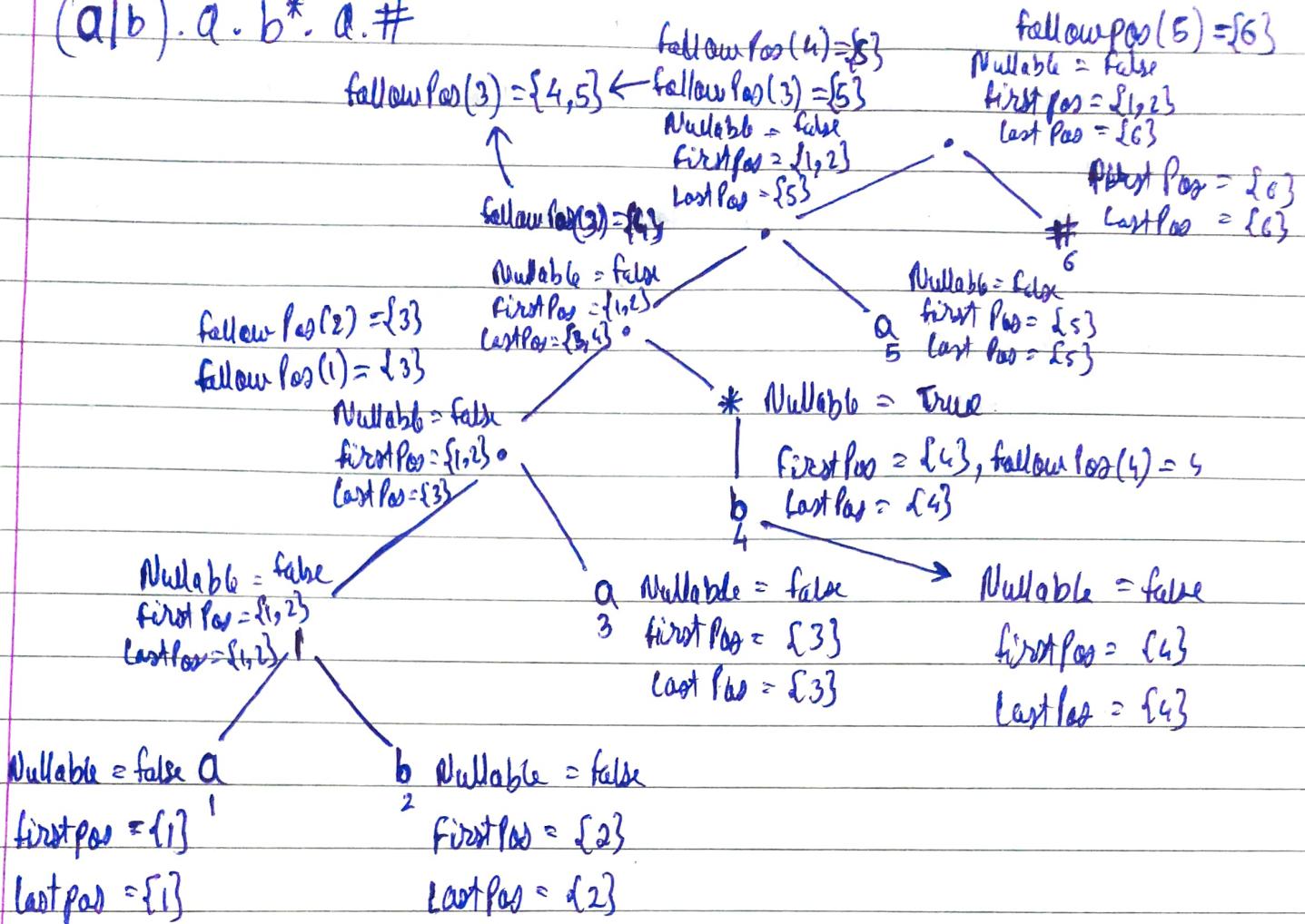


$(a|b) \cdot a \cdot b^* \cdot a \cdot \#$



$\text{followPos}(1) = \{3\}$

$\text{followPos}(2) = \{3\}$

$\text{followPos}(3) = \{4, 5\}$

$\text{followPos}(4) = \{4, 5\}$

$\text{followPos}(5) = \{6\}$

$\text{firstPos of root Node} = \{1, 2\} = A$

$\text{DFA}[A, a] = \text{followPos}(1) = \{3\} = B$

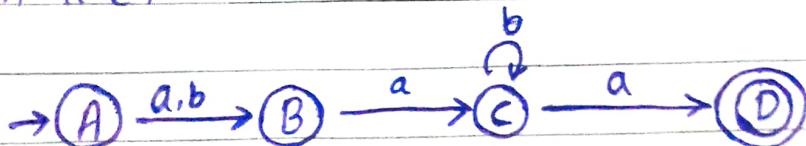
$\text{DFA}[A, b] = \text{followPos}(2) = \{3\} = B$

$\text{DFA}[B, a] = \text{followPos}(3) = \{4, 5\} = C$

$\text{DFA}[C, a] = \text{followPos}(5) = \{6\} = D$

$\text{DFA}[C, b] = \text{followPos}(4) = \{4, 5\} = C$

D.F.A for given R.E.



