MyLib-C

A Small Collection of Basic Utilities in C

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This document describes a set of basic utility functions implemented in the C language around the years 1995–2000, to be used in the software developed in the *Stochastic Simulation Laboratory* under the supervision of Pierre L'Ecuyer. Many of these tools were originally implemented earlier in the Modula-2 language, and have been reimplemented in C to facilitate the code translation of old software from Modula-2 to C. Some of these functions may have counterparts in the more recent standard C libraries, but we kept them to avoid rewriting our code. They are used in particular in the TestU01 and F2linearUnif libraries.

Contents

gdef

Platform-dependent options are defined here. These options are used by other modules to decide when platform-dependent functions must be commented out or not. Most of these options are set to their true values by the program *configure* in the installation process. The user may choose to set some of them manually. This module also contains a function that prints the current host name.

─────────────────── **Global macros** ───────────────────

```
#define FALSE 0
#define TRUE 1

typedef int lebool;
```

Defines the boolean type `lebool`, whose only possible values are `TRUE` and `FALSE`.

```
#undef USE_ANSI_CLOCK
```

The recommendation is to leave this undefined. $\boxed{1}$ On Linux/Unix platforms, if the macro `USE_ANSI_CLOCK` is defined, the timers will call the ANSI C `clock` function. However, on systems where the type `clock_t` is a 32-bit `long`, the time returned will wrap around to negative values after about 36 minutes. When the macro `USE_ANSI_CLOCK` is undefined, the module `chrono` gets the CPU time used by a program via an alternate non-ANSI C timer based on the POSIX (The Portable Operating System Interface) function `times`, assuming this function is available. The POSIX standard is described in the IEEE Std 1003.1-2001 document (see The Open Group web site at `http://www.opengroup.org/onlinepubs/007904975/toc.htm`).

On Windows platforms, we use the MS-Windows function `GetProcessTimes` to measure the CPU time used by programs (in module `chrono`).

```
#define DIR_SEPARATOR "/"
```

Used to separate directories in the pathname of a file. It is "/" on Unix-Linux and most other platforms. It may have to be set to "\\" on some platforms.

```
#undef USE_GMP
```

Define this macro if the GNU multi-precision package GMP is available. GMP is a portable library written in C for arbitrary precision arithmetic on integers, rational numbers, and floating-point numbers. See the Free Software Foundation web site at `http://www.gnu.org/software/gmp/manual`. A few random number generators in library TestU01 use arbitrary large integers, and they have been implemented with GMP functions. If one wants to use GMP, the GMP header file (`gmp.h`) must be in the search path of the C compiler for included files, and the GMP library must be linked to create executable programs.

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[1]From Pierre: Deprecated. Perhaps it should be removed altogether, or at least hidden.

```
void gdef_GetHostName (char machine[], int n);
```

Returns in `machine` the host name. Will copy at most n characters, so the array `machine[]` should have a size $\geq n$. This is useful, for example, to get the name of the machine on which a program is running.

```
void gdef_WriteHostName (void);
```

Prints the name of the machine on which a program is running. This should work on any Unix or Linux machine.

util

This module offers macros and functions used for testing, print error messages, allocate dynamic memory, and read/write Boolean variables. Some of these "functions" are implemented as macros, for better speed. The module also contains safe prototype functions to open and close files. [2]

```
#include "gdef.h"
#include <stdio.h>
#include <stdlib.h>
```

---------------------------------- **Macros** ----------------------------------

`util_Error (s);`

    Print the string `s`, then stop the program.

`util_Assert (Assertion, s);`

    If `lebool Assertion` is `FALSE` $(= 0)$, this macro prints the string `s` and stops the program.

`util_Warning (Condition, s);`

    If `lebool Condition` is `TRUE` $(\neq 0)$, this macro prints the string `s`.

`util_Max (x, y);`

    Returns the largest of the two numbers `x`, `y`.

`util_Min (x, y);`

    Returns the smallest of the two numbers `x`, `y`.

---------------------------------- **Prototypes** ----------------------------------

`FILE * util_Fopen (const char *name, const char *mode);`

    Calls `fopen` (from `stdio.h`) with the same arguments, but checks for errors. Opens or creates file with name `name` in mode `mode`. Returns a pointer to FILE that is associated with the stream. If `name` cannot be accessed, the program stops.

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[2]From Pierre: I know that in C, function names should normally be in all lowercase, but the names here use some uppercase letters for historical reasons (many functions were adapted from Modula-2 to C in the 1990's), and I think it is fine like this.

```
int util_Fclose (FILE *stream);
```

Calls `fclose` (from `stdio.h`) with the same arguments, but checks for errors. Closes the file associated with `stream`. If the file is successfully closed, `0` is returned. If an error occurs or the file was already closed, `EOF` is returned.

```
int util_GetLine (FILE *file, char *Line, char c);
```

Reads a line of data from `file`. Blank lines and comments are ignored. A comment is any line whose first non-whitespace character is `c`. If the character `c` appears anywhere on a line that is not a comment, then `c` and the rest of the line are ignored too. The function returns -1 if end-of-file or an error is encountered, otherwise it returns 0.

```
void util_ReadBool (char S[], lebool *x);
```

Reads a `lebool` value from string `S` and returns it in x. The possible values are `TRUE` and `FALSE`.

```
void util_WriteBool (lebool x, int d);
```

Writes the value of x in a field of width d. If $d < 0$, x is left-justified, otherwise right-justified.

```
void * util_Malloc (size_t size);
```

Calls `malloc` (from `stdlib.h`) with same arguments, but checks for errors. Allocates memory large enough to hold an object of size `size`. A successful call returns the base address of the allocated space, otherwise the programs stops. The standard type `size_t` is defined in `stdio.h`.

```
void * util_Calloc (size_t dim, size_t size);
```

Calls `calloc` (from `stdlib.h`) with same arguments, but checks for errors. Allocates memory large enough to hold an array of `dim` objects each of size `size`. A successful call returns the base address of the allocated space, otherwise the programs stops. The standard type `size_t` is defined in `stdio.h`.

```
void * util_Realloc (void *ptr, size_t size);
```

