

« Julia, my new friend for computing and optimization? »

- Intro to the Julia programming language, for MATLAB users
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Agenda for today [25 min]

1. What is Julia [3 min]
2. Comparison with MATLAB [3 min]
3. Examples of problems solved Julia [5 min]
4. Longer example on optimization with JuMP [10min]
5. Links for more information ? [2 min]

1. What is Julia ?

- Developed and popular from the **last 7 years**
- Open-source and free programming language (MIT license)
- Interpreted *and* compiled, very efficient
- But easy syntax, dynamic typing, inline documentation etc
- Multi-platform, imperative
- MATLAB-like syntax for linear algebra etc
- Designed and acknowledged as *simple to learn and use*
- Easy to run your code in parallel (multi-core & cluster)
- Used worldwide: research, data science, finance etc...

Ressources

- Website: JuliaLang.org for the language & Pkg.JuliaLang.org for packages
- Documentation : docs.JuliaLang.org



Comparison with MATLAB

	Julia 😊	MATLAB 😓
Cost	Free ✌️	Hundreds of euros / year
License	Open-source	1 year user license (no longer after your PhD!)
Comes from	A non-profit foundation, and the community	MathWorks company
Scope	Mainly numeric	Numeric only
Performances	Very good performance	Faster than Python, slower than Julia

Comparison with MATLAB


	Julia	MATLAB
Packaging	Pkg manager included. Based on git + GitHub, very easy to use	Toolboxes already included but 💰 have to pay if you want more!
Editor/IDE	<i>Jupyter</i> is recommended (<i>Juno</i> is also good)	Good IDE already included
Parallel computations	Very easy, low overhead cost	Possible, high overhead

Comparison with MATLAB

	Julia	MATLAB
Usage	Generic, worldwide 🌍	Research in academia and industry
Fame	Young but starts to be known	Old and known, in decline
Support?	Community ¹ (StackOverflow, mailing lists etc).	By MathWorks
Documentation	OK and growing, inline/online	OK, inline/online

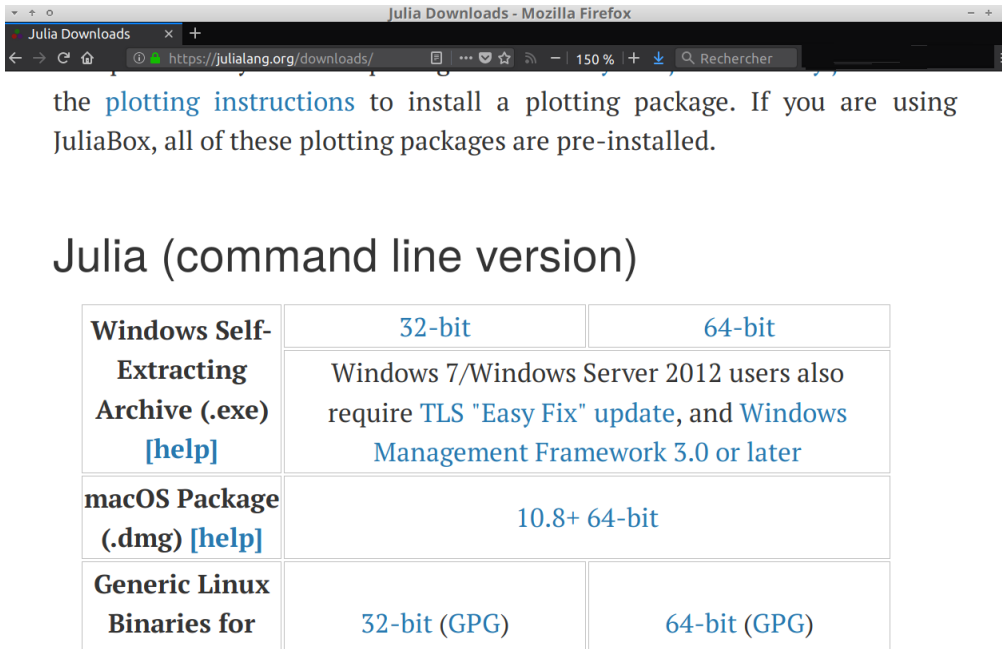
Note¹: JuliaPro offer paid licenses, if professional support is needed.





How to install Julia (1/2)

- You can try online *for free* on JuliaBox.com
- On Linux, Mac OS or Windows:
 - You can use the default installer 
from the website julialang.org/downloads
- Takes about 4 minutes... and it's free !

You also need Python 3 to use Jupyter ✨, I suggest to use Anaconda.com/download if you don't have Python yet.

How to install Julia (2/2)



1. Select the binary of your platform 
2. Run the binary  !
3. Wait  ...
4. Done  ! Test with `julia` in a terminal

Different tools to use Julia

- Use `julia` for the command line for short experiments

```
(lun. juin 11 -- 03:06:27)<lilian@jarvis:[~]> {bashv4.4} — Konsole
```

```
$ julia
```

```
      _  
    (_)  
   _(_)(_)_  
  _/___\/_/  
 |__/_/  |__/_/'_|_|\__/_'|  
|__/_/  |__/_/'_|_|\__/_'|
```

```
| A fresh approach to technical computing  
| Documentation: https://docs.julialang.org  
| Type "?help" for help.  
  
| Version 0.6.0 (2017-06-19 13:05 UTC)  
| Official http://julialang.org/ release  
| x86_64-pc-linux-gnu
```

```
julia> println("Hello world from Julia!")  
Hello world from Julia!
```

```
julia>
```

- Use the *Juno* IDE to edit large projects

Demo time 🕒 !

