(5)
$$\forall x \in \mathbb{N} : x >$$
(1) $x : \alpha$

 $x:\alpha$

 $\lambda x : \alpha . x : \alpha \to \alpha$

 $\mathbf{var} \ x : \mathbb{N}$

x > 5

x > 1

(1)

(2)

(3)

(4)

(2)

(3)

 $x > 5 \implies x > 1$ \implies -intro on (2) and (3) $\forall x \in \mathbb{N} : x > 5 \implies x > 1 \quad \forall \text{-intro on (1) and (4)}$

$$\Rightarrow$$
 -intro on \forall -intro on (1)

Assumption

Introduction of x

Arithmetic on (1) and (2)