyd Warshall O(V^3).
// inside int main()
    // precondition: AdjMat[i][j] contains the weight of edge (i, j)
    // or INF (1B) if there is no such edge
    // AdjMat is a 32-bit signed integer array
    // let p be a 2D parent matrix, where p[i][j] is the last vertex before j
     // on a shortest path from i to j, i.e. i -> ... -> p[i][j] -> j
    for (int i = 0; i < V; ++i)
        for (int j = 0; j < V; ++j)
    p[i][j] = i;  // initialize the parent matrix</pre>
    for (int k = 0; k < V; ++k)
                                       // remember that loop order is k->i->j
        for (int i = 0; i < V; ++i)
    for (int j = 0; j < V; ++j)
        if (AdjMat[i][k] + AdjMat[k][j] < AdjMat[i][j])</pre>
                      AdjMat[i][j] = AdjMat[i][k] + AdjMat[k][j];
                      p[i][j] = p[k][j];
// print shortest paths
void printPath(int i, int j)
    if (i != j) printPath(i, p[i][j]);
    printf(" %d", j);
```

# 3.2 Bipartite matching BFS by David

```
#include <iostream>
#include <cstring>
#include <cstring>
#include <cstdio>
#include <cstdio>
#include <cetcor>
#define LOCAL
using namespace std;

int fp[100010] ,fq[100010];
int vfp[100010] ,vfq[100010];
int turn = 0;
vector<int> cp[100010] , cq[100010];

int BFSBMfp(int n){
    vfp[n] = turn ;
    for(int i = 0 ; i < cp[n].size() ; i++ ){
        if(vfq[cp[n][i]] = turn) {
            vfq[cp[n][i]] = turn ;
            if(fq[cp[n][i]] = -1 || BFSBMfp(fq[cp[n][i]])){</pre>
```

```
fp[n] = cp[n][i] ;
fq[cp[n][i]] = n ;
                return 1 ;
    return 0 ;
int main()
    ios::sync_with_stdio(false);
    cin.tie(0);
    cout.tie(0);
    int n ,p ,q ,k ,x, y ;
    while (n--) {
        cin >> p >> q >> k;
        int MaxnPQ = max(p,q);
        for(int i = 1 ; i <= MaxnPQ ; i++) {</pre>
            cp[i].clear();
             fp[i] = -1;
            cq[i].clear();
            fq[i] = -1;
        int cnt = 0;
        for (int i = 0; i < k; i++) {
            cin >> x >> y ;
            cp[x].push_back(y);
             cq[y].push_back(x);
             if(fp[x] == -1 && fq[y] == -1){
                fp[x] = y;
fq[y] = x;
        for(int i = 1 ; i <= p ; i++) {
            if(fp[i] == -1){
                turn++;
                if(BFSBMfp(i))
                    cnt++;
        cout << cnt << '\n';
    return 0;
```

## 3.3 Centroid decomposition

```
#include<iostream>
#include <bits/stdc++.h>
#define LOCAL
#define MAXN 50005
using namespace std;
int n , k , a , b ;
int ans , cnt ;
int Max[MAXN] , sz[MAXN] , rt ;
int head[MAXN], dis[MAXN];
bool vis[MAXN] ;
struct node{
    int v , nx ;
}Edge[MAXN*2];
void init(int n ){
    Max[0] = n ;
    ans = cnt = 0;
    for (int i = 0; i <= n; i++) {
        head[i] = -1;
        vis[i] = 0 ;
void add(int u , int v) {
    Edge[cnt].v = v;
    Edge[cnt].nx = head[u] ;
    head[u] = cnt++;
void get_rt(int u , int fa ) {
    sz[u] = 1 ; Max[u] = 0 ;
    for(int i = head[u] ; ~i ; i=Edge[i].nx) {
        int v = Edge[i].v ;
         if(vis[v] | | v == fa ) continue;
         get_rt(v,u);
```

```
sz[u] += sz[v];
         Max[u] = max(Max[u], sz[v]);
     Max[u] = max(Max[u], n - sz[u]);
     if(Max[rt] > Max[u])
\label{eq:void_get_dis} \mbox{ (int } \mbox{ } \mbox{u , int } \mbox{fa , int } \mbox{d)} \, \{
     \textbf{for}(\textbf{int} \ i = head[u] \ ; \ \tilde{\ } i = Edge[i].nx) \{
         int v = Edge[i].v ;
         if(vis[v] || v == fa ) continue;
dis[++cnt] = d + 1;
         get_dis(v,u,dis[cnt]);
int get_ans(int u , int d ){
     dis[cnt=1] = d;
     get_dis(u,0,d) ;
     sort(dis+1 , dis+cnt+1) ;
     int 1 = 1 , ans = 0 ;
    while(1 < cnt && dis[1] + dis[cnt] < k ) 1++;
while(1 < cnt && dis[1] <= k - dis[1]){</pre>
         ans += upper_bound(dis + 1 + 1 , dis + cnt + 1 , k - dis[1]) - lower_bound(dis+1+1 , dis+cnt+1)
                , k-dis[l]);
     return ans :
void dfs(int u ) {
     vis[u] = 1;
     //cout << rt << ' ' << u << '\n' ;
    ans += get_ans(u , 0);
for(int i = head[u] ; ~i ; i = Edge[i].nx) {
   int v = Edge[i].v ;
         if(vis[v]) continue;
         ans -= get_ans(v , 1) ;
n = sz[v] , rt = 0 , get_rt(v,u);
         dfs(rt);
int main(){
//#ifdef LOCAL
      freopen("in1.txt" , "r" , stdin);
//#endif // LOCAL
     cin >> n >> k;
     init(n);
     for (int i =1; i < n; i++) {</pre>
         cin >> a >> b ;
         add(a,b):
         add(b,a);
     rt = 0 ; get_rt(1,0);
     dfs(rt);
     cout << ans << '\n' ;
```

# 3.4 Detect negative weight cycle

#### 3.5 DFS

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
int m , n , flag=1;
```

```
int Maxn_city = 0 , Maxn_path = 0 ;
vector<int>tree[200020];
int city[200020] = {};
int visit[200020] = {};
vector<int> travel ;
void BFS_to_large_path(int root ) {
    visit[root] = 1 ;
    travel.push_back(root);
    \textbf{for}(\texttt{int} \ \texttt{i} = \texttt{0} \ ; \ \texttt{i} < \texttt{tree}[\texttt{root}] . \texttt{size}(\texttt{)} \ ; \ \texttt{i++}) \, \{
        int node = tree[root][i] ;
        if(!visit[node]){
             BFS_to_large_path(node);
             travel.pop_back();
             visit[root] = 0 ;
    //debug to check large path
    //if (root == 1)
         cout << "1=" << travel.size() << ' ' << Maxn_path << ' ' << city[root] << '\n';
    if(city[root] && travel.size() > Maxn_path){
        Maxn_city = travel[travel.size()/2];
Maxn_path = travel.size();
void BFS_to_other_path(int root ,int path) {
    visit[root] = 1 :
    for(int i = 0 ; i < tree[root].size() ; i++){</pre>
        int node = tree[root][i];
        if(!visit[node]){
             BFS_to_other_path(node , path+1);
             visit[root] = 0 ;
    //debug
    if(root == 1 )
        cout << "city=" << root << " path= " << path << '\n' ;
    if(city[root] && path != Maxn_path)
        flag = 0;
int main(){
     freopen("in1.txt" , "r" , stdin);
#endif // LOCAL
    cin >> n >> m;
    int a , b ;
    for (int i = 0 : i < n-1 : i++) {
        cin >> a >> b ;
        tree[a].push_back(b) ;
        tree[b].push_back(a);
    for(int i = 0; i < m; i++) {
        cin >> a ;
        city[a] = 1;
    BFS_to_large_path(a);
    //visit[a] = 0 ;
    BFS_to_other_path(Maxn_city , 1 );
    if(flag)
        cout << "YES\n" << Maxn_city ;
    else
        cout << "NO" ;
    //debug
    cout << "Maxn_path= " << Maxn_path << " Maxn_city= " << Maxn_city << '\n';
```