$S \rightarrow aA | BC$ $A \rightarrow Aa | Ac | b$ $B \rightarrow b$

$$\alpha_1 = a \quad \alpha_2 = c \quad \beta_1 = b$$

$$A \rightarrow b \quad A'$$

$$A' \rightarrow aA' | cA' | \epsilon$$

Unit 2 Q1

* $S \rightarrow ACB | CbB | Ba$

$A \rightarrow d \alpha | \beta c$

$B \rightarrow g | \epsilon$

$C \rightarrow h | \epsilon$

Calculate First Set

$$\text{first}(S) = \text{first}(ACB) \cup \text{first}(CbB) \cup \text{first}(Ba) \rightarrow ①$$

$$\text{first}(ACB) = \text{first}(A) \rightarrow ②$$

$$\text{first}(A) = \text{first}(d\alpha) \cup \text{first}(\beta c)$$

$$\text{first}(d\alpha) = \{d\}$$

$$\text{first}(\beta c) = \text{first}(B) - ③$$

$$\text{first}(B) = \text{first}(g) \cup \text{first}(\epsilon)$$

$$= \{g, \epsilon\} \Rightarrow \text{Next Rule}$$

$$\text{first}(Cb) = \text{first}(C) - \{\epsilon\} \cup \text{first}(B) \rightarrow ④$$

$$\text{first}(C) = \{h, \epsilon\}$$

$$\text{first}(B) = \{g, \epsilon\} - \{\epsilon\} \cup \{h, \epsilon\}$$

$$\text{first}(A) = \{d\} \cup \{g, h, \epsilon\} = \{d, g, h, \epsilon\}$$

$$\text{first}(A \cup B) = \text{first}(A) - \{\epsilon\} \cup \text{first}(B)$$

$$\text{first}(CB) = \text{first}(C) = \{h, \epsilon\}$$

$$\text{first}(cB) = \text{first}(c) - \{\epsilon\} \cup \text{first}(B)$$

$$\begin{aligned}\text{first}(cB) &= \{h, g, \epsilon\} - \{\epsilon\} \cup \{g, \epsilon\} \\ &= \{g, h, \epsilon\}\end{aligned}$$

$$\begin{aligned}\text{first}(AcB) &= \{d, g, h, \epsilon\} - \{\epsilon\} \cup \{g, h, \epsilon\} \\ &= \underline{\{d, g, h, \epsilon\}}\end{aligned}$$

$$\text{first}(CbB) = \text{first}(C) = \{h, \epsilon\}$$

$$\begin{aligned}\text{first}(C, B, B) &= \text{first}(C) - \{\epsilon\} \cup \text{first}(B, B) \\ &= \{h, \epsilon\} - \{\epsilon\} \cup \{b\} \\ &= \underline{\{b, h\}}\end{aligned}$$

$$\underline{\text{first}(Ba)} = \{g, a\}$$

$$\text{first}(S) = \{a, b, d, g, h, \epsilon\}$$

* Examples on Left Recursion

$$1) A \rightarrow Aa \mid b$$

$$B \rightarrow c$$

$$\text{Considering : } A \rightarrow Aa \mid b$$

$$\alpha = a$$

$$\beta = b$$

$$\Rightarrow A \rightarrow bA'$$

$$A' \rightarrow aA' \mid \epsilon$$

Final Production Rules :

$$A \rightarrow bA'$$

$$A' \rightarrow aA' \mid \epsilon$$

$$B \rightarrow c$$

$$2) A \rightarrow AaAa \mid AbBb \mid c$$

$$B \rightarrow c$$

$$\text{Considering : } A \rightarrow AaAa \mid AbBb \mid c$$

$$\alpha_1 = aAa \quad \alpha_2 = bBb$$

$$\beta = c$$

$$\Rightarrow A \rightarrow cA'$$

$$A' \rightarrow aAaA' \mid bBbA' \mid \epsilon$$

Final Production Rules :

$$A \rightarrow cA'$$

$$A' \rightarrow aAaA' \mid bBbA' \mid \epsilon$$

$$B \rightarrow c$$

3)

$$A \rightarrow Aa \mid Ab \mid Bc \mid Bd$$

$$B \rightarrow Ba \mid d$$

Considering : $A \rightarrow Aa \mid Ab \mid Bc \mid Bd$

$$\alpha_1 = a \quad \alpha_2 = b$$

$$\beta_1 = Bc \quad \beta_2 = Bd$$

$$\Rightarrow A \rightarrow BCA' \mid Bda'$$

$$A' \rightarrow aA' \mid bA' \mid \epsilon$$

Considering : $B \rightarrow Ba \mid d$

$$\alpha = a$$

$$\beta = d$$

$$B \rightarrow dB'$$

$$B' \rightarrow aB' \mid \epsilon$$

Final Production Rules :

$$A \rightarrow BCA' \mid Bda'$$

$$A' \rightarrow aA' \mid bA' \mid \epsilon$$

$$B \rightarrow dB'$$

$$B' \rightarrow aB' \mid \epsilon$$

4) $A \rightarrow AabB \mid AbcB \mid BcB$

$$B \rightarrow c$$

Considering : $A \rightarrow AabB \mid AbcB \mid BcB \mid b \mid c$

$$\alpha_1 = abB \quad \alpha_2 = bcB$$

$$\beta_1 = b \quad \beta_2 = c$$

$$\Rightarrow A \rightarrow bA' \mid cA'$$

$$A' \rightarrow abBA' \mid bcBA' \mid \epsilon$$

Final Production Rules : $A \rightarrow bA' \mid cA'$

$$A' \rightarrow abBA' \mid bcBA' \mid \epsilon$$

$$B \rightarrow c$$

5)

