

# Hadamard Matrix

Time limit: 1 sec

A Hadamard matrix, named after the French mathematician Jacques Hadamard, is a square matrix containing only 1 or -1. There are several Hadamard matrices, each is identified by an integer **n**. The Hadamard matrix of the order n is denoted by  $H_n$  and has the size of n row and n column. The Hadamard matrix of rank 2n can be constructed from the Hadamard matrix of rank n. The construction of the Hadamard matrix of rank n can be defined recursively as follow.

$$H_1 = [1]$$

$$H_2 = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$$

$$H_n = \begin{bmatrix} H_{n/2} & H_{n/2} \\ H_{n/2} & -H_{n/2} \end{bmatrix}$$

Given a column vector of size n  $v = \begin{pmatrix} v_1 \\ v_2 \\ \vdots \\ v_n \end{pmatrix}$ , your task is to calculate  $H_n v$  which is the production

of the matrix  $H_n$  and the vector  $v$

## Input

- The first line of input contains an integers **n**. **It is guaranteed that  $n = 2^k$  where  $0 \leq k \leq 18$ .**
- The second line contains **n** integers representing  $v_1, v_2, \dots, v_n$  where  $-1,000 < v_n < 1000$ .

## Output

The output must has exactly 1 line that contains n integers that described the vector  $H_n v$ .

## Example

Input	Output
1 10	10
2 10 20	30 -10
4 1 2 4 8	15 -5 -9 3