

## Section A: Project Overview

- Start Date: 1 May 2014
- Completion Date: 30 April 2014

### 1. Project Name

Systemic risk and contagion effects on risk margins for interrelated financial institutions and sectors

### 2. Project Summary

The proposed project deals with measuring and quantifying systemic risk, contagion effects and exposure in risk margins for interrelated financial institutions and sectors and linking the same to external economic shocks. The proposal addresses the issue of assessing the effectiveness of stress testing in group structures as a means of enhancing the resilience of the group, and entities within the group, to financial and economic shocks and limiting intra-group contagion. The project and methodological developments have implications of how APRA and industry can enhance their stress testing procedures and learn more from the results of this testing.

### 3. Project Team

First Name	Surname	Position	Institution	Team Position	Email
Piet	De Jong	Professor of Actuarial Studies	FBE Macquarie University	Leader	piet.dejong@mq.edu.au
Geoff	Loudon	Associate Professor	FBE Macquarie University	Investigator	geoff.loudon@mq.edu.au
Weihao	Choo	Senior Actuarial Executive	MSIG Holdings (Asia)	Investigator	chooweihao@gmail.com

#### 4. Budget (cash request only):

Year 1 (Total)	
CIFR	Member
\$100,000	—

#### 5. Relevant CIFR Key Area of Interest

- Systemic risk

Assessing and the level systemic risk in Australia requires a coherent methodology to measure the same and implement them in the Australian financial system context. A number of methodologies have recently been proposed to assess systemic risk (see references later). A major aim of the current project is to critique, improve upon these methodologies and apply and implement such improved technologies in the Australian context.

Present regulations are based on standard approaches such as  $\text{VaR}_q$ . Such regulations and capital requirements are mainly “standalone” where individual industries are analysed on a standalone basis using similar stress scenarios. Non-standalone approaches implicit in systemic risk calculations may lead to different margins, uncover systematic biases or tighter or amplify confidence intervals around margins in line with economic cycle. Both over and underestimation of capital margins impose costs on the economy.

#### 6. Research Proposal of interest to: APRA, RB

The current proposal arises out of the following target areas identified by CIFR and drawn to my attention by Professor David Gallagher:

- Assess the level of systemic risk in the Australian economy and in the ADI, insurance and superannuation industries, and identify potential domestic and external shocks to the Australian economy, and potential methods to protect against or remediate these shocks.
- Assess the effectiveness of stress testing in group structures as a means of enhancing the resilience of the group, and entities within the group, to financial and economic shocks and limiting intra-group contagion.
- Consider how APRA and industry could enhance their stress testing procedures and learn more from the results of this testing.

*Contact with other individuals*

- APRA – Charles Littrell. On 4 March 2014 the Team Research Leader met the Mr Charles Littrell of APRA to discuss the CIFR target research areas. The discussion ranged over a number of topics related to the same and the attitude APRA may take to any proposals. The discussion also canvassed the need to design appropriate quantitative methodologies and data bases for any empirical assessments.
- RBA – no contact.

**7. Capability Paragraph**

- Piet de Jong

Forty years' experience in the quantitative modelling uncertainty and risk including risks arising in insurance (general and mortality), time series dynamics, finance, capital allocation, health economics.

- Geoff Loudon

Extensive experience in conducting and supervising empirical research in finance. Research area includes financial risk management and security pricing, modelling inter-relations among risks, returns and underlying factors, especially during times of market crisis. Expertise in financial econometrics including application of regime-switching models; multivariate GARCH style models; stochastic volatility estimation; etc.

- Weihao Choo

Fully qualified actuary (FIAA) with extensive industry experience in stress testing and capital modelling, liability valuation, portfolio monitoring and pricing, investment modelling, and business planning. Academic research expertise as evidenced in two publications in international journals (exceptional for someone his age). Presently finishing PhD while working in industry. PhD research relates to risk and risk measurement and capital modelling and allocation.

## 8. Certifications

*Certification by Team Leader*

I, Piet de Jong, certify that:

- All the details on this FP are true and complete;
- I have notified CIFR of any actual or potential conflicts of interest I may have in relation to the FP and I undertake that, if the FP is successful, I will notify CIFR of any conflicts of interest which arise subsequent to the submission of the FP;
- I will notify CIFR if there are any changes in my circumstances which may impact on my eligibility to participate in, or ability to perform, the project subsequent to the submission of this FP;
- In participating in this FP, I consent to CIFR copying, disclosing and otherwise dealing with information contained in the Proposal, for the purpose of considering this proposal and making decisions as to the funding round;
- All information contained in the FP is both current and accurate;
- The work proposed in this project is not funded elsewhere;
- The work proposed is unique and that it has not been fully or partially completed elsewhere; and
- All named researchers have agreed to participate and agree to an immediate CIFR announcement should funding be approved.

