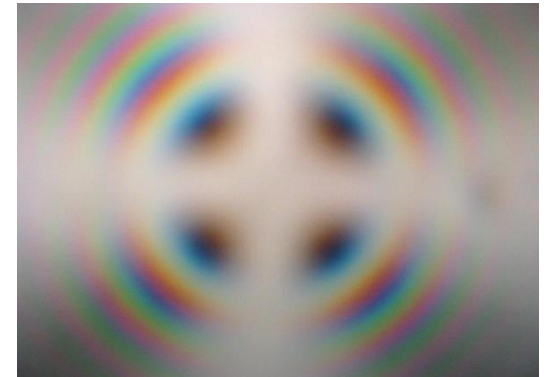
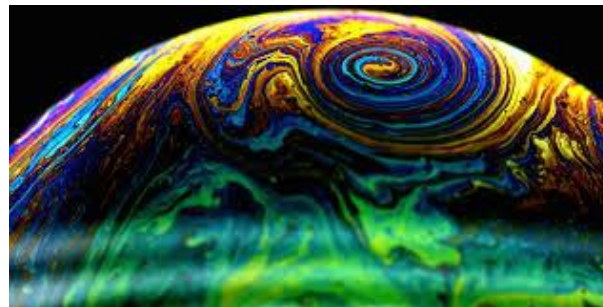
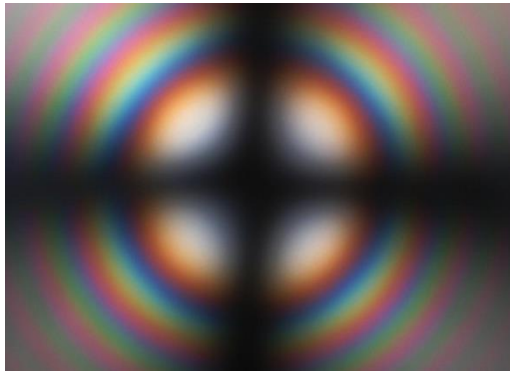


cycle « Lumière et couleurs »



Renaud Mathevet
Université Paul Sabatier

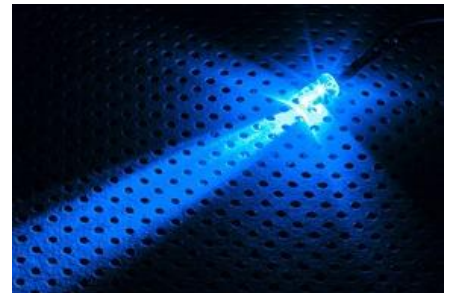
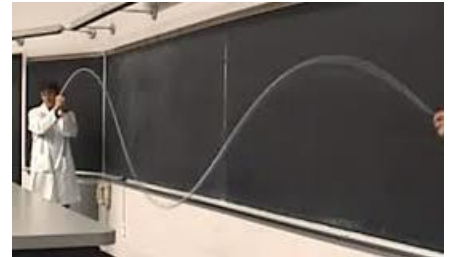
Plan

Du modèle corpusculaire au
modèle ondulatoire

De la spectroscopie au modèle
quantique de l'atome...

... jusqu'à la LED bleue

et au-delà...



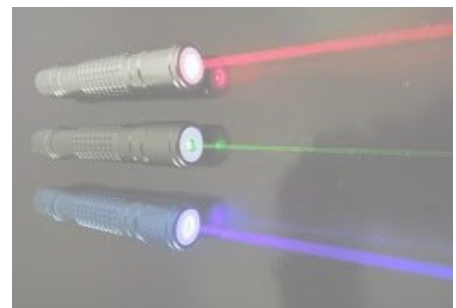
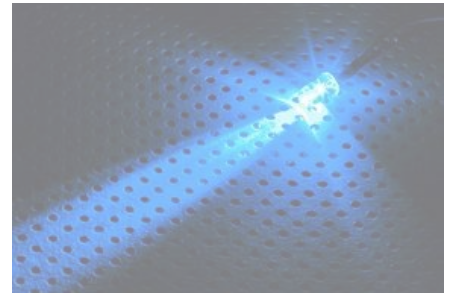
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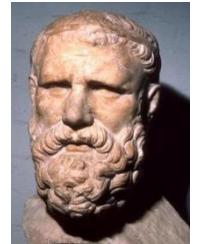


Conceptions antiques

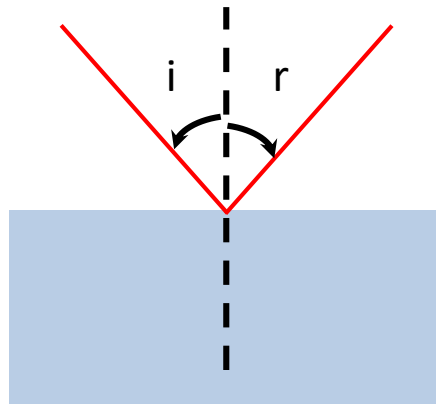


ombres portées:

- rayon lumineux
- propagation rectiligne



Eratosthène
≈ 230 av. JC

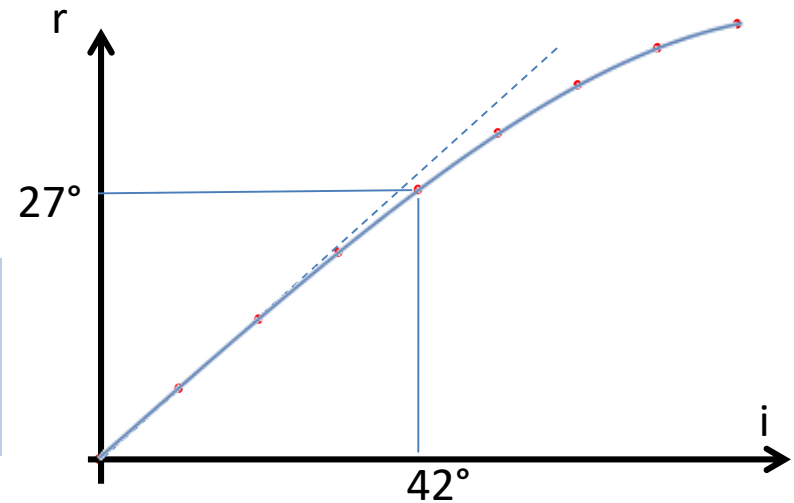
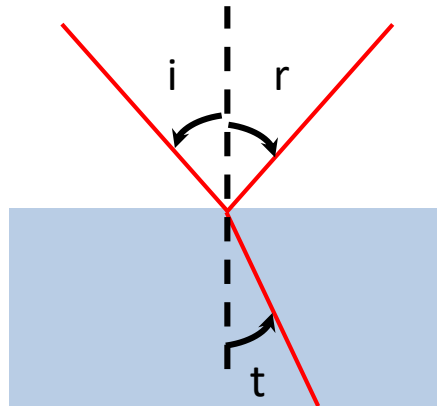
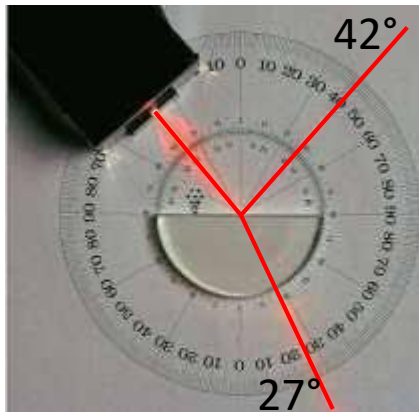
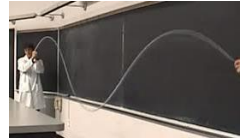


$$r = -i$$



Euclide
≈ 300 av. JC

Lois de Snell et Descartes

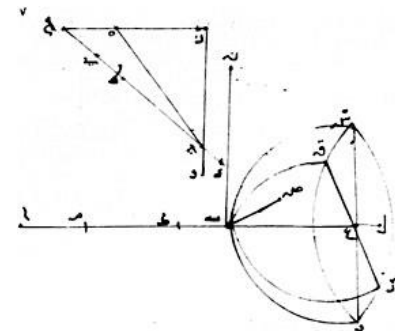


Willebrord Snell
1580-1626



René Descartes
1596-1650

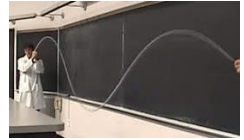
$$\sin r = n \sin i$$



لأنه انما يتولد عليه سطح مستوي غيره فلا ينفصل هذا السطح عن سطح آخر

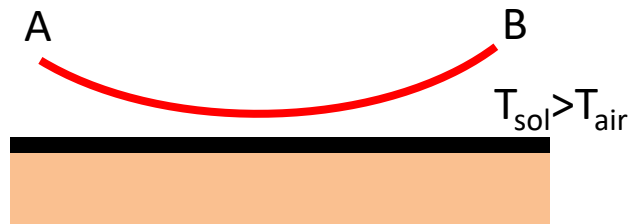
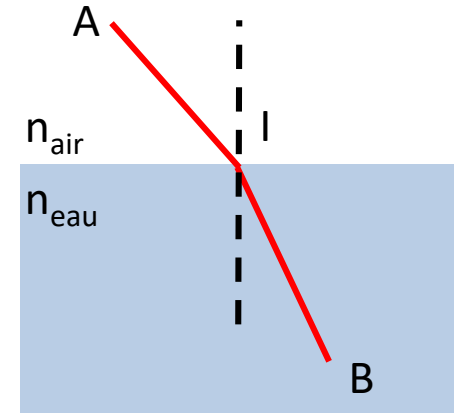
Abou Sa'd al-'Ala' ibn Sahl
vers 984

Principe de Fermat (1657)



Pierre de Fermat
(vers 1605-1665)

« La nature agit toujours par les voies les plus courtes et les plus simples. »

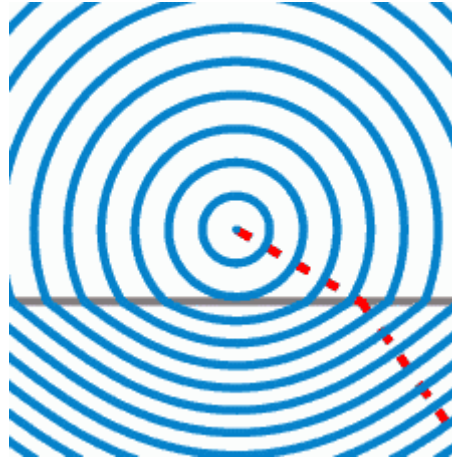


$$T_{\text{mer}} < T_{\text{air}}$$

Interprétations



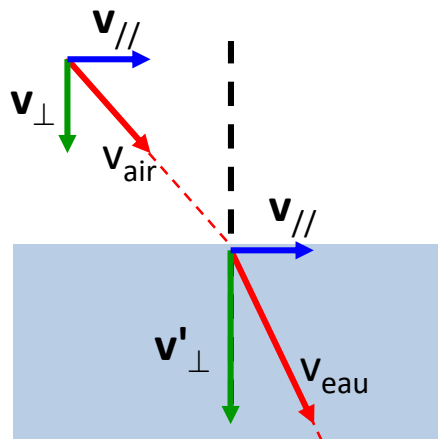
Christian Huygens
1629 -1695



$$v_{\text{eau}} < v_{\text{air}}$$



René Descartes
1596-1650

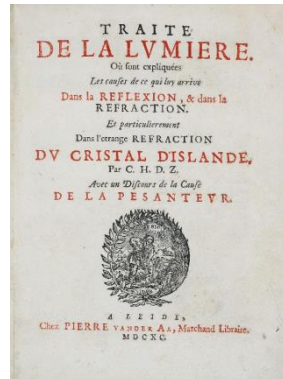


$$v_{\text{eau}} > v_{\text{air}}$$

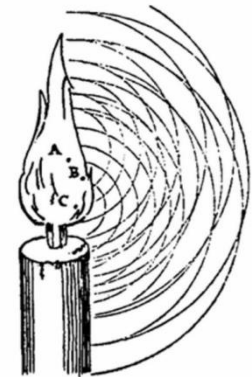
Newton vs Huygens



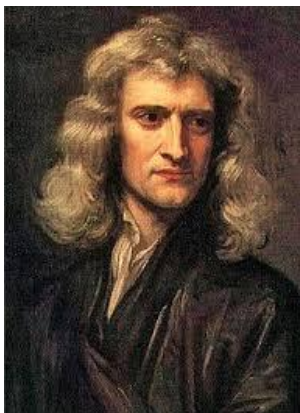
Christian Huygens
1629 -1695



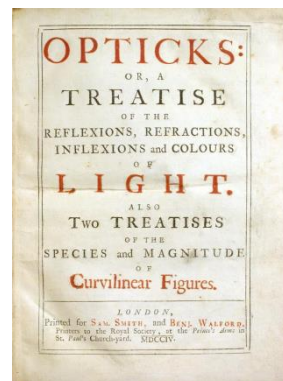
traité de la lumière
1690



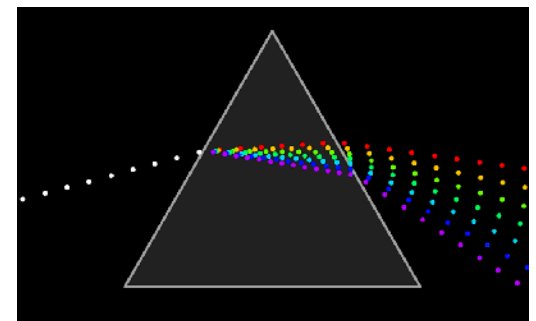
ondes



Isaac Newton
(1642 – 1727)

