

# Joint Resource Allocation and Link Association of URLLC Puncturing eMBB Traffic in Multicell Networks

Phong-Binh Tran

Department of Computer Science, National Tsing Hua University, Hsinchu,  
Taiwan

September 5, 2022

Supervised by Chair Professor Jang-Ping Sheu.

# Scenario

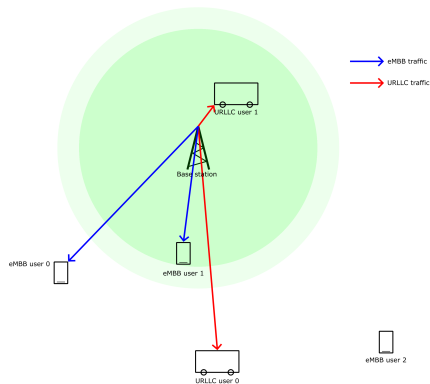


Figure: Singlecell model

- There are approximately 750 people per 1000 square meters living in suburban area<sup>1</sup>[3].
- These are potential eMBB users, who surf the Web, watching videos, and download data.
- During work hours and at night, only a few self-driving vehicles operate that employ URLLC utilities.
  - Uplink transmission (whose bandwidth is independent from that of downlink) is used to upload the vehicles' observations e.g. camera images, sensors data, etc. to the cloud for navigation processing.
  - **Downlink** transmission accounts for the automobiles' control messages.

---

<sup>1</sup>Example

# System

- Homogeneous base stations, mmWave, downlink transmission, OFDMA, multiple-input eMBB and single-input URLLC users.
- Saturated eMBB traffic [5]: Each eMBB user has **infinite** amount of data to be served.
- Strict URLLC constraint: Each URLLC has an amount of data required to be served within a minislot.
- The system aims to maximize eMBB total average rate and fairness while satisfying URLLC demands.

# Poor Edge Service

- Since mmWave is extremely vulnerable to path loss, URLLC reliability is not guaranteed.
- Similarly, eMBB users at cell edges experience low throughput.

- URLLC multicell and eMBB multiconnectivity are prominent candidates to mitigate this issue.

# Multicell

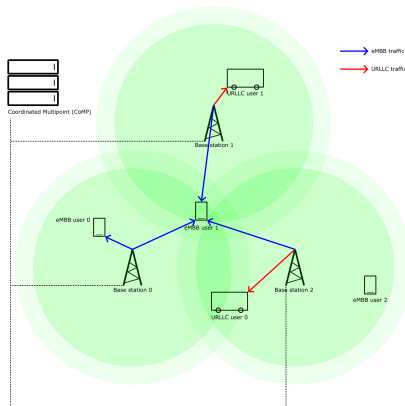


Figure: Multicell model

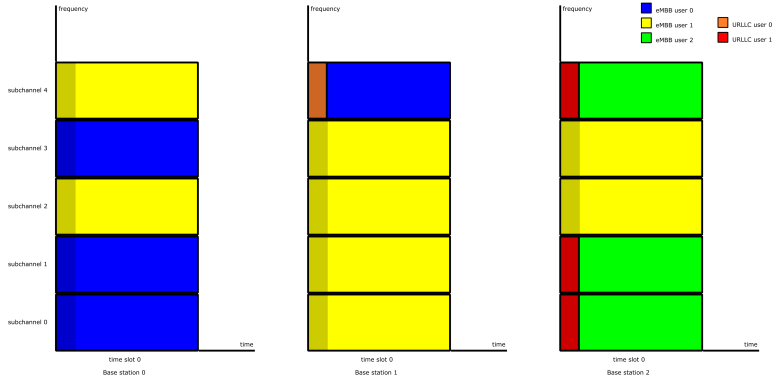


Figure: Multicell framework



# Multicell Co-channel Interference

- Since the base stations are homogeneous i.e. use the same frequency band, there exists 3 types of interference:
  - eMBB-eMBB interference e.g. at subchannel 3, signal from base station 0 to eMBB user 0 interferes with that from base station 1 to eMBB user 1.
  - eMBB-URLLC interference e.g. at subchannel 0, signal from base station 0 to eMBB user 0 interferes with that from base station 2 to URLLC user 1.
  - URLLC-URLLC interference e.g. at subchannel 4, signal from base station 1 to URLLC user 0 interferes with that from base station 2 to URLLC user 1.