Signature	Name	Position	Date
	Piet de Jong	Professor and Team Leader	03 March 2014

*Certification by Organisations contributing to the project*

I certify that:

- My organisation supports the FP and will contribute the resources outlined in the FP.
- If teaching relief is requested in the FP the Organisation approves the relief.

Signature	Name	Position	Date

## Section B: Project Objectives, Significance and Policy Implications

Our starting point for the proposed research is the recent literature and the CIFR targeted areas and APRA aims and functions. This recent literature includes [1, 2, 3] and [4]. The proposed research aims to extend and apply these techniques particularly in relation to the entities regulated by APRA. Thus our broad aim is to develop, implement and bring to bear recent developments in stress testing on the aims of APRA in general and the CIFR targeted research areas detailed above.

### *Improved measures of contagion and systematic risk*

CoVaR<sub>q</sub> as proposed in [5] suffers from a number of difficulties:

- Couched in terms of VaR<sub>q</sub> which contains the scale of the original measurements. It is worthwhile to have a scale independent measures.
- Conditioning on VaR<sub>0.5</sub> is undesirable and relatively intractable. In our proposed we reference stress with respect to the unconditional VaR<sub>q</sub>. This permits a more transparent analysis and estimation.
- Our approach will separate out the effect of marginal distributions and interdependence and econometrically relate these structures separately to external variables including shocks and drivers of systemic risk.

### *Significance of the project and policy implications*

Relating marginal and joint distributions separately to external drivers allows for a more cogent and coherent stress testing including the estimation of contagion effects, exposure effects and systemic risk across related entities and different financial sectors. Improved stress testing, estimation of risk effects and transmission of shocks through the financial system will make for more cogent prudential policy, prudential margin setting and sources of risk to the financial system.

### *Technical background and path to improved stress testing in the context of contagion and external shocks*

Our developments will be based on the following definition and econometric implementation:

$$\text{CoV}_q(x, y) \equiv \text{VaR}_q(x|y > q) - \text{VaR}_q(x) , \quad \text{CoV}_q(x) \equiv \text{CoV}_q(x, x) . \quad (1)$$

It is shown that (1) is a more robust and extensible definition than has been proposed in the literature and more readily amenable and useful to empirical work.

The proposed research agenda of this project begins by initially considering  $u$  and  $v$  uniform random variables on  $[0, 1]$ . Then obviously  $\text{VaR}_q(u) = \text{VaR}_q(v) = q$ . Define  $u^+ \equiv \text{VaR}_q(u|v > q)$  as the VaR<sub>q</sub> of  $u$  given  $v$  exceeds its VaR<sub>q</sub>:

$$P(u \leq u^+ | v > q) = q , \quad 0 < q < 1 . \quad (2)$$

The left hand side equals

$$\frac{P(u \leq u^+, v > q)}{1 - q} = \frac{u^+ - C(u^+, q)}{1 - q},$$

where  $C(u, v)$  is the joint distribution (copula) of  $u$  and  $v$ . Rearranging yields

$$u^+ \equiv \text{VaR}_q(u|v > q) = q(1 - q) + C(u^+, q). \quad (3)$$

If  $u$  and  $v$  are independent then  $C(u, v) = uv$  and  $u^+ = q$ . If  $u = v$  then  $u^+ = q + q(1 - q) = 2q - q^2$  and  $u^+ - q = q(1 - q)$ . Thus if  $u$  and  $v$  are non-negatively related,  $0 \leq u^+ - q \leq q(1 - q)$ .

- Note  $u_{t+1}^+ = q(1 - q) + C(u_t^+, q)$ . Iterate this equation and make  $C$  a function of forcing variables. e.g. a Clayton copula where the parameter is a function of forcing variables.
- If  $u$  and  $v$  are negatively dependent then define

$$\text{CoV}_q(u, v) \equiv -\text{CoV}_q(u, 1 - v)$$

In terms of  $u^+ \equiv \text{VaR}_q(u|v > q)$ , define the contagion effect of  $v$  on  $u$  as

$$\beta_{uv} \equiv \frac{u^+ - q}{q(1 - q)} = \frac{\text{CoV}_q(u, v)}{\text{CoV}_q(v)}. \quad (4)$$

Thus  $\beta_{uv}$  is the change in  $\text{VaR}_q$  of  $u$  given  $v$  becomes  $q$ -stressed as a proportion of the change if  $u = v$ . For positively dependent random variables  $0 < \beta_{uv} \leq 1$  with the lower and upper limits attained under independence and perfect dependence, respectively. If  $u$  and  $v$  are negatively dependent then  $1 - 1/(1 - q) \leq \beta_{uv} < 0$ . Negative dependence is not be studied in great detail in this project. Note  $\beta_{uv} \neq \beta_{vu}$ .

