

You're going to write a series of short essays that will, in the end, be combined into a longer essay which explains Chaos, Dynamics, Fractals, and their interconnections to a general audience.

Your essays should:

- Have a *perspective*: Do you think fractals are fundamental facts of nature? Do you think the "Butterfly effect" is a misused term in pop-culture? etc.
- *Introduce* and *explain* the topics at hand (fractals, chaos and dynamics).
- Not get into the nitty-gritty mathematical details and/or proofs.

In general, you will have to do independent research to get a broader perspective on each essay topic. In class we dive deep into specific examples, but there's a lot more out there, and you don't need to write about the same stuff we've done in class!

The hardest part of the final essay will be developing a common theme. The goal is to write a single coherent essay combining at least two of the three topics of chaos, fractals, and dynamics. Having a theme will provide a means to relate the topics and unify your previous short essays. Some examples of themes (in the form of essay titles) include:

- "From simple definitions, complex behaviour can arise"
- "To study the clouds, we need new ways of measuring"
- "In the 1800's, we thought we knew it all—but that didn't last long"

Your essay may feature equations, though they should be simple and used sparingly. You may (and should) include figures to aid your explanation. Any sources you use (including Wikipedia) should be cited with footnotes or endnotes.

Your essays must be typed in \LaTeX and should be aimed at a non-math audience. You are expected to incorporate the feedback you receive on your short essays into your final essay.

AUDIENCE

The main focus of these essays is to communicate sophisticated mathematical ideas to a non-mathematical (but intelligent) audience. To get an idea of what this means, start by reading Keith Devlin's essay "What is a mathematical proof?"

<https://mathvalues.squarespace.com/masterblog/what-is-a-mathematical-proof>

After reading the essay, think about the following:

- Did the essay have a message? If so, what was it?
- Did the essay use technical math terms? If so, were they defined or described the same way they would be in a math class?
- Who do you feel the essay was targeted towards? Was it you? Your younger sibling? Your professor?

Another excellent, albeit much-longer-than-you-should-write-for-this-course, example of technical math writing for a smart but non-technical audience is Scott Aaronson's "Who Can Name the Bigger Number?" (This one comes with some translations for non-native English speakers.)

<https://www.scottaaronson.com/writings/bignumbers.html>

PROJECT TIMELINE

In total, this writing project is worth 45% of your grade for this course. Below is a short description of each part of the project, along with its deadline.

Fractals Essay 10 % You will write a short essay on fractals. It should address some (but not all!) of the following:

- What are fractals?
- Where do they come from?
- Where (and why) do fractals appear in the real world?
- How can they be measured or classified?
- How are they different from figures in Euclidean geometry?

The Fractals essay should be ~ 2 pages, and is due by **February 5 11:59PM**.

Dynamics Essay 10 % You will write a short essay on dynamical systems. It should address some combination of the following:

- What is a dynamical system?
- Where do you encounter dynamical systems?
- How do you classify dynamical systems?
- Are some dynamical systems easier to understand? Why?

The Dynamics essay should be ~ 2 pages, and is due by **March 12 11:59PM**.

Title & Abstract 2 % You will submit the **title** of your final essay, along with a one-paragraph **abstract** explaining:

- The theme of your final essay (based on your title).
- How the topics of chaos, fractals, and dynamics relate to your theme.

Additionally, you will provide a few sentences explaining how you will unify your small essays into a single coherent piece, or whether you will go in a different direction than your previous essays.

The title & abstract is due by April 2 11:59PM.

Final Essay 20 % You will submit a final essay combining your short essays into one. You may need to significantly re-work parts of your previous essays to get them to flow together. You can put the essays together in any order (it doesn't need to be Fractals \rightarrow Dynamics, and probably shouldn't be in that order!). You may also incorporate the idea of Chaos into your final essay, even though it wasn't the focus of your shorter essays.

The final essay should be ~ 6 pages, and is due by **April 16 11:59PM**.

Reflection 3 % You will submit a few paragraphs reflecting on the following:

- How did you incorporate the feedback on your short essays into your final essay?
- How has your understanding of mathematical communication changed over the term?
- How has your perception of mathematics and definitions changed over the term?

The reflection is due at the same time as the final essay.

GRADING

The focus of this writing project is **mathematical communication**. To this end, your essays will be graded on the following criteria:

- **Writing for your audience:** You are trying to explain ideas to a non-mathematical audience. (Imagine you were writing a feature for a magazine like New Scientist.) This means you should avoid overly technical descriptions, but you should also *explain why your audience should care*.

Why are fractals interesting? How will knowing about dynamical systems impact their day-to-day life?

- **Mathematical understanding:** You need to talk about the specific ideas you've learned in the course. *An essay with little mathematical content is not acceptable.* It should be clear to a mathematician reading your essay that you know what you're talking about.
- **Quality of writing:** If your essay is hard to read, it's not going to communicate anything because people won't read it! Make sure to write in complete sentences and use effective paragraphing. Your essay should also flow logically from one paragraph to the next.

In addition, the final essay will also be graded on two extra criteria:

- **Cohesion of topics:** The end goal is a single 6-page essay, not multiple 2-page essays! You should relate each topic to your common theme and have a natural progression of ideas.
- **Creativity:** Do your best to make your essay your own. Have you used diagrams in your essay in a novel way? Have you used any interesting outside sources? Have you related math topics to your personal experiences?

Pay careful attention to the page count: the short essays should be ~ 2 pages, and the final essay should be ~ 6 pages. If your essays are much shorter than this, you probably haven't explored enough facets of your topic. If your essays are much longer than this, the TAs will only mark up to the page count!

ADVICE

Take the 2-page essays seriously! Your short essays should be coherent and have a logical flow of ideas, just like the final essay. Make sure to write in complete sentences and use effective paragraphs. Remember that each draft is worth 10% of your final grade.

Read the TA feedback. The course TAs will provide specific, constructive feedback on each of your drafts. Read their comments carefully and keep them in mind when working on the final version of your essay. Any general advice that they give can also be useful when working on the other short essays.

Make use of UofT's writing centres.

- Your college has a writing centre where they can provide support on writing both the drafts and the final essay. You can find more details here: <https://writing.utoronto.ca/writing-centres/arts-and-science/>
- The faculty runs a handful of mini-courses for English language learners designed to give students experience in writing formal, academic English: <https://www.artsci.utoronto.ca/current/academic-advising-and-support/english-language-learning>
- UofT also has a writing advice site that covers everything from planning to revising your writing: <https://advice.writing.utoronto.ca/>