

# Visualizing environmental econometrics using directed acyclic graphs

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## Abstract

Environmental economists have gravitated toward writing empirical papers with an emphasis on causal inference. Despite this development, there has not been much progress in the way of adopting an explicit framework for communicating causal hypotheses—prior beliefs about the structure of a data generating process. The shortfall reduces the transparency and accessibility of the assumptions underlying effect identification and makes the testing of causal hypotheses impossible. This article explains why an explicit framework is worthwhile and demonstrates how Directed Acyclic Graphs can augment and standardize the communication of causal knowledge.

**Keywords:** causal models, identification, research design, specification testing, communication, directed acyclic graphs (JEL: A20, C12, C51, C52, Q50)

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# A framework for communicating causal knowledge

Most empirical papers in environmental economics today are structured around a single statistical inference of interest and written to emphasize how an identification strategy supports a measurement with a causal interpretation (Segerson, 2019). In many cases, the discussion appears to take more effort than the statistics because designing clever identification strategies for causal inference is difficult. It is now the thoughtful communication of research design that defines “rigor” in empirical papers, rather than a barrage of specification tests (Angrist and Pischke, 2010).

This article considers the clarity, transparency, and testability of *causal hypotheses*—prior beliefs about the structure of a data generating process. This is thought to be addressed when testing a statistical inference’s sensitivity to varying empirical assumptions about functional form or control variables, but the exercise in showing consistency across regression specifications is not undertaken with any explicit causal model in mind. While sensitivity analyses are likely to give researchers confidence in their results, they are unable to determine whether an approach estimates an effect of interest.

The spirit of specification testing is to learn whether a statement like “the effect of  $X$  on  $Y$  is likely positive” is permissible. A test of a result’s sensitivity to an assumption about a data generating process is suitable to bolster this claim because it tests if a researcher is estimating the effect of interest. This change to a causal model will naturally motivate a specific change in an empirical strategy and highlight a critical prior belief; in contrast, the functional permutation of a regression specification fails to imply anything about the correctness of the underlying causal model. In essence, the typical regression specification test assumes that the result is always causally-interpretable—once the identification assumptions have been mentioned elsewhere in the article. When causal models are not explicit, the testing of causal hypotheses becomes impossible.

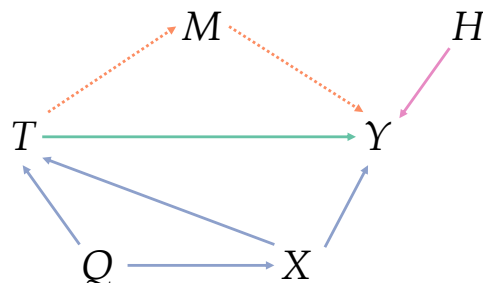
Directed Acyclic Graphs (DAGs) (Pearl, 1995) systematize the creation and testing of causal hypotheses. DAGs display a researcher’s priors and empirical assumptions, motivate identification strategies, and indicate the conditions under which a regression yields a causally-interpretable measurement. They provide a way to choose conditioning variables, sources of data, and empirical methods in a manner that can be easily understood and validated by a wider audience of researchers, students, and stakeholders. The purpose of this article is to provide a complete introduction to this visualization technique, explore how it can facilitate causal hypothesis testing over a wide swath of settings, provide a fair assessment of the costs and benefits of DAGs, and share novel econometric insights discovered while investigating their use. This article lowers the costs of adoption for an emerging method of broad applicability in environmental economics.

Several articles compare the DAG framework to competing foundations for conveying causal information. The potential outcomes framework is already widely-used in applied economics to validate identification strategies, and has the advantage over DAGs in terms of the scope of empirical assumptions and implications that can be represented (e.g. monotonicity and the local average treatment effect) (Imbens, 2020). In contrast, the DAG framework is better at making the historically “ad hoc” facets of causal inference in economics more transparent and systematic (e.g. covariate selection and the identification of bias) (Schneider, 2020; Huntington-Klein, 2022). Heckman and Pinto (2022) claims that the scope of both frameworks is limited and promotes structural equation modeling to address causal questions in non-empirical settings (e.g. general equilibrium).

The next two sections provide a primer on DAGs and several applications to illustrate their utility. The penultimate section demonstrates a review of a recent research article from the environmental economics literature with the aid of a DAG and describes the limitations of a graphical approach. The final section discusses the merits of integrating this innovation into future presentations, publications, peer reviews, and pedagogy.