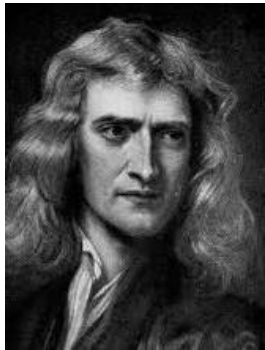
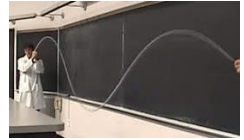


Optiks – 1704

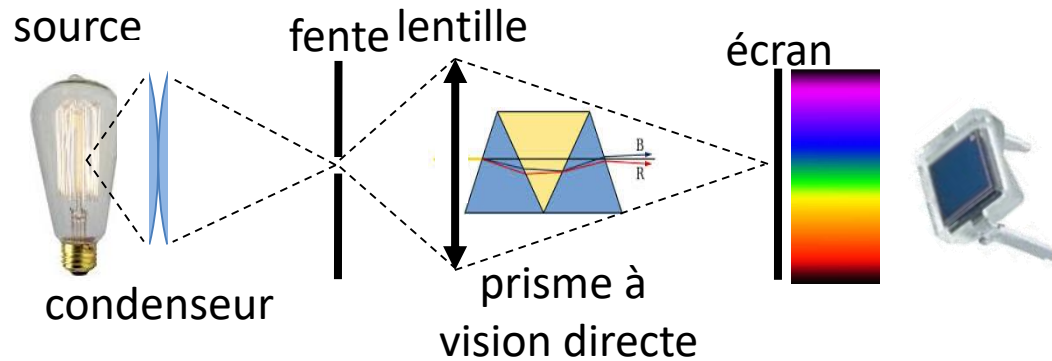


corpuscules

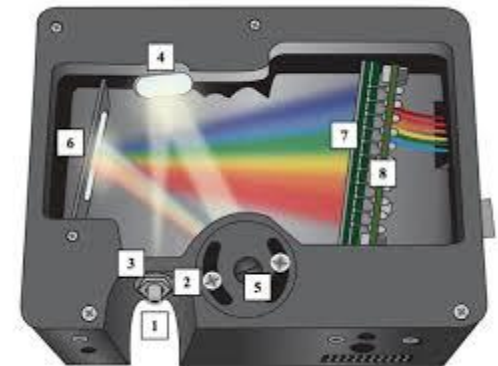
Les couleurs (1666)



Isaac Newton
1642-1726



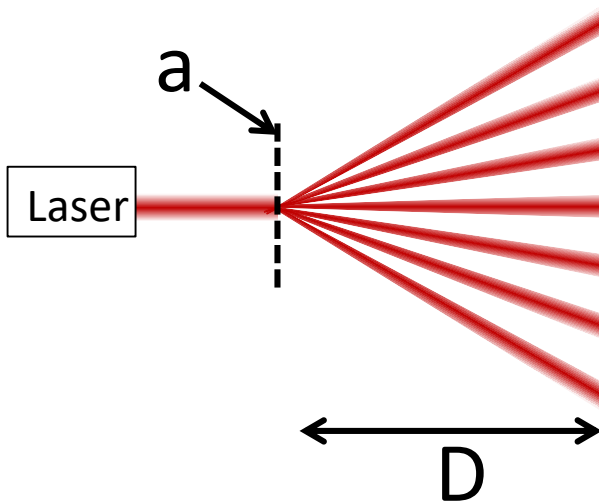
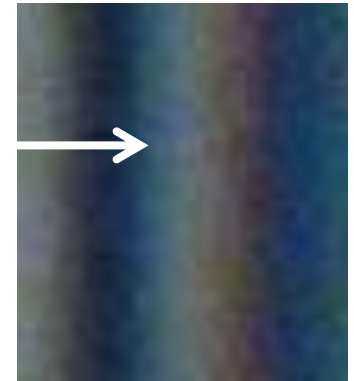
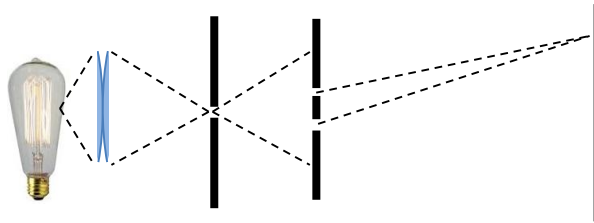
spectromètre
USB



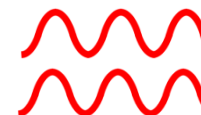
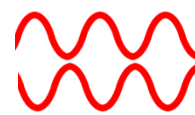
Interférences (1802)



Thomas Young
1773-1829

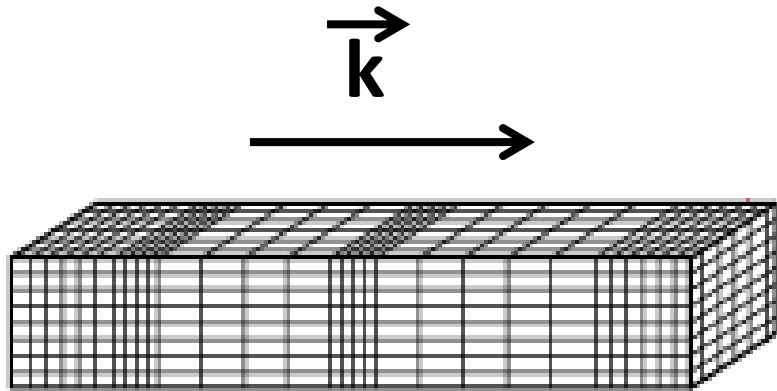


$$\updownarrow i = \lambda D / a$$



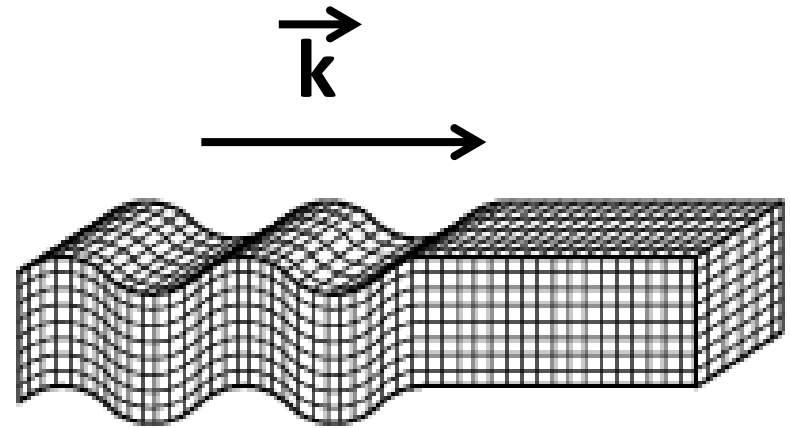
$$\lambda_{\text{typ.}} = 0.65 \mu\text{m}$$

Deux types d'ondes



$$\vec{v} // \vec{k}$$

longitudinale



$$\vec{v} \perp \vec{k}$$

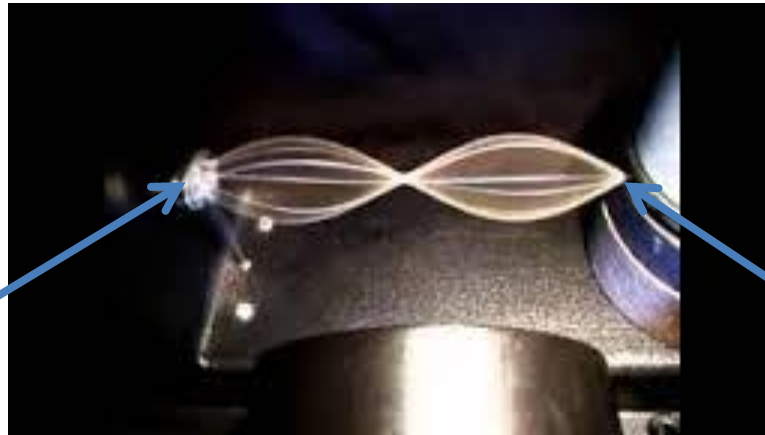
transverse



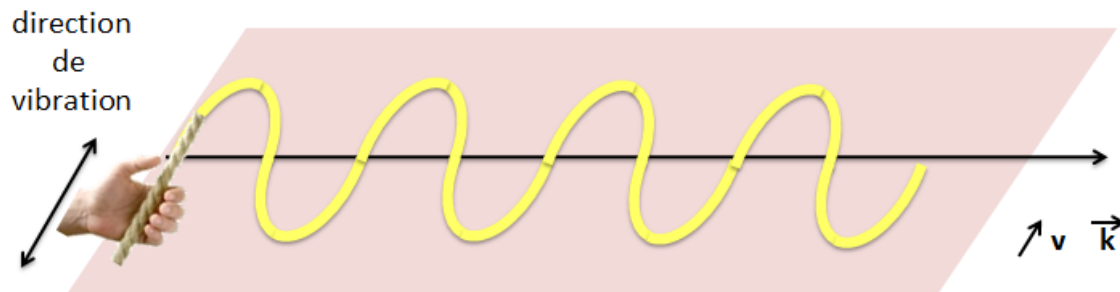
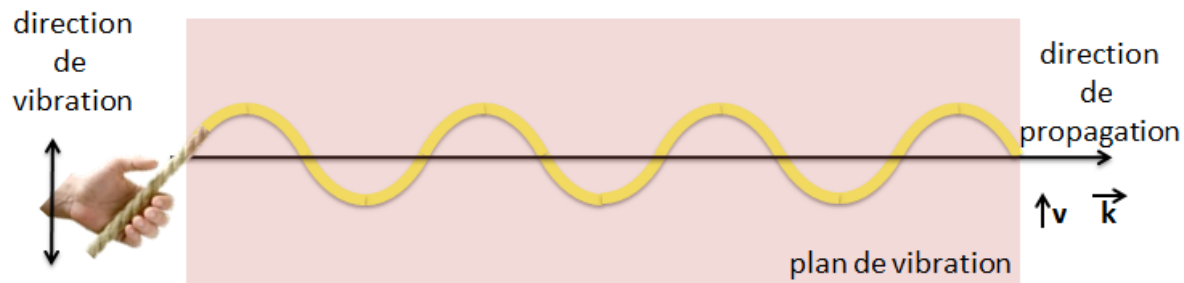
Corde de Melde



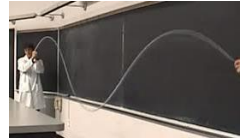
vibreux



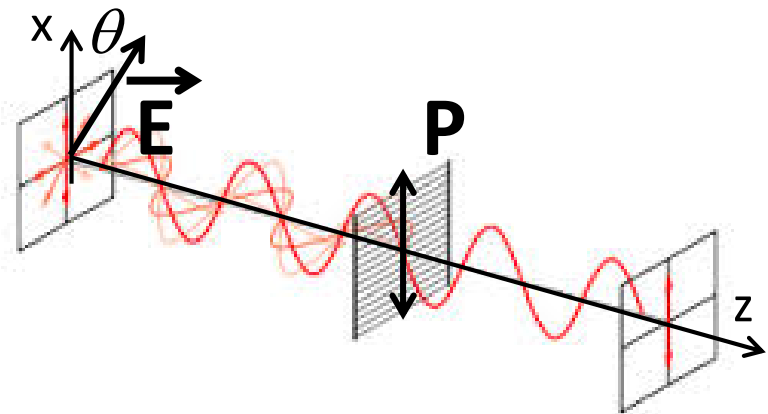
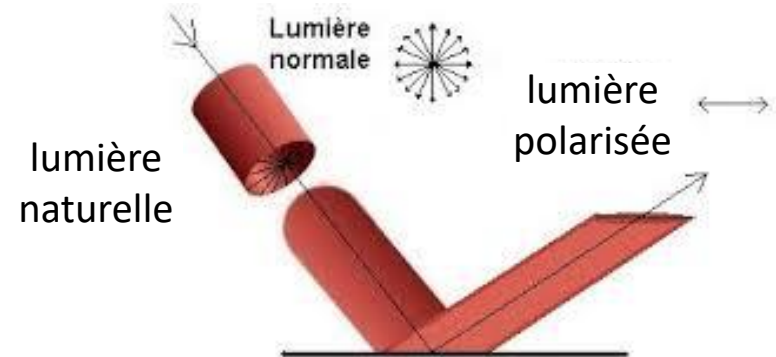
point fixe



Polarisation (1809)