Furthermore we may define quantities such as  $u^- \equiv \text{VaR}_q(u|v \leq q)$  measuring the impact of a non distressed state in  $v$ . For brevity we do not dwell on these constructs in this writeup although the ramifications and potential uses of these constructs will be investigated in the research.

#### *Contagious stress effects for financial variables and the contagion matrix*

We now discuss actual variables on actual scales. Suppose  $F_x$  and  $F_y$  are the marginal distributions of  $x$  and  $y$  with  $x = F_x^-(u)$  and  $y = F_y^-(v)$ . Then the contagion effect of  $y$  on  $x$  is defined as the change in  $\text{VaR}_q(x)$  when  $y$  becomes  $q$ -distressed as in (??), equal to

$$\text{CoVaR}_q(x, y) \equiv \text{VaR}_q\{x|y > \text{VaR}_q(y)\} - \text{VaR}_q(x) \quad (5)$$

$$= F_x^-\{q + \beta_{uv}q(1 - q)\} - F_x^-(q) \approx \frac{q\beta_{uv}}{\lambda} = \frac{\text{CoV}_q(u, v)}{q'}, \quad (6)$$

where  $'$  denotes differentiation and  $\lambda$  is the hazard of  $x$  at  $x = \text{VaR}_q(x)$ . If  $F_x$  is linear then the approximation is exact. Hence it is appropriate to scale  $x$  such that  $F_x^-$  is linear in the tail. Rescaling has no effect on the copulas connecting variables.

If  $x$  is vector then  $\text{CoV}_q(x)$  is the (non-symmetric) matrix with entries  $\text{CoV}_q(x_i, x_j)$  and

$$R \equiv \text{CoV}_q(x) = D^{-1} \times \text{CoV}_q(u) , \quad D = \text{diag}(q'_1, \dots, q'_m) ,$$

where  $m$  is the number of components in  $x$ .

#### *Econometric implementation*

The above development provides a framework for linking bivariate copulas and marginals to external variables and shocks study the impact of the same on stresses within the system and the contagious effects of crises. Proposed econometric analysis will be as in ?.



### **Section C: Data, Method and Outputs**

– Include a detailed discussion of the data needed for the project, the proposed method and the outputs (Maximum two pages).

Advice and cooperation is requested from appropriate research personal within APRA to assist in both development and implementation.

#### **Timetable for the delivery of Outputs**

Date	Output	Details (of proposed Output)

## Section D: Research Record and References

### 1. Research Record

- Piet de Jong, Team Leader.

The following publications (in no particular order) detail my expertise in designing and, where appropriate, implementing tools to quantify, assess and model uncertainty related to finance, demographics and economics. (see also joint publications with Weihao Choo given under the latter's heading)

De Jong, P. (2012). Modeling dependence between loss triangles. *North American Actuarial Journal* 16(1), 74–86.

De Jong, P. (2006). Forecasting Runoff Triangles. *North American Actuarial Journal* 10(2), 28.

De Jong, P. (1989). Smoothing and interpolation with the state-space model. *Journal of the American Statistical Association* 84(408), 1085–1088.

De Jong, P. (1991). The diffuse Kalman filter. *Annals of Statistics* 19(2), 1073–1083.

De Jong, P. and P. Boyle (1983). Monitoring mortality: a state-space approach. *Journal of Econometrics* 23, 131–146.

De Jong, P. and Chu-Chun-Lin S. (2003). Smoothing with an unknown initial condition. *Journal of Time Series Analysis* 24(2), 141–148.

De Jong, P. and S. Ferris (2006). Adverse selection spirals. *Astin Bulletin* 36(2), 589–628.

De Jong, P. and G. Heller (2008). *Generalized Linear Models for Insurance Data*. Cambridge University Press.

De Jong, P. and C. Marshall (2007). Mortality projection based on the Wang transform. *ASTIN Bulletin* (1), 149–162.

De Jong, P. and J. R. Penzer (1998). Diagnosing shocks in time series. *Journal of the American Statistical Association* 93(442), 796–806.

De Jong, P. and N. Shephard (1995). The simulation smoother for time series models. *Biometrika* 82, 339–350.

De Jong, P. and B. Zehnwirth (1983b). Claims reserving, state-space models and the Kalman filter. *Journal of the Institute of Actuaries* 110, 157–181.

- Geoff Loudon, Principal Researcher
 

Liu, J., Loudon, G., Milunovich G., Linkages between international RE-ITs: the role of economic factors, *Journal of Property Investment & Finance*, 30(5), 2012, 473-492.

Dean, W., Faff, R., Loudon, G., Asymmetry in return and volatility spillover between equity and bond markets in Australia, *Pacific Basin Finance Journal*, 18(3), 2010, 272-289.