## A primer on Directed Acyclic Graphs

When constructing a DAG, the initial task is to center thinking around a particular relationship of interest, e.g.  $T \rightarrow Y$  in Figure 1. Directed arrows like  $T \rightarrow Y$  convey statements like “the outcome  $Y$  is in part determined by the status of some treatment  $T$ .” Additional causal relationships between  $T$  and  $Y$  may be mediated by other variables (e.g.  $M$ ). A causal model is expanded to explicitly consider any variables which could distort the observed relationship between  $T$  and  $Y$  away from a causal interpretation. The complexity of a model is ultimately up to the researcher, and every inclusion or omission of a variable or arrow marks an explicit assumption about the underlying data generating process.



**Figure 1:** A representative DAG. Some variables—and the causal links between them—may not be observable, and these can be emphasized with dashed arrows. The use of color directs focus towards certain links of interest like  $T \rightarrow Y$ , although this is merely a stylistic preference.

Spurious relationships between  $T$  and  $Y$  are created by “confounding” variables—those which influence both  $T$  and  $Y$ —like  $X$  or  $Q$ . If the effects of these confounding variables are not mitigated, an estimate of the treatment effect will be biased. Conversely, variables like  $H$  will not influence the causal interpretation of a measured correlation between  $T$  and  $Y$ , since they do not contribute to a spurious relationship. Thus the DAG provides a way to differentiate between malignant and benign sources of variation.

Ideally, there would exist some experimental source of variation for  $T$ . This would sever any arrows leading towards  $T$  in Figure 1. But this ideal isn’t necessary. If data on  $X$  and  $Q$  are available, a simple matching strategy can control for these confounding variables. Regression will automatically isolate the causal relationship between  $T$  and  $Y$  from the variation induced by changes in  $X$  or  $Q$ . In the language of DAGs, this “closes” the non-causal paths between  $T$  and  $Y$ . The DAG does not keep track of the paths that are closed by a researcher’s analysis—or the paths that remain “open”—it only signals whether a path is a problem that an identification strategy needs to address.

Sometimes a confounding variable like  $Q$  isn’t observable, but this may not be a problem if data on  $X$  is available. This is because of a restriction imposed on the model via the term “acyclic.” Disallowing loops enables the endogenous variables in a model to be determined recursively, which in turn allows a DAG to yield statements about conditional independence, e.g. “ $Y$  is independent of  $Q$  conditional on  $X$ .” Since variation in  $Q$  can only impact  $Y$  through an intermediate effect on  $X$ , controlling for the variation in  $X$  halts the pass-through of information from  $Q$  to  $Y$ . Thus the requirement for closing a spurious path between  $T$  and  $Y$  can be relaxed to either controlling for a confounding variable—or one of its “descendants”—along that path. Here, once  $X$  is controlled for, the status of  $Q$  becomes immaterial in the identification of the effect of  $T$  on  $Y$ . However, the decision to include  $Q$  (or  $H$ ) as control variables may improve the *precision* of the  $T \rightarrow Y$  estimate.

Because a DAG is a non-parametric representation of a causal process, it will not recommend a particular estimation procedure or functional form. For this step, economists should rely on traditional econometric knowledge. Regardless of specification, when reporting regression output, the marginal “effect” on  $Y$  attributable to  $T$  reflects all remaining open paths from  $T$  to  $Y$ . In the present example, the direct effect cannot be disentangled from the indirect effect here, as the “mediator”  $M$  is unobservable.

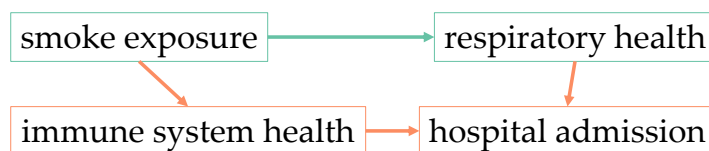
The researcher determines whether the exploited variation generates a measurement of a causal effect, and the causal claim relies on an implicit assumption that the DAG accurately models the data generating process. Thus the addition of an explicit model does not remove the potential for misspecification. However, if someone disagrees with a prior, they may make changes to the DAG and review whether the new DAG admits the same identification strategy or a completely different one.

