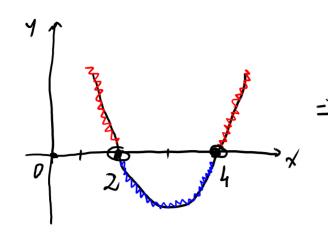
## Étude de signe d'une parabole



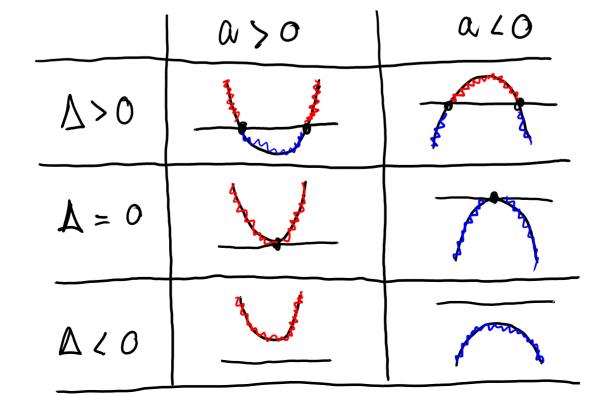
$$\alpha x^2 + bx + c$$

1) Si 
$$\omega > 0 = >$$

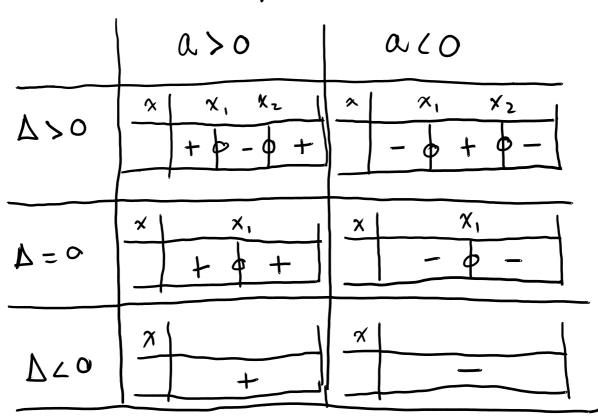




2) Calcul le 
$$\Delta = b^2 - 4 \alpha c$$



3) Tableau de signe



Exemple: Étudier le signe de  $2\alpha^2 + 3\alpha - 2$ 

2) 
$$\Delta = ?$$
  $\alpha = 2$   $b = 3$   $c = -2$ 

 $\Delta = b^2 - \mu ac = 3^2 - \mu \times 2 \times (-2) = 9 + 16 = 25 > 0$ 



3) 
$$x_1 = \frac{-b - \sqrt{\Delta}}{2\alpha} = \frac{-3 - 5}{4} = -2$$
  $x_2 = \frac{-b + \sqrt{\Delta}}{2\alpha} = \frac{-3 + 5}{4} = \frac{1}{2}$ 

Tabloau de signe.

γ	-00	-2	1/2	+ 00
	+	- 0	- 0	+

## Résordre un'équation du 200 degni

$$\Delta = b^2 - hac = (-h)^2 - hxlxh = 16 - 16 = 0$$



$$x_1 = -\frac{b}{2a} = -\frac{-4}{2} = \frac{4}{2} = 2$$

Tobleau de signe 
$$\frac{x - x}{+ b} + \frac{2}{+ b}$$

$$S = J - \infty$$
;  $2 \left[ U \right] 2$ ;  $+ \infty \left[ = R \setminus \{2\} \right]$ 

## Exercices:

2) 
$$x^2 + x + 3 > 0$$

3) 
$$3x^2 + 5x - 220$$

$$5) - x^2 + 8x - 12 > 0$$

10) 
$$(2x-1)(4x^2+2x+1) \leq 0$$

## Correction

$$a = 4 > 0$$
  $b = -4$   $c = 1$ 

$$\Delta = (-h)^2 - 4 \times 4 \times 1 = 16 - 16 = 0$$



$$\chi_1 = -\frac{-4}{2} = 2 = 2$$

$$\chi_1 = -\frac{4}{2} = 2 \Rightarrow \frac{\chi_1 - \chi_2}{1 + \varphi_1}$$

$$2) \qquad \chi^2 + \chi + 3 > 0$$



$$a = 1 > 0$$
  $b = 1$   $c = 3$ 

$$\Delta = 1^2 - 4 \times 1 \times 3 = 1 - 12 = -11 \times 0 = >$$



3) 
$$3x^2 + 5x - 2 \angle 0$$

$$\alpha = 3 > 0$$



$$c = -2$$

$$\Delta = 5^2 - 4 \times 3 \times (-2) = 25 + 24 = 43 > 0$$



$$x_1 = \frac{-5-7}{2} = -2$$

$$\chi_2 = \frac{-5+7}{6} = \frac{1}{3}$$

$$x_1 = \frac{-5-7}{6} = -2$$
  $x_2 = \frac{-5+7}{6} = \frac{1}{3}$   $\frac{x_1 - x_2 - \frac{1}{3} + x_3}{4 - x_4 - x_4}$ 

