```
1 from numpy.random import randint
2 import numpy as np
3 from tensorflow import keras
4 from keras import layers
5 import matplotlib.pyplot as plt
```

OPTIMIZATION 1. Take best model 2. round

1% of permutation, 5 array length, 10 max digit, 100 epochs, 16 batch, 32 32 == 5% error

1% of permutation, 5 array length, 10 max digit, 100 epochs, 16 batch, 16 16 == 6% error

1% of permutation, 5 array length, 10 max digit, 100 epochs, 16 batch, 64 64 == 3% error

1% of permutation, 5 array length, 10 max digit, 100 epochs, 16 batch, 64 64 64 == 2% error

1% of permutation, 5 array length, 10 max digit, 100 epochs, 16 batch, 64 64 64 == 1.5% error

1% of permutation, 5 array length, 10 max digit, 150 epochs, 16 batch, 64 64 64 == 1.5% error

CHANGE to 10 length array

10^-5% of permutation, 10 array length, 10 max digit, 100 epochs, 16 batch, 64 64 64 64 == 5% error

Anche se ha visto molto meno da un buon risultato

10^-4% of permutation, 10 array length, 10 max digit, 100 epochs, 16 batch, 64 64 64 64 == 3% error

```
1  # parameters
2
3  modelPath = ""
4  modelName = "NNMedian.keras"
5
6  n_arrays = 2000
7  array_length = 5
8  max_digit = 10
9  epochs = 100
10  batch_size = 8
```

```
1 # calculate number of permutation
2 print("number of permutation: ", max_digit**array_length)
3 print("percentage of view:", (n_arrays * 0.5) * 100 / max_digit**array_length)
```

```
number of permutation: 100000
percentage of view: 1.0
```

```
1 # generate input and output data
2
3 input_arrays = []
4 label_arrays = []
5 for _ in range(n_arrays):
6     temp_array = randint(0, max_digit, array_length)
7     temp_label = np.median(temp_array)
8     input_arrays.append(temp_array)
9     label_arrays.append(temp_label)
```

```
1 print(len(input_arrays), len(label_arrays))
```

2000 2000

```
1 # normalize
2
3 for i in range(len(input_arrays)):
4    input_arrays[i] = input_arrays[i].astype("float32") / (max_digit - 1)
5    label_arrays[i] = label_arrays[i].astype("float32") / (max_digit - 1)
```

```
1 # make np array
2 input_arrays = np.array(input_arrays)
3 label_arrays = np.array(label_arrays)
```

```
1 print(input_arrays[:10])
2 print(label_arrays[:10])
```

```
[[0.7777778 0.8888889 0.22222222 0.7777778 0.22222222]
```

```
[0.7777778 0.33333334 0.8888889 0.22222222 0.7777778 ]
[0.5555556 0.11111111 0.8888889 0.33333334 0. ]
[0.5555556 0.44444445 0.11111111 0.7777778 0.5555556 ]
[0.44444444 0.66666667 0.7777778 0.11111111 0.5555556 ]
[0.5555556 0.2222222 0.11111111 0.5555556 0.33333334]
[0.11111111 0. 0.11111111 0.2222222 1. ]
[0.44444445 0.44444445 0.11111111 0.2222222 1. ]
[0.11111111 0.33333334 0.8888889 1. 0.5555556 ]
[1. 0.11111111 0.1111111 0.8888889 0.7777778 ]]
[0.7777778 0.7777778 0.33333333 0.55555556 0.5555556 0.33333333 0.111111111 0.44444444 0.555555556 0.77777778]
```

```
1 # split data
2
3 n_train = int(0.5 * n_arrays)
4 n_val = int(0.25 * n_arrays)
5 n_eval = n_arrays - n_train - n_val
6
7 data_test = input_arrays[:n_train]
8 data_validation = input_arrays[n_train:(n_train+n_val)]
9 data_evaluation = input_arrays[n_train + n_val:]
10
11 label_test = label_arrays[:n_train]
12 label_validation = label_arrays[n_train:(n_train+n_val)]
13 label_evaluation = label_arrays[n_train + n_val:]
```

```
1 print(data_test.shape, data_validation.shape, data_evaluation.shape)
2 print(label_test.shape, label_validation.shape, label_evaluation.shape)
```

```
(1000, 5) (500, 5) (500, 5)
(1000,) (500,) (500,)
```

```
1 from tensorflow import keras
2 from keras import layers
3
4 inputs = keras.Input(shape=(array_length))
5 x = layers.Dense(64, activation="relu") (inputs)
6 x = layers.Dense(64, activation="relu") (x)
7 x = layers.Dense(64, activation="relu") (x)
8 x = layers.Dense(64, activation="relu") (x)
9 outputs = layers.Dense(1, activation="sigmoid") (x)
10
11 model = keras.Model(inputs=inputs, outputs=outputs)
12
13 model.summary()
```