# Applications of DAGs to environmental economics

This section demonstrates how to implement DAGs through the use of several examples from environmental economics. Despite their simplicity, the following examples would be fairly difficult to explain without the use of DAGs. This suggests that discussions of research design can be made more clearly and succinctly with the aid of the graphical approach. In this way, DAGs are hardly redundant, but augmentative.

## Bad controls are usually collider variables

Some research design strategies can inadvertently introduce bias to estimators. To illustrate, the following example concerns the long run impact of cumulative wildfire smoke exposure on respiratory health using hypothetical data from hospital admissions. Figure 2 provides a model of a data generating process that considers how the sample is being collected. Because smoke exposure also has negative long run impacts on immune system health, it increases the likelihood of a hospital visit through a second causal channel that is unrelated to respiratory health. For expositional clarity, no variables are assumed to confound the relationship between smoke exposure and respiratory health.



**Figure 2:** Collecting data using a selected sub-sample will not only result in a lack of external validity, but a lack of internal validity as well, due to collider bias.

Certain variables create spurious correlations between treatment and outcome only once they are included as controls—or in this case, baked into the data collection. In the present example, weakened immune system health and weakened respiratory health are both sufficient conditions for being more likely to showing up in the hospital data. But the sufficiency of either condition implies that among hospital admits, those with poorer immune system health are more likely to have better respiratory health (and vice versa). This is not a causal claim, but a spurious correlation created by the data generating process. Since people impacted by wildfires are more likely to have worsened immune system health than the unaffected, the spurious link will contribute to an under-estimation of the negative respiratory health effect.

DAGs alert researchers to potential identification pitfalls that would be difficult to explain without a graphical aid. Whenever a variable invites a collision of two arrows, the variable is called a “collider.” Stratifying on a collider variable—through inclusion in the

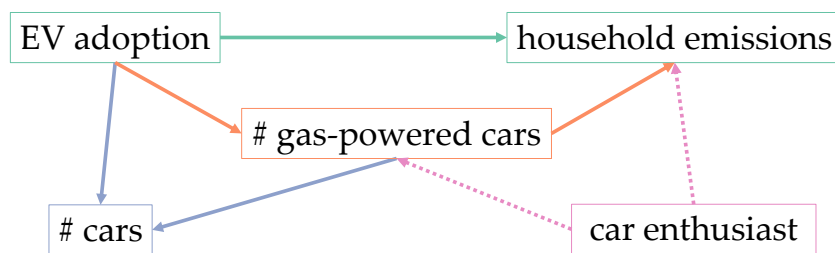
control set or the data collection process—will open an otherwise closed path. The abstraction of the identification problem to a graphical one makes the detection and discussion of a collider bias simple. Without the concept of a collider, these biases are easily missed.

A common mistake is to reduce this example to an external validity concern. However, the measured relationship between smoke exposure and respiratory health won't even be *internally*-valid here. The collider bias will reduce the measured smoke exposure effect for the hospitalized sub-sample. However, since the second mechanism through which smoke exposure increases the likelihood of hospital admission is known, an identification strategy that conditioned on immune system health would close the non-causal path from smoke exposure to respiratory health, even when the collider is in play. This allows the estimation of an unbiased respiratory health effect for the hospitalized population.

## The role of a variable matters

Does adopting an electric vehicle decrease household emissions? The direct effect is likely positive due to increased mineral extraction and fossil fuel-derived electricity demand. However, the bulk of the adoption effect is likely indirect and negative, through the replacement of a gas-powered car. As a straw-man, consider the economist who controls for the number of gas-powered cars in the household. This would clearly be a mistake, as they are conditioning on a mediator that facilitates a causal effect; i.e. they have closed a causal path that should have been left open. By controlling for the number of gas-powered cars, they removed the replacement channel.

But this economist wouldn't even measure the direct effect with their strategy, given the understanding of car buying preferences implied by Figure 3. Other relevant household characteristics will manifest a collider bias when controlling for the number of gas-powered cars. For example, households with car enthusiasts are drawn to gas-powered cars and driving more often, both for the sake of leisure. The control variable is a collider on the enthusiast path—conditioning on the number of gas-powered cars introduces a spurious correlation between electric vehicle adoption and enthusiasm.