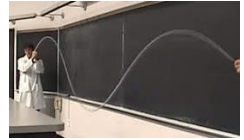


Etienne Malus
1775-1812

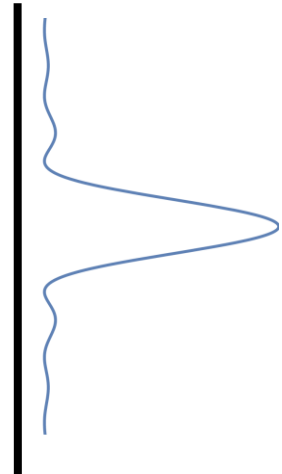
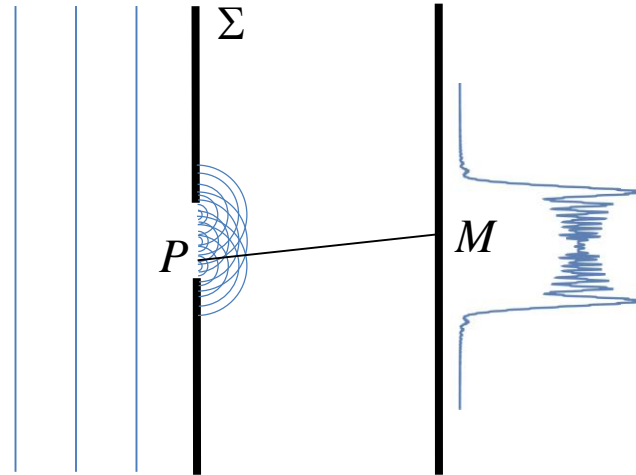


onde *transverse*

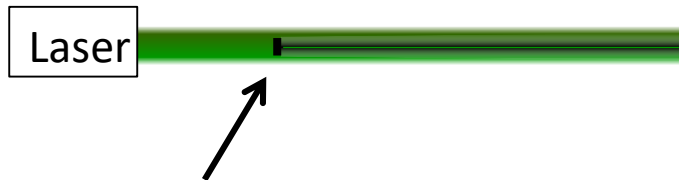
Diffraction (1815)



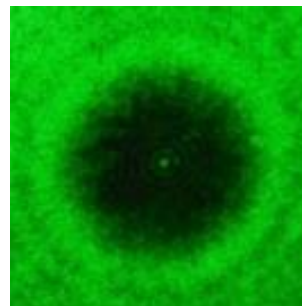
Augustin Fresnel
1788-1827



$$\Psi(M) = -\frac{i}{\lambda} \iint_{\Sigma} Q(P; M) \Psi_i(P) \frac{e^{ikPM}}{PM} d^2 P$$



écran circulaire



point de Poisson
1818

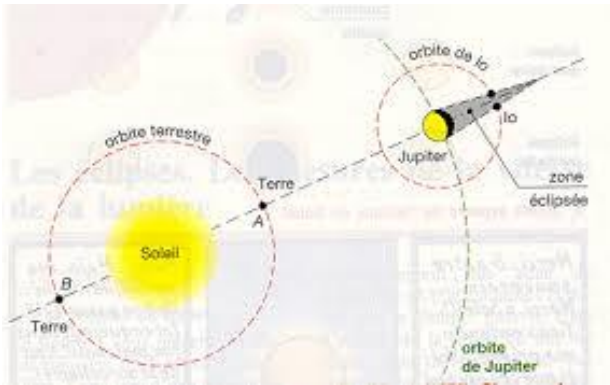


Denis Poisson
1781-1840



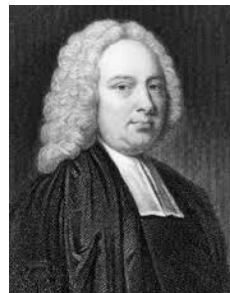
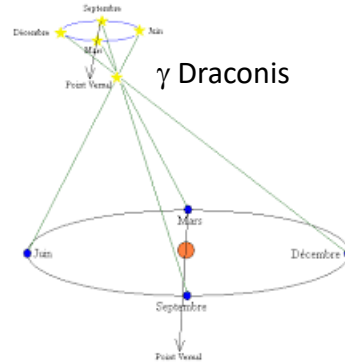
François Arago
1786-1853

Vitesse de la lumière



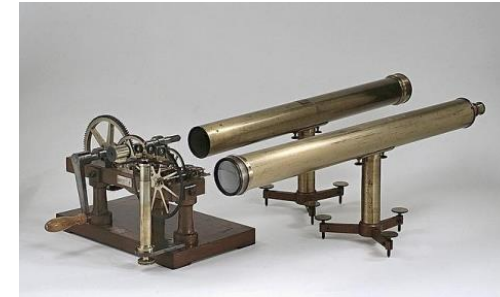
1676

Ole Christensen Rømer
1644-1710

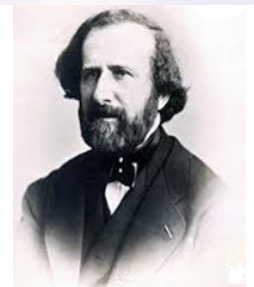


1725

James Bradley
1693-1762



1849



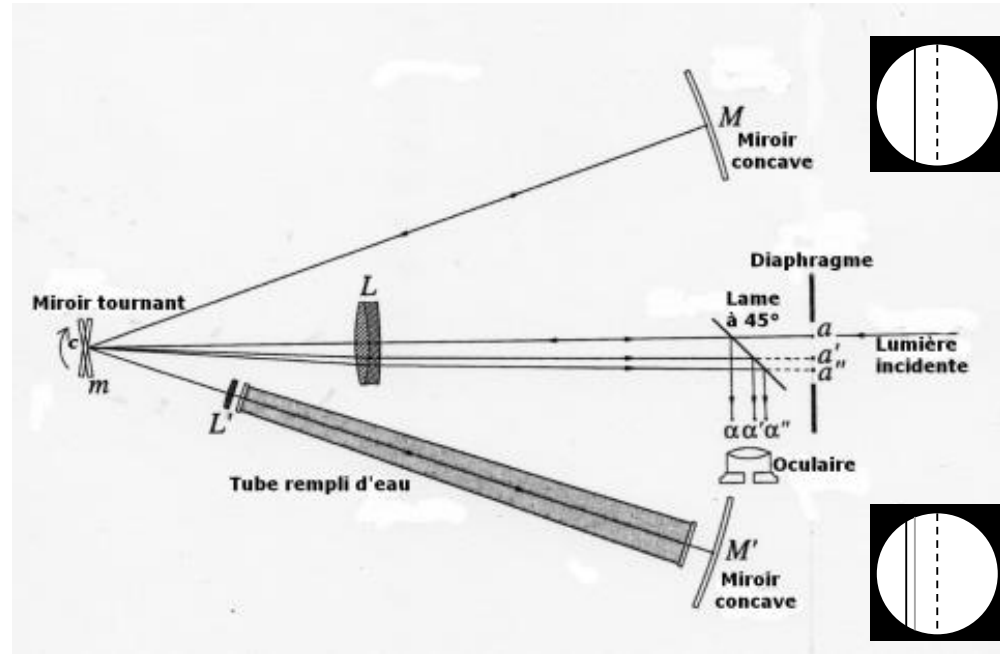
Hippolyte Fizeau
1819-1896

$$c \approx 3 \times 10^8 \text{ m.s}^{-1}$$

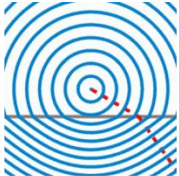
Foucault – Fizeau (1850)



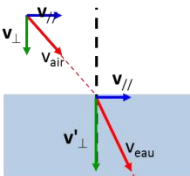
Léon Foucault
(1819-1868)



$$v_{\text{eau}} < v_{\text{air}}$$



$$v_{\text{eau}} < v_{\text{air}}$$



$$v_{\text{eau}} > v_{\text{air}}$$



Electromagnétisme (1865)

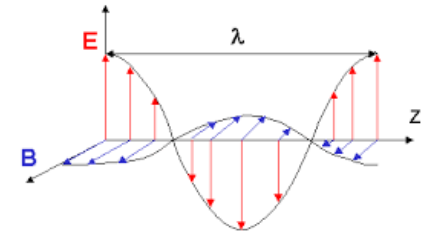


James Clerck Maxwell
1831-1879

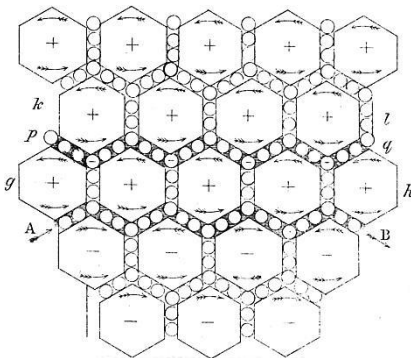
$$\left. \begin{aligned} \nabla \cdot \mathbf{E} &= 0 \\ \nabla \cdot \mathbf{B} &= 0 \end{aligned} \right\}$$

$$\nabla \times \mathbf{E} + \frac{\partial \mathbf{B}}{\partial t} = 0$$

$$\nabla \times \mathbf{B} - \epsilon_0 \mu_0 \frac{\partial \mathbf{E}}{\partial t} = 0$$



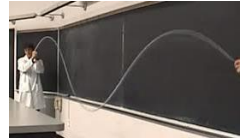
$$\lambda = c/\nu$$



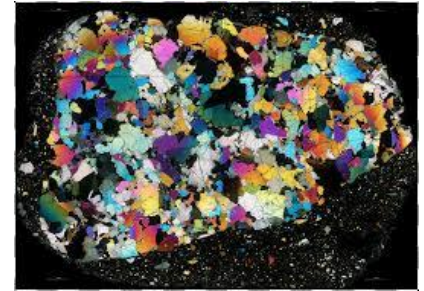
$$\frac{\partial^2 \mathbf{E}}{\partial t^2} - \frac{1}{\epsilon_0 \mu_0} \frac{\partial^2 \mathbf{E}}{\partial z^2} = 0 \quad c \approx 3 \times 10^8 \text{ m.s}^{-1}$$

« Nous pouvons difficilement éviter la conclusion que la lumière consiste en des ondulations du même milieu que celui qui est la cause des phénomènes électriques et magnétiques »

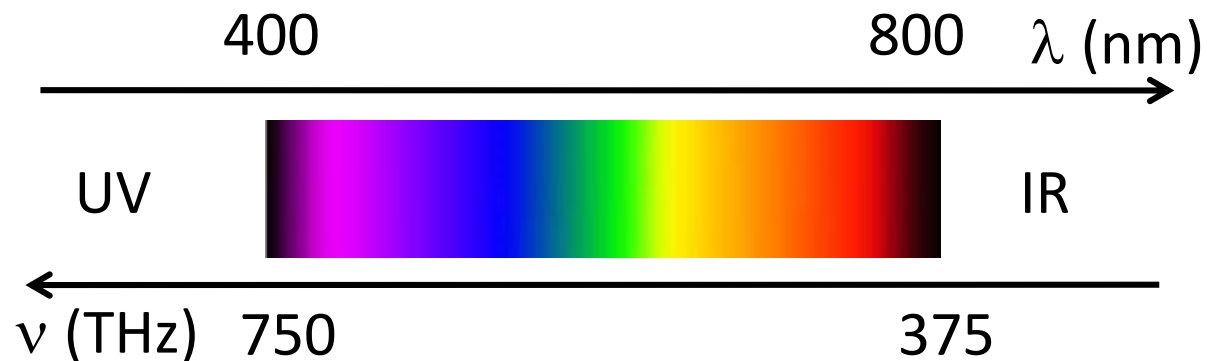
La lumière fin XIX^{ème} siècle



Onde électromagnétique transverse

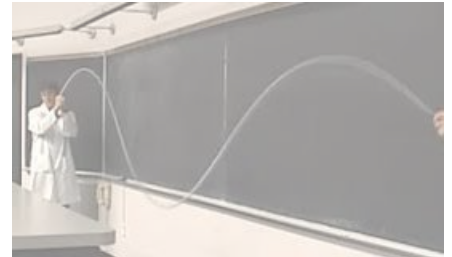


$$c \approx 3 \times 10^8 \text{ m.s}^{-1}$$



Plan

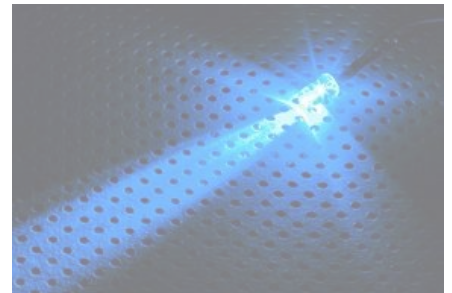
Du modèle corpusculaire au
modèle ondulatoire



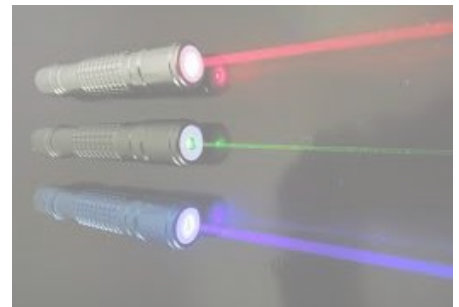
De la spectroscopie au modèle
quantique de l'atome...



... jusqu'à la LED bleue



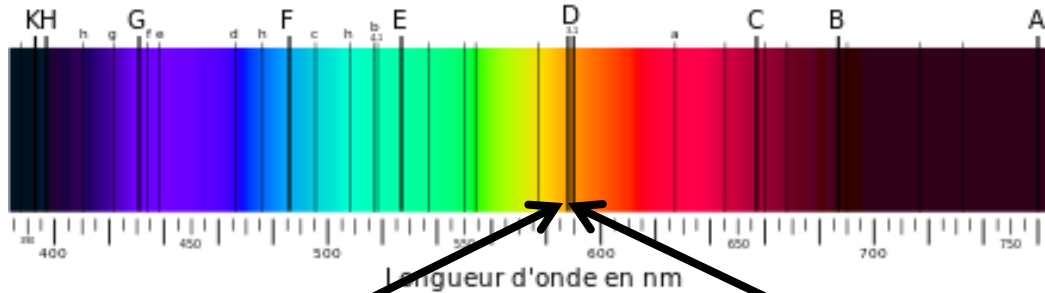
et au-delà...