Calls `realloc` (from `stdlib.h`) with same arguments, but checks for errors. Takes a pointer to a memory region previously allocated and referenced by `ptr`, then changes its size to `size` while preserving its content. A successful call returns the base address of the resized (or new) space, otherwise the programs stops. The standard type `size_t` is defined in `stdio.h`.

```
void * util_Free (void *p);
```

Calls `free (p)` (from `stdlib.h`) to free memory allocated by util_Malloc, util_Calloc or util_Realloc. Always returns a `NULL` pointer.

num

This module provides some useful constants and basic tools to manipulate numbers represented in different forms.

```
#include "gdef.h"
```

──────────────────────── **Constants** ────────────────────────

```
#define num_Pi     3.14159265358979323846
```

   The number π.

```
#define num_ebase  2.71828182845904523543
```

   The Euler number e.

```
#define num_Rac2    1.41421356237309504880
```

   $\sqrt{2}$, the square root of 2.

```
#define num_1Rac2   0.70710678118654752440
```

   $1/\sqrt{2}$.

```
#define num_Ln2      0.69314718055994530941
```

   ln(2), the natural logarithm of 2.

```
#define num_1Ln2     1.44269504088896340737
```

   $1/\ln(2)$.

```
#define num_MaxIntDouble     9007199254740992.0
```

   Largest integer $n_0 = 2^{53}$ such that all integers $n \le n_0$ are represented exactly as a `double`.

──────────────────────── **Precomputed powers** ────────────────────────

```
#define num_MaxTwoExp     64
```

   Powers of 2 up to `num_MaxTwoExp` are stored exactly in the array `num_TwoExp`.

```
extern double num_TwoExp[];
```

   Contains precomputed powers of 2. One has `num_TwoExp[i]` $= 2^i$ for $0 \le i \le$ `num_MaxTwoExp`.

```
#define num_MAXTENNEGPOW     16
```

   Negative powers of 10 up to `num_MAXTENNEGPOW` are stored in the array `num_TENNEGPOW`.

```
extern double num_TENNEGPOW[];
```

Contains the precomputed negative powers of 10. One has `TENNEGPOW[j]`$= 10^{-j}$, for $j = 0, \ldots,$ `num_MAXTENNEGPOW`.

-- **Prototypes** --

```
#define num_Log2(x) (num_1Ln2 * log(x))
```

Gives the logarithm of x in base 2.

```
int64_t num_Round64 (double x);
```

Rounds x to the nearest (`int64_t`) integer and returns it. [3]

```
double num_RoundD (double x);
```

Rounds x to the nearest (`double`) integer and returns it.

```
int num_IsNumber (char S[]);
```

Returns `1` if the string `S` begins with a number (with the possibility of spaces and a $+/-$ sign before the number). For example, " $+ 2$" and "4hello" return `1`, while "$- +2$" and "hello" return `0`.

```
void num_IntToStrBase (int64_t k, int b, char S[]);
```

Returns in `S` the string representation of `k` in base `b`. [4]

```
void num_Uint2Uchar (unsigned char output[], uint64_t input[], int L);
```

Transforms the L 64-bit unsigned integers contained in `input` into $8L$ characters and puts them into `output`. The order is such that the 8 most significant bits of `input[0]` will be in `output[0]`, the 8 least significant bits of `input[0]` will be in `output[7]`, and the 8 least significant bits of `input[L-1]` will be in `output[8L-1]`. Array `output` must have at least $8L$ elements. [5]

```
void num_WriteD (double x, int i, int j, int k);
```

Writes `x` to current output. Uses a total of at least `i` positions (including the sign and point when they appear), `j` digits after the decimal point and at least `k` significant digits. The number is rounded if necessary. If there is not enough space to print the number in decimal notation with

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[3]From Pierre: Changed from `long` to `int64_t`. Some of these might be defined as macros!
[4]From Pierre: Changes from `long`...
[5]From Pierre: Change `unsigned int` to `uint64_t`.

at least `k` significant digits (`j` or `i` is too small), it will be printed in scientific notation with at least `k` significant digits. In that case, `i` is increased if necessary. Restriction: `j` and `k` must be strictly smaller than `i`.

`void num_WriteBits (uint64_t x, int k);`

Writes `x` in base 2 in a field of at least $\max\{64, |k|\}$ positions. If $k > 0$, the number will be right-justified, otherwise left-justified.

`int64_t num_MultMod (int64_t a, int64_t s, int64_t c, int64_t m);`

Returns $(as+c) \mod m$. Uses the decomposition technique of [4] to avoid overflow. Assumptions: $\max(a, s, c) < m < 2^{63}$.

`int64_t num_MultModDirect (int64_t a, int64_t s, int64_t c, int64_t m);`

Returns $(as + c) \mod m$. Uses direct multiplication and addition. Assumptions: $m < 2^{63}$ and $as + c < 2^{63}$.

`double num_MultModDouble (double a, double s, double c, double m);`

Returns $(as+c) \mod m$, assuming that a, s, c, and m are all *integers* less than 2^{35} (represented exactly). Works under the assumption that all positive integers less than 2^{53} are represented exactly in floating-point (in `double`).

`int64_t num_InvEuclid (int64_t m, int64_t x);`

This function computes the inverse $z^{-1} \mod m$ by the modified Euclid algorithm (see [3, p. 325]) and returns the result. If the inverse does not exist, returns 0. This function can handle higher values than num_InvEuclid.

`long num_InvEuclid32 (long m, long z);`

Same as num_InvEuclid, but for 32-bit integers. [6]

`uint64_t num_InvExpon (int e, uint64_t z);`

This function computes the inverse $z^{-1} \mod 2^e$ by exponentiation and returns the result. If the inverse does not exist, returns 0. Restriction: $e \leq 64$.

`long num_InvExpon32 (int e, long Z);`

Same as num_InvExpon, but for 32-bit integers. Restriction: $e \leq 32$. [7]

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[6]From Pierre: Needed?

[7]From Pierre: Needed? We can at least hide them from the doc.

