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In[2]:= (* Explain the meaning of each line *)
In[3]:= (*xn is drawn from a uniform distribution in [0,1]*)
x[n_] := RandomReal[]

In[4]:= (*x1*)
x[1]

Out[4]= 0.289361

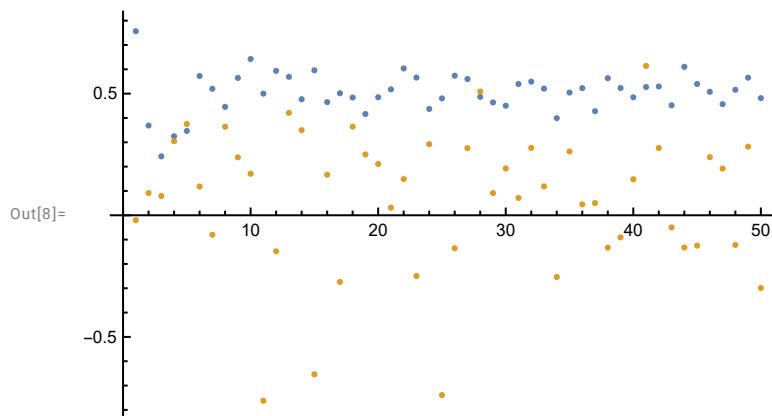
In[5]:= (*x2*)
x[2]

Out[5]= 0.839529

In[6]:= (*Average of x1, x2, x3... upto xn, in the limit n→∞,
the distribution of this average approaches to a gaussian with 0 standard deviation,
which is a dirac delta distribution*)
AvgX[n_] := Sum[x[j], {j, 1, n}] / n
(*Average of x1, x2, x3... upto xn, subtracted from mean of the uniform distribution,
scaled by √n. This is the random variate appearing in the Central Limit Theorem,
its distribution approaches towards a Gaussian with finite standard deviation*)
CLTX[n_] := (Sum[x[j], {j, 1, n}] / n - 0.5) √n

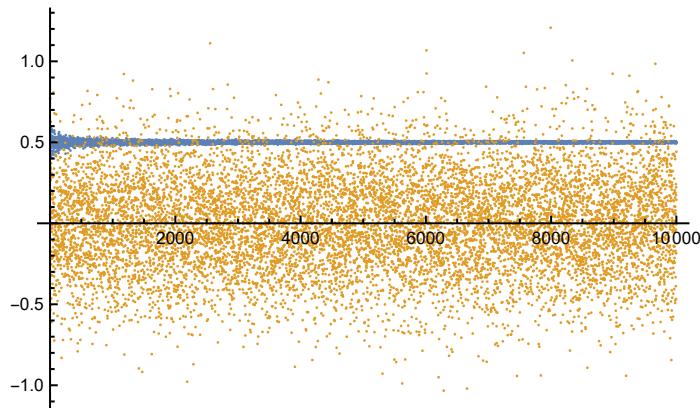
In[8]:= (*As we can indeed see, the distribution of the average is being squished for
large n but the random variate appearing in CLT has an almost constant σ*)
ListPlot[ {Table[AvgX[n], {n, 1, 50}], Table[CLTX[n], {n, 1, 50}]}]

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In[11]:= (*As we can indeed see, the distribution of the average is being
squished for large n(approaching a  $\delta$  distribution) but the random
variate appearing in CLT is a Gaussian with almost constant  $\sigma$ *)
ListPlot[ {Table[AvgX[n], {n, 1, 10^4}], Table[CLTX[n], {n, 1, 10^4}]}]
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Out[11]=



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In[12]:= (*A better representation is the histogram, where we can see the distributions*)
Histogram[{Table[AvgX[n], {n, 1, 10^4}], Table[CLTX[n], {n, 1, 10^4}]},
Automatic, "Probability", ChartLabels -> {"Average", "CLT"}]
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Out[12]=