## 3.6 DFS ICPC 2019 Russia problem E

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
int m, n, flag=1;
int Maxn_city = 0, Maxn_path = 0;
vector<int>rec[200020];
int city[200020] = {};
int visit[200020] = {};
vector<int> travel;
void BFS_to_large_path(int root) {
```

```
visit[root] = 1;
travel.push_back(root);
    for(int i = 0 ; i < tree[root].size() ; i++){
   int node = tree[root][i];</pre>
        if(!visit[node]){
             BFS_to_large_path(node);
             travel.pop_back();
             visit[root] = 0;
    //debug to check large path
    //if (root == 1)
          cout << "1=" << travel.size() << ' ' << Maxn path << ' ' << city[root] << '\n';
    if(city[root] && travel.size() > Maxn_path) {
   Maxn_city = travel[travel.size()/2];
        Maxn_path = travel.size();
void BFS_to_other_path(int root ,int path) {
    visit[root] = 1;
    for(int i = 0 ; i < tree[root].size() ; i++){</pre>
        int node = tree[root][i] ;
        if(!visit[node]){
             BFS_to_other_path(node , path+1);
             visit[root] = 0 ;
     //debug
    if(root == 1 )
        cout << "city=" << root << " path= " << path << '\n' ;
    if(city[root] && path != Maxn_path)
int main(){
#ifdef LOCAL
    freopen("in1.txt" , "r" , stdin);
#endif // LOCAL
    cin >> n >> m;
    int a , b ;
    for (int i = 0; i < n-1; i++) {
        cin >> a >> b ;
        tree[a] push_back(b);
        tree[b].push_back(a);
    for(int i = 0 ; i < m ; i++) {</pre>
        cin >> a ;
        city[a] = 1;
    BFS_to_large_path(a);
    //visit[a] = 0 ;
    BFS_to_other_path(Maxn_city , 1 );
    if(flag)
        cout << "YES\n" << Maxn_city ;
    else
        cout << "NO" ;
    cout << "Maxn_path= " << Maxn_path << " Maxn_city= " << Maxn_city << '\n';</pre>
```

## 3.7 Dijkstra by Bill

```
// Dijkstra implementation for negative weight edges O((V + E) \log V)
    vi dist(V, INF); dist[s] = 0;
    priority_queue< ii, vii, greater<ii>> pq;
    pq.push( ii(0, s) );
    while (!pq.empty())
        ii front = pq.top(); pq.pop();
        int d = front.first;
        int u = front.second;
        if (d > dist[u]) continue;
        for (int i = 0; i < (int)AL[u].size(); ++i) // [A]djacency [L]ist</pre>
            ii vw = AL[u][i];
            int v = vw.first;
int w = vw.second;
            if (dist[u] + w < dist[v])</pre>
                dist[v] = dist[u] + w;
                                           // relax operation
                pq.push( ii(dist[v], v) );
```

```
}
}/this variant can cause duplicate items in the priority queue
```

# 3.8 Dijkstra by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define TNF 99999999
using namespace std:
int intMap[1010][1010] = {};
int m . n :
struct Node {
     void read( int _x , int _y , int _v) {
          x = _x ; y = _y ; v = _v ;
     bool operator < (const Node &a) const{
         return v > a.v ;
| nodNode;
void print_map() {
    for(int i = 1 ; i <= n ; i++) {</pre>
         for(int j = 1; j <= m; j++) {
   if(intValue[i][j] == 99999999)
        cout << 'r' << ' ';</pre>
                   cout << intValue[i][j] << ' ';
         cout << '\n' ;
     cout << '\n' ;
void bfs(){
    int x , y , intDirection[4][2] = {-1,0,0,1,1,0,0,-1};
     int intDx , intDy ;
     Node nodTemp ;
     priority_queue<Node> deqNode ;
     nodTemp.read(1,1,0);
     deqNode .push (nodTemp);
     while (deqNode.size()) {
         x = deqNode.top().x;
          y = deqNode.top().y;
         deqNode.pop() ;
         for(int i = 0 ; i < 4 ; i++) {
   intDx = intDirection[i][0] + x ;</pre>
              intDy = intDirection[i][1] + y;
              //cout << intDx << ' ' << intDy << ' ' << intValue[x][y] + intMap[intDx][intDy] << ' ' <<
              if(intValue[x][y] + intMap[intDx][intDy] < intValue[intDx][intDy] ){</pre>
                   intValue[intDx][intDy] = intValue[x][y] + intMap[intDx][intDy];
nodTemp.read(intDx , intDy , intValue[intDx][intDy]);
                   deqNode.push(nodTemp) ;
          //print map() :
int main() {
#ifdef LOCAL
     freopen("in1.txt" , "r" , stdin );
     freopen("out.txt" , "w" , stdout) ;
#endif
 ios::sync_with_stdio(false);
     int intCase ;
     cin >> intCase ;
     while (intCase --) {
         cin >> n >> m;
         for(int i = 1; i <= n; i++) {
   for(int j = 1; j <= m; j++) {
      cin >> intMap[i][j];
      intValue[i][j] = INF;
```

```
for (int i = 1 ; i <= n ; i++) {
    intValue[i][0] = 0 ;
    intValue[i][m+1] = 0 ;
    intMap[i][0] = INF +1 ;
    intMap[i][m+1] = INF +1 ;
}
for (int i = 1 ; i <= m ; i++) {
    intValue[0][i] = 0 ;
    intValue[n+1][i] = 0 ;
    intMap[0][i] = INF +1 ;
    intMap[n+1][i] = INF +1 ;
}
intValue[1][1] = intMap[1][1] ;

//debug
//cout << intValue[1][1] << '\n' ;
bfs();
    cout << intValue[n][m] << '\n' ;
}
return 0;</pre>
```