$$A \rightarrow Aabc | ABac | Bac | bAB$$

$$B \rightarrow b$$

Considering : $A \rightarrow Aabc | ABac | Bac | bAB$

$$\alpha_1 = abc \quad \alpha_2 = Bac$$

$$\beta_1 = Bac \quad \beta_2 = bAB$$

$$\Rightarrow A \rightarrow BacA' | baBA'$$

$$A' \rightarrow abcA' | BacA' | \epsilon$$

Final Production Rules :

$$A \rightarrow BacA' | baBA'$$

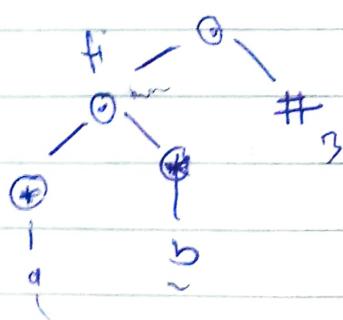
$$A' \rightarrow abcA' | BacA' | \epsilon$$

$$B \rightarrow b$$

$$a^* b^*$$

$$a^* b^*$$

$$ab$$



Q1:

$$\begin{array}{ll}
 S \rightarrow aBDh & S \rightarrow aBDh \\
 D \rightarrow Bb|c & B \rightarrow cB' \\
 D \rightarrow EF & B' \rightarrow bB'|e \\
 E \rightarrow g|\varepsilon & E \rightarrow g|\varepsilon \\
 F \rightarrow f|\varepsilon & F \rightarrow f|\varepsilon
 \end{array}$$

$$\text{First}(S) = \text{First}(aBDh) = \{a\}$$

$$\text{First}(B) = \{c\}$$

$$\text{First}(B') = \{b, \varepsilon\}$$

$$\text{First}(D) = \text{First}(EF) = \text{First}(E) = \{g, \varepsilon\}$$

$$\begin{aligned}
 \text{First}(D) &= \text{First}(E) - \{\varepsilon\} \cup \text{First}(F) \\
 &= \{g, \varepsilon\} - \{\varepsilon\} \cup \{f, \varepsilon\} \\
 &= \{g, f, \varepsilon\}
 \end{aligned}$$

$$\text{First}(E) = \{g, \varepsilon\}$$

$$\text{First}(F) = \{f, \varepsilon\}$$

Q2:

$$\begin{array}{l}
 A \rightarrow BCc|gDB \\
 B \rightarrow bCD\varepsilon|\varepsilon \\
 C \rightarrow DAB|C \\
 D \rightarrow \varepsilon|dD
 \end{array}$$

$$\begin{array}{l}
 E \rightarrow Eaf|c \rightarrow E \rightarrow cE' \\
 E' \rightarrow afE'|\varepsilon
 \end{array}$$

$$\text{First}(B) = \{b, \varepsilon\}$$

$$\text{First}(D) = \{d, \varepsilon\}$$

$$\text{First}(C) = \{c\}$$

$$\text{First}(E') = \{a, \varepsilon\}$$

$$\begin{array}{l}
 \text{First}(Cc) = \text{First}(c) \\
 = \text{First}(DAB) \cup \text{First}(Ca) \\
 = \text{First}(DAB) = \text{First}(D) \\
 = \{d, \varepsilon\} \\
 = \{d, \varepsilon\} - \{g\} \cup \text{First}(ab) \\
 = \{a, d\} \\
 \text{First}(Cc) = \{a, c, d\}
 \end{array}$$

$$\text{First}(A) = \text{First}(BCc) \cup \text{First}(gDB)$$

$$\begin{aligned}
 \text{First}(BCc) &= \text{First}(B) = \{b, \varepsilon\} \\
 &= \text{First}(B) - \{\varepsilon\} \cup \text{First}(Cc) \\
 &= \{a, b, c, d\}
 \end{aligned}$$

$$\text{First}(A) = \{a, b, c, d, g\}$$

② Follow Information

Calculated for Non-terminal symbols of RHS

$$A \rightarrow \alpha \beta \beta$$

$$\text{follow}(B) = \text{first}(\beta)$$

if $\text{first}(\beta)$ contains ϵ

$$\text{follow}(B) = \text{first}(\beta) - \{\epsilon\} \cup \text{follow}(A)$$

$$S \rightarrow aBDh$$

$$B \rightarrow cB'$$

$$B' \rightarrow bB' | \epsilon$$

$$D \rightarrow EF$$

$$E \rightarrow g | \epsilon$$

$$F \rightarrow f | \epsilon$$

	Direct	Follow
S	{a}	{\\$}
B	{c}	{g, h, n}
B'	{b, \epsilon}	{g, h, n}
D	{g, f, \epsilon}	{h}
E	{g, \epsilon}	{f, h}
F	{f, \epsilon}	{h}

* Design of LL(1) Parser

Ex(1) : Grammar \rightarrow (String)
 \downarrow Parser \downarrow

$$S \rightarrow PQR$$

$$P \rightarrow aB|bC$$

$$Q \rightarrow q|\lambda P$$

Step 1 (FIRST)

$$\text{first}(S) = \text{first}(PQR) = \text{first}(P)$$

$$\text{first}(P) = \text{first}(aP) \cup \text{first}(b) \cup \text{first}(c) = \{a, b, c\} = \text{first}(S)$$

$$\text{first}(Q) = \text{first}(q) \cup \text{first}(\lambda P) = \{q, \lambda\}$$