Different tools to use Julia

- Use **Jupyter** notebooks to write or share your experiments (examples: github.com/Nareen/notebooks)

demo — Jupyter Notebook - Chromium

demo (autosaved) Logout

File Edit View Insert Cell Kernel Navigate Widgets Help Snippets Trusted Julia 0.6.0

Enter/Exit RISE Slideshow Table of Contents Toggle spell checking on markdown cells

This is a short demo of Julia

To learn more, check the [Julia documentation!](#)

Hello world

In [14]: `println("Hello from Julia + Jupyter!")`

Hello from Julia + Jupyter!

A simple math example

For $x \in \mathbb{R}^{n,n}$, $iFFT(FFT(x)) = x$?

In [2]: `x = rand(10, 10)`

Out[2]: 10×10 Array{Float64,2}:

0.414411	0.304796	0.239104	0.36513	...	0.0458627	0.801216	0.245571
0.0540293	0.79935	0.455725	0.523839		0.158364	0.971185	0.595249
0.26901	0.276373	0.804781	0.308718		0.562864	0.240393	0.477163
0.550455	0.393096	0.415986	0.934639		0.0959417	0.166348	0.95397
0.050985	0.929405	0.535396	0.85512		0.363232	0.979027	0.13972

Demo time 🕒 !

How to install modules in Julia ?

- Installing is **easy** !

```
julia> Pkg.add("IJulia") # installs IJulia
```

- Updating also!

```
julia> Pkg.update()
```

How to find the module you need ?

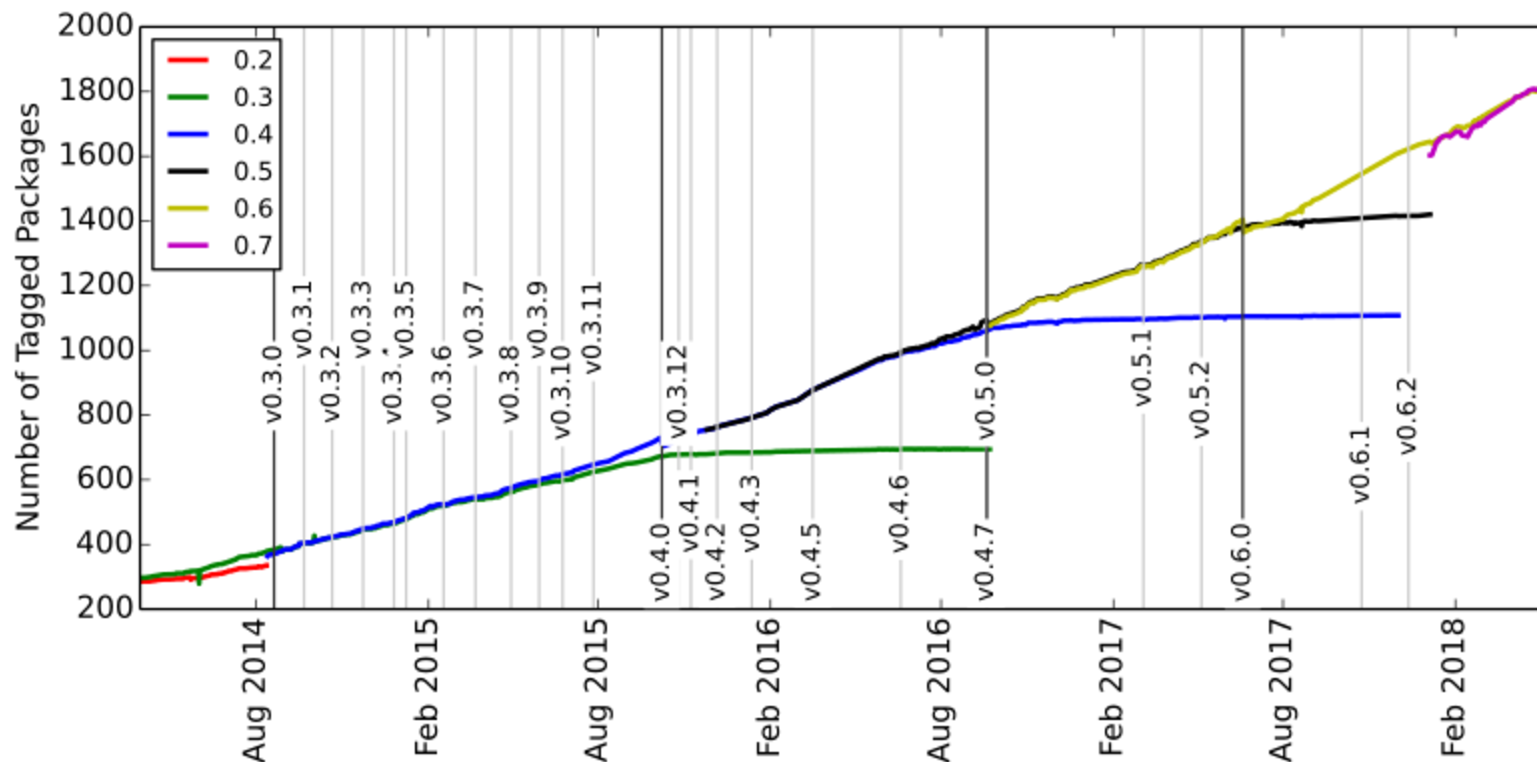
- First... ask your colleagues 😊 !
- Complete list on pkg.julialang.org

Overview of famous Julia modules

- Plotting:
 - `Winston.jl` for easy plotting like MATLAB
 - `PyPlot` : interface to Matplotlib (Python)
- The `JuliaDiffEq` collection for **differential equations**
- The `JuliaOpt` collection for **optimization**
- The `JuliaStats` collection for **statistics**
- And many more!