Model: "model_3"

Layer (type)	Output Shape	Param #
input_4 (InputLayer)	[(None, 5)]	0
dense_15 (Dense)	(None, 64)	384
dense_16 (Dense)	(None, 64)	4160
dense_17 (Dense)	(None, 64)	4160
dense_18 (Dense)	(None, 64)	4160
dense_19 (Dense)	(None, 1)	65
	=======================================	
Total params: 12,929 Trainable params: 12,929 Non-trainable params: 0		

```
1 callbacks = [
2 keras.callbacks.ModelCheckpoint(
3    filepath=modelPath + modelName,
4    monitor="val_mae",
```

```
save best only=True,)
1 history = model.fit(data test,
2
               label_test,
3
               epochs=epochs.
4
               batch size=batch size,
5
               validation data=(data validation, label validation),
               callbacks=callbacks)
  Epoch 72/100
  125/125 [======
                   ============== ] - 0s 4ms/step - loss: 0.5951 - mae: 0.0253 - val loss: 0.5927 - val mae: (
  Epoch 73/100
  125/125 [======
               Epoch 74/100
  Epoch 75/100
              ========== ] - 0s 3ms/step - loss: 0.5948 - mae: 0.0245 - val_loss: 0.5914 - val_mae: (
  125/125 [======
  Epoch 76/100
  125/125 [====
                   =========] - 0s 3ms/step - loss: 0.5948 - mae: 0.0242 - val loss: 0.5928 - val mae: (
  Epoch 77/100
  125/125 [============== ] - 0s 4ms/step - loss: 0.5951 - mae: 0.0253 - val_loss: 0.5911 - val_mae: (
  Epoch 78/100
  125/125 [=====
               =========] - 0s 3ms/step - loss: 0.5950 - mae: 0.0246 - val loss: 0.5921 - val mae: (
  Epoch 79/100
              ========================== - 0s 3ms/step - loss: 0.5951 - mae: 0.0254 - val loss: 0.5911 - val mae: (
  125/125 [======
  Epoch 80/100
  125/125 [=====
                 ========= ] - 0s 3ms/step - loss: 0.5949 - mae: 0.0242 - val loss: 0.5949 - val mae: (
  Epoch 81/100
  Epoch 82/100
  Epoch 83/100
  125/125 [=====
                 Epoch 84/100
  125/125 [==========] - 0s 4ms/step - loss: 0.5946 - mae: 0.0234 - val loss: 0.5925 - val mae: (
  Epoch 85/100
  125/125 [=====
                Epoch 86/100
  125/125 [============= ] - 0s 3ms/step - loss: 0.5948 - mae: 0.0237 - val loss: 0.5906 - val mae: (
  Epoch 87/100
  125/125 [=====
              =========] - 0s 3ms/step - loss: 0.5946 - mae: 0.0229 - val_loss: 0.5919 - val_mae: (
  Epoch 88/100
  125/125 [=========================== ] - 0s 3ms/step - loss: 0.5945 - mae: 0.0227 - val_loss: 0.5935 - val_mae: (
  Epoch 89/100
  125/125 [============ 1 - 0s 3ms/step - loss: 0.5945 - mae: 0.0226 - val loss: 0.5908 - val mae: (
  Epoch 90/100
  125/125 [==========] - 0s 3ms/step - loss: 0.5945 - mae: 0.0228 - val loss: 0.5916 - val mae: (
  Epoch 91/100
  125/125 [==================== ] - 0s 3ms/step - loss: 0.5947 - mae: 0.0236 - val loss: 0.5919 - val mae: (
  Epoch 92/100
  125/125 [============== ] - 0s 3ms/step - loss: 0.5945 - mae: 0.0235 - val_loss: 0.5906 - val_mae: (
  Epoch 93/100
  125/125 [======
              Epoch 94/100
  125/125 [==========] - 0s 3ms/step - loss: 0.5944 - mae: 0.0227 - val loss: 0.5903 - val mae: (
  Epoch 95/100
  125/125 [=====
               =========] - 0s 3ms/step - loss: 0.5944 - mae: 0.0218 - val loss: 0.5924 - val mae: (
  Epoch 96/100
  125/125 [==========] - Os 3ms/step - loss: 0.5944 - mae: 0.0226 - val loss: 0.5909 - val mae: (
  Epoch 97/100
  125/125 [======
                Epoch 98/100
  125/125 [======
              Epoch 99/100
  125/125 [============ ] - 0s 3ms/step - loss: 0.5943 - mae: 0.0221 - val loss: 0.5907 - val mae: (
  Epoch 100/100
  1 mae = history.history["mae"]
2 val_mae = history.history["val_mae"]
3 loss = history.history["loss"]
4 val loss = history.history["val loss"]
5 x_epochs = range(1, len(val_mae) + 1)
1 plt.plot(x_epochs, mae, "bo", label="Training mae")
2 plt.plot(x_epochs, val_mae, "b", label="Validation mae")
3 plt.title("Training and validation accuracy")
4 plt.legend()
5 plt.figure()
6 plt.plot(x_epochs, loss, "bo", label="Training loss")
7 plt.plot(x_epochs, val_loss, "b", label="Validation loss")
8 plt.title("Training and validation loss")
```

```
9 plt.legend()
10 plt.show()
```

```
Training and validation accuracy
                                                     Training mae
0.12
                                                      Validation mae
0.10
0.08
0.06
0.04
0.02
                     Training and validation loss
                                                      Training loss
0.65
                                                      Validation loss
0.64
0.63
0.62
0.61
0.60
0.59
                  20
                              40
                                          60
                                                                 100
                                                      80
```

```
1 model_best = keras.models.load_model(modelPath + modelName)
2
3 eval_loss, eval_mae = model_best.evaluate(data_evaluation, label_evaluation)
4 print(f"Evaluation accuracy: {eval_mae:.3f}")
5 eval_mae_perc = eval_mae * (max_digit - 1)
6 print(f"Evaluation mae denormalized: {eval_mae_perc:.2f}")
```

