

2B. Curve sketching

2a)

$$y = x^3 - 3x + 1$$

$$y' = 3x^2 - 3$$

$$y'' = 6x$$

inflection point at $x=0$

2e)

$$y = \frac{x}{x+4}$$

$$y' = \frac{4}{(x+4)^2}$$

$$y'' = \frac{-8}{(x+4)^3}$$

no inflection points

2h)

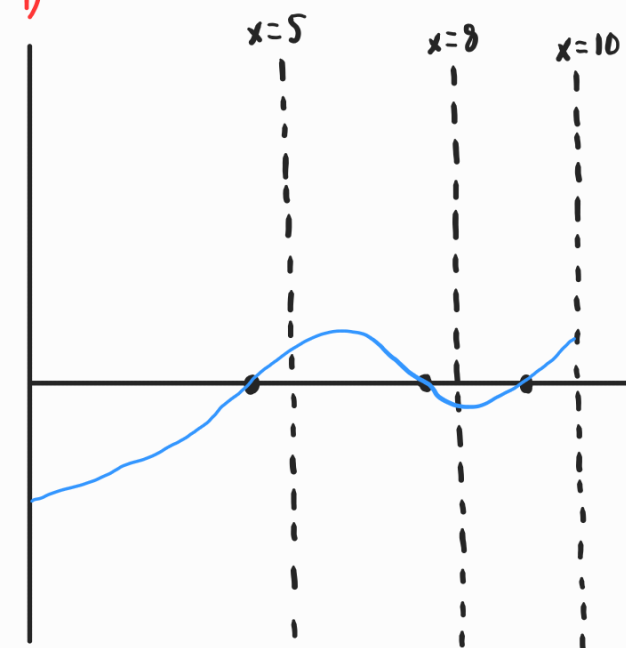
$$y = e^{-x^2} = e^u$$

$$y' = e^u u' = -2x e^{-x^2}$$

$$y'' = -2e^{-x^2} + 4x^2 e^{-x^2}$$

inflection points at $x = \pm \frac{1}{\sqrt{2}}$

4)



6a)

$$f(x) = ax^3 + bx^2 + cx + d$$

$$f'(x) = 3ax^2 + 2bx + c$$

$$3a + 2b + c = 0$$

$$3a - 2b + c = 0$$

$$6a + 2c = 0$$

$$c = -3a$$

$$b = 0$$

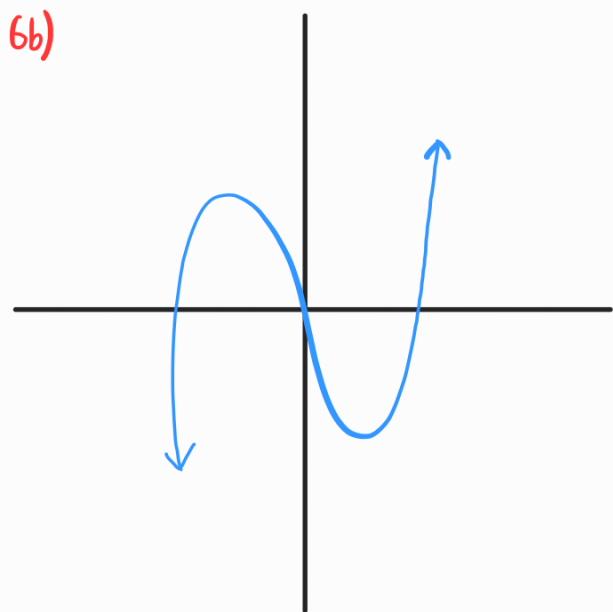
$$a > 0$$

$$b = 0$$

$$c = -3a$$

$$d = \text{any real number}$$

6b)



7a)

$$f'(a) = \lim_{\Delta x \rightarrow 0} \frac{\Delta y}{\Delta x}$$

$$y \text{ increasing} \Rightarrow (\Delta y \text{ and } \Delta x > 0) \text{ or } (\Delta y \text{ and } \Delta x < 0) \Rightarrow \frac{\Delta y}{\Delta x} > 0 \Rightarrow \lim_{\Delta x \rightarrow 0} \frac{\Delta y}{\Delta x} > 0$$

7b)

?