Find more specific packages on [GitHub.com/svaksha/Julia.jl/](https://github.com/svaksha/Julia.jl/)

Many packages, and a quickly growing community



Julia is still in development, in version v0.6 but version 1.0 is planned soon!

2. Main differences in syntax between Julia and MATLAB

Ref: cheatsheets.quantecon.org

	Julia	MATLAB
File ext.	<code>.jl</code>	<code>.m</code>
Comment	<code># blabla...</code>	<code>% blabla...</code>
Indexing	<code>a[1]</code> to <code>a[end]</code>	<code>a(1)</code> to <code>a(end)</code>
Slicing	<code>a[1:100]</code> (view)	<code>a(1:100)</code> (⚠ copy)
Operations	Linear algebra by default	Linear algebra by default
Block	Use <code>end</code> to close all blocks	Use <code>endif</code> <code>endfor</code> etc

	Julia	MATLAB
Help	<code>?func</code>	<code>help func</code>
And	<code>a & b</code>	<code>a && b</code>
Or	<code>a b</code>	<code>a b</code>
Datatype	Array of <i>any</i> type	multi-dim doubles array
Array	<code>[1 2; 3 4]</code>	<code>[1 2; 3 4]</code>
Size	<code>size(a)</code>	<code>size(a)</code>
Nb Dim	<code>ndims(a)</code>	<code>ndims(a)</code>
Last	<code>a[end]</code>	<code>a(end)</code>

	Julia	MATLAB
Tranpose	<code>a.'</code>	<code>a.'</code>
Conj. transpose	<code>a'</code>	<code>a'</code>
Matrix x	<code>a * b</code>	<code>a * b</code>
Element-wise x	<code>a .* b</code>	<code>a .* b</code>
Element-wise /	<code>a ./ b</code>	<code>a ./ b</code>
Element-wise ^	<code>a ^ 3</code>	<code>a .^ 3</code>
Zeros	<code>zeros(2, 3, 5)</code>	<code>zeros(2, 3, 5)</code>
Ones	<code>ones(2, 3, 5)</code>	<code>ones(2, 3, 5)</code>
Identity	<code>eye(10)</code>	<code>eye(10)</code>
Range	<code>range(0, 100, 2)</code> or <code>1:2:100</code>	<code>1:2:100</code>

	Julia	MATLAB
Maximum	<code>max(a)</code>	<code>max(max(a))</code> ?
Random matrix	<code>rand(3, 4)</code>	<code>rand(3, 4)</code>
L2 Norm	<code>norm(v)</code>	<code>norm(v)</code>
Inverse	<code>inv(a)</code>	<code>inv(a)</code>
Solve syst.	<code>a \ b</code>	<code>a \ b</code>
Eigen vals	<code>V, D = eig(a)</code>	<code>[V,D]=eig(a)</code>
FFT/IFFT	<code>fft(a)</code> , <code>ifft(a)</code>	<code>fft(a)</code> , <code>ifft(a)</code>

Very close to MATLAB for linear algebra!

3. Scientific problems solved with Julia

Just to give examples of syntax and modules

1. 1D numerical integration and plot
2. Solving a 2nd order Ordinary Differential Equation

3.1. 1D numerical integration and plot

Exercise : evaluate and plot this function on $[-1, 1]$:

$$\text{Ei}(x) := \int_{-x}^{\infty} \frac{e^u}{u} du$$

How to?

Use packages and everything is easy!

