

$$f(x) = f(a) + \frac{f'(a)}{1!}(x-a) + \frac{f^{(2)}(a)}{2!}(x-a)^2 + \dots + \frac{f^{(n)}(a)}{n!}(x-a)^n + R_n(x)$$

$$f(x) = e^x \quad a=0$$

$$f(0) = 1$$

$$f'(x) = e^x \quad f'(0) = 1$$

$$f''(x) = e^x \quad f''(0) = 1$$

Au voisinage de 0 on a :

$$f(x) = 1 + 1(x-0) + \frac{1}{2}(x-0)^2 + \dots = 1 + x + \frac{x^2}{2} + \dots$$