#### 3.9 Print Euler tour

```
// Given an Eulerian-tour graph - a connected undirected graph whose vertices a-
// 11 have even degrees, produce its Euler tour. The graph is unweighted, stored
// in an adjacency list where the second attribute in edge info pair is a boole-// an '1' (edge can still be used) or '0' (edge can no longer be used).
list<int> cyc; // we need list for fast insertion in the middle
void EulerTour(list<int>::iterator i, int u)
    for (int j = 0; j < (int)AL[u].size(); ++j) // [A]djacency [L]ist</pre>
        ii& vw = AL[u][j];
        int v = vw.first;
        if (vw.second) // if this edge can still be used
             vw.second = 0; // remove this edge
             // remove bi-directional edge
             for (int k = 0; k < (int) AL[v].size(); ++k)</pre>
                 ii& uw = AL[v][k];
                 if (uw.first == u && uw.second)
                     uw.second = 0:
                     break;
             // continue the tour
             EulerTour(cyc.insert(i, u), v);
// inside int main()
    cyc.clear();
    EulerTour(cyc.end(), 0); // 'cyc' contains an Euler tour starting at vertex '0'
    for (list<int>::iterator i = cyc.begin(); i != cyc.end(); ++i)
        printf("%d\n", *i);
```

# 3.10 Find articulation points and bridges for undirected graph

```
if (dfs_low[v] > dfs_num[u]) printf("Edge (%d, %d) is a bridge\n", u, v);
             dfs_low[u] = min( dfs_low[u], dfs_low[v] );  // update dfs_low[u]
        else if (v != dfs_parent[u]) dfs_low[u] = min( dfs_low[u], dfs_num[v] ); // update dfs_low[u]
// inside int main()
    dfsNumberCounter = 0;
    dfs_num.assign(V, UNVISITED);
    dfs_low.assign(V, 0);
    dfs_parent.assign(V, 0);
    articulation_vertex.assign(V, 0);
    printf("Bridges:\n");
for (int u = 0; u < V; ++u)</pre>
        if (dfs_num[u] == UNVISITED)
             dfsRoot = u;
             rootChildren = 0;
             articulationPointAndBridge(u);
             articulation_vertex[dfsRoot] = (rootChildren > 1);  // special case
    printf("Articulation Points:\n");
    for (int u = 0; u < V; ++u)
         \begin{tabular}{ll} \textbf{if} & (articulation\_vertex[u]) & printf(" Vertex $d\n", u); \end{tabular}
```

### 3.11 Floyd Warshall by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
char before[520][520] = {};
int after[520][520] = {};
int main()
#ifdef LOCAL
    freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
    int n :
    cin >> n ;
    for (int i = 0 ; i < n ; i++) {
   for (int j = 0 ; j < n ; j++)</pre>
            cin >> before[i][j];
    for (int i = 0; i < n; i++) {
        for (int j = i+1; j < n; j++) {
             int sum = 0 ;
             for(int k = i + 1 ; k < j ; k++) {
                if(after[i][k])
                    sum += before[k][j]-'0';
            if( (sum +1) % 10 == before[i][j] - '0'){
                 after[i][j] = 1;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++)
           cout << after[i][j];</pre>
        cout << '\n' ;
    return 0:
```

# 3.12 Graph edges property check

# 3.13 Kruskal by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define 11 long long
using namespace std;
int parent[1020];
struct edge{
    11 n1 , n2 , w ;
}node[25020];
int compare(edge A , edge B ) {
    return A.w < B.w ;
int find_root(int a) {
    if(a != parent[a] )
       return parent[a] = find_root(parent[a]);
    return a ;
int main()
#ifdef LOCAL
    freopen("in1.txt" , "r" , stdin );
freopen("out.txt" , "w" , stdout );
#endif // LOCAL
    int n , m , p_n1 , p_n2 ; // parent_n1 , parent_n2
    vector<int> hce ; //heavy edge circle
    while (cin >> n >> m && n + m != 0 ) {
        for(int i = 0; i < m; i++) {
            cin >> node[i].n1 >> node[i].n2 >> node[i].w ;
        for (int i = 0; i < n; i++)
            parent[i] = i ;
        sort(node , node + m , compare ) ;
        hce.clear() :
        //kruskal
        for(int i = 0; i < m; i++) {
            p_n1 = find_root(node[i].n1);
            p_n2 = find_root(node[i].n2);
            if (p_n1 != p_n2 )
                parent[p_n2] = p_n1 ;
                hce.push_back(node[i].w);
            //debug
            for(int i = 0 ; i < n ; i++)
                cout << parent[i] << ' ';
            cout << '\n';
        sort(hce.begin() , hce.end());
        if(hce.size()){
            for(int i = 0 ; i < hce.size()-1 ; i++)</pre>
                cout << hce[i] << ' ';
```

#### 3.14 Max flow

```
int res[MAX_V][MAX_V], mf, f, s, t;
vi p; // p stores the BFS spanning tree from s
void augment(int v, int minEdge)
    if (v == s) { f = minEdge; return; }
    else if ( p[v] != -1 )
         augment( p[v], min(minEdge, res[ p[v] ][ v ]) );
res[ p[v] ][ v ] -= f;
res[ v ][ p[v] ] += f;
// inside int main(): set up 'res', 's', and 't' with appropriate values
    while (true) // O(V^3 * E) Edmonds Karp's algorithm
         vi dist(MAX_V, INF); dist[s] = 0;
         queue<int> q; q.push(s);
p.assign(MAX_V, -1);
         while (!q.empty())
              int u = q.front(); q.pop();
if (u == t) break; // immediately stop BFS if we already reach sink t
              for (int v = 0; v < MAX_V; ++v)</pre>
                   if (res[u][v] > 0 && dist[v] == INF)
                        dist[v] = dist[u] + 1, q.push(v), p[v] = u;
         augment(t, INF); // find the min edge weight 'f' in this path, if any if (f == 0) break; // we cannot send any more flow ('f' = 0), terminate
         mf += f;
                                // we can still send a flow, increase the max flow!
    printf("%d\n", mf);
```