- `QuadGK.jl` for integration
- `Winston.jl` for 2D plotting

```

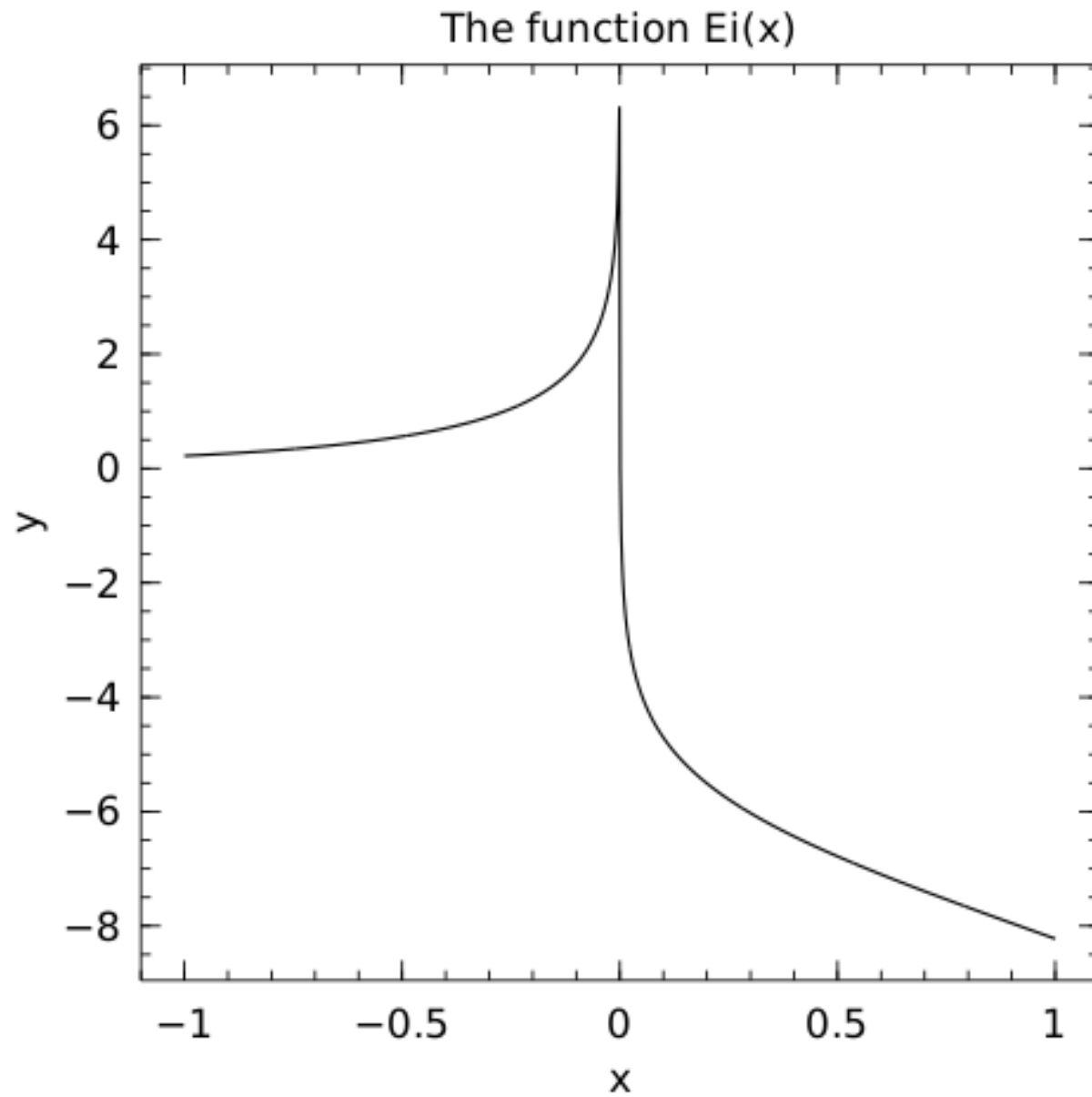
using QuadGK

function Ei(x, minfloat=1e-3, maxfloat=100)
    f = t -> exp(-t) / t # inline function, with '- >'
    if x > 0
        return quadgk(f, -x, -minfloat)[1]
            + quadgk(f, minfloat, maxfloat)[1]
    else
        return quadgk(f, -x, maxfloat)[1]
    end
end

X = linspace(-1, 1, 1000) # 1000 points
Y = [ Ei(x) for x in X ]

using Winston
plot(X, Y)
title("The function Ei(x)")
xlabel("x"); ylabel("y")
savefig("figures/Ei_integral.png")

```



3.2. Solving a 2nd order ODE

Goal : solve and plot the differential equation of a pendulum:

$$\theta''(t) + b \theta'(t) + c \sin(\theta(t)) = 0$$

For $b = 1/4, c = 5, \theta(0) = \pi - 0.1, \theta'(0) = 0, t \in [0, 10]$

How to?

Use packages!

- `DifferentialEquations.jl` function for ODE integration
- `Winston.jl` for 2D plotting

```

using DifferentialEquations

b, c = 0.25, 5.0

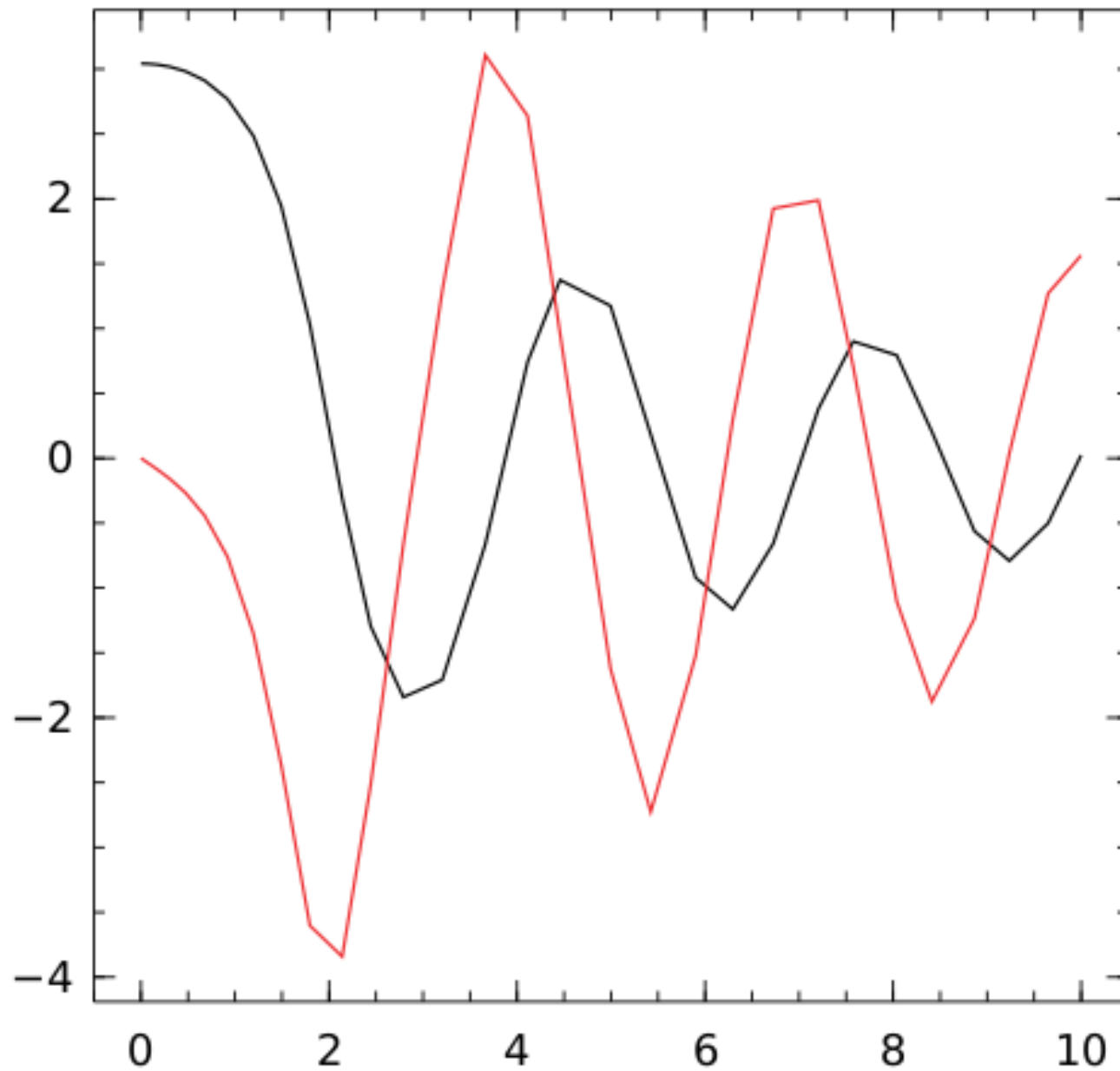
# macro magic!
pend2 = @code_def Pendulum begin
    dθ = ω # <-- yes, this is UTF8
    dω = (-b * ω) - (c * sin(θ))
end

prob = ODEProblem(pend, y0, (0.0, 10.0))
sol = solve(prob) # ↑ solve on interval [0,10]
t, y = sol.t, hcat(sol.u...)

using Winston
plot(t, y[:, 1], t, y[:, 2])
title("2D Differential Equation")
savefig("figures/Pendulum_solution.png")