Un formidable outil...

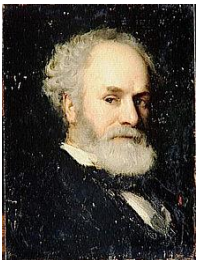


Joseph von Fraunhofer
(1814)



587,5nm
?

589,0 et 589,6nm



Jules Janssen



Norman Lockyer

découverte de l'Hélium
(1848)



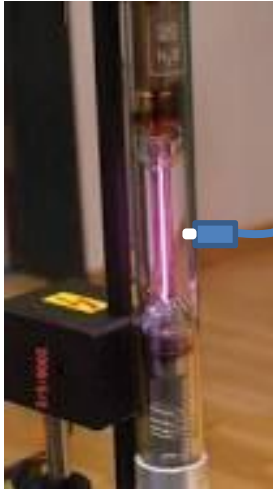
Na



He

587,5nm

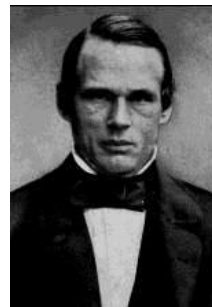
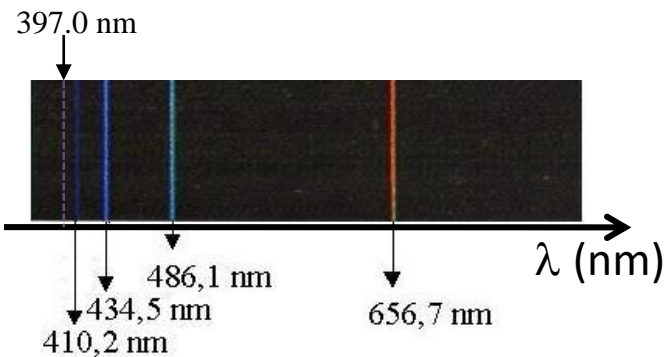
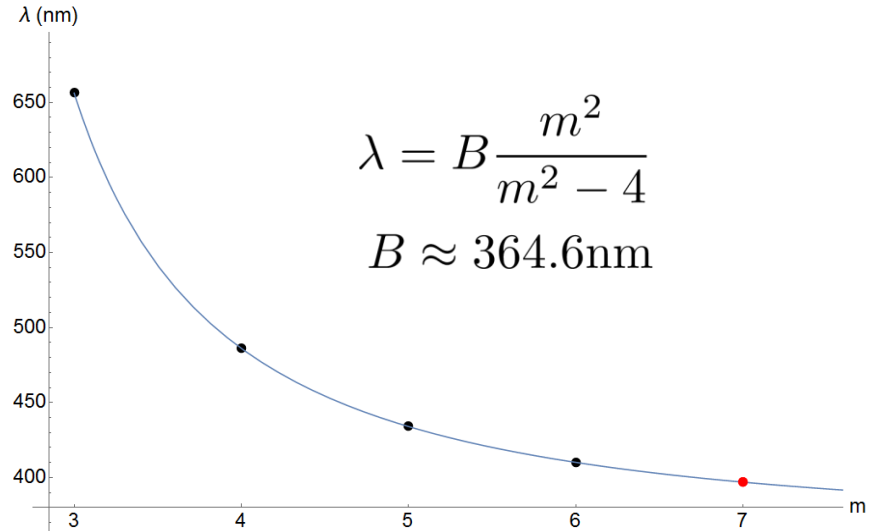
Spectre de raies (1885)



lampe H₂O



spectromètre USB



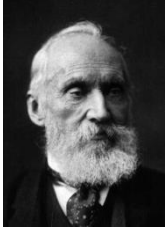
Anders Ångström
 1814-1874

m=7



Johann Balmer
 1825-1898

Michelson-Morley (1887)

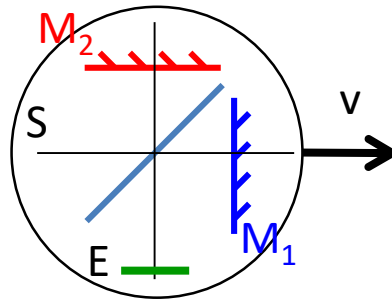


Lord Kelvin
(1824-1907)

« La connaissance en physique est semblable à un grand ciel bleu, à l'horizon duquel subsistent seulement deux petits nuages d'incompréhension. »



Albert Michelson
(1852-1931)

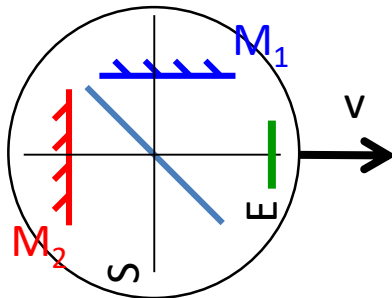


c : lumière / éther

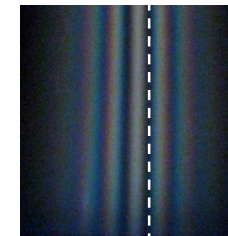
v : terre / éther

$$t_{\parallel} \approx \frac{2L}{c}(1 + v^2/c^2) \quad t_{\perp} \approx \frac{2L}{c}(1 + v^2/2c^2)$$

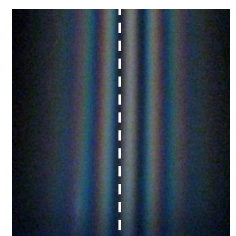
$$\delta t_0 = t_1 - t_2 = t_{\parallel} - t_{\perp} \approx +\frac{2L}{c}(v^2/2c^2)$$



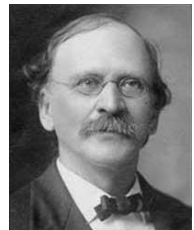
$$\delta t_{90} = t_1 - t_2 = t_{\perp} - t_{\parallel} \approx -\frac{2L}{c}(v^2/2c^2)$$



0°

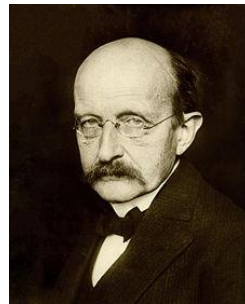
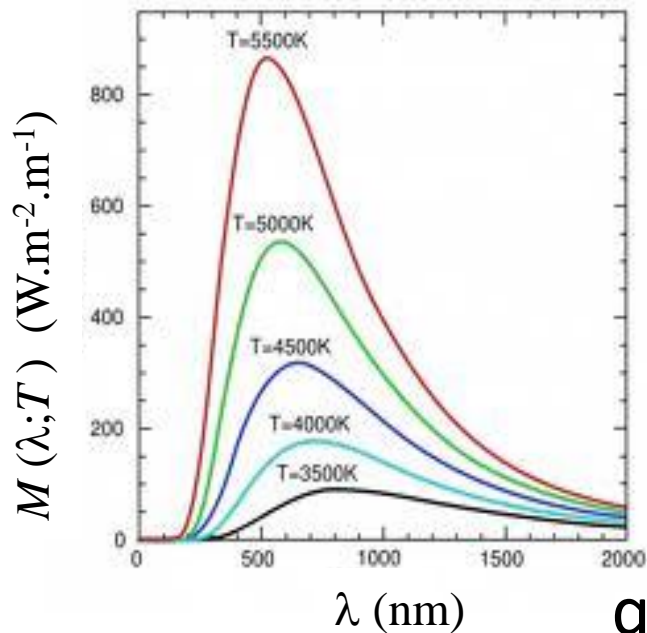


90°



Edward Morley
(1838-1923)

Corps noir (1900)



Max Planck
(1858-1947)

$$E = h\nu$$

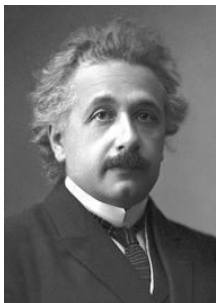
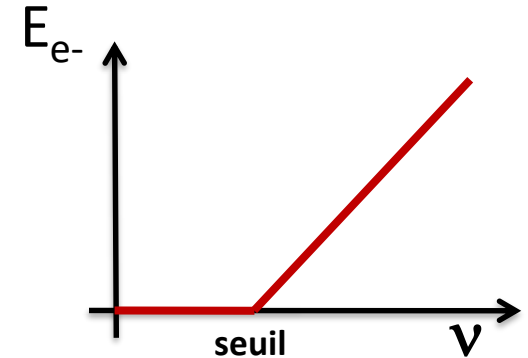
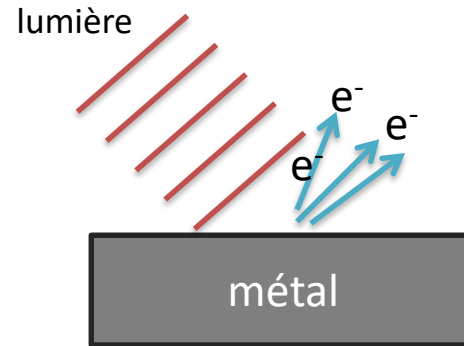
quantification des échanges d'énergie

Effet Photoélectrique



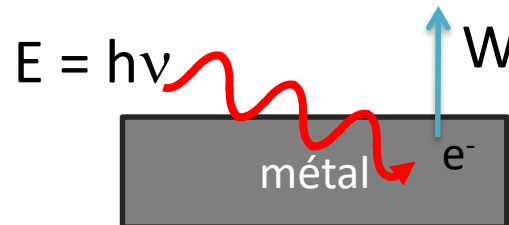
Heinrich Hertz
1857-1894

1887



Albert Einstein
1879-1955

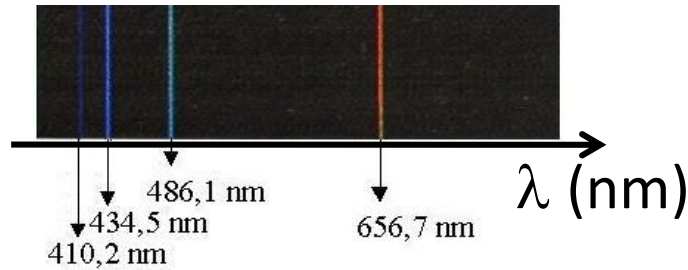
1905



$$E_{e^-} = h\nu - W$$

Photon

Quantification de l'énergie



$$\lambda = B \frac{m^2}{m^2 - 4}$$

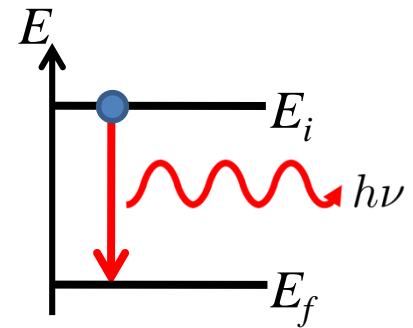


Johannes Rydberg
1854-1919



Walther Ritz
1878-1909

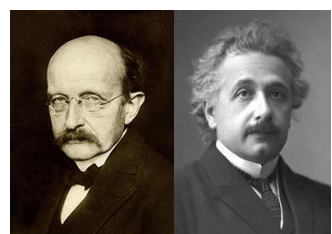
$$\frac{1}{\lambda} = R_y \left(\frac{1}{m^2} - \frac{1}{n^2} \right)$$



$$E = h\nu = hc/\lambda$$

$$h\nu = R_H \left(\frac{1}{2^2} - \frac{1}{n^2} \right)$$

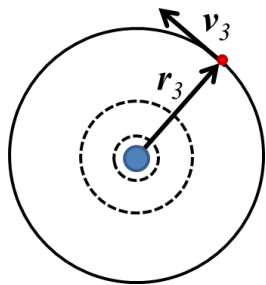
$E_f \quad E_i$



Synthèse quantique



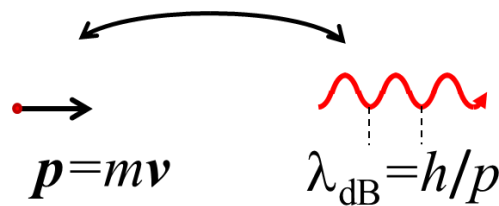
Niels Bohr
1885-1962



(1913)



Louis de Broglie
(1892-1987)

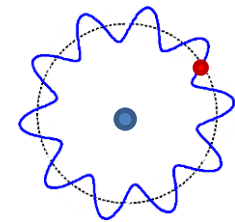


(1924)



Erwin Schrödinger
(1887-1961)

$$i\hbar \frac{\partial \psi}{\partial t} = \left[-\frac{\hbar^2}{2m} \Delta + V \right] \psi$$



(1926)

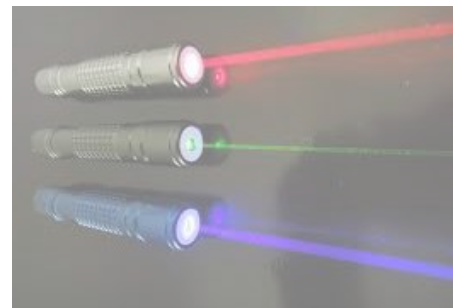
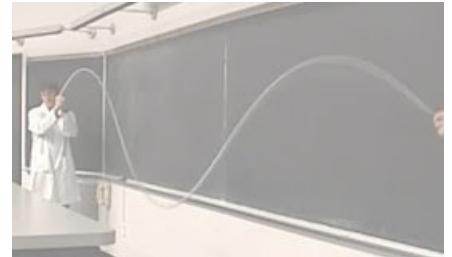
Plan