Step 2 (Follow)

$$\text{follow}(S) = \{\$\}$$

$$\text{follow}(P) = \text{first}(q, \lambda) = \text{first}(q) = \{q, \lambda\}$$

$$\text{follow}(q) = \text{follow}(\lambda) = \{\$\}$$

$$\text{follow}(P) = \text{follow}(P) = \{q, \lambda\} = \{q, \lambda\}$$

$$\text{follow}(P) = \text{follow}(q) = \{\lambda\} =$$

Step 3 First - Follow Table

NT	First	Follow
S	{a, b, c}	{\\$}
P	{a, b, c}	{q, \lambda}
q	{q, \lambda}	{\\$}

Step 4 Parse

NF\T	a	b	c	q	r	\$
s	$s \rightarrow Pqr$	$\lambda \rightarrow Pqr$	$\lambda \rightarrow Pqr$			
p	$P \rightarrow qP$	$P \rightarrow b$	$P \rightarrow c$			
q				$q \rightarrow q$	$q \rightarrow qp$	

String $\Rightarrow acabrb$

Buffer	Stack	Action
$\$ r b r c @$	$(\$)$	$s \rightarrow Ps@$
$\$ r b r c @$	$(P)r\$$	$P \rightarrow qP$
$\$ r b r c @$	$(q)qr\$$	Matched
$\$ r b r c @$	$(P)q\$$	$P \rightarrow c$
$\$ r b r c @$	$(C)qr\$$	Matched
$\$ r b @$	$(Q)r\$$	$Q \rightarrow qp$
$\$ r b @$	$(Q)P r (\$)$	Matched
$\$ r @$	$(P)r \$$	$P \rightarrow b$
$\$ r @$	$(B)r \$$	Matched
$\$ @$	$(R)\$$	Matched
$\$$	$\$$	Accepted

Example 2:

$$\begin{aligned} S &\rightarrow Abc | ad \\ A &\rightarrow eS | Cx | E \\ C &\rightarrow f | p | \epsilon \end{aligned}$$

$$J(N(Abc)) = \{e, f, p, \epsilon, \$\}$$

$$J(N(Cx)) = \{f, p, \epsilon\}$$

	$J(\lambda)$	FOLLOW
S	{a, b, e, f, p, \\$}	{b, \\$}
A	{e, f, p, \epsilon, \\$}	{b}
C	{f, p, \epsilon}	{\lambda}

	a	b	c	f	p	r	\$
S	$\Rightarrow Abc$	$\Rightarrow Abc$	$\Rightarrow Abc$	$\Rightarrow Abc$	$\Rightarrow Abc$	$\Rightarrow Abc$	
A		$A \Rightarrow \epsilon$	$A \Rightarrow eS$	$A \Rightarrow Cr$	$A \Rightarrow Cr$	$A \Rightarrow Cr$	
C				$C \Rightarrow f$	$C \Rightarrow p$	$C \Rightarrow \epsilon$	

String $\Rightarrow frbc$

Buffer	Stack	Action
\$ cbNF	$\$ \$$	$S \Rightarrow Abc$
\$ cbNr(f)	(A)bc \$	$A \Rightarrow Cr$
\$ cbNr(f)	(C)bc \$	$C \Rightarrow f$
\$ cbNr(f)	(f)rbc \$	Matched
\$ cbNr	(r)bc \$	Match
\$ b	(r)\$	Match
\$	\$	Match
		Accepted

$SPL \rightarrow C \times b c \quad bc$

\$

* $S \rightarrow S i L U E V E T | a$

$L \rightarrow LS | \epsilon \quad \rightarrow \text{left Recursion}$

$E \rightarrow b$

$T \rightarrow d - e | E$

$L \rightarrow LS | \epsilon$

$L \rightarrow \epsilon L' \Rightarrow L \rightarrow L'$
 $L' \rightarrow SL' | \epsilon$

\Rightarrow

$S \rightarrow S i L U E V E T | a$

$L \rightarrow SL | \epsilon$

$E \rightarrow b$

$T \rightarrow de | \epsilon$

$$\text{first}(S) = \{i, a\}$$

$$\text{first}(L) = \{i, a, \epsilon\}$$

$$\text{first}(E) = \{b\}$$

$$\text{first}(T) = \{d, \epsilon\}$$

$$\text{Follow}(S) = \{\$, i, a, v\}$$

$$\text{Follow}(L) = \{v\}$$

$$\text{Follow}(E) = \{d, e, \$\}$$

Tutorial Question on LL(1) Parsing Technique

$$Q1: S \rightarrow cTUYZ | a$$

$$T \rightarrow TS | c$$

$$Y \rightarrow b | \epsilon$$

$$Z \rightarrow dTe | \epsilon$$

Rule with left Recursion

$$T \rightarrow TS | c$$

Removing left Recursion

$$T \rightarrow cT'$$

$$T' \rightarrow ST' | \epsilon$$

New Production Rules

$$S \rightarrow cTUYZ | a$$

$$T \rightarrow cT'$$

$$T' \rightarrow ST' | \epsilon$$

$$Y \rightarrow b | \epsilon$$

$$Z \rightarrow dTe | \epsilon$$

$$\begin{aligned} \text{first}(S) &= \text{first}(cTUYZ) \cup \text{first}(a) \\ &= \{c\} \cup \{a\} \\ &= \{c, a\} \end{aligned}$$

$$\begin{aligned} \text{first}(T) &= \text{first}(cT') \\ &= \{c\} \end{aligned}$$

$$\begin{aligned} \text{first}(T') &= \text{first}(ST') \cup \text{first}(\epsilon) \\ &= \text{first}(S) \cup \{\epsilon\} \\ &= \{c, a, \epsilon\} \end{aligned}$$