- A viable solution might be 5G Non-orthogonal Multiple Access (NOMA) with Successive Interference Cancellation (SIC).
- Inspired by Low Energy Adaptive Clustering Hierarchy (LEACH), a modified Code Division Multiple Access (CDMA) scheme is proposed to tackle the problem<sup>2</sup>.

---

<sup>2</sup>Example

- Our scheme works well with the often small number of base stations.
- Our scheme encompasses URLLC **multiconnectivity** via joint transmission.
- This hence introduces a joint CDMA/OFDMA scheme.

# Spectrum Inefficiency

- Dedicated URLLC bandwidth wastes spectral resources significantly in multicell systems.
  - If 2 subchannels of each base station are dedicated to URLLC traffic, then we would have 6 subchannels sitting **idle for most of the time** in the aforementioned scenario.

- This problem can be addressed by leveraging URLLC superposition/puncturing scheme.
- URLLC superposition scheme employs 5G NOMA SIC, whose performance equals to puncturing when the considered eMBB and URLLC users have the same channel gain.
- URLLC puncturing scheme is discussed here.

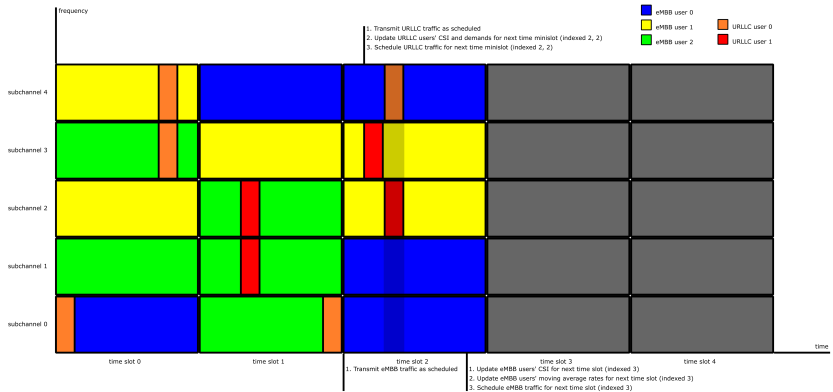


Figure: Singlecell framework

# Stochastic Problem

$$\begin{aligned} & \underset{\alpha, \beta, \delta}{\text{maximize}} && \sum_u \ln \bar{R}_u \end{aligned} \quad (1a)$$

$$\text{subject to} \quad \sum_u \alpha_{u,n,s,l} \leq 1 \quad \forall n \forall s \forall l, \quad (1b)$$

$$\alpha_{u,n,s,l} \in \{0, 1\} \quad \forall u \forall n \forall s \forall l, \quad (1c)$$

$$\sum_s \delta_{v,n,m,s} \leq 1 \quad \forall v \forall n \forall m, \quad (1d)$$

$$\beta_{v,u,n,m,s,l} \leq \delta_{v,n,m,s} \quad \forall v \forall u \forall n \forall m \forall s \forall l, \quad (1e)$$

$$\delta_{v,n,m,s} \in \{0, 1\} \quad \forall v \forall n \forall m \forall s, \quad (1f)$$

$$\sum_v \beta_{v,u,n,m,s,l} \leq \alpha_{u,n,s,l} \quad \forall u \forall n \forall m \forall s \forall l, \quad (1g)$$

$$R_{v,n,m} \geq R_{v,n,m}^{dm} \quad \forall v \forall n \forall m, \quad (1h)$$

$$\beta_{v,u,n,m,s,l} \in \{0, 1\} \quad \forall v \forall u \forall n \forall m \forall s \forall l \quad (1i)$$

- The system maximizes eMBB traffic's total average rate and fairness (1a).
- For each time slot, the system
  - schedules a subchannel to at most one eMBB user (1b).
  - either un-schedules or schedules a subchannel to an eMBB user (1c).