La lumière

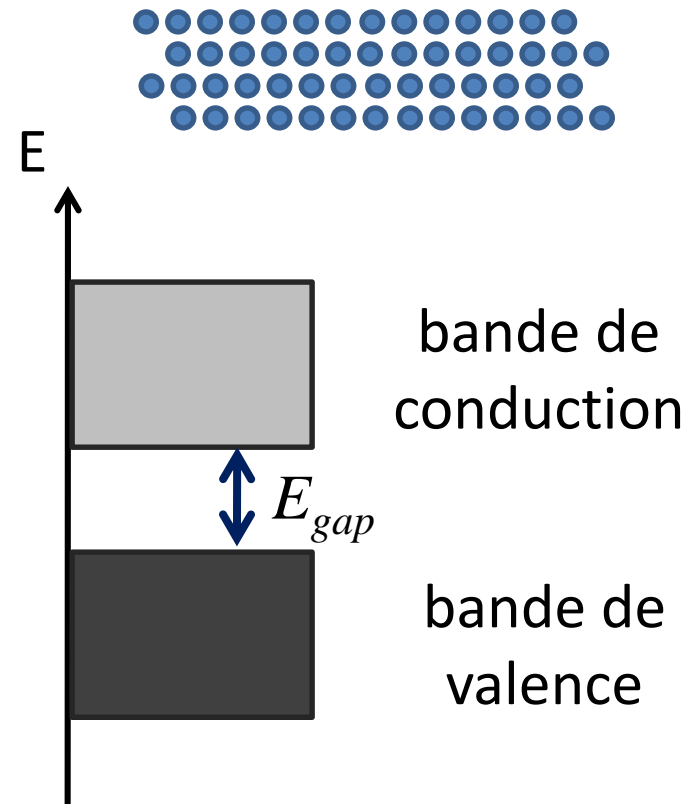
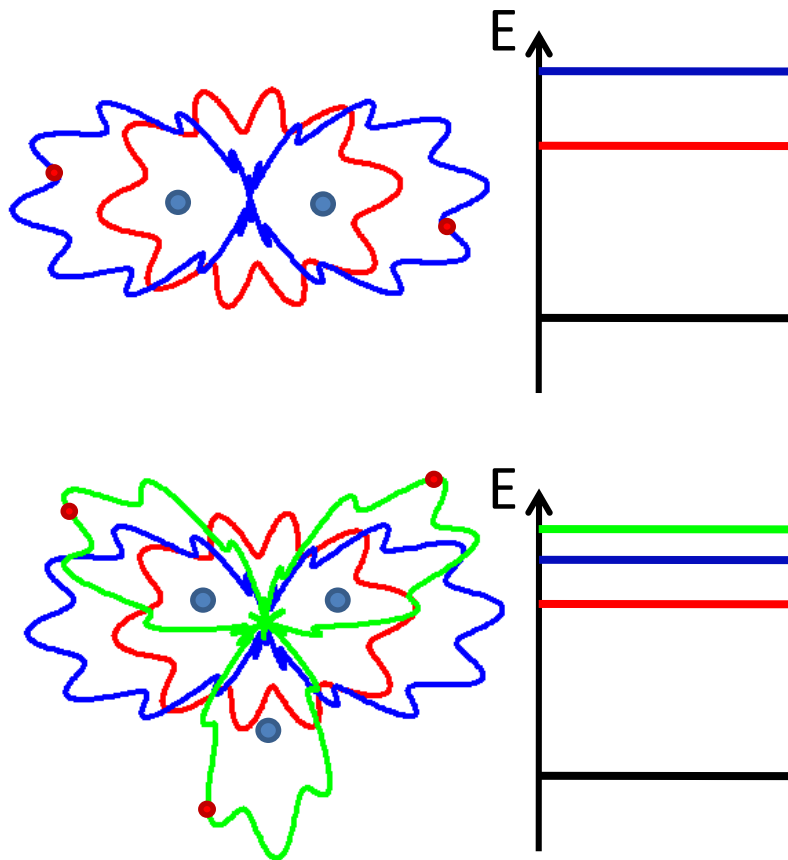
De la spectroscopie au modèle
quantique de l'atome...

... jusqu'à la LED bleue

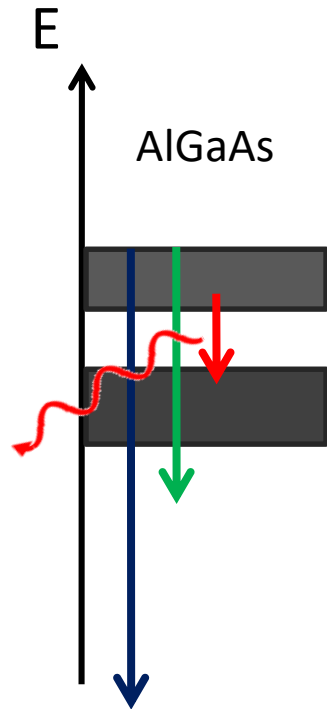
et au-delà...



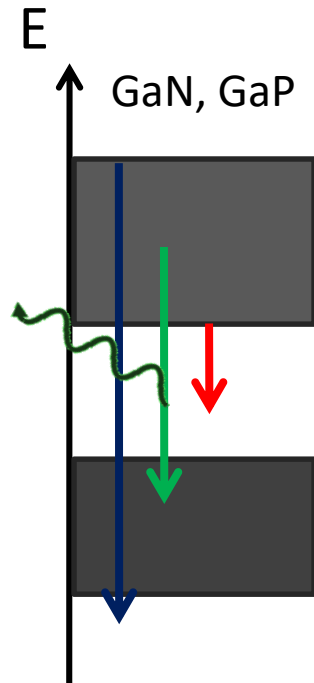
De l'atome au cristal



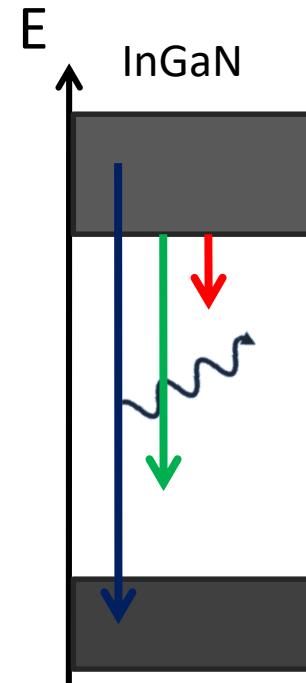
Spectre de bandes



faible gap
rouge



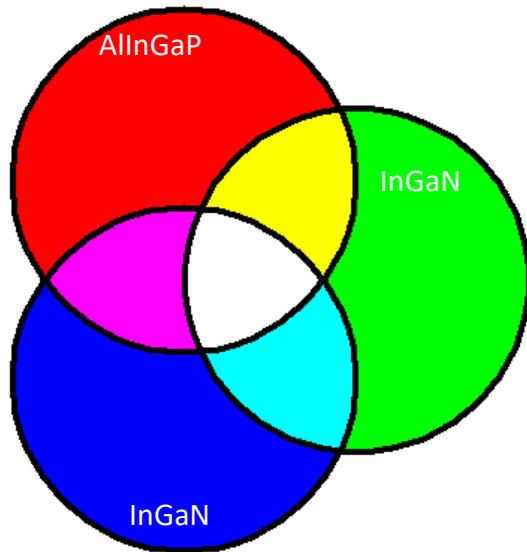
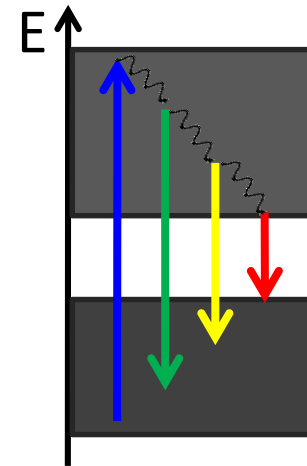
gap moyen
vert



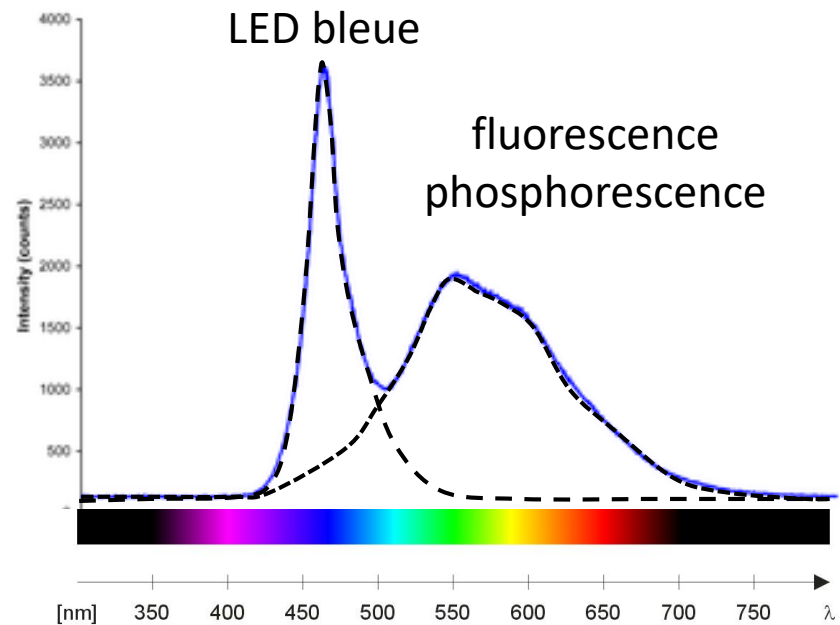
grand gap
bleu



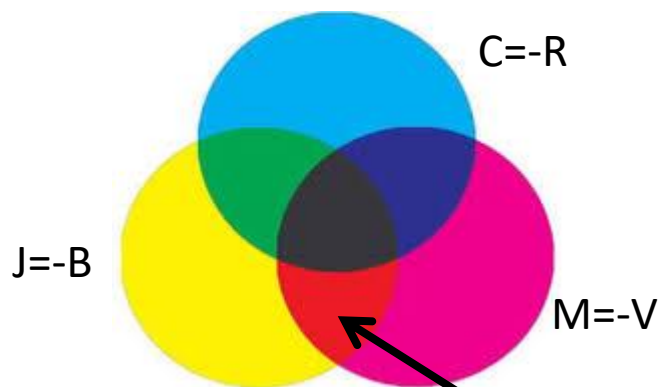
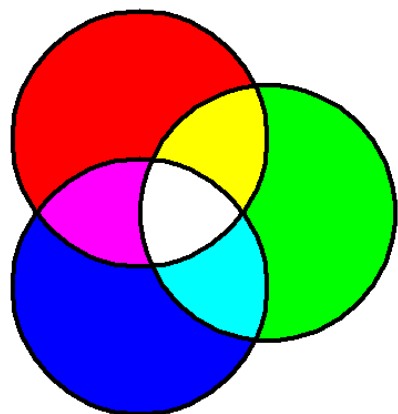
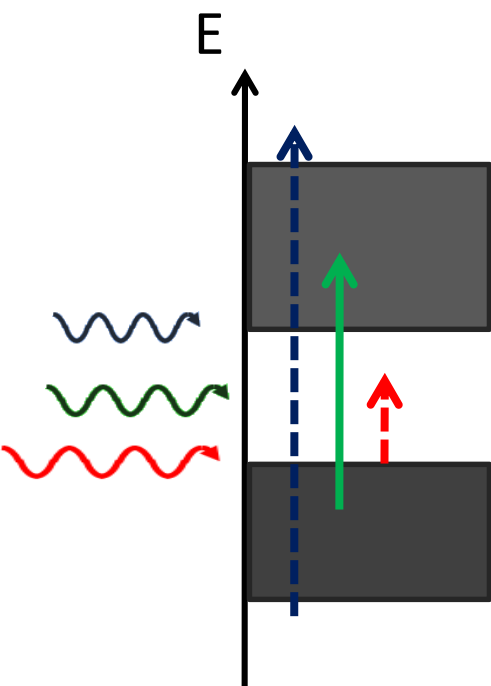
LED Blanche



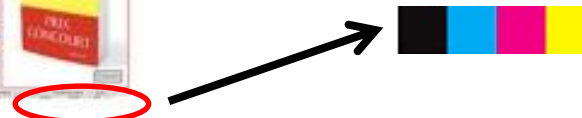
synthèse additive



Synthèse soustractive



$M+J=-V-B=R$



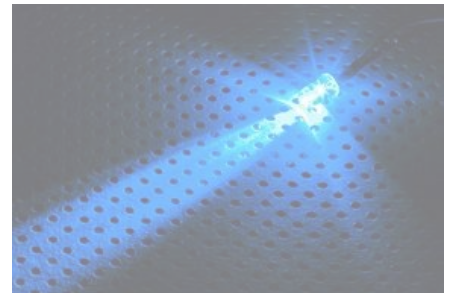
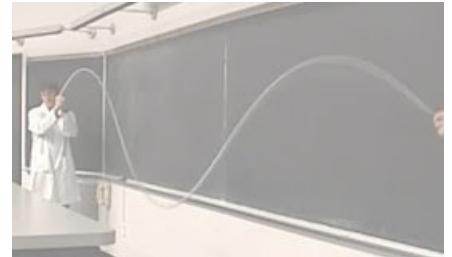
Plan

Du modèle corpusculaire au
modèle ondulatoire

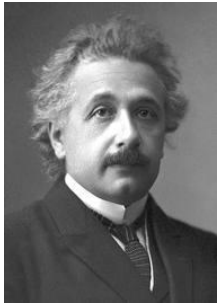
De la spectroscopie au modèle
quantique de l'atome...