$$\text{First}(Y) = \{b, \epsilon\}$$

$$\text{First}(Z) = \{d, \epsilon\}$$

$$\text{Follow}(S) = \{\$\}$$

$$\begin{aligned}\text{Follow}(T) &= \text{First}(U \vee Z) \\ &= \{u\} = \{u, e\}\end{aligned}$$

$$\begin{aligned}\text{Follow}(T') &= \text{Follow}(T) \\ &= \{u\} = \{u, e\}\end{aligned}$$

$$\begin{aligned}\text{Follow}(Y) &= \text{First}(Z) \\ &= \{d, \epsilon\} \\ &= \{d, \epsilon\} - \{\epsilon\} \cup \text{Follow}(S) \\ &= \{d, \$\}\end{aligned}$$

$$\begin{aligned}\text{Follow}(Z) &= \text{Follow}(S) \\ &= \{\$\} \cup \{c, a, u, \epsilon\}\end{aligned}$$

$$\text{Follow}(T) = \{e\} = \{e, u\}$$

Non Terminal

First set

Follow set

S	$\{c, a\}$	$\{c, a, u, v, e, c, \$\}$
T	$\{c\}$	$\{u, e\}$
T'	$\{c, a, \epsilon\}$	$\{u, e\}$
P	$\{b, \epsilon\}$	$\{c, a, u, v, d, \$\}$
Z	$\{d, \epsilon\}$	$\{c, a, u, e, \$\}$

Q1.	NT	a	b	c	d	e	v	\$
S	$S \rightarrow a$			$S \rightarrow cT \cup \epsilon$				
T				$T \rightarrow cT'$				
Y	$Y \rightarrow \epsilon$	$Y \rightarrow b$	$Y \rightarrow \epsilon$	$Y \rightarrow \epsilon$	$Y \rightarrow \epsilon$	$Y \rightarrow \epsilon$	$Y \rightarrow \epsilon$	$Y \rightarrow \epsilon$
Z	$Z \rightarrow \epsilon$		$Z \rightarrow \epsilon$	$Z \rightarrow dT$	$Z \rightarrow \epsilon$	$Z \rightarrow \epsilon$	$Z \rightarrow \epsilon$	$Z \rightarrow \epsilon$
T'	$T' \rightarrow ST'$		$T' \rightarrow ST'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$		

LR Parser

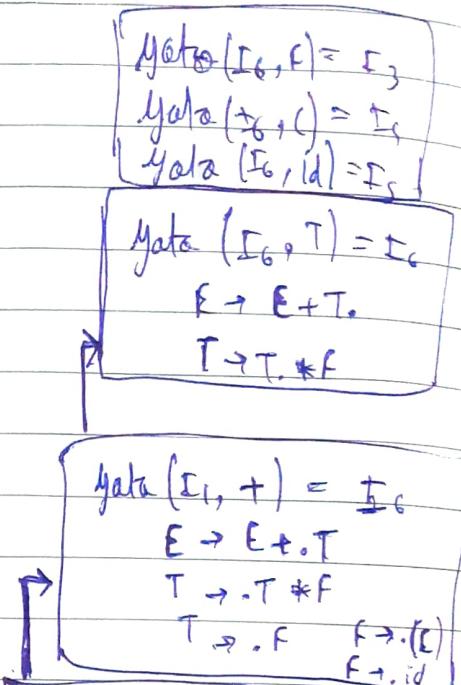
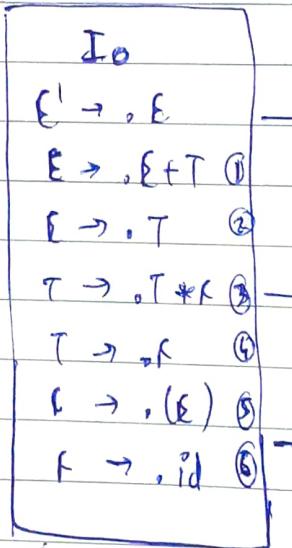
SLR - Simple LR
- LR(0)

Construct - Parser
"Canonical"

- Steps:
- 1) Grammar Augmentation
 - 2) DOT addition
 - 3) Closure : string. $\frac{N_T}{T}$ or

Ex. Grammar

$E \rightarrow E + T$
 $E \rightarrow T$
 $T \rightarrow T * F \Rightarrow$
 ~~$F \rightarrow F$~~
 $F \rightarrow (E)$
 $F \rightarrow id$



$Yata(I_0, +) = I_6$
 $F \rightarrow (E).$

$Yata(I_0, *) = I_7$

$Yata(I_0, id) = I_8$

$Yata(I_0, E) = I_4$
 $F \rightarrow (E.E)$

$E \rightarrow . E + T$

$E \rightarrow . T$

$T \rightarrow . T * F$

$T \rightarrow . F$

$F \rightarrow . (E)$

$F \rightarrow . id$

$Yata(I_0, id) = I_5$
 $F \rightarrow id.$

$Yata(I_0, E) = I_8$
 $F \rightarrow (E.E)$

$E \rightarrow E. + T$

$Yata(I_4, E) = I_4$
 $Yata(I_4, id) = I_5$

$Yata(I_4, T) = I_2$

$Yata(I_4, F) = I_3$

$Yata(I_2, *) = I_7$
 $T \rightarrow T. * F$
 $F \rightarrow . (E)$
 $F \rightarrow . id$

