Task: forecast the real price of gasoline for the US.

Dataset: gasoline.xlsx contains two monthly time series. The nominal price of gasoline and the CPI.

- 1. Create the real price of gasoline
- 2. Plot real and nominal prices over time
- 3. From now on you will work with logs:  $y_t = log$  (Real Price<sub>t</sub>). Consider the sample from obs 1 to Dec 2014. Plot the sample ACF of  $y_t$  and that of  $\Delta y_t = (y_t y_{t-1})$ .
- 4. Using the same sample above fit two AR(1) models: the first for  $y_t$  and the second for  $\Delta y_t$ . Report in both cases the coefficient associated with the lagged dependent variable.
- 5. Produce a series of 1 step-ahead forecasts for  $y_t$ . Use the following models: random walk (no drift), ARIMA(1,1,0), ARIMA(0,1,1), ARIMA(1,1,1). To produce forecasts start from the sample that ends in Dec 2014 and add 1 observation at the time (i.e. expanding/recursive scheme)
- 6. Transform the forecasts to levels (i.e. real prices)
- 7. Compute the mean squared forecast error and comment.

US Regular All Formulations Gas Price, Dollars per Gallon, Monthly, Not Seasonally
Adjusted
Consumer Price Index for All Urban Consumers: All Items in U.S. City Average, Index
1982-1984=100, Monthly, Seasonally Adjusted