

### 3) Lemma 2

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- An entry  $(e, f, \Delta)$  gets deleted if  $f \leq 1$  when reaching a bucket boundary
- We know that  $b_{\text{current}}$  keeps track of the number of new buckets that were started
- $f$  is incremented everytime when  $e$  is processed after creation of  $(e, f, \Delta)$
- Also,  $f$  can only be decremented by 1 if a bucket ends
- Suppose that  $(e, f, \Delta)$  gets deleted:  
 $\Rightarrow$  Since  $f$  might have been  $f_e$  at some point of the past, at least  $f_e - 1$  decrements by 1 must have happened to ensure  $f \leq 1$
- The number of decrements is bounded by the number of bucket boundaries that were reached  
 $\Rightarrow b_{\text{current}} \geq f_e \checkmark$