$Yata(I_7, E) = I_{10}$
 $T \rightarrow T. * F.$

$Yata(I_7, C) = I_5$
 $Yata(I_7, id) = I_8$

Parsing table

- Shift
- Reduce

Two Parts

Action → Terminal

go to → Non-terminal

State	Action	go to								
		id	+	*	()	\$	E	T	F
I ₀	S ₅				S ₄			I	2	3
I ₁		S ₆					Accept			
I ₂		R ₂	S ₇		R ₂	R ₂				
I ₃		R ₄	R ₄		R ₄	R ₆				
I ₄	S ₅				S ₄			8	2	3
I ₅		R ₆	R ₆		R ₆	R ₆				
I ₆								9	3	
I ₇	S ₅				S ₄					10
I ₈		S ₆	R ₆		S ₁₁					
I ₉		R ₁	S ₇		R ₁	R ₁				
I ₁₀		R ₃	R ₃		R ₃	R ₃				
I ₁₁		R ₅	R ₅		R ₅	R ₅				



$$\text{Follow}(E) = \{\$, +,)\}$$

$$\text{Follow}(T) = \{\$, +,), *\}$$

$$\text{Follow}(F) = \{\$, +,), *\}$$

No Multiple Entries

⇒ Valid LR(0) / SLR

Ex.

$$S \rightarrow AxB \mid Bc$$

$$A \rightarrow yA \mid z$$

$$B \rightarrow xB \mid \epsilon$$

Step 1:

$$S' \rightarrow S \quad (0)$$

$$S \rightarrow \cdot AxB \quad (1)$$

$$S \rightarrow \cdot Bc \quad (2)$$

$$A \rightarrow \cdot yA \quad (3)$$

$$A \rightarrow \cdot z \quad (4)$$

$$B \rightarrow \cdot xB \quad (5)$$

$$B \rightarrow \cdot \quad (6)$$

Step 2:

$$\text{Closure}(S' \rightarrow \cdot, S) = I_0$$

$$S' \rightarrow S$$

$$S \rightarrow \cdot AxB$$

$$S \rightarrow \cdot Bc$$

$$A \rightarrow \cdot yA$$

$$A \rightarrow \cdot z$$

$$B \rightarrow \cdot xB$$

$$B \rightarrow \cdot$$

$$\text{Follow}(S) = \{ \$ \}$$

$$\text{Follow}(B) = \{ z, c \}$$

$$\text{Follow}(A) = \{ z \}$$

$$\text{Yata}(I_0, S) = I_1$$

$$S' \rightarrow S.$$

$$\text{Yata}(I_0, A) = I_2$$

$$S \rightarrow A \cdot xB$$

$$\text{Yata}(I_0, y) = I_4$$

$$A \rightarrow y \cdot A$$

$$A \rightarrow \cdot yA$$

$$A \rightarrow \cdot z$$

$$\text{Yata}(I_2, n) = I_3$$

$$S \rightarrow A \cdot xB$$

$$B \rightarrow \cdot xB$$

$$B \rightarrow \cdot$$

$$\text{Yata}(I_3, \cdot) = I_5$$

$$S \rightarrow Bc.$$

$$\text{Yata}(I_3, n) = I_6$$

$$A \rightarrow yA.$$

$$\text{Yata}(I_0, z) = I_5$$

$$A \rightarrow z.$$

$$\text{Yata}(I_0, z) = I_6$$

$$B \rightarrow x \cdot B$$

$$B \rightarrow x \cdot n$$

$$B \rightarrow \cdot$$

$$\text{Yata}(I_4, y) = I_7$$

$$\text{Yata}(I_4, z) = I_5$$

$$\text{Yata}(I_6, B) = I_{10}$$

$$B \rightarrow x \cdot B.$$

	x	y	z	c	$\$$	s	A	B
I_0	s_6	s_4	s_5	x_6	x_6			
I_1						Accept		
I_2	s_7							
I_3			s_8					
I_4		s_4	s_5					
I_5	r_4							
I_6	s_6			x_6	x_6			
I_7	s_6			x_6	x_6			

• String Parser Using Stack

String $w = yzxn$

$w \in yzxn\$$

Number \Rightarrow state Stack	Buffer	Action
0	$yzxn\$$	$\text{Table}(0, y) = s_4$
$0y4$	$zx\$$	$\text{Table}(4, z) = s_5$
$0y4z5$	$xn\$$	$\text{Table}(5, x) = r_4$
$0y4zA9$	$nx\$$	$\text{Table}(9, n) = R_3$
$0A2$	$xn\$$	$\text{Table}(2, x) = s_7$
$0Axnx7$	$n\$$	$\text{Table}(7, n) = s_6$
$0Axnx7x6$	$\$$	$\text{Table}(6, \$) = x_6$
$0A7x7Bx1$	$\$$	$\text{Table}(11, \$) = x_1$
$0S1$	$\$$	Accept

Given Production Rules

$$E \rightarrow E + T \quad ①$$

$$E \rightarrow T \quad ②$$

$$T \rightarrow T * F \quad ③$$

$$T \rightarrow F \quad ④$$

$$F \rightarrow (E) \quad ⑤$$

$$F \rightarrow id \quad ⑥$$

Parsing Table

State	Action							Yoto		
	id	+	*	()	\$	E	T	F	
0	S5				S4			1	2	3
1		S6					Accept			
2		R2	S7			R2	R2			
3		R4	R4			R4	R4			
4	S5			S4				8	2	3
5		R6	R6		R6	R6				
6	S5			S4				9	3	
7	S5			S4						10
8		S6			S11					
9		R1	S7		R1	R1				
10		R3	R3		R3	R3				
11		R5	R5		R5	R5				