```


2D Differential Equation



Conclusion (1/2)

Sum-up

- I hope you got a good introduction to Julia
- It's not hard to migrate from MATLAB to Julia
- Good start:

docs.julialang.org/en/stable/manual/getting-started

Conclusion (2/2)

Thanks for joining 🙌 !

Your mission, if you accept it... ✨

1. 🧑🎓 *Padawan level*: Train yourself a little bit on Julia
↳ [JuliaBox.com](https://julia-box.com) ? Or install it on your laptop!
And read [introduction in the Julia manual](#)!
2. 🎓 *Jedi level*: Try to solve a numerical system, from your research or teaching, **in Julia instead of MATLAB**
3. 🗡️ *Master level*: From now on, try to use open-source & free tools for your research (Julia, Python and others)... 💰

Examples

1. **Iterative computation:** signal filtering
2. **Optimization:** robust regression on RADAR data

Iterative computation

The classical saying:

“Vectorized code often runs much faster than the corresponding code containing loops.” ([MATLAB doc](#))

does not hold for Julia, because of its **just-in-time compiler**.

Example for the smoothing of a signal $\{u_k\}_{k \in \mathbb{N}}$:

$$y_k = ay_{k-1} + (1 - a)u_k, \quad k \in \mathbb{N}^+$$

Parameter a tunes the smoothing, between none ($a = 0$) and strong smoothing ($a \rightarrow 1^-$).

Optimization problem

Example problem: Identifying the sea clutter in Weather Radar data.

- is a **robust regression** problem
 - is an optimization problem

An “IETR-colored” example, inspired by:

- Radar data: P.-J. Trombe *et al.*, “Weather radars – the new eyes for offshore wind farms?,” *Wind Energy*, 2014.
- Regression methods: S. Boyd and L. Vandenberghe, *Convex Optimization*. Cambridge University Press, 2004. (Example 6.2)

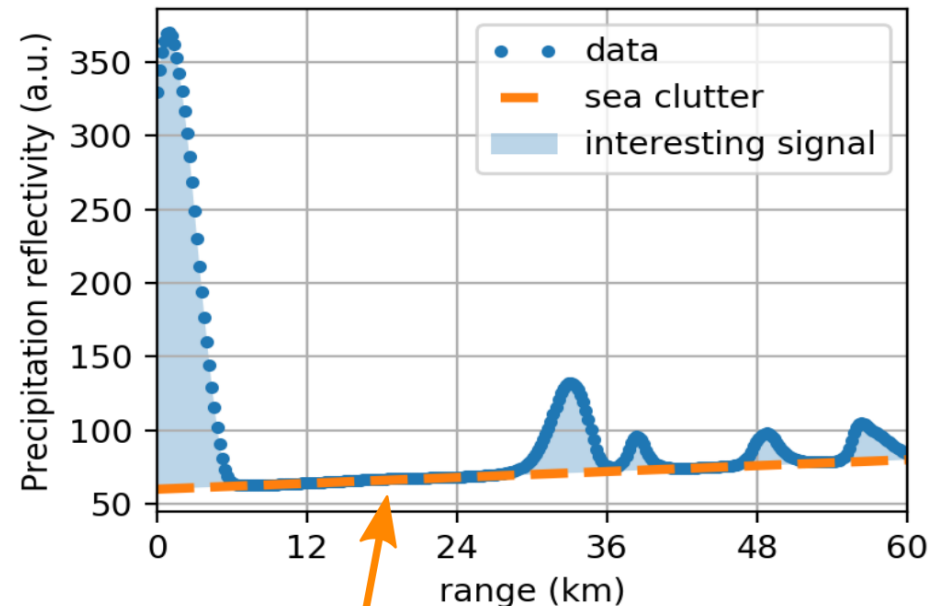
Weather radar: the problem of sea clutter

Offshore wind farm (Horns Rev, Denmark)



Weather radar: X-band (9.41 GHz), 60 km range

Reflection data, for one azimuth



Objective: fit this trend (to substract it)

Given n data points (x_i, y_i) , fit a linear trend:

$$\hat{y} = a.x + b$$

An optimization problem with two parameters: a (slope), b (intercept)

Regression as an optimization problem

The parameters for the trend (a, b) should minimize a criterion J which penalizes the residuals $r_i = y_i - \hat{y} = y_i - a.x + b$:

$$J(a, b) = \sum_i \phi(r_i)$$

where ϕ is the *penalty function*, to be chosen:

- $\phi(r) = r^2$: quadratic deviation \rightarrow least squares regression
- $\phi(r) = |r|$: absolute value deviation
- $\phi(r) = h(r)$: [Huber loss](#)
- ...

