Binary to Octal

1 Generally Useful Math

Trig Properties

$$\sin^2 x + \cos^2 x = 1 \qquad \frac{d}{dx} \sin x = \cos x$$

$$\tan x = \frac{\sin x}{\cos x} \qquad \frac{d}{dx} \cos x = -\sin x$$

$$\frac{d}{dx} \tan x = \sec^2 x \qquad \frac{d}{dx} \cot x = -\csc^2 x$$

$$\frac{d}{dx} \arcsin x = \frac{1}{\sqrt{1 - x^2}} \qquad \frac{d}{dx} \arccos x = \frac{-1}{\sqrt{1 - x^2}}$$

$$\frac{d}{dx} \arctan x = \frac{1}{1 + x^2}$$

Simply follow the table:
$$000 \rightarrow 0.001 \rightarrow 1.002 \rightarrow 2.003 \rightarrow 3.004 \rightarrow 4.005 \rightarrow 5.006 \rightarrow 6.007 \rightarrow 7.000$$

Log & Exp Properties

$$\frac{x}{dx}b^{x} = b^{x} \ln x \qquad \log(\frac{1}{x}) = -\log x$$

$$\log_{a} x = \frac{\log_{b} x}{\log_{a} x} \qquad \frac{d}{dx}e^{ax} = ae^{ax}$$

$$\frac{d}{dx}a^{x} = a^{x} \ln a \qquad \frac{d}{dx} \ln x = \frac{1}{x}$$

$$x^{0} = 1 \qquad x^{n} \cdot x^{m} = x^{n+m} \qquad x^{-n} = \frac{1}{x^{n}}$$

$$\log_{a} x^{n} = n\log_{a} x \qquad \frac{e^{-nx}}{e^{x}} = e^{-(n+1)x}$$

$$\log_{a}(\frac{x}{y}) = \log_{a} x - \log_{a} y$$

$$\log_{a}(xy) = \log_{a} x + \log_{a} y$$

Binary to Hex

Useful Series

$$r^0 + r^1 + r^2 + r^3 = \frac{r^n - 1}{r - 1}$$
 for an alternating series the following will work to start:

will work to start: $\sum_{n=0}^{\infty} (-1)^n \text{ or } \sum_{n=0}^{\infty} (-1)^{n+1}$

This identical to the Octal method, the Hex symbols range from 0 to *F* and binary from 0000 to 1111. Simply count up un binary and there is a simple conversion.

In Class Terminology

the relative error formula:
$$\frac{|x-\hat{x}|}{x}$$

 $x' = f(t, x)$
this was represed strangely in class:
If $x'' = xx'$ then $x''' = xx'' + x'x'$

One & Two's Complement

2 Base Conversion

Decimal to Binary

For this simply find the place of the largest binary number that (of the form 2^n) that is within the number. Successivley subtract these numbers while keeping track of their place to generate the binary number.

3 Runge-Kutta Methods

RK4

Binary to Decimal

For this notice that each place in the decimal number has a corresponding power of 2. If the decimal number has a floating point then the power is negative counting from zero. This generates a sum of the form: $2^{n} + \dots + 2^{2} + 2^{1} + 2^{-1} + 2^{-2} + \dots + 2^{-m}$ Where n is the most significant digit and

m is the least. The 2^{-1} term is the begin-

ning of the floating point numbers.

This is the 4th order (RK4) Runge-Kutta method for the Initial Value Problem (IVP):

$$x(t+h) = x(t)\frac{1}{6}(K_1 + 2K_2 + 2K_3 + K_4)$$

where the following are values of K_n :
 $K_1 = hf(t,x)$
 $K_2 = hf(t + \frac{1}{2}h, x + \frac{1}{2}K_1)$

$$K_3 = hf(t + \frac{1}{2}h, x + \frac{1}{2}K_2)$$

 $K_4 = hf(t + h, x + K_2)$

 $K_4 = hf(t + h, x + K_3)$ first, the K_n values are calculated in succession. They the K_n values are filled into the first formula above.