8

num2

This module provides procedures to compute certain numerical quantities such as factorials, combinations, Stirling numbers, Bessel functions, gamma functions, and so on. These functions are more involved than those provided by `num`.

```
#include "gdef.h"
#include <math.h>
```

Prototypes

```
double num2_Factorial (int n);
```

The factorial function. Returns the value of $n!$

```
double num2_LnFactorial (int n);
```

Returns the value of $\ln(n!)$, the natural logarithm of the factorial of n. Gives at least 16 decimal digits of precision (relative error $< 0.5 \times 10^{-15}$)

```
double num2_Combination (int n, int s);
```

Returns the value of $\binom{n}{s}$, the number of different combinations of s objects amongst n.

```
#ifdef HAVE_LGAMMA
#define num2_LnGamma lgamma
#else
   double num2_LnGamma (double x);
#endif
```

Calculates the natural logarithm of the gamma function $\Gamma(x)$ at `x`. Our `num2_LnGamma` gives 16 decimal digits of precision, but is implemented only for $x > 0$. The function `lgamma` is from the `ISO C99` standard math library.

```
double num2_Digamma (double x);
```

Returns the value of the logarithmic derivative of the Gamma function $\psi(x) = \Gamma'(x)/\Gamma(x)$.

```
#ifdef HAVE_LOG1P
#define num2_log1p log1p
#else
   double num2_log1p (double x);
#endif
```

Returns an approximation of `log(1 + x)` which is accurate for small x. The function `log1p` is from the `ISO C99` standard math library.

```
void num2_CalcMatStirling (double *** M, int m, int n);
```

Calculates the Stirling numbers of the second kind and returns them in matrix M with

$$M[i,j] = \left\{ \begin{array}{c} j \\ i \end{array} \right\} \quad \text{for } 0 \le i \le m \text{ and } 0 \le i \le j \le n. \tag{1}$$

See [2], Section 1.2.6. Our matrix M is the transpose of that in [2]. This procedure allocates memory for the two-dimensional matrix M, and fills it with the values of Stirling numbers; the memory should be released later by invoking num2_FreeMatStirling.

```
void num2_FreeMatStirling (double *** M, int m);
```

Frees the memory space used by the Stirling matrix created by calling num2_CalcMatStirling. The parameter m must be the same as the m in num2_CalcMatStirling.

```
double num2_VolumeSphere (double p, int t);
```

Calculates the volume V of a sphere of radius 1 in t dimensions using the norm L_p, according to the formula
$$V = \frac{[2\Gamma(1 + 1/p)]^t}{\Gamma(1 + t/p)}, \qquad p > 0,$$
where Γ is the well-known gamma function. The case of the sup norm L_∞ is obtained by choosing $p = 0$. Restrictions: $p \ge 0$ and $t \ge 1$.

```
double num2_EvalCheby (const double a[], int n, double x);
```

Evaluates a series of Chebyshev polynomials T_j, at point $x \in [-1,\ 1]$, using the method of Clenshaw [1], i.e. calculates and returns

$$y = \frac{a_0}{2} + \sum_{j=1}^{n} a_j T_j(x),$$

where $a_0, \ldots, a_n$ are given in array a[0..n].

```
double num2_BesselK025 (double x);
```

Returns the value of $K_{1/4}(x)$, where K_ν is the modified Bessel's function of the second kind. The relative error on the returned value is less than 0.5×10^{-6} for $x > 10^{-300}$.

mystr

This module offers some tools for the manipulation of character strings.

`void mystr_Delete (char S[], unsigned int index, unsigned int len);`

Deletes `len` characters from S, starting at position `index`.

`void mystr_Insert (char Res[], char Source[], unsigned int Pos);`

Inserts the string `Source` into `Res`, starting at position `Pos`.

`void mystr_ItemS (char R[], char S[], const char T[], unsigned int N);`

Returns in R the N-th substring of S (counting from 0). Substrings are delimited by any character from the set T.

`int mystr_Match (char Source[], char Pattern[]);`

Returns `1` if the string `Source` matches the string `Pattern`, and `0` otherwise. The characters "?" and "*" are recognized as wild characters in the string `Pattern`.

`void mystr_Slice (char R[], char S[], unsigned int P, unsigned int L);`

Returns in `R` the substring in `S` beginning at position `P` and of length `L`.

`void mystr_Subst (char Source[], char OldPattern[], char NewPattern[]);`

Searches for the string `OldPattern` in the string `Source`, and replaces its first occurence with `NewPattern`.

`void mystr_Position (char Substring[], char Source[], unsigned int at,`
`                     unsigned int * pos, int * found);`

Searches for the string `Substring` in the string `Source`, starting at position `at`, and returns the position of its first occurence in `pos`.

addstr

The functions described here are convenient tools for constructing character strings that contain a series of numeric parameters, with their values. For example, suppose one wishes to put "LCG with m = 101, a = 12, s = 1" in the string `str`, where the actual numbers 101, 12, and 1 must be taken as the values of `uint64_t` variables `m`, `a`, and `s`. This can be achieved by the instructions:

```
strcpy (str, "LCG with ");
addstr_uint64 (str, " m = ", m);
addstr_uint64 (str, ", a = ", m);
addstr_uint64 (str, ", s = ", s);
```

Each function `addstr_...  (char *to, const char *add, ...)` first appends the string `add` to the string `to`, then appends to it a character string representation of the number (or array of numbers) specified by its last parameter. In the case of an array of numbers (e.g., `addstr_array_uint64`), the parameter `high` specifies the size of the array, and the elements `[0..high-1]` are added to `str`. The `..._int64` and `..._uint64` versions are for 64-bit integers. In all cases, the string `to` should be large enough to accomodate what is appended.

```
#include "gdef.h"
```

