

Ex 54

$$f(x) = 2x^2 - 8x - 5 \quad ; \quad g(x) = -x^2 + 3x$$

$$f'(x) = 4x - 8 \quad ; \quad g'(x) = -2x + 3$$

Ex 55

$$f(x) = x^3 + x + 1 \quad ; \quad g(x) = x^4 - 3x^2 + 2$$

$$f'(x) = 3x^2 + 1 \quad ; \quad g'(x) = 4x^3 - 6x$$

Ex 56

$$f(x) = (2x+1)^3 \quad ; \quad g(x) = (x+2)(e^x + 1)$$

$$f(x) = u^3 \quad \text{avec} \quad u = 2x+1 \quad \Rightarrow \quad u' = 2$$

$$f'(x) = 3u^2 u' = 3(2x+1)^2 \cdot 2 = 6(2x+1)^2$$

$$g(x) = uv \quad \text{avec} \quad u = x+2 \quad \text{et} \quad v = e^x + 1$$
$$u' = 1 \quad \quad \quad v' = e^x$$

$$g'(x) = u'v + uv' = 1(e^x + 1) + (x+2)e^x = e^x + 1 + e^x(x+2) = e^x + 1 + xe^x + 2e^x =$$
$$= xe^x + 3e^x + 1$$

Ex 57

$$f(x) = \frac{x-1}{x^2+4x+1} \quad ; \quad g(x) = \frac{1}{x^2+1}$$

$$f(x) = \frac{u}{v} \quad \text{avec} \quad u = x-1 \quad \text{et} \quad v = x^2+4x+1$$
$$u' = 1 \quad \quad \quad v' = 2x+4$$

$$f'(x) = \frac{u'v - uv'}{v^2} = \frac{x^2+4x+1 - (x-1)(2x+4)}{(x^2+4x+1)^2} = \frac{x^2+4x+1 - (2x^2+4x-2x-4)}{(x^2+4x+1)^2} =$$
$$= \frac{x^2+4x+1 - 2x^2 - 4x + 2x + 4}{(x^2+4x+1)^2} = \frac{-x^2 + 2x + 5}{(x^2+4x+1)^2}$$

$$g = \frac{u}{v} \quad \text{avec} \quad u = 1 \quad \text{et} \quad v = x^2+1$$
$$u' = 0 \quad \quad \quad v' = 2x$$

$$g'(x) = \frac{u'v - uv'}{v^2} = \frac{-2x}{(x^2+1)^2}$$