... jusqu'à la LED bleue

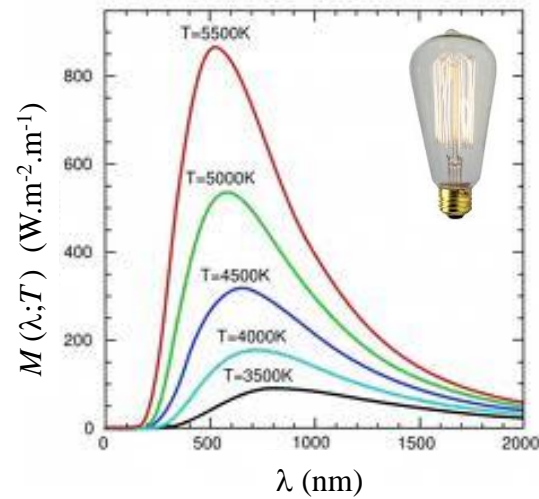
et au-delà...



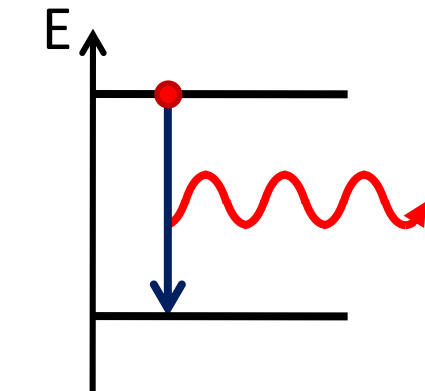
Théorie quantique du rayonnement



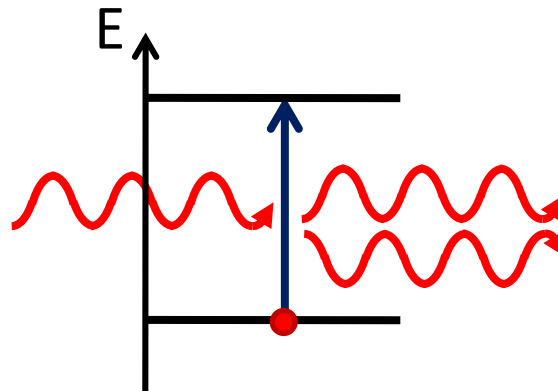
Albert Einstein
(1917)



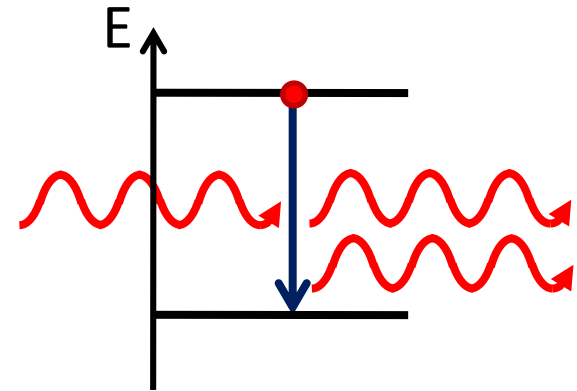
corps noir



émission spontanée



absorption



émission stimulée

Tout quantique (1927)



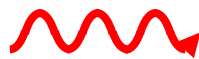
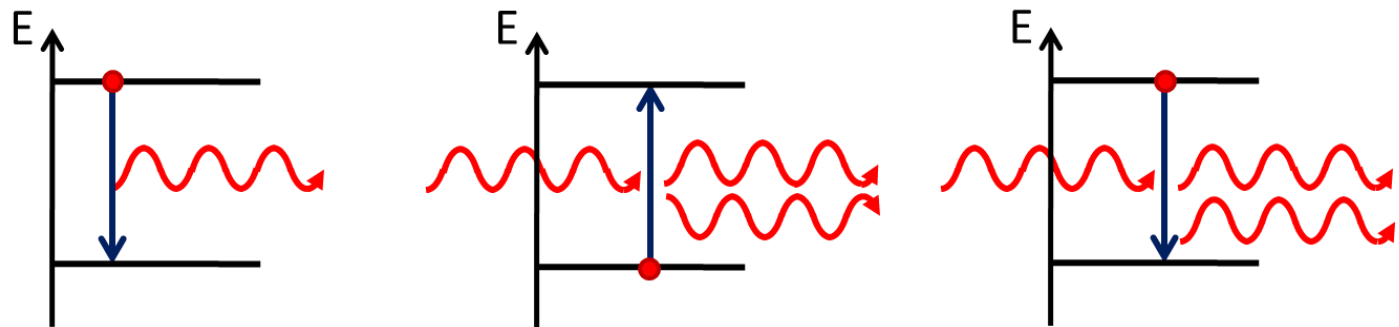
Pascual Jordan
(1902-1980)



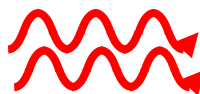
Paul Dirac
(1902-1984)



Wolfgang Pauli
(1900-1958)

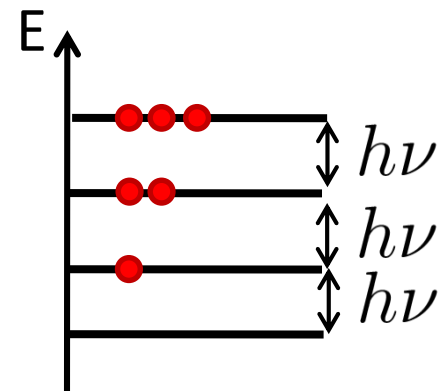


$|1\rangle$



$|2\rangle$

...



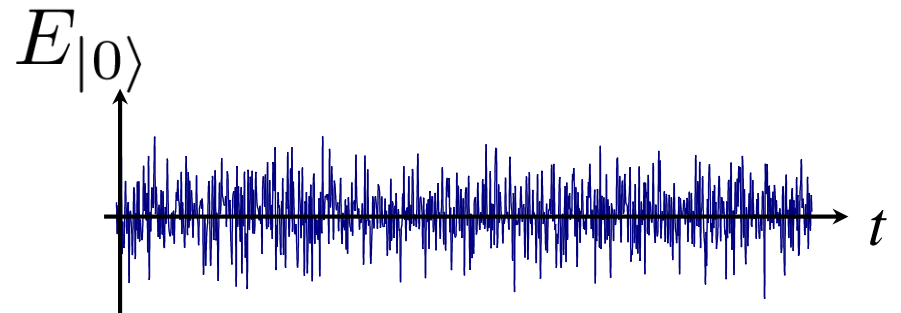
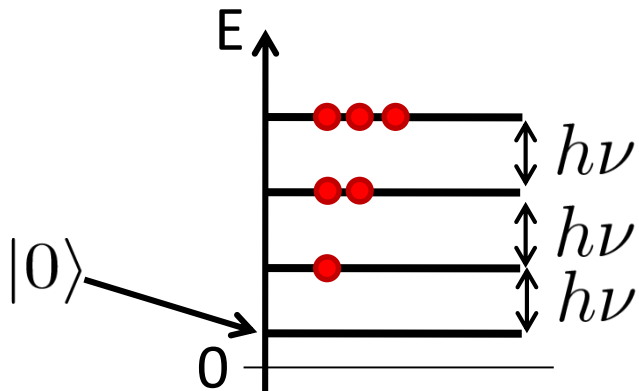
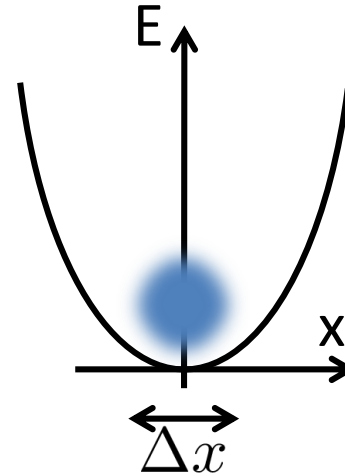
$|0\rangle$: vide quantique

Fluctuations du vide

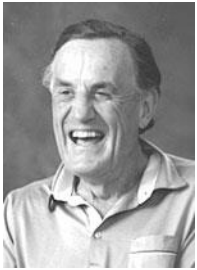


Werner Heisenberg
(1901-1976)

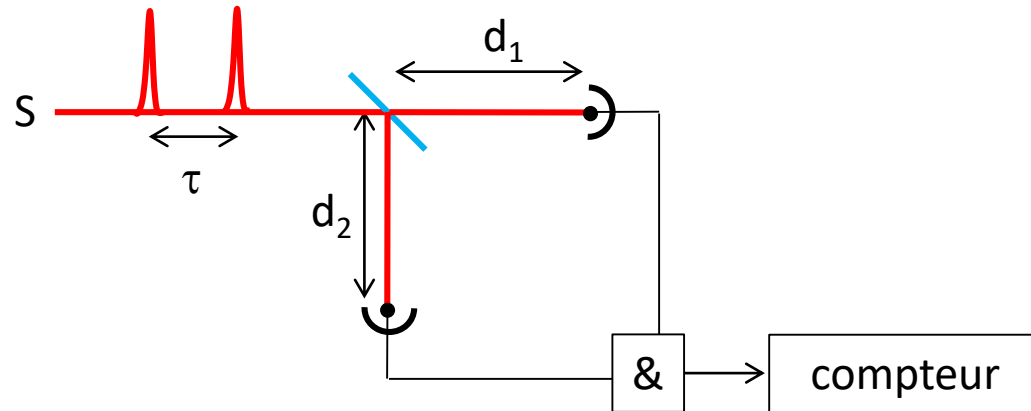
$$\Delta x \Delta p \geq \hbar/2$$



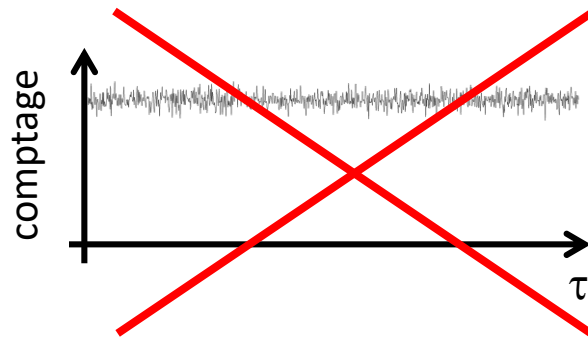
Corrélations d'intensité (1950's)



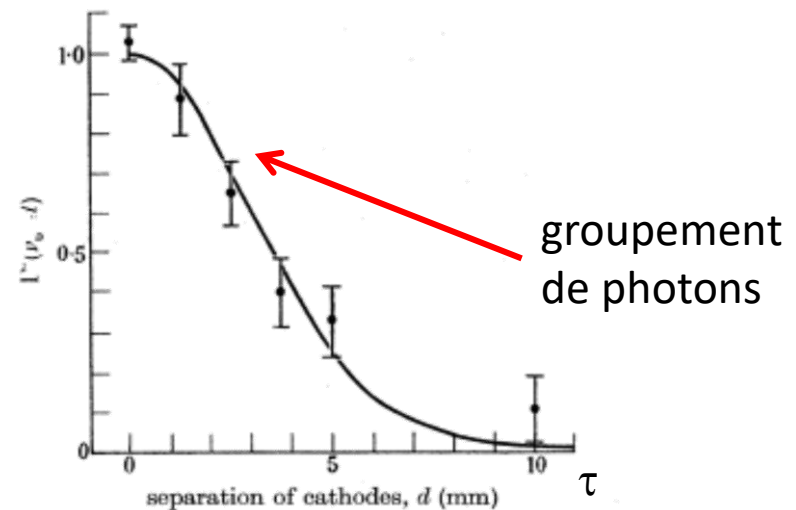
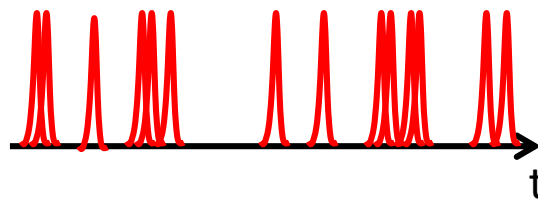
Robert Hanbury-Brown



