

a)

$$\frac{dy}{dx} = ry$$

$$\frac{dy}{y} = r dx$$

$$\int \frac{dy}{y} = \int r dx$$

$$\ln y = rx + C$$

$$y = e^{rx+C}$$

b)

$$\frac{dy}{dx} = ry(s-y)$$

$$\frac{dy}{y(s-y)} = r dx$$

$$\int \frac{dy}{y(s-y)} = \int r dx$$

$$\frac{1}{s} \ln \left| \frac{y}{s-y} \right| = rx + C$$

$$\frac{y}{s-y} = \pm e^{s(rx+C)}$$

$$y = \pm \left(se^{s(rx+C)} - ye^{s(rx+C)} \right)$$

$$y(1 \pm e^{s(rx+C)}) = \pm se^{s(rx+C)}$$

$$y = \pm \frac{se^{s(rx+C)}}{1 \pm e^{s(rx+C)}}$$