- For each time minislot, the system
  - associates at most one base station to a URLLC user (1d).
  - schedules a subchannel to a URLLC user only if it associates the corresponding base station to the user (1e).
  - either un-associates or associates a base station to a URLLC user (1f).
  - schedules a subchannel to at most one URLLC user, and punctures the subchannel for a URLLC user only if it schedules the subchannel to the corresponding eMBB user (1g)<sup>3</sup>.
  - serves demands of URLLC users without delays (1h).
  - employs URLLC puncturing scheme instead of superposition (1i).

---

<sup>3</sup>Proof in supplementary

- Do note that current eMBB users' rate models for URLLC puncturing scheme in the literature are mostly non-linear [2].
- Whilst proposed linear models are either intractable [6] or inappropriate [1] for discrete subchannel scheduling with multiple URLLC users.

## eMBB Problem

$$\underset{\alpha}{\text{maximize}} \quad \sum_u \ln \bar{R}_u \quad (2a)$$

$$\text{subject to} \quad \sum_u \alpha_{u,n,s,l} \leq 1 \quad \forall n \forall s \forall l, \quad (2b)$$

$$\alpha_{u,n,s,l} \in \{0, 1\} \forall u \forall n \forall s \forall l \quad (2c)$$

# Relaxed eMBB Problem

$$\underset{\alpha'}{\text{maximize}} \quad \sum_u \ln \bar{R}'_u \quad (3a)$$

$$\text{subject to} \quad \sum_u \alpha'_{u,n,s,l} \leq 1 \forall n \forall s \forall l, \quad (3b)$$

$$\alpha'_{u,n,s,l} \geq 0 \forall u \forall n \forall s \forall l \quad (3c)$$

# Gradient Problem

$$\underset{\alpha'_{n_0}}{\text{maximize}} \quad \sum_u \frac{r'_{u,n_0}}{\tilde{r}'_{u,n_0}} \quad (4a)$$

$$\text{subject to} \quad \sum_u \alpha'_{u,n_0,s,l} \leq 1 \forall s \forall l, \quad (4b)$$

$$\alpha'_{u,n_0,s,l} \geq 0 \forall u \forall s \forall l \quad (4c)$$

- The relaxed moving average rate of eMBB user is defined based on exponential moving average (EMA) as

$$\forall u: \tilde{r}'_{u,n} = \begin{cases} \frac{1}{n} \sum_{s,l} \frac{1}{u} \mathbf{r}_{u,n,s,l} & n = 0 \\ (1 - \epsilon) \tilde{r}'_{u,n-1} + \epsilon r'_{u,n-1} & n = 1, \dots, n-1 \end{cases} \left[ \frac{\text{bits}}{\text{slot}} \right]. \quad (5)$$

- The initial value of which is defined by the feasible policy  $\hat{\alpha}'$  for the relaxed eMBB problem where<sup>4</sup>

$$\forall u: \forall s: \forall l: \hat{\alpha}'_{u,n,s,l} = \begin{cases} \frac{1}{u} & n = 0 \\ 0 & n = 1, \dots, n-1 \end{cases}. \quad (6)$$

---

<sup>4</sup>Proof in supplementary

- Given a policy  $\hat{\alpha}$  where for  $n = 0, \dots, N - 1$ ,  $\hat{\alpha}_n$  is a basic optimal point for the  $n^{th}$  gradient problem, then  $\hat{\alpha}$  is an asymptotically optimal policy for the eMBB problem<sup>5</sup>.

---

<sup>5</sup>Proof in supplementary



- However, simplex methods run in exponential time in worst-case scenarios.