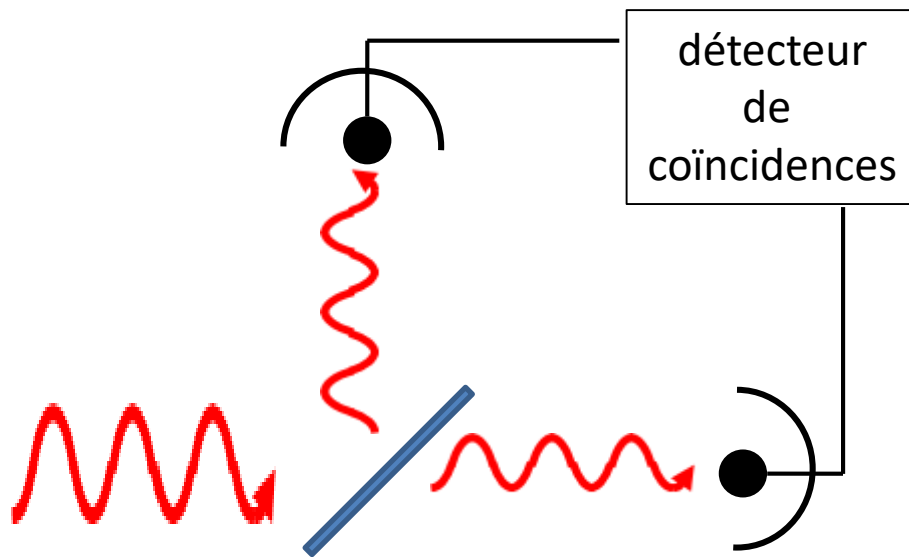
Richard Twiss



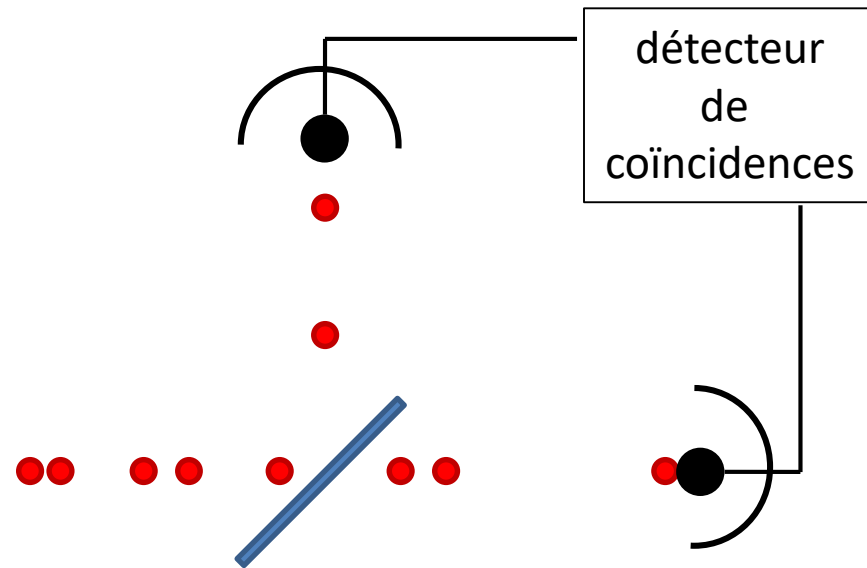
Roy Glauber
(1925-)



La séparatrice...

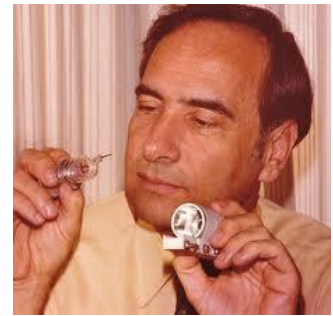
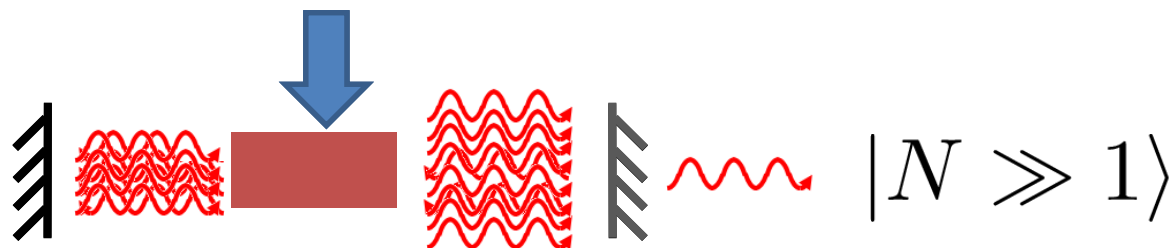
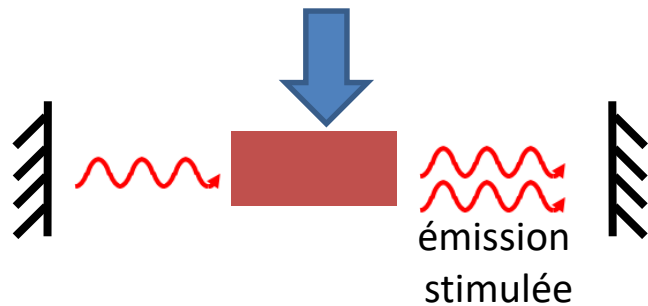
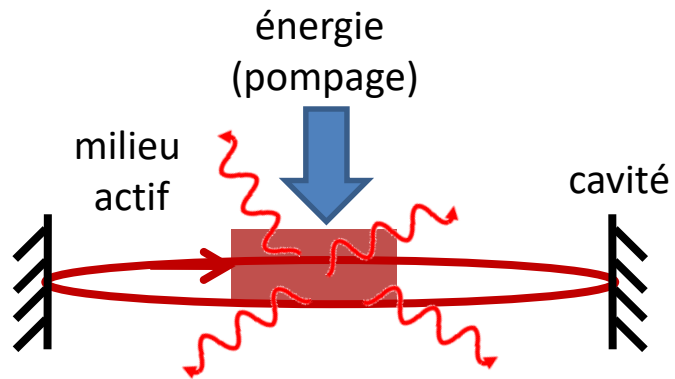


coïncidences fortuites

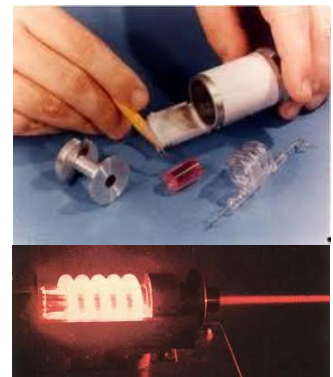


pas de coïncidences

Laser (1960)



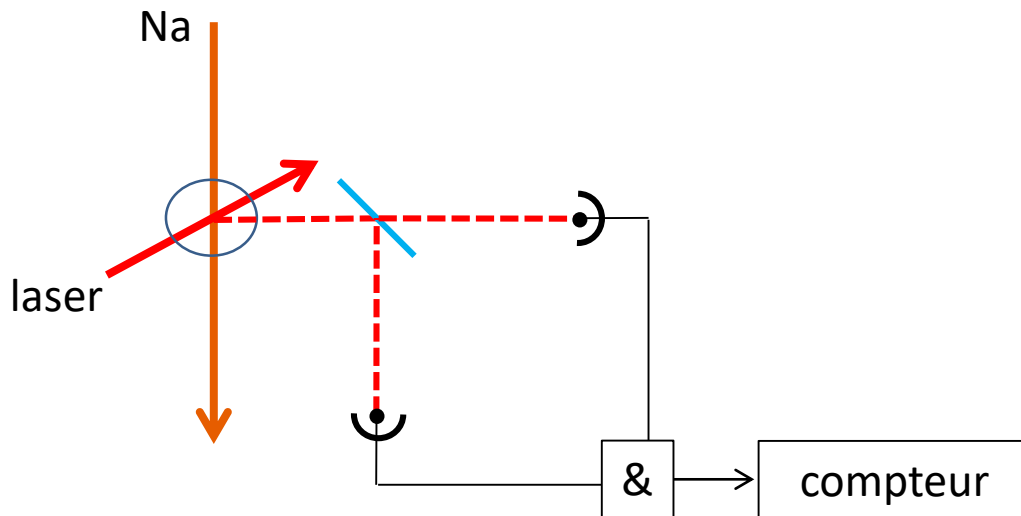
Theodore Maiman
(1927 - 2007)



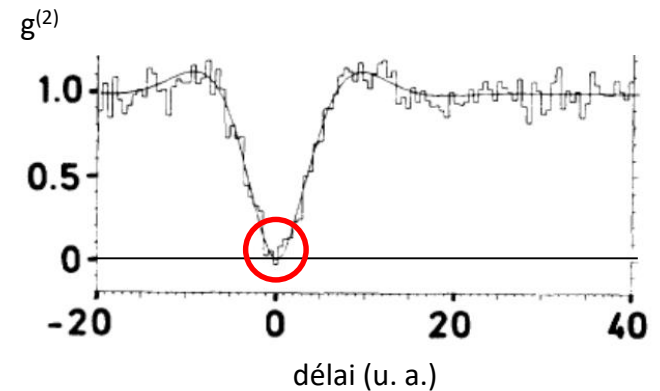
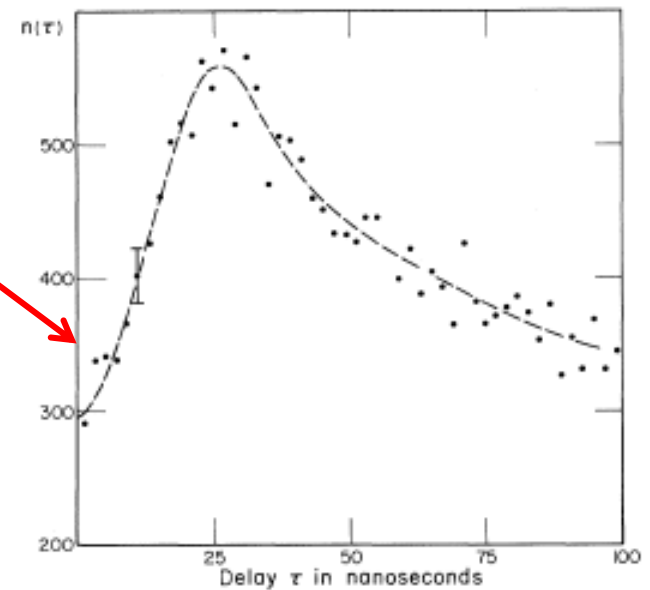
Couper un photon? (1977)



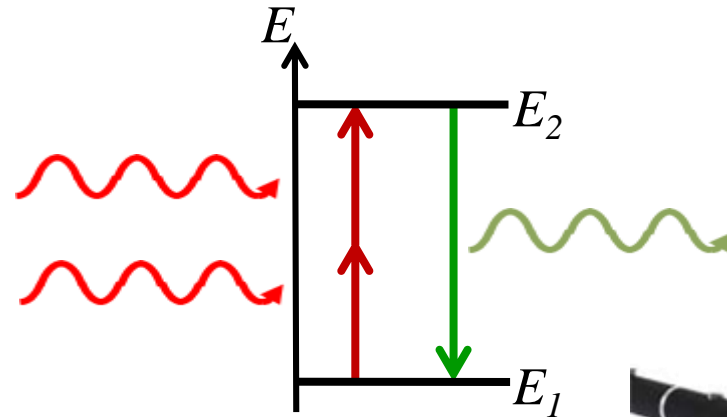
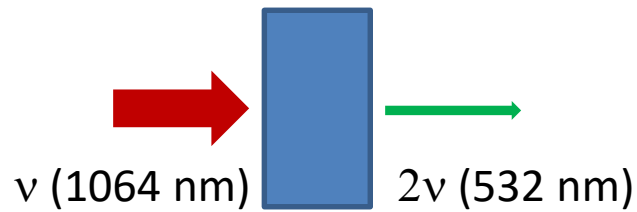
Kimble – Dagenais – Mandel (1977)



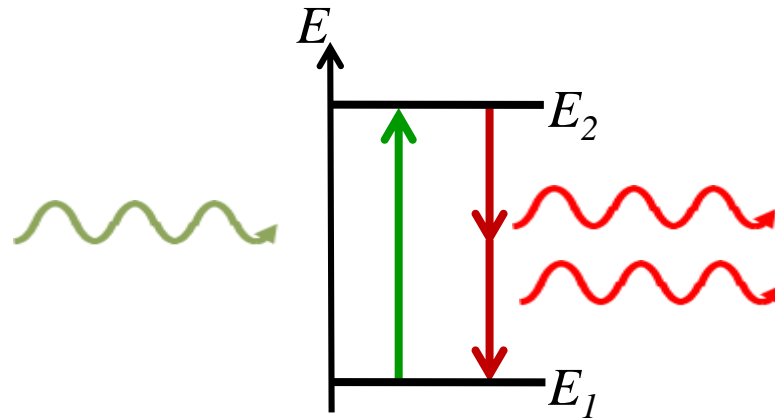
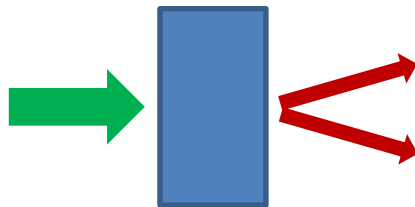
dégrouperment
de photons