16/16 [============] - 0s 2ms/step - loss: 0.6008 - mae: 0.0308 Evaluation accuracy: 0.031 Evaluation mae denormalized: 0.28

```
1 def denormalize(x):
2     x = x * (max_digit - 1)
3     return x
4
5 def rounding(x):
6     x = round(x, 0)
7     return x
8
9 predictions = model_best.predict(data_evaluation)
10 targets = label_evaluation
```

16/16 [======] - 0s 2ms/step

```
1 \times = []
 2 predictions_denorm = []
 3 predictions_denorm_round = []
 4 targets_denorm = []
 5 for i in range(len(predictions)):
      x.append(i)
      predictions_denorm.append(denormalize(float(predictions[i])))
      predictions_denorm_round.append(rounding(denormalize(float(predictions[i]))))
 9
      targets_denorm.append(denormalize(targets[i]))
11 print(predictions_denorm[:25])
12 print(predictions denorm round[:25])
13 print(targets_denorm[:25])
14
15 plt.plot(x[:25], predictions_denorm[:25], label="predictions_denorm")
16 plt.plot(x[:25], targets_denorm[:25], label="target")
17 plt.legend(loc="upper left")
18 plt.show()
20 plt.plot(x[:25], predictions_denorm_round[:25], label="predictions_denorm_round")
21 plt.plot(x[:25], targets_denorm[:25], label="target")
```

23 mlt.show()

22 plt.legend(loc="upper left")

```
[4.0, 6.0, 7.0, 1.0, 5.0, 7.0, 7.0, 6.0, 8.0, 2.0, 2.0, 4.0, 4.0, 2.0, 4.0, 6.0, 7.0, 6.0, 6.0, 5.0, 4.0, 2.0, 6.0 [4.0, 6.0, 7.0, 0.0, 5.0, 6.0, 7.0, 6.0, 8.0, 2.0, 2.0, 4.0, 4.0, 2.0, 4.0, 6.0, 7.0, 6.0, 6.0, 5.0, 4.0, 2.0, 6.0
            target
 7
 6
 5
 4
 3
 2
 1
 0
       ó
                                                 15
                                                               20
                                                                             25
 8
            predictions_denorm_round
            target
 7
 5
 3
 2
 1
 0
```

15

20

10

```
def mean_absolute_error(pre, tar):
    sum = 0
    n = len(pre)
    for i in range(n):
        sum += abs(tar[i] - pre[i])
    error = sum/n
    return error
```

```
print("MAE of denormalized: ", mean_absolute_error(predictions_denorm, targets_denorm))
print("MAE of denormalized rounded: ", mean_absolute_error(predictions_denorm_round, targets_denorm))
print("Percentage error: ", round(mean_absolute_error(predictions_denorm_round, targets_denorm) * 100 / max_digit,
```

```
MAE of denormalized: 0.27704644679650664
MAE of denormalized rounded: 0.154
Percentage error: 1.54 %
```

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