# 3.15 Max cardinality bipartite matching (MCBM)

```
// Max Cardinality Bipartite Matching (MCBM) solved with augmenting path algorithm O(VE).
vi match, vis:
                 // return 1 if an augmenting path is found & 0 otherwise
int Aug(int 1)
    if (vis[1]) return 0;
    vis[1] = 1;
    for (int i = 0; i < (int)AL[1].size(); ++i) // [A]djacency [L]ist</pre>
       int r = AL[1][i];
                            // edge weight not needed -> vector< vi > AL
       if ( match[r] == -1 || Aug(match[r]) )
            match[r] = 1;
           return 1; // found 1 matching
    return 0:
                        // no matchings
// inside int main()
    // build unweighted bipartite graph with directed edge left->right set
    // left vertices [0..N-1], right vertices [N..V-1]
    match.assign(V, -1); // V is the number of vertices in bipartite graph
    for (int l = 0; l < N; ++1) // N = size of the left set
                           // reset before each recursion
        vis.assign(N, 0);
       MCBM += Aug(1);
   printf("Found %d matchings\n", MCBM);
```

## 3.16 Minimum spanning tree (MST)

# 3.17 Strongly connected component (SCC)

```
// Tarjan O(V + E)
vi dfs_num, dfs_low, visited;
int dfsNumberCounter, numSCC;
vi S:
void tarjanSCC(int u)
    dfs_low[u] = dfs_num[u] = dfsNumberCounter++; // dfs_low[u] <= dfs_num[u]</pre>
                      // stores 'u' in a vector baesd on order of visitation
    S.push back(u):
    visited[u] = 1;
    for (int i = 0; i < (int)AL[u].size(); ++i) // [A]djacency [L]ist</pre>
        int v = AL[u][i].first;
        if (dfs_num[v] == UNVISITED) tarjanSCC(v);
        if (visited[v]) dfs_low[u] = min( dfs_low[u], dfs_low[v] ); // condition for update
    if (dfs_low[u] == dfs_num[u])
                                    // if this is a root (start) of an SCC
                                     // this part is done after recursion
        printf("SCC %d:", ++numSCC);
        while (true)
           int v = S.back(); S.pop_back();
           visited[v] = 0;
            printf(" %d", v);
           if (u == v) break;
       printf("\n");
// inside int main()
    dfs_num.assign(V, UNVISITED);
    dfs_low.assign(V, 0);
    visited.assign(V, 0);
    dfsNumberCounter = numSCC = 0:
    for (int u = 0; u < V; ++u)
        if (dfs_num[u] == UNVISITED)
           tarjanSCC(u);
```

# 4 Greedy algorithms

# 4.1 Interval covering

```
// This is a solution for UVa 10382 - Watering Grass. The problem is a variant
// of Interval Covering problem, which is solved by O(n) Greedy algorithm.
#include <bits/stdc++.h>
#define pb push_back
```

```
using namespace std;
typedef pair<double, double> dd;
typedef vector<dd> vdd;
typedef enum { STOP = 0,
               CONTINUE } status;
int n, 1, w;
vdd spinklers;
int answer;
double pivot;
struct sort compare t {
    bool operator()(dd a, dd b) const {
        return a.first < b.first || (a.first == b.first && a.second > b.second);
} sort_compare;
void InputSpinklers() {
    for (int i = 0; i < n; i++) {
   double x, r; // must be double otherwise WA.
   scanf("%lf %lf", &x, &r);</pre>
        if (w > 2 * r) // ignore spinklers that cannot cover the width of the strip.
            continue:
        if (w == 2 * r) // ignore spinklers that produce no intervals.
            continue;
        double dx = sqrt(r * r - w * w / 4.0);
        spinklers.pb(dd(x - dx, x + dx));
status Check(int& j) {
    if (j == not_set) // there is an interval after pivot that cannot be covered.
        return STOP:
    // record j.
    answer++;
    pivot = spinklers[j].second;
    if (pivot >= 1) // solution found!
     j = not_set;
    return CONTINUE:
void SolveIntervalCovering() {
    sort(spinklers.begin(), spinklers.end(), sort_compare);
    answer = 0:
    pivot = 0.0;
    int j = not_set;
    int iter = 0;
    while (true) {
        if (iter == spinklers.size()) // iterated through all spinklers/intervals.
            Check(j);
            break;
        if (spinklers[iter].first <= pivot) {</pre>
            if (pivot < spinklers[iter].second) // note the next candidate down!</pre>
                if (j == not_set || spinklers[iter].second > spinklers[j].second) // note down the
                      most right candidate.
                    j = iter;
                iter++;
             } else // skip intervals that are completely covered by the previously selected ones.
         else // out bound.
            if (Check(j) == STOP) {
                break:
    if (pivot >= 1) {
        printf("%d\n", answer);
        printf("-1\n");
```

#define not\_set -1

```
int main() {
    while (scanf("%d %d %d", &n, &l, &w) != EOF) {
        spinklers.clear();
        InputSpinklers();
        SolveIntervalCovering();
    }
}
```

# 4.2 Longest increasing subsequence (LIS)

```
#include <bits/stdc++.h>
using namespace std:
typedef vector<int> vi;
int n;
void print_array(const char *s, vi &L, int n) {
 for (int i = 0; i < n; ++i) {
  if (i) printf(", ");</pre>
    else printf("%s: [", s);
    printf("%d", L[i]);
 printf("]\n");
                                                     // predecessor array
vi p;
void print_LIS(int i) {
                                                     // backtracking routine
 if (p[i] == -1) { printf("%d", A[i]); return; }// base case
  print_LIS(p[i]);
 printf(" %d", A[i]);
int memo[10010];
                                                     // old limit: up to 10^4
int LIS(int i) {
                                                     // O(n^2) overall
 if (i == 0) return 1;
  int &ans = memo[i];
  if (ans != -1) return ans;
                                                     // was computed before
  ans = 1:
                                                     // LIS can start anywhere
 for (int j = 0; j < i; ++j)
  if (A[j] < A[i])</pre>
                                                     // O(n) here
                                                     // increasing condition
      ans = max(ans, LIS(j)+1);
                                                     // pick the max
int main() {
 // note: A[n-1] must be set as the largest value ("INF") // so that all LIS (that can start anywhere) will end at n-1
  srand(time(NULL)):
  int n = 10 + rand() %11;
                                                     // [10..201
  A.assign(n, 0);
  A[n-1] = 99;
                                                     // set A[n-1] = INF
  for (int i = 0; i < n-1; ++i)
   A[i] = rand() %101-50;
                                                     // [-50..50]
  vi sample({-7, 10, 9, 2, 3, 8, 8, 1, 2, 3, 4, 99});
  A = sample;
  printf("n = %d:", n);
for (int i = 0; i < n; ++i)</pre>
   printf(" %d", A[i]);
  printf("\n");
  // early 2000 problems usually accept O(n^2) solution
  memset (memo, -1, sizeof memo);
  printf("LIS length is %d\n\n", LIS(n-1));
                                                    // with O(n^2) DP
  // 2020s problems will likely only accept O(n log k) solution
  // new limit: n can be up to 200K
  int k = 0, lis\_end = 0;
  vi L(n, 0), L_id(n, 0);
  p.assign(n, -1);
  for (int i = 0; i < n; ++i) {</pre>
                                                     // O(n)
    int pos = lower_bound(L.begin(), L.begin()+k, A[i]) - L.begin();
    L[pos] = A[i];
                                                     // greedily overwrite this
                                                     // remember the index too
    L_id[pos] = i;
    p[i] = pos ? L_id[pos-1] : -1;
                                                     // predecessor info
    if (pos == k) {
                                                     // can extend LIS?
                                                     // k = longer LIS by +1
      k = pos+1;
      lis_end = i;
                                                     // keep best ending i
```

```
printf("Considering element A[%d] = %d\n", i, A[i]);
printf("LIS ending at A[%d] is of length %d: ", i, pos+1);
printf("[");
print_LIS(i);
print_LIS(i);
print_array("L is now", L, k);
printf("\n");
}
printf("Final LIS is of length %d: ", k);
print_LIS(lis_end); printf("\n");

assert(LIS(n-1) == k);  // both must be identical
return 0;
```