Hobbes, G., Lam, F., Loudon, G., Regime shifts in the stock-bond relation in Australia, *Review of Pacific Basin Financial Markets and Policies*, 10(1), 2007, 81-99.

Loudon, G., Okunev, J., White, D., Hedge fund risk factors and the Value-at-Risk of fixed income trading strategies, *The Journal of Fixed Income* 16(2), 2006, 46-61.

Loudon, G., Is the risk-return relation positive? Further evidence from a stochastic volatility in mean approach, *Applied Financial Economics* 16(13), 2006, 981-992.

Loudon, G., Financial risk exposures in the airline industry: evidence from Australia and New Zealand, *Australian Journal of Management* 29(2), 2004, 295-316.

Loudon, G., Watt, E., Yadav, P., An empirical analysis of alternative parametric ARCH models, *Journal of Applied Econometrics* 15(2), 2000, 117-136.

Loudon, G., Foreign exchange exposure and the pricing of currency risk in equity returns: Some Australian evidence, *Pacific Basin Finance Journal* 1(4), 1993, 335-354.

Loudon, G., The foreign exchange operating exposure of Australian stocks, *Accounting and Finance* 33(1), 1993, 19-32.

Loudon, G., American put pricing: Australian evidence, *Journal of Business Finance and Accounting* 17(2), 1990, 297-321.
- Weihao Choo, Principal Researcher
 

Choo, W. and P. De Jong (2009). Loss reserving using loss aversion functions. *Insurance Mathematics and Economics* 45(2), 271-277.

Choo, W. and P. De Jong (2010). Determining and Allocating Diversification Benefits for a Portfolio of Risks. *Astin Bulletin* 40(1), 257-269.

## 2. Grants

- Piet de Jong, Team Leader

Most of my research requires limited money – just lots of time and concentration. Despite this I have held a number of research grants mainly to facilitate my ongoing research program:

- While at the University of British Columbia from 1982-2001 (Professor of Statistics) I held NSERC operating grants to facilitate my ongoing research program. These are equivalent to ARC discovery grants except that the grant is based on performance rather than detailed aspirations to research one or other issue. The individual research program and operating grant led to many highly cited publications in A\* international academic journals.
- While at the University of Amsterdam (Visiting Research Fellow) in 1987 I was funded under the Dutch government's ZWO initiative. This led to a number of world class highly cited academic publications.
- While at the London School of Economics (Reader in Statistics) from 1995-1998. I held NSERC operating grants. Again this led to a number of highly cited A\* international academic publications.
- While at Macquarie University 2003-2014 (Professor of Actuarial Studies) I have held grants from Macquarie University (jointly funded with APRA) and the Institute of Actuaries. Again this has led to my more recent A\* international publications including a jointly authored book published by Cambridge University Press.

- Geoff Loudon, Principal Researcher

No recent grants

- Weihao Choo, Principal Researcher

Early stage researcher. Just now finishing PhD.

## Section E: Detailed Budget and Justifications

Expenditure	Year 1 – Total			
	Cash (CIFR)	Cash (Member)	In Kind	Other
Staff				
– Teaching relief for De Jong for 2 months, 28% for oncosts & 30% infrastructure: $172,363 \times 1.28 \times 2/12 \times 1.3$			47,802	
– Teaching relief for Loudon for 1 month, 28% for oncosts & 30% infrastructure: $135,000 \times 1.28 \times 1/12 \times 1.3$			18,720	
Equipment	2,500	2,500		
Computer and related items				
Data				
Travel	10,000	10,000		
2 researchers x 2 conferences				
Fellowships	25,000	25,000		
Weihaio Choo				
Scholarships				
Research Assistant	25,531	25,531	15,319	
Cash: RA, top of Level 6 band grossed up by on costs, 3 days pw: $66487 \times 1.28 \times 0.6$				
In kind: Infrastructure @ 30% : $51,062.02 \times 0.3$				
Other costs				
Total				

### *Basis for teaching-relief request*

De Jong requests funding for one months teaching relief, during the second half of 2014. The purpose is to give effective direction to the project for a period without the burden of teaching and convening courses.

### *Basis for RA request*

A research assistant at the top of the Level 6 band is required for data analysis and assistance with programming. His or her tasks will be supervised by the researchers, and the appointment would be for 3 days per week for the duration of the project. The tasks are twofold. The first is to gather appropriate data and secondly to program methods in R.

*Basis for Fellowship request*

The fellowship will facilitate one of the researchers (Weihao Choo) to devote appropriate time to the project.

*Basis for Travel request*

Present research at two international conference. Note that workshopping the paper with industry practitioners and researchers at one international conference is required to maximise the impact of this research.

## Bibliography