- The following policy is asymptotically optimal with respect to the eMBB problem<sup>6</sup>:

$$\forall n: \forall s: \forall l: \hat{\alpha}_{u,n,s,l} = \begin{cases} 1 & u = \min_{\hat{u}} \arg \max_{\hat{u}} \frac{r_{\hat{u},n,s,l}}{\tilde{r}'_{\hat{u},n}} \\ 0 & \text{otherwise} \end{cases} \quad (7)$$

---

<sup>6</sup>Proof in supplementary

- This is a direct generalization of the proportional fairness algorithm [4] in multiconnectivity-based networks.

# URLLC Problem

$$\begin{aligned} & \underset{\beta_{n_0}, \delta_{n_0}}{\text{maximize}} && \sum_u \frac{r'_{u,n_0}}{\tilde{r}'_{u,n_0}} \end{aligned} \quad (8a)$$

$$\text{subject to} \quad \sum_s \delta_{v,n_0,m,s} \leq 1 \quad \forall v \forall m, \quad (8b)$$

$$\beta_{v,u,n_0,m,s,l} \leq \delta_{v,n_0,m,s} \quad \forall v \forall u \forall m \forall s \forall l, \quad (8c)$$

$$\delta_{v,n_0,m,s} \in \{0, 1\} \quad \forall v \forall m \forall s, \quad (8d)$$

$$\sum_v \beta_{v,u,n_0,m,s,l} \leq \hat{\alpha}_{u,n_0,s,l} \quad \forall u \forall m \forall s \forall l, \quad (8e)$$

$$R_{v,n_0,m} \geq R_{v,n_0,m}^{dm} \quad \forall v \forall m, \quad (8f)$$

$$\beta_{v,u,n_0,m,s,l} \in \{0, 1\} \quad \forall v \forall u \forall m \forall s \forall l \quad (8g)$$

# Puncturing Problem

$$\underset{\beta_{n_0, m_0}, \delta_{n_0, m_0}}{\text{minimize}} \quad \sum_{v, u, s, l} \frac{r_{u, n_0, s, l}}{\tilde{r}_{u, n_0}'} \beta_{v, u, n_0, m_0, s, l} \quad (9a)$$

$$\text{subject to} \quad \sum_s \delta_{v, n_0, m_0, s} \leq 1 \quad \forall v, \quad (9b)$$

$$\beta_{v, u, n_0, m_0, s, l} \leq \delta_{v, n_0, m_0, s} \quad \forall v \forall u \forall s \forall l, \quad (9c)$$

$$\delta_{v, n_0, m_0, s} \in \{0, 1\} \quad \forall v \forall s, \quad (9d)$$

$$\sum_v \beta_{v, u, n_0, m_0, s, l} \leq \hat{\alpha}_{u, n_0, s, l} \quad \forall u \forall s \forall l, \quad (9e)$$

$$r_{v, n_0, m_0} \geq r_{v, n_0, m_0}^{dm} \quad \forall v, \quad (9f)$$

$$\beta_{v, u, n_0, m_0, s, l} \in \{0, 1\} \quad \forall v \forall u \forall s \forall l \quad (9g)$$

- Given a time slot policy  $(\hat{\beta}_{n_0}, \hat{\delta}_{n_0})$  where for  $m = 0, \dots, m-1$ ,  $(\hat{\beta}_{n_0, m}, \hat{\delta}_{n_0, m})$  solves the  $m^{th}$  puncturing problem, then  $(\hat{\beta}_{n_0}, \hat{\delta}_{n_0})$  is an optimal point for the URLLC problem<sup>7</sup>.