#### 4.3 Max 1D range sum

```
// Max 1D Range Sum solved with Jay Kadane O(n).
// inside int main()
int n = 9;
int A[] = { 4, -5, 4, -3, 4, 4, -4, 4, -5 }; // a sample array A
int sum = 0;
int ans = 0; // important, 'ans' must be initialized to 0
for (int i = 0; i < n; ++i)
{
    sum += A[i];
    ans = max(ans, sum);
    if (sum < 0) sum = 0;
}
printf("Max 1D Range Sum = %d\n", ans);</pre>
```

# 5 Math algorithms

#### 5.1 Chinese remainder theorem

```
#include <bits/stdc++.h>
#define qtr ios::sync_with_stdio(0); cin.tie(0);
#define endl '\n'
#define int long long
#define MOD 1000000
using namespace std;
int inv(int a, int m) {
   int m0 = m, t, q;
int x0 = 0, x1 = 1;
    if(m == 1){
        return 0;
    while (a > 1) {
        q = a/m;
t = m;
        m = a%m, a = t;
        t = x0;
        x0 = x1 - q * x0;
        x1 = t;
    if(x1 < 0){
        x1 += m0:
    return x1:
int findMinX(vector<int> num, vector<int> rem, int k){
    int prod = 1;
    for (int i = 0; i < k; i++) prod *= num[i];</pre>
    int result = 0;
    for(int i = 0; i < k; i++) {</pre>
        int pp = prod / num[i];
        result += rem[i] * inv(pp, num[i]) * pp;
    return result % prod;
int32_t main() { //qtr
    int n = 3;
    vector<int> rem, factor;
    rem.resize(n);
```

```
factor.resize(n);
for(int i = 0; i < n; i++) {
    cin >> factor[i];
}
for(int i = 0; i < n; i++) {
    cin >> rem[i];
}
cout << findMinX(factor, rem, n) << endl;</pre>
```

#### 5.2 Extended greatest common divisor (Ext-GCD)

```
// ax mod b = 1
// ax + by = 1,x=y=0
// a,b Relatively Prime
LL exgcd(LL a,LL b,LL &x,LL &y) {
   if(b) {
      LL tmd=exgcd(b,a%b,y,x);
      y=a/b*x;
   return tmd;
   }
   x=1,y=0;
   return a;
}
```

# 5.3 Greatest common divisor (GCD) and least common multiple (LCM)

```
// or _gcd(a, b) in gcc
int gcd(int a, int b) {
            return a*b?gcd(b,a*b):b;
}
int lcm(int a, int b) {
            return a*b/gcd(a,b);
}
```

#### 5.4 Generate list of prime numbers

```
// Generate list of prime numbers using Sieve of Eratosthenes.
bitset<10000010> bs; // [b]it [s]et 10^7 should be enough for most cases
vi primes;
             // compact list of primes
void sieve(ll upperbound) // create list of primes in [0..upperbound]
    _sieve_size = upperbound + 1; // add 1 to include upperbound
    bs.set():
                        // set all bits to 1
// exception index 0 and 1
    bs[0] = bs[1] = 0; // exce

for (11 i = 2; i <= _sieve_size; ++i)
        if (bs[i])
            // cross out multiples of i starting from i * i!
            for (ll j = i * i; j <= _sieve_size; j += i) bs[j] = 0;</pre>
            primes.push_back( (int) i );
bool isPrime(11 N) // a good enough deterministic prime tester
    if (N <= _sieve_size) return bs[N]; // O(1) for small primes</pre>
    for (int i = 0; i < (int)primes.size(); ++i)</pre>
    if (N % primes[i] == 0) return false;
return true;  // it takes longer if N is a large prime!
                    // note: only work for N <= (last prime in vi 'primes')^2
// inside int main()
    sieve(10000000); // can go up to 10^7 (need few seconds)
    printf("%d\n", isPrime(2147483647)); // 10-digit prime
    printf("%d\n", isPrime(136117223861LL)); // not a prime, 104729 * 1299709
```

## 5.5 N choose R combination (nCr)

```
#define MAXN 100
long long ncr[MAXN+5] [MAXN+5];
// ncr[i][j] = \\((C_{n})^{-}r\)\)
void build_nCr() {
   for(int i = 1; i < MAXN+5; i++) {
      if(i = j)
        ncr[i][j] = 1;
      else if(i > j)
        ncr[i][j] = ncr[i-1][j] * i / (i-j);
   }
}
}
```

# 5.6 Stirling's approximation

```
double Stirling(int n) {
    return (0.5*log(2.0*acos(-1.0)*n)+n*log(n+0.0)-n)/log(10.0);
}// n! Digits
```