Prototypes

```
void  addstr_int (char *to, const char *add, int n);

void  addstr_uint (char *to, const char *add, unsigned int n);

void  addstr_long (char *to, const char *add, long n);

void  addstr_ulong (char *to, const char *add, unsigned long n);

void  addstr_int64 (char *to, const char *add, int64_t n);

void  addstr_uint64 (char *to, const char *add, uint64_t n);

void  addstr_double (char *to, const char *add, double x);

void  addstr_char (char *to, const char *add, char c);

void  addstr_bool (char *to, const char *add, int b);
```

```
void  addstr_array_int (char *to, const char *add, int high, int []);

void  addstr_array_uint (char *to, const char *add, int high,
                         unsigned int []);

void  addstr_array_long (char *to, const char *add, int high, long []);

void  addstr_array_ulong (char *to, const char *add, int high,
                          unsigned long []);

void  addstr_array_int64 (char *to, const char *add, int high, int64_t []);

void  addstr_array_uint64 (char *to, const char *add, int high, uint64_t[]);

void  addstr_array_double (char *to, const char *add, int high, double []);

void  addstr_array_char (char *to, const char *add, int high, char []);
```

tables

This module provides an implementation of variable-sized arrays (matrices), and procedures to manipulate them. The advantage is that the size of the array needs not be known at compile time; it can be specified only during the program execution. There are also procedures to sort arrays, to print arrays in different formats, and a few tools for hashing tables. The functions `tables_CreateMatrix...` and `tables_DeleteMatrix...` manage memory allocation for these dynamic matrices.

As an illustration, the following piece of code declares and creates a 100×500 table of floating point numbers, assigns a value to one table entry, and eventually deletes the table:

```
double ** T;
T = tables_CreateMatrix_double (100, 500);
T[3][7] = 1.234;
...
tables_DeleteMatrix_double (&T);
```

```
#include "gdef.h"
```

--------------------------- **Printing styles** ---------------------------

```
typedef enum {
   tables_Plain,
   tables_Mathematica,
   tables_Matlab
   } tables_StyleType;
```

Printing styles for matrices.

--------------- **Functions to create, delete, sort, and print tables** ---------------

```
long ** tables_CreateMatrix_long  (int m, int n);
unsigned long ** tables_CreateMatrix_ulong (int m, int n);
int64_t ** tables_CreateMatrix_int64  (int m, int n);
uint64_t long ** tables_CreateMatrix_uint64 (int m, int n);
double ** tables_CreateMatrix_double  (int m, int n);
```

Allocates contiguous memory for a dynamic matrix of m rows and n columns. Returns the base address of the allocated space.

```
void tables_DeleteMatrix_long  (long *** mat);
void tables_DeleteMatrix_ulong (unsigned long *** mat);
void tables_DeleteMatrix_int64  (int64_t *** mat);
void tables_DeleteMatrix_uint64 (uint64_t *** mat);
void tables_DeleteMatrix_double  (double *** mat);
```

Releases the memory used by the matrix mat (see `tables_CreateMatrix`) passed by reference;

i.e., using the `&` symbol. Then, `mat` is set to `NULL`.

```
void tables_CopyTab_long (long mat1[], long mat2[], int n1, int n2);
void tables_CopyTab_int64 (long mat1[], long mat2[], int n1, int n2);
void tables_CopyTab_uint64 (long mat1[], long mat2[], int n1, int n2);
void tables_CopyTab_double (double mat1[], double mat2[], int n1, int n2);
```

Copies `mat1[n1..n2]` in `mat2[n1..n2]`. [8]

```
void tables_QuickSort_long (long mat[], int n1, int n2);
void tables_QuickSort_int64 (int64_t mat[], int n1, int n2);
void tables_QuickSort_uint64 (uint64_t mat[], int n1, int n2);
void tables_QuickSort_double (double mat[], int n1, int n2);
```

Sort the tables `mat[n1..n2]` in increasing order.

```
void tables_WriteTab_long (long mat[], int n1, int n2, int k, int p,
                           char desc[]);
void tables_WriteTab_int64 (int64_t mat[], int n1, int n2, int k, int p,
                            char desc[]);
void tables_WriteTab_uint64 (uint64_t mat[], int n1, int n2, int k, int p,
                             char desc[]);
```

Write the elements `n1` to `n2` of table `mat`, `k` per line, `p` positions per element. If `k = 1`, the index will also be printed. `desc` contains a description of the table.

```
void tables_WriteTab_double (double mat[], int n1, int n2, int k,
                             int p1, int p2, int p3, char desc[]);
```

Writes the elements `n1` to `n2` of table `mat`, `k` per line, with at least `p1` positions per element, `p2` digits after the decimal point, and at least `p3` significant digits. If `k = 1`, the index will also be printed. `desc` contains a description of the table.

```
void tables_WriteSubmatrix_double (double** mat, int i1, int i2, int j1, int j2,
                                   int w, int p, tables_StyleType style, char name[]);
```

Writes the submatrix with lines `i1 ≤ i ≤ i2` and columns `j1 ≤ j ≤ j2` of the matrix `mat` with format `style`. The elements are printed in `w` positions with a precision of `p` digits. `name` is an identifier for the submatrix.

For `Matlab`, the file containing the printed submatrix should have the extension `.m`. For example, if it is named `poil.m`, it will be accessed by the simple call `poil` in `Matlab`. For `Mathematica`, if the file is named `poil`, it will be read using `<< poil;`.

```
void tables_WriteSubmatrix_long (long** mat, int i1, int i2, int j1, int j2,
                                 int w, tables_StyleType style, char name[]);
void tables_WriteSubmatrix_int64 (int64** mat, int i1, int i2, int j1, int j2,
                                  int w, tables_StyleType style, char name[]);
void tables_WriteSubmatrix_uint64 (uint64** mat, int i1, int i2, int j1, int j2,
                                   int w, tables_StyleType style, char name[]);
```

Similar to `tables_WriteMatrix_double`.