**Figure 3:** The true impact of electric vehicle adoption on household emissions is only revealed if controls for the number of cars in the household—gas-powered or otherwise—are omitted.

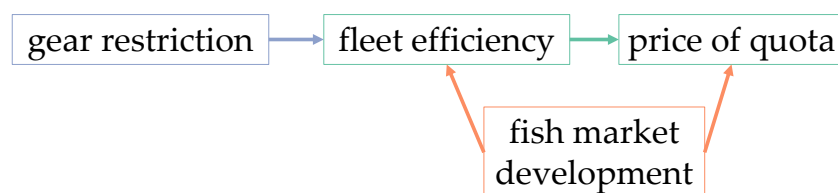
To many environmental economists, the replacement story is probably obvious, although the collider story is likely not. But the recommended solution might be to control for the total number of cars instead. According to Figure 3, this is also a blunder. In that causal model, the total number of cars acts as another collider. By stratifying on the number of cars in the household, it is assumed that there is a one-to-one replacement of a gas-powered car for every electric vehicle adopted—which is unlikely. Some households may move from two to three total cars with their adoption, but they will be compared to three [gas-powered] car households instead of two car households. The proposed solution moves the result from an underestimate to an overestimate of the decrease in emissions.

This model says that controls for the number of gas-powered cars and the number of total cars in the household should both be avoided. A different data source or setting may imply a different causal structure than the one in Figure 3. In that case, the no-control strategy can be re-validated by checking the new DAG for any threats to identification.

## Efficient communication of identification assumptions

Fishing quota systems have revolutionized the organization of fisheries, ensuring the biological sustainability of the targeted species and maximizing the value of an authorized total allowable catch. In these systems, fishers explicitly own shares of this total allowable catch and are free to trade these fishing rights among themselves. The market for quota shares autonomously guides ownership into the hands of the most efficient fishers, therefore increasing the economic rents that accrue to each share.

How much of the variation in the price of quota is due to changes in fleet efficiency (i.e. catch per unit effort), as opposed to changes in the demand for fish? A potential problem with separating these two impacts is the fact that any market development that increases the value of the quota may additionally incentivize investment that leads to greater efficiency. Figure 4 shows how uncontrolled demand side factors create spurious relationships when interpreting the effect of changes in fleet efficiency on the price of quota.



**Figure 4:** Given the mental model above, the corresponding DAG reflects the assumptions required for the gear restriction variable to be a useful instrument.

Consider a potential regulation enacted due to concerns about the bycatch of an endangered species often found co-mingling with the targeted species. This could manifest

as a restriction on a certain type of gear or fishing location. The restriction reduces the efficiency of the fleet, impacts the value of fishing quota through this efficiency mechanism, and is plausibly exogenous with respect to shifts in demand.

Figure 4 is consistent with this fishery story, and it suggests using the gear restriction variable as a solution to the identification problem. The regulation turns fleet efficiency into a collider variable along the spurious path from gear restriction to the quota price, and it acts as a mediator on the causal path. Thus an unconditional regression of the price of quota on the gear restriction variable provides a causally-interpretable estimate. A regression of fleet efficiency on the gear restriction is similarly unbiased. Dividing the two relevant regression coefficients yields the instrumental variables estimator for the effect of fleet efficiency on the price of quota—another causally-interpretable estimate.

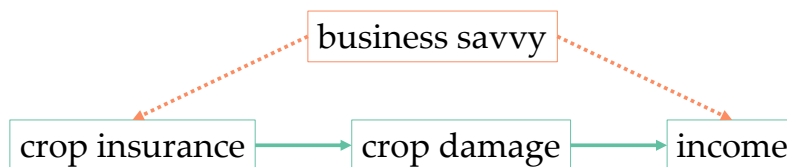
The DAG above reveals the familiar identification assumptions for the instrumental variables approach—relevance, independence, and validity—by checking for the presence or absence of three key arrows involving the gear restriction variable. The fishery story admits an arrow from gear restriction to fleet efficiency (relevance—though the strength of the instrument must be checked separately), but not to or from the price of quota or fish market development variables (validity and independence, respectively). Figure 4 transparently communicates what is believed to be true about the instrument, and readers can more easily follow (or dispute) these assumptions.