# 6 String algorithms

#### 6.1 Knuth-Morris-Pratt algorithm

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define MAXN 100020
using namespace std;
string strA , strB ;
int b[MAXN] , p[MAXN]
void kmp_process() {
   int n = strB.length() ,i = 0 , j = -1 ;
b[0] = -1;
    while(i < n ) {
        while(j >= 0 && strB[i] != strB[j]) j = b[j];
        b[i] = j;
    //debug
     for(int k = 0; k <= n; k++)
cout << b[k] << ' ';
     cout << '\n' ;
int kmp(){
    int n = strA.length() , m=strB.length() , i=0 , j=0 ;
    while(i < n ){
        while(j >= 0 && strA[i] != strB[j]) j = b[j];
        i++ ; j++ ;
    return j ;
int main()
#ifdef LOCAL
    freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
    while(cin >> strA) {
        strB = strA;
        reverse(strB.begin() , strB.end());
        kmp_process();
        int n = kmp();
        cout << strA << strB.substr(n) << '\n' ;</pre>
    return 0;
```

# 6.2 Longest palindromic substring

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define MAXN 1010
using namespace std;
int dp[MAXN][MAXN] = {};
string strA , strB ;
int lcs(){
     n = strA.length();
m = strB.length();
     m = strb.length();
for(int i = 0 ; i <= n ; i++) dp[i][0] = 0 ;
for(int j = 0 ; j <= m ; j++) dp[j][0] = 0 ;
for(int i = 1 ; i <= n ; i++) {
    for(int j = 1 ; j <= m ; j++) {
        if(strA[i-1] == strB[j-1]) dp[i][j] = dp[i-1][j-1]+1 ;
    }
}</pre>
                 else dp[i][j] = max(dp[i-1][j], dp[i][j-1]);
      return dp[n][m];
int main()
#ifdef LOCAL
freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
     int t :
     cin >> t :
      cin.ignore();
            strB = strA ;
           reverse(strB.begin() , strB.end());
           cout << lcs() << '\n' ;
      return 0;
```

#### 6.3 Minimum edit distance

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define MAXN 100
using namespace std;
int dis[MAXN][MAXN] , back_table[MAXN][MAXN] ;
int cnt , m , n ;
void backtracking(int i , int j ){
    if(i==0 || j==0){
        while( i > 0 ){
            cout << cnt++ << " Delete " << i << '\n' ;
             i--:
        while( j > 0) {
            cout << cnt++ << " Insert " << i+1 << "," << strB[j-1] << '\n' ;
        return ;
    if(strA[i-1] == strB[j-1])
        backtracking(i-1,j-1);
    else
        if(dis[i][j] == dis[i-1][j-1]+1){
    cout << cnt++ << " Replace " << i << "," << strB[j-1] << '\n';</pre>
             backtracking(i-1, j-1);
        else if(dis[i][j] == dis[i-1][j]+1){
             cout << cnt++ << " Delete " << i << '\n' ;
             backtracking(i-1, j);
        else if(dis[i][j] == dis[i][j-1]+1){
    cout << cnt++ << " Insert " << i+1 << "," << strB[j-1] <<'\n' ;</pre>
             backtracking(i, j-1);
void med(){ //Minimum Edit Distance
    for(int i = 0 ; i <= n ; i++) dis[i][0] = i ;</pre>
    for(int j = 0; j <= m; j++) dis[0][j] = j;
```

```
for (int i = 1; i \le n; i++) {
        for(int j = 1; j <= m; j++) {
   if(strA[i-1] == strB[j-1]) dis[i][j] = dis[i-1][j-1];</pre>
             else dis[i][j] = min(dis[i-1][j-1], min(dis[i-1][j], dis[i][j-1]))+1;
int main()
#ifdef LOCAL
    freopen("in1.txt" , "r" , stdin );
freopen("out.txt" , "w" , stdout);
#endif // LOCAL
    cin.tie(0);
    cout.tie(0);
    ios::sync_with_stdio(false);
    int flag = 0 ;
    while (getline (cin , strA) && getline (cin , strB)) {
         n=strA.length();
         m=strB.length();
         cnt = 1;
         med();
         if(flag) cout << '\n';</pre>
         flag = 1;
         cout << dis[n][m] << '\n';
         backtracking(n.m);
    return 0:
```

## 6.4 Z-algorithm

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
#define MAXN 1000020
using namespace std;
int z[MAXN] = \{\};
int x=0 , y=0 , maxn = 0;
string s ;
int main()
#ifdef LOCAL
    freopen("in1.txt", "r", stdin);
#endif // LOCAL
    cin >> s ;
    for(int i = 1; i < s.length(); i++){
   z[i] = max(0,min(z[i-x], y - i + 1));
   while(i + z[i] < s.length() && s[z[i]] == s[i+z[i]]){</pre>
              y = i + z[i];
              z[i]++;
    for(int i = 0 ; i < s.length() ; i++)</pre>
         if(z[i] == s.length() - i && maxn >= s.length()-i ){
              cout << s.substr(0,z[i]);</pre>
              return 0 :
         maxn = max(maxn . z[i]);
    cout << "Just a legend" ;
    return 0:
```

#### 7 Data structures

# 7.1 Union-find disjoint sets (UFDS) by David

```
#include <iostream>
#include <bits/stdc++.h>
#define LOCAL
using namespace std;
```

```
int intSum[200080] , intParent[200080] , intSet[200080] ;
int find_root(int intA){
     if(intParent[intA] == intA)
         return intA ;
    intParent[intA] = find_root(intParent[intA]);
return intParent[intA];
int each_debug(int n ) {
    system("Pause");
int main()
#ifdef LOCAL
freopen("in1.txt","r", stdin);
freopen("out.txt","w", stdout);
#endif // LOCAL
     \mbox{int } \mbox{n, m , operation , p , q ;}
     while (cin >> n >> m) {
         for(int i = 1; i <= n; i++) {
              intParent[i] = i+n ;
              intParent[i+n] = i+n ;
              intSum[i+n] = i;
              intSet[i+n] = 1;
         while (m--) {
               cin >> operation ;
              if(operation == 1 ){
                   cin >> p >> q;
int intRoot_p , intRoot_q;
                  intRoot_p = find_root(intParent[p]);
intRoot_p = find_root(intParent[q]);
if(intRoot_p != intRoot_q);
if(intRoot_p != intRoot_q) = intRoot_p;
intSum[intRoot_p] += intSum[intRoot_q];
intSet[intRoot_p] += intSet[intRoot_q];
                   //debug
                   //each_debug(n);
              else if (operation == 2 ) {
                   cin >> p >> q;
                   int intRoot_p , intRoot_q ;
                   intRoot_p = find_root(intParent[p]);
                   intRoot_q = find_root(intParent[q]);
if(intRoot_p != intRoot_q){
                        intParent[p] = intRoot_q;
                        intSum[intRoot_q] += p;
                        intSum[intRoot_p] -= p;
                        intSet[intRoot_q] ++ ;
                        intSet[intRoot_p] -- ;
                   //debug
                   //each_debug(n);
              else if (operation == 3) {
                   cout << intSet[find_root(p)] << ' ' << intSum[find_root(p)] << '\n';</pre>
     return 0;
```