---

[8]From Pierre: Oups... I think in C, the copy order is usually the other way! Check this.

```
int64_t tables_HashPrime (int64_t n, double load);
```

Returns a prime number p to be used as the size (the number of elements) of a hashing table. p will be such that the load factor n/p do not exceed `load`. If `load` is small, an important part of the table will be unused; that will accelerate searches and insertions. This function uses a small sequence of prime numbers; the real load factor may be significantly smaller than `load` because only a limited number of prime numbers are in the table. In case of failure, returns -1.

```
long tables_HashPrime32 (long n, double load);
```

Same as `tables_HashPrime`, but with 32-bit integers.

bitset

This module defines sets of bits and useful operations for such sets. Some of these operations are implemented as macros. Each bit set is stored as a 64-bit unsigned integer, whose bits are simply interpreted as indicators of which elements belong to the set. The bits are numbered from 0 to 63, and *bit 0 is the least significant bit* of this word, which means that the bits are numbered from right to left. If bit j is 1, then element j is a member of the set, otherwise it is not. Other operations not described here can also be applied directly to the `uint64_t` variable.

---------- **Constants** ----------

```
const uint64_t bitset_ONE = 1;
const uint64_t bitset_ALLONES = 18446744073709551615;
```

The two constants 1 and $2^{64} - 1$ (a bitset with all ones).

---------- **Types** ----------

```
typedef uint64_t bitset_BitSet;
```

A set of bits. The bits are numbered starting from 0 for the least significant bit.

---------- **Macros** ----------

```
#define bitset_Mask1(b) (bitset_ONE << b)
```

Gives a bit set with only bit b set to 1 and all other bits set to 0.

```
#define bitset_MaskLow(b) (bitset_ALLONES >> (64-b))
```

Gives a bit set with all *the lowest (rightmost) b bits* set to 1 and all other bits set to 0.

```
#define bitset_SetBit(s, b) ((s) |= (bitset_Mask1(b)));
```

Sets bit `b` in set `s` to 1.

```
#define bitset_ClearBit(s, b) ((s) &=  (bitset_Mask1(b)))
```

Sets bit `b` in set `s` to 0.

```
#define bitset_FlipBit(s, b) ((s) ^= (bitset_Mask1(b)))
```

Flips bit `b` in set `s`; thus, $0 \rightarrow 1$ and $1 \rightarrow 0$.

```
#define bitset_GetBit(s, b)  ((s) & (bitset_Mask1(b)) ? 1 : 0)
```

Returns the value of bit `b` in set `s` (0 or 1).

```
#define bitset_RotateLeft(s, r)  ((s << r) | (s >> (64 - r)))
```

Rotates the bit set `s` by `r` positions to the left.

```
#define bitset_RotateRight(s, r)  ((s >> r) | (s << (64 - r)))
```

Rotates the bit set `s` by `r` positions to the right.

```
#define bitset_RotateLeftLocal(s, b, r) ...
```

Rotates the `b` lowest (least significant) bits of the set `s` by `r` positions to the left. Here, `s` is considered as a `b`-bit number kept in the least significant bits of `s`.

```
#define bitset_RotateRightLocal(s, b, r) ...
```

Rotates the `b` lowest (least significant) bits of the set `s` by `r` positions to the right. Here, `s` is considered as a `b`-bit number kept in the least significant bits of `s`.

——————————————————— **Prototypes** ———————————————————

```
bitset_BitSet bitset_ReverseOrder (bitset_BitSet z, int b);
```

Reverses the order of the `b` least significant bits of `z`. Thus, if `b = 4` and `z = ...0011`, the returned value is ...1100. [9]

```
void bitset_Write (char *desc, bitset_BitSet z, int b);
```

[10] Prints the string `desc` (which may be empty), then writes the `b` least significant bits of `z` considered as an unsigned binary number. This corresponds to the `b` first elements of `z`.

---

[9]From Pierre: The current implementation of this function is simple and very inefficient. More efficient methods use lookup tables. See `https://graphics.stanford.edu/~seander/bithacks.html`. I think this is implemented somewhere in TestU01.

[10]From Pierre: Should return the string, not print it. Then we can do whatever we want with the string.

bitvector

This module offers facilities to store and manipulate bit vectors of arbitrary length. The bit vectors are stored in arrays of 64-bit unsigned integers, and their length is always rounded up to the nearest multiple of 64. The bit indexation goes from left to right (which is unusual) and starts at 0. This left-to-right ordering is because these vectors are used to construct binary matrices (see `bitmatrix`), for which the elements are usually ordered from left to right. If the required length is not a multiple of 64, the unused bits are simply set to 0. [11]

```
#include "gdef.h"

typedef struct{
    int n;
    uint64_t *vect;
} bitvector_vector;
```

This structure contains a bit vector of 64n bits, stored in **n** blocks of 64 bits. Storage space for the `bitvector_vector` should be allocated via `bitvector_allocate()`.

`void bitvector_allocate (bitvector_vector *v, int b);`

Allocates memory for a bit vector of **b** bits. There will be $n = \lceil b/64 \rceil$ blocks of 64 bits in the structure and the value of b is not saved. [12]

`void bitvector_free (bitvector_vector *v);`

Releases the memory space used by `bitvector_vector` pointed by **v**.

`void bitvector_canonical (bitvector_vector *v, int t);`

Sets **v** to the $(\mathtt{t}+1)$-th unit vector, with a 1 in position t. That is, for `t = 0`, we get te first unit vector $\mathbf{e}_1 = (1, 0, 0, \dots)$.

`void bitvector_setAllOnes (bitvector_vector *v);`

Sets **v** to the bit vector $(1, 1, 1, 1, \dots, 1)$.

`void bitvector_setMaskLow (bitvector_vector *v, int t);`

Fills **v** with **t** ones followed by zeros.

`void bitvector_setInvMaskLow (bitvector_vector *v, int t);`

Fills **v** with **t** zeros followed by ones.

`void bitvector_setBit (bitvector_vector *v, int b);`

Sets bit **b** of **v** to 1.

---

[11]From Pierre: We may add functions to compute the Hamming weight (number of ones) and perhaps other tools commonly available for bit vectors.