## Discovering new methods

The previous section used a DAG to identify multiple links between variables that could be estimated without bias. The resulting strategy emulated the familiar instrumental variables approach. But each new DAG structure provides an opportunity to discover a novel identification strategy that would have otherwise remained hidden. This last example illustrates the “random filter” identification strategy (Donovan, 2023) for deriving an unbiased estimate of a treatment effect amid selection into treatment.

How beneficial are climate resilience-motivated crop insurance programs in developing nations? The savvier farmers will likely have the most interest in an insurance program if made available, as well as the most sophisticated farming operations. Any naïve regression strategy would clearly pick up this selection bias. Figure 5 shows how to remedy this selection problem. Consider the mechanism through which insurance would lead to a benefit. If there is no adverse weather event (and thus no crop damage/insurance claim), then crop insurance will have no positive impact on income. If this crop damage variable isn’t correlated with business savvy, the two links in the chain from crop insurance to income can be estimated separately, without bias.





**Figure 5:** When an exogenous mediator exists between treatment and outcome, a researcher can separately identify the effects of treatment on the mediator and mediator on the outcome, then chain these effects together.

The first link in the causal chain can be identified with a simple regression of crop damage on crop insurance. The spurious path from crop insurance to crop damage is not an issue, since income assumes the role of a collider and omitting income closes this path. The second link is identified by regressing income on crop damage while controlling for crop insurance to close the other non-causal path. Multiplying these impacts together recovers a causally-interpretable estimate of the effect of crop insurance on income.

Figure 5 states three assumptions about this mediator. First, the mediator must intercept all causal paths from crop insurance to income. If another causal path existed outside of the mediator’s reach, the identification strategy will close that path. The other two assumptions require the crop damage variable to have unconfounded relationships with crop insurance and income. This means the business savvy variable—or any other unobservable—may not create a non-causal path between treatment and outcome that involves the mediator. If these assumptions hold, i.e. if one can genuinely draw the data generating process like Figure 5, then the identification strategy above is valid.

The savviest of farmers could potentially mitigate their exposure to weather-related damages through siting or some other mechanism; this creates a confounding path involving the mediator. In this case, a modification to the DAG presents a more robust identification strategy. Conditional on the known risk of a disastrous weather event, the event itself is now plausibly-exogenous with respect to the business savvy of individual farmers. Adding a measurable control variable like “risk of damage” in between the business savvy and crop damage variables would signal that a control strategy is available to close the spurious path. A researcher should run the two aforementioned regressions while controlling for exposure risk.

## An enhanced review of a recent JAERE article

In early July, 2015, the water utility serving the city of Burbank, California sent warnings to households who would be violating upcoming summer irrigation restrictions based on their behavior in late-June. The notices contained details about a new monitoring sys-



Figure 6 aids a reviewer in running through the requirements for a satisfactory fuzzy regression discontinuity design. The previously mentioned instrumental variables assumptions are conditionally satisfied. Clearly, the instrument—indicating if the stricter peak consumption threshold is exceeded—partly determines whether a household receives an irrigation restriction violation notice (it was a necessary precondition). And because the crossing of the peak consumption threshold is defined entirely by a household’s peak water consumption, conditional on the running variable, the instrument is independent of the unobserved confounder—the household consumption tier. Lastly, the instrument only impacts household water use through the delivery of a notice.

There are still the assumptions specific to the regression discontinuity approach to discuss. First, the goal of this regression discontinuity design is to separate the drop in water use due to receiving a notice from the [increasing] water use trend in the peak consumption running variable. Upon controlling for the running variable, any paths that utilize continuous variation in water use across the threshold are closed, leaving only the potential discontinuity to be measured.

Second, there shouldn’t be an additional cause for a discrete change in water use when comparing households just over the threshold to those just below it. For expositional clarity, the “local randomization” assumption is symbolized here by a non-path from the threshold to the outcome using the bold ‘X’s in Figure 6. Because water use will be regressed on the peak consumption threshold—and not the notice status itself—the authors hope to attribute the threshold-derived jump in outcomes to the notice, rather than some other factor. They make this assertion easy to believe, as no concurrent intervention utilizing the threshold existed (eliminating the arrow from the threshold to a potential intervention mediator), and no households were privy to the threshold or the automated detection algorithm (eliminating the arrow from a potential sorting confounder to the threshold).