---

<sup>7</sup>Proof in supplementary

# Scheduling Problem

$$\underset{\gamma_{n_0, m_0}, \delta_{n_0, m_0}}{\text{minimize}} \quad \sum_{v, s, l} c_{n_0, s, l} \gamma_{v, n_0, m_0, s, l} \quad (10a)$$

$$\text{subject to} \quad \sum_s \delta_{v, n_0, m_0, s} \leq 1 \quad \forall v, \quad (10b)$$

$$\gamma_{v, n_0, m_0, s, l} \leq \delta_{v, n_0, m_0, s} \quad \forall v \forall s \forall l, \quad (10c)$$

$$\delta_{v, n_0, m_0, s} \in \{0, 1\} \quad \forall v \forall s, \quad (10d)$$

$$\sum_v \gamma_{v, n_0, m_0, s, l} \leq 1 \quad \forall s \forall l, \quad (10e)$$

$$\sum_{s, l} \gamma_{v, n_0, m_0, s, l} \mathbf{r}_{v, n_0, m_0, s} \geq \mathbf{r}_{v, n_0, m_0}^{dm} \quad \forall v, \quad (10f)$$

$$\gamma_{v, n_0, m_0, s, l} \in \{0, 1\} \quad \forall v \forall s \forall l \quad (10g)$$

- The puncturing cost of subchannel is defined as

$$\forall n: \forall s: \forall l: c_{n,s,l} = \max_u \frac{\tau_{u,n,s,l}}{\tilde{r}'_{u,n}}. \quad (11)$$



- The scheduling problem is equivalent to the puncturing problem<sup>8</sup>.

---

<sup>8</sup>Proof in supplementary

- The scheduling problem is independent from  $\alpha$ .

# Homogeneous Problem

$$\begin{aligned} & \underset{\gamma_{n_0, m_0}, \delta_{n_0, m_0}}{\text{minimize}} && c_{n_0}^{mn} \sum_{v, s, l} \gamma_{v, n_0, m_0, s, l} \end{aligned} \quad (12a)$$

$$\text{subject to} \quad \sum_s \delta_{v, n_0, m_0, s} \leq 1 \quad \forall v, \quad (12b)$$

$$\gamma_{v, n_0, m_0, s, l} \leq \delta_{v, n_0, m_0, s} \quad \forall v \forall s \forall l, \quad (12c)$$

$$\delta_{v, n_0, m_0, s} \in \{0, 1\} \quad \forall v \forall s, \quad (12d)$$

$$\sum_v \gamma_{v, n_0, m_0, s, l} \leq 1 \quad \forall s \forall l, \quad (12e)$$

$$\sum_{s, l} \gamma_{v, n_0, m_0, s, l} \geq \frac{\tau_{v, n_0, m_0}^{dm}}{\tau_{v, n_0, m_0}^{mx}} \quad \forall v, \quad (12f)$$

$$\gamma_{v, n_0, m_0, s, l} \in \{0, 1\} \quad \forall v \forall s \forall l \quad (12g)$$

- The minimum puncturing cost is defined as

$$\forall n: c_n^{mn} = \min_{s,l} c_{n,s,l}. \quad (13)$$

- The maximum rate of URLLC user is defined as

$$\forall n: \forall m: \forall v: \mathfrak{r}_{v,n,m}^{mx} = \max_s \mathfrak{r}_{v,n,m,s}. \quad (14)$$

- $c_{n_0}^{mn} \sum_v \left[ \frac{\tau_{v,n_0,m_0}^{dm}}{\tau_{v,n_0,m_0}^{mx}} \right]$  is the optimal value for the homogeneous problem.

- The nearest association algorithm defines the following point:

$$\forall v: \hat{\delta}_{v,n_0,m_0,s} = \begin{cases} 1 & s = \min_{\hat{s}} \arg \max_{\hat{s}} \mathbf{r}_{v,n_0,m_0,\hat{s}}, \\ 0 & \text{otherwise} \end{cases}$$

$$\forall s: \forall v: \hat{\gamma}_{v,n_0,m_0,s,l} = \begin{cases} 1 & \sum_{\hat{v}=0}^{v-1} \left\lceil \frac{\mathbf{r}_{\hat{v},n_0,m_0}^{dm}}{\mathbf{r}_{\hat{v},n_0,m_0}^{mx}} \right\rceil \hat{\delta}_{\hat{v},n_0,m_0,s} \leq l \\ \leq \left( \sum_{\hat{v}=0}^v \left\lceil \frac{\mathbf{r}_{\hat{v},n_0,m_0}^{dm}}{\mathbf{r}_{\hat{v},n_0,m_0}^{mx}} \right\rceil \hat{\delta}_{\hat{v},n_0,m_0,s} \right) - 1 & \\ 0 & \text{otherwise} \end{cases}.$$

- The nearest association algorithm is a  $\frac{c_{n_0}^{mx}}{c_{n_0}^{mn}}$ -approximation algorithm for the scheduling problem<sup>9</sup>.