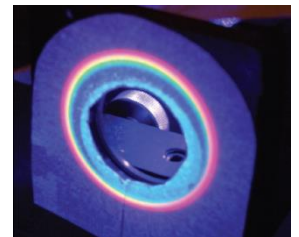
Lasers et optique non linéaire (70's)



doublage
de
fréquence



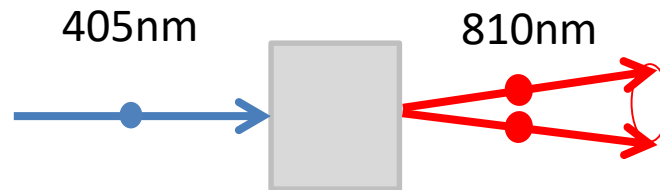
génération
paramétrique



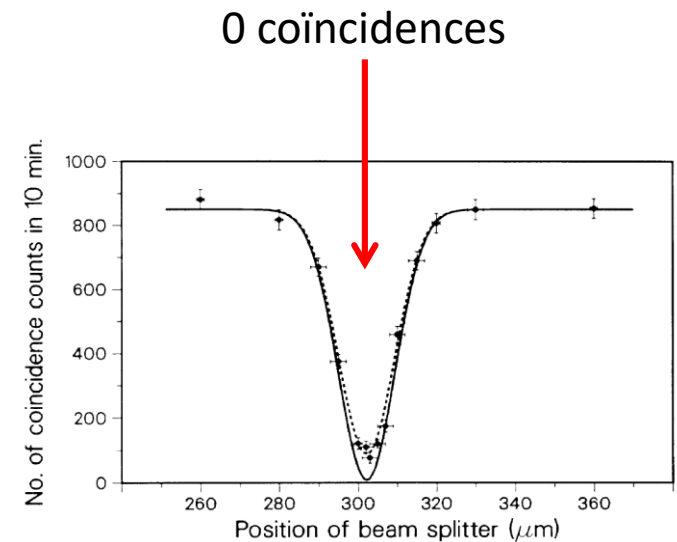
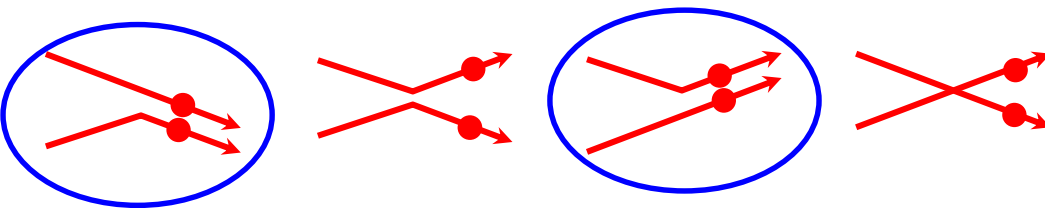
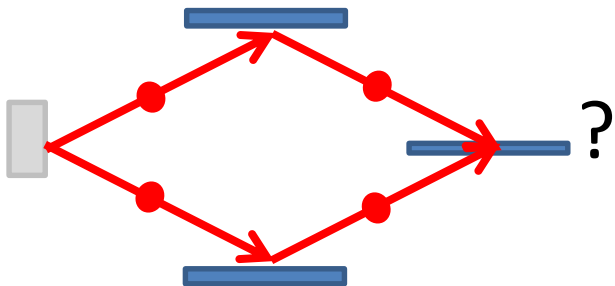
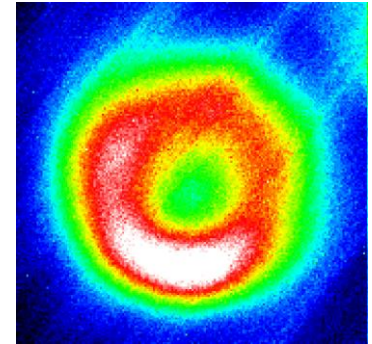
2 photons uniques (1986)



Hong - Ou - Mandel



photons jumeaux



Incroyable mais vrai



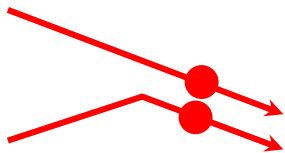
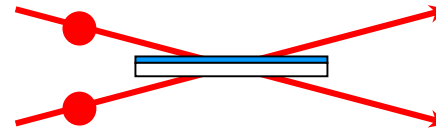
Voir film...

Interprétation

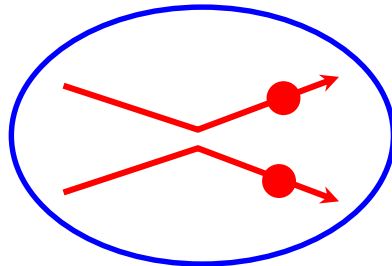


onde classique : toujours des coïncidences

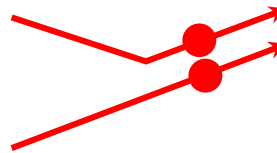
photons, particules classiques :



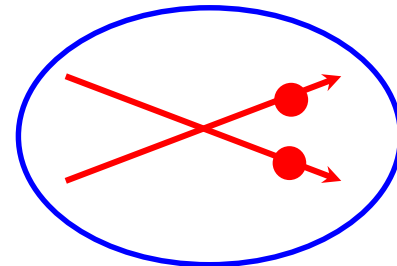
(1)



(2)

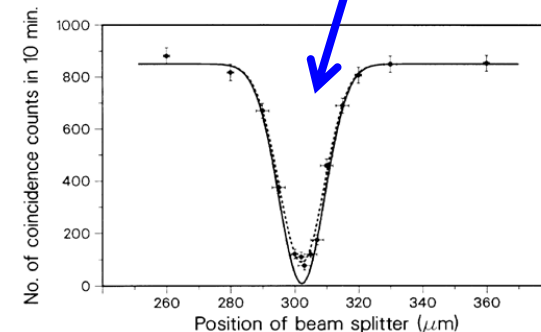


(3)

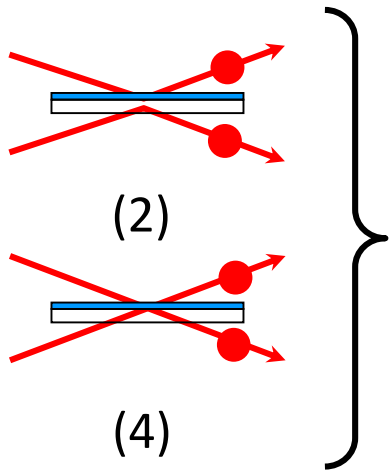


(4)

toujours des coïncidences



Interférences



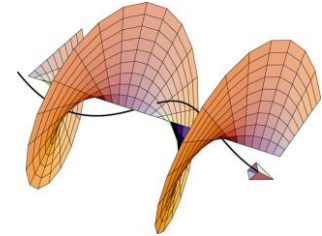
indistinguishables $|t, t\rangle + |r, r\rangle = 0$

dans le monde quantique,
de la probabilité plus de la probabilité
peut donner une probabilité nulle !!

Au-delà de la dualité

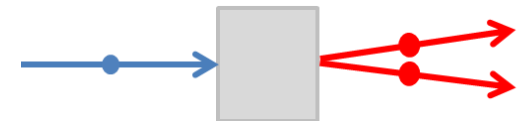
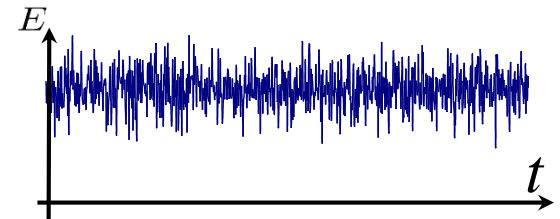


la particule de lumière n'est pas un « fort petit corpuscule »
c'est l'excitation élémentaire d'un mode classique du champ
dont il hérite des propriétés



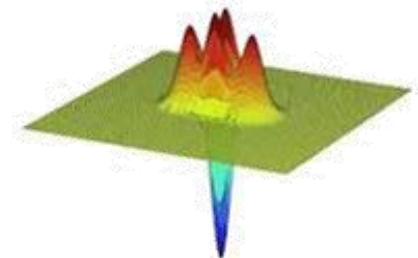
l'onde lumineuse n'est pas une onde de Maxwell classique

- fluctuations quantiques
- corrélations quantiques non-locales
(violation de l'inégalité de Bell)



le vide $|0\rangle$ n'est pas rien $|0\rangle + |1\rangle \neq |1\rangle$

états cohérents $|\alpha = +2\rangle$
"quasi-classiques" $|\alpha = -2\rangle$ mais $|\alpha = +2\rangle + |\alpha = -2\rangle$

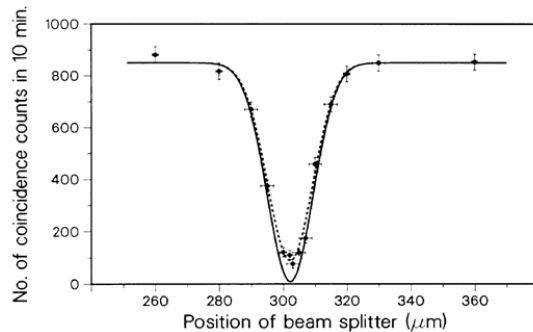


chaton de Schrödinger

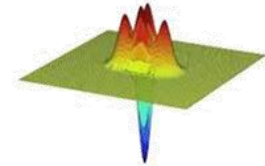
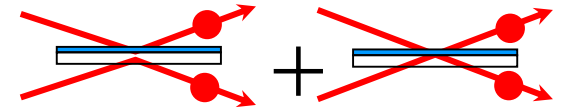
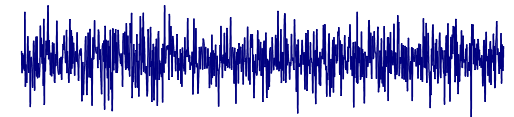
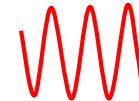
Une autre dualité

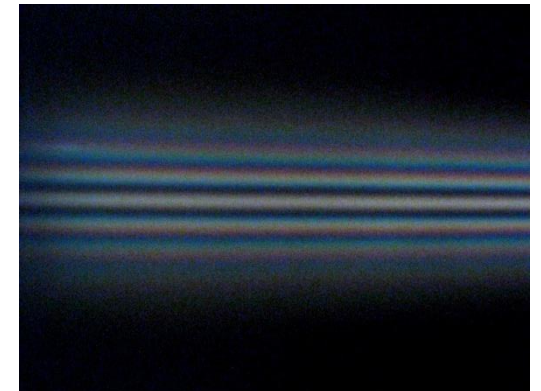
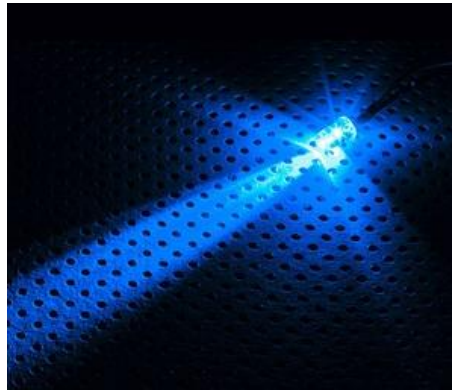


$$\begin{aligned}
 H_n(a) H_m(a^\dagger) &= \frac{d^n}{dt^n} e^{2ta-t^2} \Big|_{t=0} \frac{d^m}{d\tau^m} e^{2\tau a^\dagger - \tau^2} \Big|_{\tau=0} \\
 &= \frac{d^n d^m}{dt^n d\tau^m} : e^{-t^2 - \tau^2 + 2ta + 2\tau a^\dagger + 4t\tau} : \Big|_{t=\tau=0} \\
 &= : \frac{d^n}{dt^n} [e^{-t^2 + 2ta} H_m(2t + a^\dagger)] : \Big|_{t=0} \\
 &= : \sum_{l=0}^n \binom{n}{l} \frac{d^{n-l}}{dt^{n-l}} e^{-t^2 + 2ta} \frac{d^l}{dt^l} H_m(2t + a^\dagger) \Big|_{t=0} :
 \end{aligned}$$

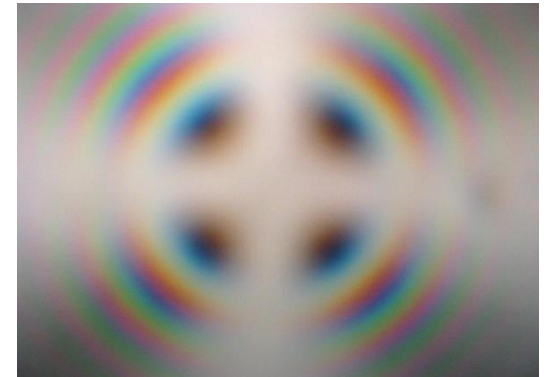
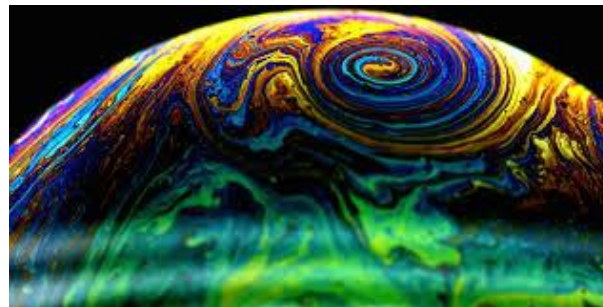
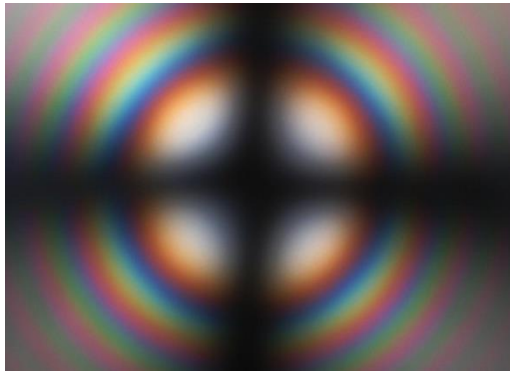


$$G^{(2)}(0) = \langle 1, 1 | \hat{E}_1^\dagger \hat{E}_2^\dagger \hat{E}_1 \hat{E}_2 | 1, 1 \rangle = 0$$





cycle « Lumière et couleurs »



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