From this discussion, the authors’ fuzzy regression discontinuity approach appears to generate an unbiased estimate of the effect of the irrigation restriction violation notices on summertime water use. But the DAG cannot fully cover the scope of an empirical review. This is discussed below.

## **DAGs are not the be-all and end-all**

It should be clear that DAGs cannot provide a one-to-one mapping to everything commonly taught in econometrics classes, and for this reason their main role must be augmentative. For example, Figure 6 cannot suggest a particular implementation of fuzzy regression discontinuity (two stage least squares, local linear regression, bandwidth, etc.), and these decisions involve a separate set of assumptions from the causal ones shown by

the DAG. The DAG does provide some guidance, however. As the introduction of this article establishes, the sensitivity of results to these additional assumptions should be analyzed across specifications consistent with the same causal model.

Another shortcoming is that a DAG misses nuance relating to the estimate of interest. In the [common] case of heterogeneous treatment effects, an instrumental variables strategy typically makes use of a monotonicity assumption to show that an estimate is a local average treatment effect (equivalent to an average treatment effect on the treated in the present example, due to a lack of “always-takers”). The additional reliance on the extrapolation of counterfactuals in regression discontinuity designs means that this treatment effect is also limited in scope to settings where the peak consumption threshold for notice eligibility is around 125 gallons. The traditional potential outcomes logic embedded in these statements does not map to any feature in the graph.

An analysis aided by DAGs will still be subject to model misspecification. Where variations of functional form may instill a false sense of confidence in an inference’s robustness, a DAG may instill a similar confidence in a causal model. The interpretability of a result still depends on the accuracy of the causal model—even if it is explicitly represented by a DAG. While this remains a strong assumption, the transparency provided by the DAG admits an opportunity to test it during peer review. A reviewer can start with a DAG that communicates the assumptions that must hold in order for the empirical strategy to be successful. If the setting in a paper admits an arrow inconsistent with the approach, the reviewer has a reason to be critical. If an author supplies a DAG that doesn’t seem to match their story, the reviewer can point this out as well.

Even as environmental economists become more comfortable with the graphical approach, it is evident that additional discussion outside of the DAG framework will still be needed in empirical research. And as seen in the primer, certain questions involving non-recursive model designs cannot be conveyed via DAGs. These two facts are occasionally taken as evidence that DAG adoption is impractical (e.g. Imbens (2020); Heckman and Pinto (2022)), but this extreme view ignores their potential for improving the communication of causal knowledge in a majority of settings. In reality, nothing is sacrificed by using a new tool in conjunction with the old ones.

## Opportunities for implementation

Economics is one of the rare disciplines that uses presentations to improve work in progress. For a presentation to be beneficial, it is crucial to remember that identification strategies are nuanced and borne out from a place of deep familiarity with specific data and settings. The inclusion of a DAG increases the value of presenting research because

it makes these things clear to others. This leads to higher-quality feedback. It is easy to evaluate whether a speaker’s DAG represents the data generating process in their setting, turn any discrepancy into a question for the presenter, and test if a variation still admits the use of the proposed identification strategy.

DAGs provide an opportunity to make the research process more transparent and responsive to criticism. When reviewers ask for some sort of sensitivity analysis, they can use the graphical language for raising concerns about causal hypotheses. A new causal hypothesis generates a modification to a DAG, which then organically motivates a new regression. This first-principles style approach to testing model robustness is more academically rigorous than suggesting modifications to a regression with language concerning functional form alone. It matches the spirit of specification testing, which aims to build confidence that an effect of interest is being measured without bias.

The integration of DAGs in econometrics education creates significant value for pedagogy (e.g. Cunningham (2021); Huntington-Klein (2022)). Indeed, graduate studies in economics already highlight causal effect identification, yet several of the insights shared in this article are absent from applied econometrics instruction. At the undergraduate level, DAGs facilitate discussion of research design; for example, the introductory econometrics course at the University of Nevada, Reno attracts a diverse group of students to economics through its primary emphasis on discussing empirical research. The use of DAGs increases access to this class and builds a desirable competency.

This accessibility can be extended to communication with policymakers and stakeholders. By simplifying explanations of causal effect identification while retaining rigor, DAGs can elevate a non-expert’s understanding of an empirical method. Perhaps the most promising consequence is that lawmakers would have an opportunity to engage with empirical work more critically, reducing the reliance on trust as the mechanism for informing environmental policy.

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