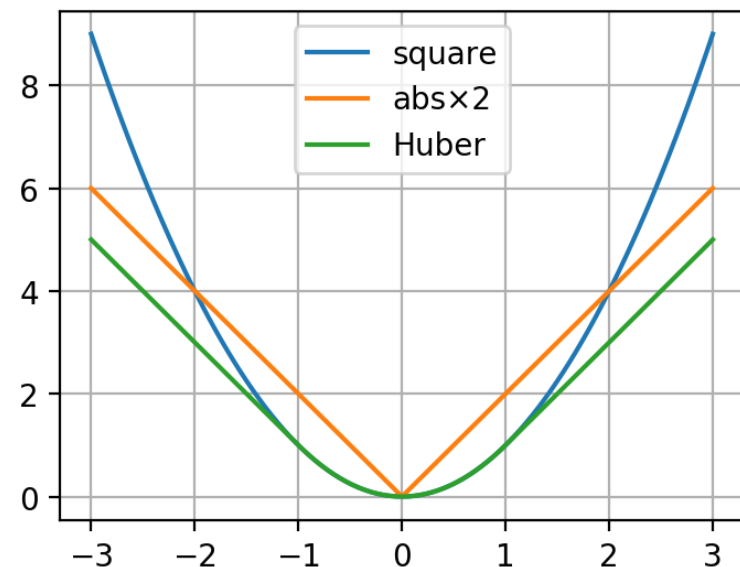
Choice of penalty function

The choice of the loss function influences:

- the optimization result (fit quality)
 - e.g. in the presence of outliers
- the properties of optimization problem: convexity, smoothness

Properties of each function

- quadratic: convex, smooth, heavy weight for strong deviations
- absolute value: convex, not smooth
- Huber: a mix of the two



How to solve the regression problem

Option 1: specific tools

a specific tool for each type of regression:

- “least square toolbox” (→ [MultivariateStats.jl](#))
- “least absolute value toolbox” (→ [quantile regression](#))
- “Huber toolbox” (i.e. robust regression → ???)
- ...

Option 2: a generic tool

→ a **Modeling Language for Optimization**

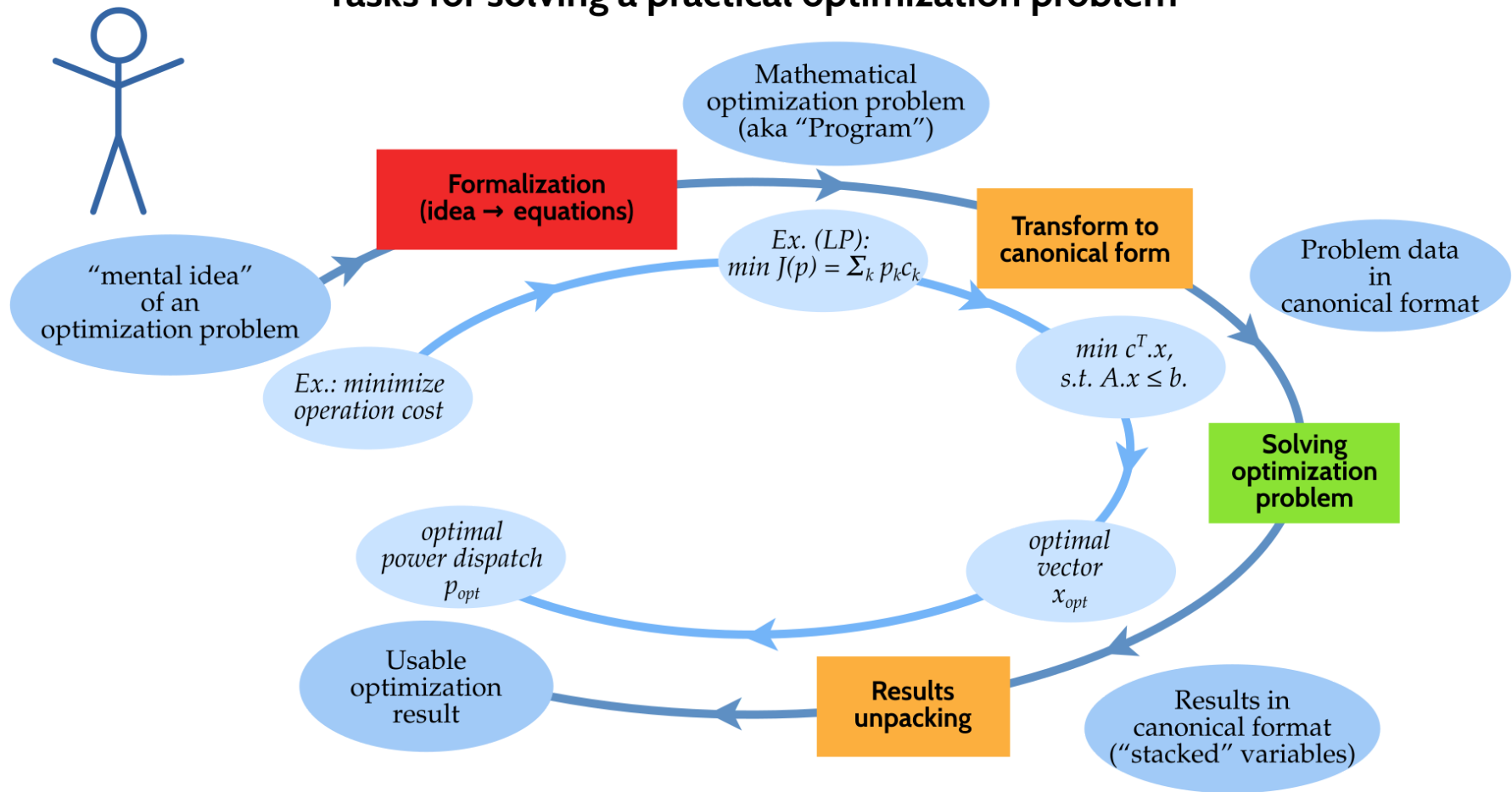
+more freedom to explore variants of the problem

