

II. Exponentials and Logarithms: Calculus

1c)

$$\frac{d}{dx} e^{-x^2} = e^{-x^2} \cdot \frac{d}{dx} -x^2 = \boxed{-2e^{-x^2}x}$$

1d)

$$\frac{d}{dx} (x \ln x - x) = 1 \cdot \ln x + x \cdot \frac{1}{x} - 1 = \boxed{\ln x}$$

1e)

$$\frac{d}{dx} \ln x^2 = \frac{1}{x^2} \cdot 2x = \boxed{\frac{2}{x}}$$

1f)

$$\frac{d}{dx} (\ln x)^2 = (2 \ln x) \cdot \frac{1}{x} = \boxed{\frac{2 \ln x}{x}}$$

1m)

$$\frac{d}{dx} \left(\frac{1 - e^x}{1 + e^x} \right) = \frac{-e^x(1 + e^x) - e^x(1 - e^x)}{(1 + e^x)^2} = \boxed{\frac{-2e^x}{(1 + e^x)^2}}$$

4a)

$$\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n} \right)^{3n} = e^3$$