[12]From Pierre: We may want to save it if needed, later.

```
void bitvector_clearBit (bitvector_vector *v, int b);
```

   Sets bit `b` of `v` to 0.

```
void bitvector_clearVector (bitvector_vector *v);
```

   Resets all the bits of `v` to zero.

```
int bitvector_getGit (bitvector_vector *v, int b);
```

   Returns the value of the `b`-th bit of `v`.

```
lebool bitvector_isZero (bitvector_vector *v);
```

   Returns `TRUE` if `v` is the zero vector. Returns `FALSE` otherwise.

```
lebool bitvector_areEqual (bitvector_vector *v1, bitvector_vector *v2);
```

   Returns `TRUE` if the bit vectors `v1` and `v2` are the same, and `FALSE` otherwise.

```
lebool bitvector_haveCommonBit (bitvector_vector *v1, bitvector_vector *v2);
```

   Returns `TRUE` if at least one bit set to 1 in `ds1` is also set to 1 in `ds2` (they have at least one
   common bit). Returns `FALSE` otherwise.

```
void bitvector_copy (bitvector_vector *v1, bitvector_vector *v2);
```

   Copies the entire contents of `v2` into `v1`.

```
void bitvector_copyPart (bitvector_vector *v1, bitvector_vector *v2, int b);
```

   Copies the lowest `b` bits of `v2` into `v1`.

```
void bitvector_xor (bitvector_vector *v1, bitvector_vector *v2, bitvector_vector
*v3);
```

   Performs a bitwise exclusive-or of the contents of `v2` and `v3`, and puts the result in `v1`.

```
void bitvector_xor3 (bitvector_vector *v1, bitvector_vector *v2,
                     bitvector_vector *v3, bitvector_vector *v4);
```

   Performs a bitwise exclusive-or of the contents of `v2`, `v3`, and `v4`, and puts the result in `v1`.

```
void bitvector_and (bitvector_vector *v1, bitvector_vector *v2, bitvector_vector
*v3);
```

   Performs a bitwise "and" of the contents of `v2` and `v3`, and puts the result in `v1`.

```
void bitvector_andSelf (bitvector_vector *v1, bitvector_vector *v2);
```

   Performs a bitwise "and" of the contents of `v1` and `v2`, and puts the result in `v1`.

```
void bitvector_andMaskLow (bitvector_vector *v1, bitvector_vector *v2, int t);
```

Applies the mask comprised of `t` ones followed by zeros to the bit vector `v2` and puts the result in `v1`.

```
void bitvector_andInvMaskLow (bitvector_vector *v1, bitvector_vector *v2, int t);
```

Applies the mask comprised of `t` zeros followed by ones to the bit vector `v2` and puts the result in `v1`.

```
void bitvector_xorSelf (bitvector_vector *v1, bitvector_vector *v2);
```

Performs a bitwise exclusive-or of the contents of `v1` and `v2`, and puts the result in `v1`.

```
void bitvector_leftShift (bitvector_vector *v1, bitvector_vector *v2, int b);
```

Performs a left shift of `v2` by `b` bits and puts the result in `v1`.

```
void bitvector_rightShift (bitvector_vector *v1, bitvector_vector *v2, int b);
```

Performs a right shift of `v2` by `b` bits and puts the result in `v1`.

```
void bitvector_leftShiftSelf (bitvector_vector *v, int b);
```

Performs a left shift of `v` by `b` bits and puts the result in `v`.

```
void bitvector_leftShift1Self (bitvector_vector *v);
```

Performs a left shift of `v` by one bit and puts the result in `v`.

```
void bitvector_rightShiftSelf (bitvector_vector *v, int b);
```

Performs a right shift of `v` by `b` bits and puts the result in `v`.

```
void bitvector_flip (bitvector_vector *v);
```

Flips (or toggle) the values of all the bits of `v` (exchange 0 for 1, and vice-versa).

```
string bitvector_display (bitvector_vector *v, int b);
```

Returns a character string that contains the first `b` bits of the bit vector `v`.

```
void bitvector_displayMathematica (bitvector_vector *b, int v);
```

Returns a character string that contains the first `b` bits of the bit vector `v`, in a format compatible for Mathematica input. [13]

```
void bitvector_fillRandomBits (bitvector_vector *v);
```

Fills the vector `v` with random bits. [14]

---

[13]From Pierre: Needed?

[14]From Pierre: We need to provide a local implementation of this!!! To be done later.

Other popular implementations of bit vectors:

Simple tools for bit vectors in C: `http://c-faq.com/misc/bitsets.html`. Bits are counted from the left, starting at 0, as far as I understand.

Another nice set of macros in C: `https://github.com/iplinux/x11proto-trap/blob/master/xtrapbits.h`

In `https://www.gnu.org/software/guile/docs/docs-1.8/guile-ref/Bit-Vectors.html`, bits are counted from left to right, starting at 0. Different operations are available, such as Hamming weight of bit string.

See `https://en.wikipedia.org/wiki/Bit_array` for bit vectors in various languages. In `LatNet Builder` we use `dynamic_bitset`, available in the Boost C++ library: `https://www.boost.org/doc/libs/1\_73\_0/libs/dynamic\_bitset/dynamic\_bitset.html`.

In the dynamic bitsets of Boost, we find the following: "Each bit represents either the Boolean value true or false (1 or 0). To set a bit is to assign it 1. To clear or reset a bit is to assign it 0. To flip a bit is to change the value to 1 if it was 0 and to 0 if it was 1. Each bit has a non-negative position. A bitset x contains x.size() bits, with each bit assigned a unique position in the range [0,x.size()). The bit at position 0 is called the least significant bit and the bit at position size() - 1 is the most significant bit. When converting an instance of dynamic_bitset to or from an unsigned long n, the bit at position i of the bitset has the same value as `(n >> i) & 1`."

bitmatrix

This module offers facilities to manipulate matrices of binary vectors (from the module `bitvector`). More specifically, each matrix has `r` rows and `t` columns, and each entry is an `b`-bit binary vector. By taking `t=1`, we get an ordinary binary matrix of `r` rows and `b` columns of bits. The more general for with `t > 1` is very convenient for the analysis of equidistribution properties of $\mathbb{F}_2$-linear random number generators [5, 6, 7].

```
#include "gdef.h"
#include "bitvector.h"

typedef struct{
  bitvector_vector **rows;
  int r;
  int b;
  int t;
} bitmatrix_matrix;
```