---

<sup>9</sup>Proof in supplementary

- The maximum puncturing cost is defined as

$$\forall n: c_n^{mx} = \max_{s,l} c_{n,s,l}. \quad (15)$$



- The opportunistic nearest association algorithm defines the following point:

$$\forall v: \hat{\delta}_{v,n_0,m_0,s} = \begin{cases} 1 & s = \min_{\hat{s}} \arg \max_{\hat{s}} \tau_{v,n_0,m_0,\hat{s}}, \\ 0 & \text{otherwise} \end{cases},$$

$$\forall s: \forall v: \hat{\gamma}_{v,n_0,m_0,s,l} = \begin{cases} \left( \sum_{\hat{v}=0}^{v-1} \left\lceil \frac{\tau_{\hat{v},n_0,m_0}^{dm}}{\tau_{\hat{v},n_0,m_0}^{mx}} \right\rceil \hat{\delta}_{\hat{v},n_0,m_0,s} \right) + 1 \\ 1 & \leq \text{card} \left\{ \hat{l} \mid c_{n_0,s,l} > c_{n_0,s,\hat{l}} \vee (c_{n_0,s,l} = c_{n_0,s,\hat{l}} \wedge l > \hat{l}) \right\} \\ \leq \sum_{\hat{v}=0}^v \left\lceil \frac{\tau_{\hat{v},n_0,m_0}^{dm}}{\tau_{\hat{v},n_0,m_0}^{mx}} \right\rceil \hat{\delta}_{\hat{v},n_0,m_0,s} \\ 0 & \text{otherwise} \end{cases}.$$

- The opportunistic nearest association algorithm is an optimal algorithm for the scheduling problem in single-cell networks<sup>10</sup>.

---

<sup>10</sup>Proof in supplementary

# Contributions

# References

- [1] Arjun Anand, Gustavo de Veciana, and Sanjay Shakkottai. "Joint Scheduling of URLLC and eMBB Traffic in 5G Wireless Networks". In: *IEEE/ACM Transactions on Networking* 28.2 (2020), pp. 477–490. DOI: 10.1109/TNET.2020.2968373.
- [2] Anupam Kumar Bairagi et al. "Coexistence Mechanism Between eMBB and URLLC in 5G Wireless Networks". In: *IEEE Transactions on Communications* 69.3 (2021), pp. 1736–1749. DOI: 10.1109/TCOMM.2020.3040307.
- [3] Richard Florida. *How Should We Define the Suburbs?* 2019. URL: <https://www.bloomberg.com/news/articles/2019-06-12/why-we-need-a-standard-definition-of-the-suburbs> (visited on 07/13/2022).
- [4] Harold J. Kushner and Philip A. Whiting. "Asymptotic Properties of Proportional-Fair Sharing Algorithms". In: *40th Annual Allerton Conference on Communication, Control, and Computing*. 2002, pp. 1051–1059.
- [5] Alexander L. Stolyar. "On the Asymptotic Optimality of the Gradient Scheduling Algorithm for Multiuser Throughput Allocation". In: *Operations Research* 53.1 (2005), pp. 12–25. DOI: 10.1287/opre.1040.0156.
- [6] Hao Yin, Lyutianyang Zhang, and Sumit Roy. "Multiplexing URLLC Traffic Within eMBB Services in 5G NR: Fair Scheduling". In: *IEEE Transactions on Communications* 69.2 (2021), pp. 1080–1093. DOI: 10.1109/TCOMM.2020.3035582.