$$a = 4 > 0$$
  $b = 0$   $c = -3$ 

$$\Delta = 0^2 - 4 \times 4 \times (-3) = 144 > 0 = 7$$

$$\chi_1 = \frac{0-12}{2} = -\frac{3}{2}$$

$$\chi_2 = \frac{0+12}{8} = \frac{3}{2}$$

$$\chi_1 = \frac{0 - 12}{3} = -\frac{3}{2}$$
 $\chi_2 = \frac{0 + 12}{8} = \frac{3}{2}$ 
 $\frac{\chi_1 - \omega_2 - \frac{3}{2}}{4} = \frac{3}{2}$ 

$$S = ]-\infty; -\frac{3}{2}[U]^{\frac{3}{2}}; +\infty[$$

5) 
$$-x^2 + 8x - 12 > 0$$

$$a = -120$$
  $b = 8$   $c = -12$ 

$$c = -12$$

$$\Delta = 8^2 - 4 \times (-1) \times (-12) = 64 - 48 = 14 > 0 = 7$$



$$x_1 = \frac{-8-h}{-2} = k$$

$$x_1 = \frac{-3+k}{-1}$$
 = 2

$$x_1 = \frac{-8-h}{-2} = 6$$
  $x_2 = \frac{-3+h}{-2} = 2$   $x_1 = \frac{-3+h}{-2} = 2$ 

6) 
$$6x^2 - 5x + 1 > 0$$



$$\Delta = (-5)^2 - h \times 6 \times 1 = 25 - 24 = 1 > 0 = >$$



$$x_1 = \frac{5-1}{12} = \frac{1}{3}$$

$$\gamma_2 = \frac{\varsigma + 1}{12} = \frac{1}{2}$$

$$x_1 = \frac{5-1}{12} = \frac{1}{3}$$
  $x_2 = \frac{5+1}{12} = \frac{1}{2}$   $\frac{x_1 - \alpha + \frac{1}{3} + \frac{1}{2} + \alpha}{1 + \alpha - \alpha + \frac{1}{3}}$ 

$$S = ]-\infty; \frac{1}{3} ] \cup \left[ \frac{1}{2}; +\infty \right[$$

$$\Delta = 0^2 - h \times (-1) \times h = 16 > 0 \Rightarrow$$

$$\chi_1 = \frac{0-h}{-7} = 2$$

$$x_2 = \frac{0+4}{-7} = -2$$

$$x_1 = \frac{0-h}{-2} = 2$$
  $x_2 = \frac{0+h}{-2} = -2$   $\frac{x_1 - x_2 - 2}{-2} = -2$ 

$$S = ]-\infty; -2] \cup [2; +\infty[$$

$$a = h > 0$$
 |  $b = -4$   $c = -3$ 

$$\Delta = (-h)^2 - h \times h \times (-3) = 16 + 48 = 64 > 0 = >$$

$$\chi_1 = \frac{4-8}{9} = -\frac{1}{2}$$

$$x_2 = \frac{4+8}{3} = \frac{3}{2}$$

$$x_1 = \frac{4-8}{8} = -\frac{1}{2}$$
 $x_2 = \frac{4+8}{8} = \frac{3}{2}$ 
 $\frac{x_1 - x_2 - \frac{1}{2} - \frac{3}{2}}{x_2 - x_3} + \frac{x_4 - x_4 - \frac{1}{2}}{x_4 - x_4 - x_4}$ 

9) 
$$(x+5)(x^2-5x+25)$$
 40

$$x+5>0$$
  $\Rightarrow$   $x^2-5x+25$   $\alpha=1>0$   $b=-5$   $c=25$   $x>-5$  à draite  $\Delta=(-5)^2-h\times1\times25=-7520$   $\Delta=(-5)^2-h\times1\times25=-7520$ 

$$S = ]-\infty; -5[$$

$$2x-1>0$$

$$x>\frac{1}{2}$$

$$S = \left[ \frac{1}{2} - \infty \right]$$