This structure represents a matrix of `r` rows and `t` columns, for which each entry is an `b`-bit binary vector. This gives a matrix with `r` rows of `t` × `b` bits each. The variable `rows` contains an array of `r` arrays of `t` `b`-bit vectors. Storage space for this array should be allocated via `bitmatrix_allocate()`. Note that the number `b` is not stored in the binary vectors, but it is stored here. [15]

```
void bitmatrix_allocate (bitmatrix_matrix* m, int r, int b, int t);
```

Allocates space for a `bitmatrix_matrix` with `r` rows and `t` columns, for which each entry is an `b`-bit binary vector. On each row, the function allocates space for `t` bit vectors of `b` bits each. To allocate a simple 128 × 128 binary matrix, for example, one can invoke `bitmatrix_allocate (m, 128, 128, 1)`.

```
void bitmatrix_free (bitmatrix_matrix *m);
```

Releases the space taken by the binary matrix `m`.

```
void bitmatrix_copypart (bitmatrix_matrix *m1, bitmatrix_matrix *m2,
                         int r, int t);
```

Copies the first `t` bit vectors of the first `r` rows of `m2` into the first `t` bit vectors of the first `r` rows of `m1`.

```
void bitmatrix_copySpecial (bitmatrix_matrix *m1, bitmatrix_matrix *m2,
                            int nl, int *col, int t);
```

Copies the (`t`-1) bit vectors indicated by the array `col`, plus the first bit vector, on each of the `nl` first rows of the matrix `m2` to the first `t` bit vectors on each of the first `nl` rows of the matrix `m1`. [16]

---

[15]From Pierre: The order of arguments was not the same here as in the allocate, so I changed it here. Beware!

[16]From Pierre: Seems very specialized. Why is this useful?

```
lebool bitmatrix_diagonalize (bitmatrix_matrix *m, int kg, int t, int l, int *gr);
```

Diagonalizes the sub matrix of `m` that consist of the first `kg` rows and the first `l` bits of the first `t` bit vectors on each row. Returns `TRUE` if the sub matrix is of full rank `t*l`. In this case, the variable pointed by `gr` remains unchanged. Otherwise, returns FALSE and the variable pointed by `gr` is changed to the value of `t` for which the function would have returned `TRUE`.

```
int bitmatrix_gaussianElimination (bitmatrix_matrix *m, int r, int l, int t);
```

Returns the rank of the submatrix of `m` comprised of the first `r` rows and the first `l` bits of the first `t` bit vectors on each row.

```
int bitmatrix_completeElimination (bitmatrix_matrix *m, int r, int l, int t);
```

This function tries to form an identity matrix by elimination. It returns the rank of the submatrix of `m` comprised of the first `r` rows and the first `l` bits of the first `t` bit vectors on each row.

```
int bitmatrix_specialGaussianElimination (bitmatrix_matrix *m,
                                           int r, int l, int t, int *indices);
```

Returns the rank of the submatrix of `m` formed by the first `r` rows and the first `l` bits of the bit vectors indicated by the array `indices`.

```
void bitmatrix_productByVector (bitmatrix_matrix *m1, bitmatrix_matrix *m2,
                                bitvector_vector *v);
```

Puts in `m1` the product of **m2** by the vector `v`.

```
void bitmatrix_transpose (bitmatrix_matrix *m1, bitmatrix_matrix *m2,
                          int r, int t, int l);
```

Transposes the `t` matrices of dimension `r`×`l` found in `m2` and puts the result in `m1`.

```
void bitmatrix_exchangeRows (bitmatrix_matrix *m, int i, int j);
```

Exchanges rows `i` and `j` in the binary matrix `*m`.

```
void bitmatrix_xorVect (bitmatrix_matrix *m, int r, int s, int min, int max);
```

Performs a exclusive-or between the `s`-th and `r`-th rows of `m`, for the `min`-th to the (`max`-1)-th bit vectors only. The result is put in row `r` of `m`.

```
lebool bitmatrix_inverse (bitmatrix_matrix *minv, bitmatrix_matrix *m);
```

Computes the inverse of `m` and puts the results in `minv`. The sub matrices of the `Matrixs` pointed by `m` and `minv` that are considered are the ones composed of only the first columns of the bit vectors. [17]

---

[17]From Pierre: Not clear enough...

```
void bitmatrix_product (bitmatrix_matrix *m1, bitmatrix_matrix *m2,
                        bitmatrix_matrix *m3);
```

Compute the matrix product of `m2` by `m3` and puts the results in `m1`. Only the first submatrices are considered. [18]

```
void bitmatrix_power (bitmatrix_matrix *m1, bitmatrix_matrix *m2, int64_t e);
```

Raises binary matrix `m2` to the power `e` and puts the results in `m1`. The exponent e can be negative, in which case, the inverse of `m2` will be raised to the power $|e|$. [19]

```
void bitmatrix_powerOfTwo (bitmatrix_matrix *m1, bitmatrix_matrix *m2,
                           unsigned int e);
```

Raises binary matrix `m2` to the power 2^e and puts the results in `m1`. We get $m1 = m2^{2^e}$.

```
void bitmatrix_display (bitmatrix_matrix *m, int t, int l, int r);
```

Displays the submatrix of `*m` defined by the first `r` rows and the first `l` bits of the first `t` bit vectors. [20]

```
void bitmatrix_displayMathematica (bitmatrix_matrix *m, int t, int l, int r);
```

Same as `bitmatrix_display` but produces a display compatible for Mathematica input.

---

[18]From Pierre: Meaning? Sizes must be compatible!
[19]From Pierre: Matrix must be square?
[20]From Pierre: Make this clearer. Return in a character string?

chrono

This module acts as an interface to the system clock to compute the CPU time used by parts of a program. Even though the ANSI/ISO macro `CLOCKS_PER_SEC = 1000000` is the number of clock ticks per second for the value returned by the `clock` function (so this function returns the number of microseconds), on some systems where the 32-bit type `long` is used to measure time, the value returned by `clock` wraps around to negative values after about 36 minutes. On some other systems where time is measured using the 32-bit type `unsigned long`, the clock may wrap around to 0 after about 72 minutes. When the macro `USE_ANSI_CLOCK` in module `gdef` is undefined, a non-ANSI-C clock is used. On Linux-Unix systems, it calls the POSIX function `times` to get the CPU time used by a program. On a Windows platform (when the macro `HAVE_WINDOWS_H` is defined), the Windows function `GetProcessTimes` will be used to measure the CPU time used by programs.