# 7.2 Binary indexed/fenwick tree (BIT)

```
#include <iostream>
using namespace std;

#define LOGSZ 17

int tree[(1<<LOGSZ)+1];
int N = (1<<LOGSZ);

// add v to value at x</pre>
```

```
void set(int x, int v) {
  while (x \le N) {
    tree[x] += v;
    x += (x & -x);
// get cumulative sum up to and including x
int get(int x) {
 int res = 0;
  while(x) {
   res += tree[x];
   x -= (x & -x);
  return res:
// get largest value with cumulative sum less than or equal to x;
// for smallest, pass x-1 and add 1 to result
int getind(int x) {
  int idx = 0, mask = N;
  while (mask && idx < N)
    int t = idx + mask;
   if(x >= tree[t]) {
     idx = t:
     x -= tree[t]:
   mask >>= 1:
  return idx:
```

## **7.3** Rope

```
#include <iostream>
#include <bits/stdc++.h>
#include <ext/rope>
#define LOCAL
#define MAXN 50020
using namespace std:
using namespace __gnu_cxx ;
int main()
    freopen("in1.txt" , "r" , stdin );
#endif // LOCAL
   int n , t , a , b , c , d=0 ;
    int v = 0;
    string strA ;
    rope<char> r[MAXN] , rtmp ;
    cin >> n ;
    while (n--) {
       cin >> t;
       if(t==1){
           cin >> a ;
            cin >> strA ;
            a -= d;
            r[++v] = r[v] ;
            r[v].insert(a,strA.c_str());
            //debug
            //cout << r[v] << '\n' ;
        else if(t==2) {
           cin >> a >> b;
            a -= d; b -= d;
            r[++v] = r[v];
            r[v].erase(a-1.b);
            //debug
            //cout << r[v] << ' ' << r[v-1] << '\n';
        else if(t==3) {
           cin >> a >> b >> c;
            a -= d; b -= d; c -= d;
            rtmp = r[a].substr(b-1,c);
            cout << rtmp << '\n' ;
            d += count(rtmp.begin() , rtmp.end() , 'c' );
    return 0:
```

#### 7.4 Segment tree

```
#include <iostream>
#include <bits/stdc++.h>
#include <string>
#define LOCAL
#define Lson(x) ((x << 1) +1)
#define Rson(x) ((x << 1) +2)
#define INF 99999999
using namespace std;
const int N = 100005;
int shift[35] , num[N] , len_shift;
string strLine :
struct Node {
    int left , right , Min_Value ;
}node[4 * N ];
void build(int left , int right , int x = 0 ){
    node[x].left = left ;
     node[x].right = right ;
    if(left == right){
        node[x].Min_Value = num[left] ;
         return ;
    int mid = (left + right ) / 2;
    //debug
    //cout << mid << '\n';
    //cout << x << ' ' << node[x].left << ' ' << node[x].right << ' ' << '\n';
    build(left , mid , Lson(x));
    build(mid + 1 , right , Rson(x));
    node[x].Min_Value = min(node[Lson(x)].Min_Value , node[Rson(x)].Min_Value);
void handle(){
    len shift = 0 :
     shift[len_shift] = 0;
    for(int i = 6; i < strLine.length(); i++){</pre>
        if(strLine[i] >= '0' && strLine[i] <= '9' ){
    shift[len_shift] = shift[len_shift] * 10 + (int) (strLine[i] - '0');</pre>
             shift[++len_shift] = 0;
    //finaly char is ')' , so len_shift is right
sort(shift , shift + len_shift ) ;
    //debug
    for(int i = 0 ; i < len_shift ; i++)
    cout << shift[i] << ' ';</pre>
    cout << '\n' ;
int query(int left , int right , int x = 0 ){
    if(node[x].left >= left && node[x].right <= right)</pre>
        return node[x].Min_Value ;
    int mid = (node[x].left + node[x].right ) / 2;
int ans = INF;
    //cout << x << ' ' << node[x].left << ' ' << node[x].right << ' ' << node[x].Min_Value << '\n';
    if( left <= mid )</pre>
        ans = min(ans , query(left , right , Lson(x))) ;
    if(mid < right )</pre>
         ans = min(ans , query(left , right , Rson(x)));
    return ans ;
void set_num(int position , int value , int x = 0 ){
    if(node[x].left == position && node[x].right == position ) {
       node[x].Min_Value = value ;
        return ;
    int mid = (node[x].left + node[x].right ) / 2;
    if(position <= mid )</pre>
         set_num(position , value , Lson(x) );
    if(mid < position )</pre>
```

```
set_num(position , value , Rson(x));
    node[x].Min_Value = min(node[Lson(x)].Min_Value , node[Rson(x)].Min_Value );
int main()
    int n , q , intTemp ;
    ios::sync_with_stdio(0);
#ifdef LOCAL
    freopen("out txt" , "w" , stdout ) ;
freopen("in1 txt" , "r" , stdin ) ;
#endif // LOCAL

cin >> n >> q;

for (int i = 1; i <= n; i++)
        cin >> num[i] ;
    build(1,n);
    //debug
    for(int i = 0; i < 13; i++){
    cout << node[i].left << ' ' << node[i].right << ' ' << node[i].Min_Value << '\n';</pre>
    return 0 ;
    while(q--){
         cin >> strLine ;
         if(strLine[0] == 'q'){
              handle();
              cout << query(shift[0] , shift[1] ) << '\n';</pre>
         else if (strLine[0] == 's'){
              intTemp = num[shift[0]] ;
              for(int i = 1 ; i < len_shift ; i++) {</pre>
                  set_num(shift[i-1] , num[shift[i]]) ;
                  num[shift[i-1]] = num[shift[i]];
             num[shift[len_shift-1]] = intTemp;
set_num(shift[len_shift-1], intTemp);
              //cout << intTemp << ' ' << shift[len_shift-1] << '\n' ;
              //for(int i = 1 ; i <= n ; i++)
                   cout << num[i] << ' ';
    return 0:
```

# 7.5 Union-find disjoint sets (UFDS) by Bill

```
class UnionFind
public:
   UnionFind(int N)
      rank.assign(N, 0);
      p.assign(N, 0);
      for (int i = 0; i < N; ++i) p[i] = i;
   bool isSameSet(int i, int j) { return findSet(i) == findSet(j); }
   void unionSet(int i, int j)
      if ( !isSameSet(i, j) )
          int x = findSet(i);
          int y = findSet(j);
          if (rank[x] > rank[y]) p[y] = x; // rank keeps the tree short
             if (rank[x] == rank[y]) ++rank[y];
private:
   vi p, rank;
```

# 8 Utilities

# 8.1 Bit manipulation

```
#define isOn(S, j) (S & (1<<j)) #define setBit(S, j) (S |= (1<<j)) #define clearBit(S, j) (S &= ^{\circ}(1<<j)) #define toggleBit(S, j) (S ^{\circ} = (1<<j)) #define lowBit(S) (S & (-S)) #define setAll(S, n) (S = (1<<n)-1)
```