Modeling Languages for Optimization

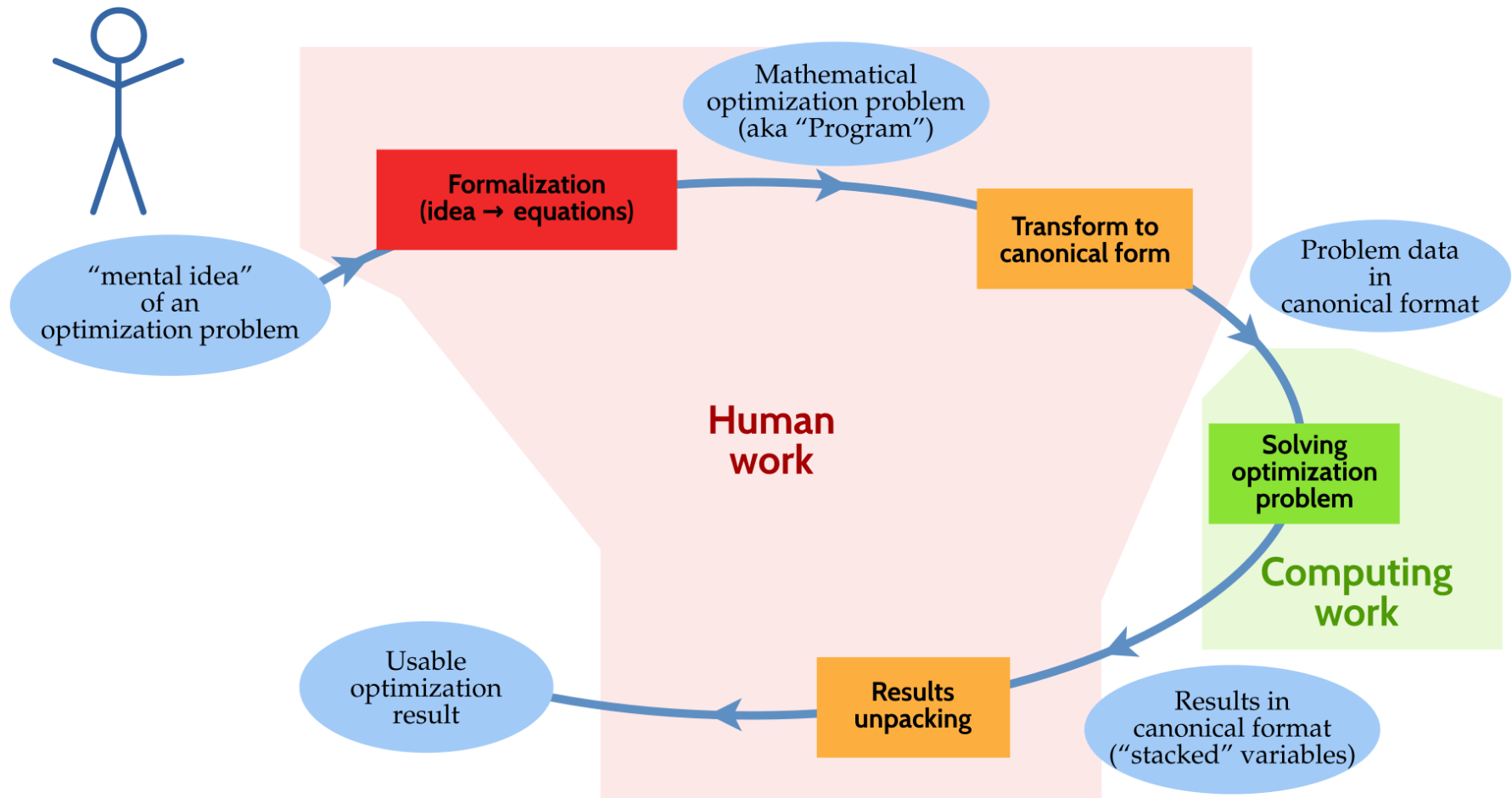
Purpose: make it easy to specify and solve optimization problems without expert knowledge.