Every variable of type `chrono_Chrono` acts as an independent *stopwatch*. Several such stopwatchs can run at any given time. An object of type `chrono_Chrono` must be declared for each of them. The function `chrono_Init` resets the stopwatch to zero, `chrono_Val` returns its current reading, and `chrono_Write` writes this reading to the current output. The returned value includes part of the execution time of the functions from module `chrono`. The `chrono_TimeFormat` allows one to choose the kind of time units that are used.

Below is an example of how the functions may be used. A stopwatch named `mytimer` is declared and created. After 2.1 seconds of CPU time have been consumed, the stopwatch is read and reset. Then, after an additional 330 seconds (or 5.5 minutes) of CPU time the stopwatch is read again, printed to the output and deleted.

```
    double t;
    chrono_Chrono *mytimer = chrono_Create ();
        ⋮       (suppose 2.1 CPU seconds are used here.)

    t = chrono_Val (mytimer, chrono_sec);      /* Here, t = 2.1 */
    chrono_Init (mytimer);
        ⋮       (suppose 330 CPU seconds are used here.)

    t = chrono_Val (mytimer, chrono_min);      /* Here, t = 5.5 */
    chrono_Write (mytimer, chrono_hms);        /* Prints:  00:05:30.00 */
    chrono_Delete (mytimer);
```

```
typedef struct {
   unsigned long microsec;
   unsigned long second;
   } chrono_Chrono;
```

For every stopwatch needed, the user must declare a variable of this type and initialize it by calling chrono_Create.

```
typedef enum {
   chrono_sec,
   chrono_min,
   chrono_hours,
   chrono_days,
   chrono_hms
   } chrono_TimeFormat;
```

Types of units in which the time on a chrono_Chrono can be read or printed: in seconds (sec)), minutes (min), hours (hour), days (days), or in the HH:MM:SS.xx format, with hours, minutes, seconds and hundreths of a second (hms).

_____ **Timing functions** _____

```
chrono_Chrono * chrono_Create (void);
```

Creates and returns a stopwatch, after initializing it to zero. This function must be called for each new chrono_Chrono used. One may reinitializes it later by calling chrono_Init.

```
void chrono_Delete (chrono_Chrono * C);
```

Deletes the stopwatch C.

```
void chrono_Init (chrono_Chrono * C);
```

Initializes the stopwatch C to zero.

```
double chrono_Val (chrono_Chrono * C, chrono_TimeFormat Unit);
```

Returns the time used by the program since the last call to chrono_Init(C). The parameter Unit specifies the time unit. Restriction: Unit = chrono_hms is not allowed here.

```
void chrono_Write (chrono_Chrono * C, chrono_TimeFormat Unit);
```

Prints the CPU time used by the program since its last call to chrono_Init(C). The parameter Unit specifies the time unit.

tcode

This small program extracts compilable code from a TEX or LATEX document that contains the documentation. It creates a file `FOut` for a compiler like cc (or any other), starting from a file `FIn`. The names of these two files must be given by the user, with appropriate extensions, when calling the program. The two file names (with the extensions) must be different.

Only the text included between the `\code` and `\endcode` delimiters will appear in the second file. Only the following LATEX commands are allowed between `\code` and `\endcode`:

`\hide, \endhide, \iffalse, \fi, \smallcode, \smallc.`

Everything else between `\code` and `\endcode` must be legal code in the output file, apart from two exceptions: the TEX command `\def\code`, defining `\code` will not start a region of valid code, nor will `\code` appearing on a line after a TEX comment character `%`.

If one wants code to appear in the compilable file, but be invisible in the LATEX output file (e.g., `.pdf` or `.dvi`), it suffices to put this code between the delimiters `\hide` and `\endhide`, or between the delimiters `\iffalse` and `\fi`.

The program is called as:

tcode ⟨FIn⟩ ⟨FOut⟩

Examples: The following command extracts the *C* code from the LATEX file `chrono.tex`, and place it in the header file `chrono.h`:

tcode chrono.tex chrono.h

To extract *Java* code from the LATEX file `Event.tex`, and place it in the file `Event.java`, one would use:

tcode Event.tex Event.java

References

[1] C. W. Clenshaw. Chebychev series for mathematical functions. National Physical Laboratory Mathematical Tables 5, Her Majesty's Stationery Office, London, 1962.

[2] D. E. Knuth. *The Art of Computer Programming, Vol. 1.* Addison-Wesley, Reading, MA, second edition, 1973.

[3] D. E. Knuth. *The Art of Computer Programming, Vol. 2.* Addison-Wesley, Reading, MA, second edition, 1981.

[4] P. L'Ecuyer and S. Côté. Implementing a random number package with splitting facilities. *ACM Transactions on Mathematical Software*, 17(1):98–111, 1991.

[5] P. L'Ecuyer and F. Panneton. Fast random number generators based on linear recurrences modulo 2: Overview and comparison. In *Proceedings of the 2005 Winter Simulation Conference*, pages 110–119. IEEE Press, 2005.

[6] P. L'Ecuyer and F. Panneton. $\mathbf{F}_2$-linear random number generators. In C. Alexopoulos, D. Goldsman, and J. R. Wilson, editors, *Advancing the Frontiers of Simulation: A Festschrift in Honor of George Samuel Fishman*, pages 169–193. Springer-Verlag, New York, 2009.

[7] F. Panneton. *Construction d'ensembles de points basée sur des récurrences linéaires dans un corps fini de caractéristique 2 pour la simulation Monte Carlo et l'intégration quasi-Monte Carlo.* PhD thesis, Département d'informatique et de recherche opérationnelle, Université de Montréal, Canada, August 2004.