# 8.2 C++ input output

```
#include <iostream>
#include <iomanip>
using namespace std;
    // Ouput a specific number of digits past the decimal point,
    // in this case 5
    cout.setf(ios::fixed); cout << setprecision(5);</pre>
    cout << 100.0/7.0 << endl;
    cout.unsetf(ios::fixed);
    // Output the decimal point and trailing zeros
    cout.setf(ios::showpoint);
    cout << 100.0 << endl;
    cout.unsetf(ios::showpoint);
    // Output a '+' before positive values
    cout.setf(ios::showpos);
cout << 100 << " " << -100 << endl;</pre>
    cout.unsetf(ios::showpos);
    // Output numerical values in hexadecimal
    cout << hex << 100 << " " << 1000 << " " << 10000 << dec << endl;
```

# 8.3 C++ STL

```
// Example for using stringstreams and next permutation
#include <algorithm>
#include <iostream>
#include <sstream>
#include <vector>
using namespace std;
int main(void) {
  vector<int> v;
  v.push_back(1);
 v.push_back(2);
  v.push back(3);
  v.push back(4);
  // Expected output: 1 2 3 4
                      1 2 4 3
                       4 3 2 1
   ostringstream oss;
oss << v[0] << " " << v[1] << " " << v[2] << " " << v[3];
    // for input from a string s,
    // istringstream iss(s);
    // iss >> variable:
    cout << oss.str() << endl;
  } while (next_permutation (v.begin(), v.end()));
  v.clear();
  v.push_back(1);
```

#### 8.4 Dates

```
// Routines for performing computations on dates. In these routines,
// months are expressed as integers from 1 to 12, days are expressed
// as integers from 1 to 31, and years are expressed as 4-digit
// integers.
#include <iostream>
#include <string>
using namespace std;
string dayOfWeek[] = {"Mon", "Tue", "Wed", "Thu", "Fri", "Sat", "Sun"};
// converts Gregorian date to integer (Julian day number)
int dateToInt (int m, int d, int y) {
  return
    1461 * (y + 4800 + (m - 14) / 12) / 4 +
    367 * (m - 2 - (m - 14) / 12 * 12) / 12 -
    3 * ((y + 4900 + (m - 14) / 12) / 100) / 4 +
    d - 32075;
// converts integer (Julian day number) to Gregorian date: month/day/year
void intToDate (int jd, int &m, int &d, int &y) {
 int x, n, i, j;
  x = jd + 68569;
 n = 4 * x / 146097:
  x -= (146097 * n + 3) / 4;
 i = (4000 * (x + 1)) / 1461001;

x = 1461 * i / 4 - 31;
  j = 80 * x / 2447;
  d = x - 2447 * j / 80;
 x = j / 11;

m = j + 2 - 12 * x;
  y = 100 * (n - 49) + i + x;
// converts integer (Julian day number) to day of week
string intToDay (int jd) {
  return dayOfWeek[jd % 7];
int main (int arge, char **argv) {
 int jd = dateToInt (3, 24, 2004);
  int m, d, y;
  intToDate (jd, m, d, y);
  string day = intToDay (jd);
```

```
// expected output:

// 2453089

// 3/24/2004

// Wed

cout << jd << endl

<< m << "\" << d << "\" << y << endl

<< day << endl;
```

#### 8.5 Prime numbers

```
// O(sqrt(x)) Exhaustive Primality Test
#include <cmath>
#define EPS 1e-7
typedef long long LL;
bool IsPrimeSlow (LL x)
  if(x<=1) return false;</pre>
  if(x<=3) return true;</pre>
  if (!(x%2) || !(x%3)) return false;
  LL s=(LL) (sqrt((double)(x))+EPS);
  for(LL i=5;i<=s;i+=6)
    if (!(x%i) || !(x%(i+2))) return false;
 // Primes less than 1000:
                                     13
                                                              29
79
                                     61
                                           67
                                                       73
             4.3
                               59
                                                 71
                                                                   83
                                                                          89
                              109
179
241
                        107
173
                                    113
                                                       137
                                                             139
       97
                  103
                                                                   149
                                    181
251
317
      157
227
                 167
                                                 193
                                                      197
                                                            199
271
                                                                  211
277
            163
                                          191
                                                                         223
            229
                        239
                                          257
                                                 263
                                                      269
                                                                         281
                                                 337
                                          331
                                                      347
      283
                                                                   3.5.3
            293
                  307
                        311
                                                             349
      367
                  379
                        383
                              389
                                    397
                                          401
                                                 409
                                                       419
                                                             421
                                                                         4.3.3
                                                                   4.31
      439
                        457
                                    463
                                                 479
                                                       487
            443
                  449
                              461
                                                             491
                                                                         503
                                          467
                                                                   499
                              547
                                    557
                                                 569
                                                      571
                                                             577
      509
            521
                  523
                        541
                                          563
                                                                   587
                                                                         593
      599
            601
                  607
                        613
                              617
                                    619
                                          631
                                                 641
                                                       643
                                                             647
                                                                   653
                                                                         659
                                                 719
                                                       727
                                                                         743
      661
            673
                  677
                        683
                              691
                                           709
                                                                   739
      751
                  761
                        769
                                                 809
                                                       811
                                                             821
                                                                   823
                                                                         827
                              859
      829
            839
                  853
                        857
                                    863
                                          877
                                                 881
                                                       883
                                                             887
                                                                   907
                                                                         911
      919
            929
                  937
                        941
                              947
                                    953
                                          967
                                                 971
                                                       977
                                                             983
                                                                   991
                                                                         997
// Other primes:
     The largest prime smaller than 10 is 7.
      The largest prime smaller than 100 is 97.
      The largest prime smaller than 1000 is 997.
      The largest prime smaller than 10000 is 9973.
      The largest prime smaller than 100000 is 99991.
      The largest prime smaller than 1000000 is 999983.
      The largest prime smaller than 10000000 is 99999991.
      The largest prime smaller than 100000000 is 99999989.
      The largest prime smaller than 1000000000 is 999999937.
      The largest prime smaller than 10000000000 is 9999999967.
      The largest prime smaller than 10000000000 is 99999999977.
      The largest prime smaller than 100000000000 is 999999999999.
      The largest prime smaller than 1000000000000 is 999999999971.
      The largest prime smaller than 10000000000000 is 9999999999973.
      The largest prime smaller than 10000000000000 is 999999999999999.

The largest prime smaller than 10000000000000 is 99999999999937.
      The largest prime smaller than 1000000000000000 is 99999999999999997.
```