Tasks for solving a practical optimization problem

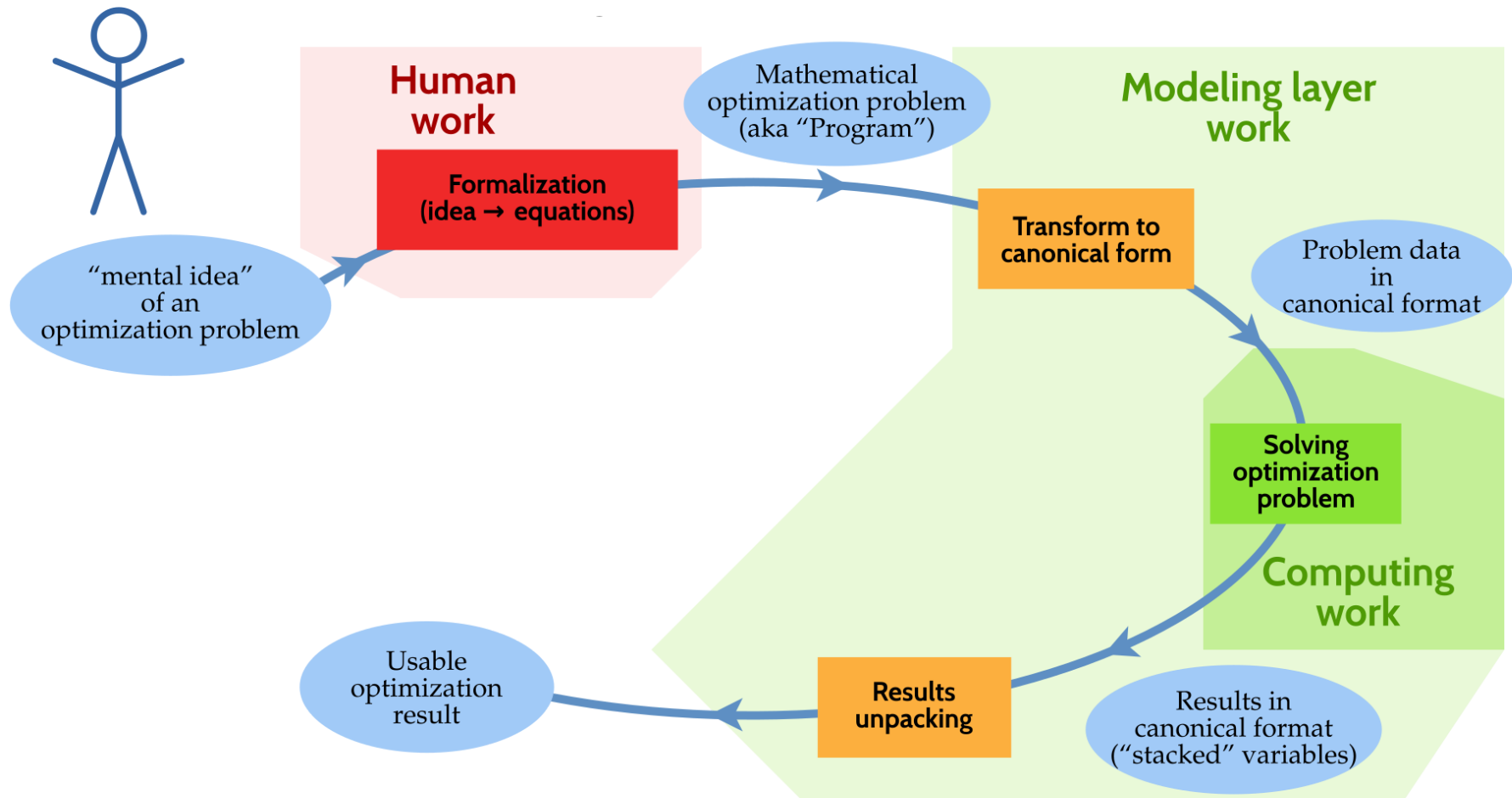
Tasks for solving a practical optimization problem



Tasks for solving a practical optimization problem



Tasks for solving a practical optimization problem



JuMP: optimization modeling in Julia

The [JuMP](#) package offers a domain-specific modeling language for mathematical optimization.

JuMP interfaces to many optimization solvers: open-source (Ipopt, GLPK, Clp, ECOS...) and commercial (CPLEX, Gurobi, MOSEK...).

Other Modeling Languages for Optimization:

- Standalone software: AMPL, GAMS
- Matlab: YALMIP ([previous seminar](#)), CVX
- Python: Pyomo, PuLP, CVXPY

Claim: JuMP is fast, thanks to Julia's [metaprogramming](#) capabilities (generation of Julia code within Julia code).

Regression with JuMP

Given `x` and `y` the 300 data points, common part:

```
m = Model(solver = ECOSolver())  
  
@variable(m, a)  
@variable(m, b)  
  
res = a*x .- y +b
```

`res` (“residuals”) is an Array of 300 elements of type `JuMP.GenericAffExpr{Float64, JuMP.Variable}`, i.e. a semi-symbolic affine expression.

Now, we need to specify the penalty on those residuals

Regression choice: least squares

$$\min \sum_i r_i^2$$

reformulated as a [Second-Order Cone Program](#) (SOCP):

$$\min j, \quad \text{such that } \|r\|_2 \leq j$$

```
@variable(m, j)
@constraint(m, norm(res) <= j);
@objective(m, Min, j)
```

(SOCP → [ECOS](#) solver)

Regression choice: least absolute deviation

$$\min \sum_i |r_i|$$

reformulated as a **Linear Program** (LP)

$$\min \sum_i t_i, \quad \text{such that} \quad -t_i \leq r_i \leq t_i$$

```
@variable(m, t[1:n] )  
@constraint(m, res .<= t)  
@constraint(m, res .>= -t)  
@objective(m, Min, sum(t));
```

Solve! ⚙️<

```
julia> solve(m)
[solver blabla... ⌚ ]
:Optimal # hopefully
```

```
> getvalue(a), getvalue(b)
(-1.094, 127.52) # for least squares
```