String $w = id * id + id \$$

CLR Parsing / LR(1) Parsing

Canonical LR Stack

$LR(1)$	\rightarrow	Extension of $LR(0)$
$G \rightarrow N^*$ ($LR(0)$)	$\left \begin{array}{l} \text{Conflict} \\ \text{- Shift + Reduce} \end{array} \right.$	
$\rightarrow LP(1)$	$\left \begin{array}{l} \text{- Reduce + Reduce} \end{array} \right.$	

$LR(1) \rightarrow$ optimise $LR(0)$ Shift - Red. Conflict
operator overloading

* $S \rightarrow CC$

$C \rightarrow eC \mid d$

solⁿ: Step 1 - Augments

$S' \rightarrow .S$ ⑥

$S \rightarrow .CC$ ①

$C \rightarrow .eC$ ②

$C \rightarrow .\emptyset$ ③

Step 2:

Closure of $(S' \rightarrow S, \$) = I_0$

$S' \rightarrow .S, \$$

$S \rightarrow .(C, \$) \quad T_{\text{first}}(C) = \{e, d\}$

$C \rightarrow .eC, eCd$

$C \rightarrow .\emptyset, C/d$

$\text{Mata}(I_0, S) = I_1$

$S' \rightarrow S., \$$

$\text{Mata}(I_0, C) = I_2$

$S \rightarrow (.C, \$)$

$C \rightarrow .eC, \$$

$C \rightarrow .\emptyset, \$$

$\text{Yata } (I_0, e) = I_3$

$C \rightarrow \underline{e.C}, e/d$

$C \rightarrow .eC, e/d$

$C \rightarrow .d$

$\text{Yata } (I_0, d) = I_4$

$C \rightarrow d., e/d$

$\text{Yata } (I_2, c) = I_5$

$S \rightarrow C(.), \$$

$\text{Yata } (I_2, e) = I_6$

$C \rightarrow eC, \$$

$C \rightarrow .eC, \$$

$C \rightarrow .d$

$\text{Yata } (I_2, d) = I_7$

$C \rightarrow d., \$$

State	e	d	\$	s	c
I_0	s_3	s_4		1	2
I_1			Accept		
I_2	s_6	s_7			5
I_3	s_3	s_4			8
I_4	r_3	r_3			
I_5				r_1	
I_6	s_6	s_7			9
I_7			s_3		
I_8	r_2	r_2			
I_9			s_2		

LALR

↳ Look Ahead

I_{3c}

$C \rightarrow e.C \quad e/d/\$$

$C \rightarrow .eC \quad e/d/\$$

$C \rightarrow .d \quad e/d/\$$

I_{4c}

I_{5c}

$C \rightarrow d. \quad e/d/\$ \quad C \rightarrow d. \quad e/d/\$$

Ex:

$$A \rightarrow aCDg | aBg | \epsilon$$

$$D \rightarrow d | c$$

$$B \rightarrow e | \epsilon$$

$$C \rightarrow Ct | p | BD | \lambda AB | \epsilon$$

$$A' \rightarrow A$$

$$A \rightarrow .aCDg \quad ①$$

$$A \rightarrow .aBg \quad ②$$

$$A \rightarrow . \quad ③$$

$$D \rightarrow .d \quad ④$$

$$D \rightarrow . \quad ⑤$$

$$B \rightarrow .e \quad ⑥$$

$$B \rightarrow . \quad ⑦$$

$$C \rightarrow .Ct \quad ⑧$$

$$C \rightarrow .p \quad ⑨$$

$$C \rightarrow .BD \quad ⑩$$

$$C \rightarrow .\lambda AB \quad ⑪$$

$$C \rightarrow . \quad ⑫$$

Closure of $A' \rightarrow .A, \$ = I_a$

$$A' \rightarrow .A, \$$$

$$A \rightarrow .aCDg, \$$$

$$A \rightarrow .aBg, \$$$

$$A \rightarrow . , \$$$

$$Hata(I_a, A) = I_a$$

$$A' \rightarrow A., \$$$

$$yota(I_0, a) = I_2$$

$$A \rightarrow a \cdot CDg, \$$$

$$A \rightarrow a \cdot Bg, \$$$

$$B \rightarrow \cdot e, g, d, q, t$$

$$B \rightarrow \cdot ., g, d, q, t$$

$$C \rightarrow \cdot ct, d, q, t$$

$$C \rightarrow \cdot p, d, q, t$$

$$C \rightarrow \cdot BD, d, q, t$$

$$C \rightarrow \cdot \lambda AB, d, q, t$$

$$C \rightarrow \cdot ., d, q, t$$

$$yota(I_2, C) = I_3$$

$$A \rightarrow ac \cdot Dg, \$$$

$$C \rightarrow c \cdot t, d, q, t$$

$$D \rightarrow \cdot d, q$$

$$D \rightarrow \cdot ., q$$

$$yota(I_2, B) = I_4$$

$$A \rightarrow aB \cdot g, \$$$

$$C \rightarrow B \cdot D, d, q, t$$

$$D \rightarrow \cdot d, d, q, t$$

$$D \rightarrow \cdot ., d, q, t$$

$$yota(I_2, E) = I_5$$

$$B \rightarrow e, g, d, q, t$$

$$yota(I_2, P) = I_6$$

$$C \rightarrow p, d, q, t$$

~~$$yota(I_2, X) = I_7$$~~

~~$$C \rightarrow \lambda AB, d, q, t$$~~

~~$$A \rightarrow \cdot ac$$~~

$$yota(I_2, R) = I_7$$

$$C \rightarrow \lambda AB, d, q, t$$

$$A \rightarrow a \cdot Cg, e, d, q, t$$

$$A \rightarrow \cdot aBg, e, d, q, t$$

$$yota(I_3, D) = I_8$$

$$A \rightarrow QCD \cdot g, \$$$

$$yota(I_3, t) = I_9$$

$$E \rightarrow ct, d, q, t$$

$$yota(I_3, d) = I_{10}$$

$$D \rightarrow d, ., q$$

$$yota(I_4, g) = I_{11}$$

$$A \rightarrow aBg, \$$$

$$yota(I_4, D) = I_{12}$$

$$C \rightarrow BD, d, q, t$$

$$yota(I_4, d) = I_{13}$$

$$D \rightarrow d, ., d, q, t$$

$$yoto(I_7, \lambda) = I_4$$

$$C \rightarrow \lambda A \cdot B \quad , d, q, t$$

$$B \rightarrow \cdot e \quad , d, q, t$$

$$e \rightarrow \cdot \quad , d, q, t$$

$$yoto(I_7, \alpha) = I_{15}$$

$$A \rightarrow \alpha \cdot CDq \quad e, d, q, t$$

$$A \rightarrow \alpha \cdot Bg \quad e, d, q, t$$

$$B \rightarrow \cdot e \quad g, d, q, t$$

$$B \rightarrow \cdot \quad g, d, q, t$$

$$C \rightarrow \cdot Ct \quad d, q, t$$

$$C \rightarrow \cdot P \quad d, q, t$$

$$C \rightarrow \cdot BD \quad d, q, t$$

$$C \rightarrow \cdot \lambda AB \quad d, q, t$$

$$C \rightarrow \cdot \quad d, q, t$$

$$yoto(I_8, \alpha) = I_{16}$$

$$A \rightarrow \alpha CDq \quad , \$$$

$$yoto(I_4, B) = I_{17}$$

$$C \rightarrow \cancel{\lambda} B \cdot \quad , d, q, t$$

$$yoto(I_5, C) = I_{18}$$

$$A \rightarrow \alpha C \cdot Dq \quad e, d, q, t$$

$$D \rightarrow \cdot d \quad , q$$

$$D \rightarrow \cdot \quad , q$$

$$yoto(I_5, B) = I_{19}$$

$$A \rightarrow \alpha B \cdot g \quad e, d, q, t$$

$$C \rightarrow \beta \cdot D \quad d, q, t$$

$$D \rightarrow \cdot d \quad d, q, t$$

$$D \rightarrow \cdot \quad d, q, t$$

$$yoto(I_{15}, e) = I_5$$

$$yoto(I_{15}, p) = I_6$$

$$yoto(I_{15}, \lambda) = I_7$$

$$yoto(I_{18}, D) = I_{20}$$

$$A \rightarrow \alpha C D \cdot g \quad , e, d, q, t$$

$$yoto(I_{18}, d) = I_{20}$$

$$yoto(I_{19}, g) = I_{21}$$

$$A \rightarrow \alpha B \cdot g \quad , e, d, q, t$$

$$yoto(F_{19}, D) = I_{12}$$

$$yoto(F_{19}, d) = I_{13}$$

$$yoto(I_{20}, q) = I_{22}$$

~~$$A \rightarrow \alpha C D \cdot g \quad , e, d, q, t$$~~

$$A \rightarrow \alpha C D q \quad , e, d, q, t$$

For LALR parser sets are

$$I_2 = I_{15} \Rightarrow I_{215}$$

$A \rightarrow a \cdot CDq$	$\$, e, d, q, t$
$A \rightarrow a \cdot Bg$	$\$, e, d, q, t$
$B \rightarrow \cdot e$	g, d, q, t
$B \rightarrow \cdot$	g, d, q, t
$C \rightarrow \cdot Ct$	d, f, t
$C \rightarrow \cdot p$	d, q, t
$C \rightarrow \cdot BD$	d, q, t
$C \rightarrow \cdot \lambda AB$	d, q, t
$C \rightarrow \cdot$	d, q, t

$$I_3 = I_{18} = I_{318}$$

$A \rightarrow ac \cdot Dq$	$\$, e, d, q, t$
$D \rightarrow \cdot d$	$, q$
$D \rightarrow \cdot$	$, q$

$$I_4 = I_{19} = I_{419}$$

$A \rightarrow aB \cdot g$	$\$, e, d, q, t$
$C \rightarrow B \cdot D$	$, d, q, t$
$D \rightarrow \cdot d$	$, d, q, t$
$D \rightarrow \cdot$	$, d, q, t$

$$I_8 = I_{20} = I_{820}$$

$A \rightarrow aCD \cdot f$	$\$, e, d, q, t$
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$$I_{16} = I_{22} = I_{1622}$$

$A \rightarrow acDq$	$\$, e, d, q, t$
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Parser Table

state	a	q	g	d	e	t	p	x	\$	A	B	C	D
0	S ₂₁₅								λ ₃	1			
1										Accept			
215	λ ₇ , λ ₁₁	λ ₇	λ ₇ , λ ₁₁	S ₅	λ ₇ , λ ₁₁	S ₆	S ₇			4B	318		
318	λ ₅		S ₁₀		S ₉					6		820	
419	λ ₅ , S ₁₁		λ ₅		λ ₅						12		
5	λ ₆	λ ₆	λ ₆		λ ₆								
6	λ ₉		λ ₉		λ ₉								
7	S ₂₁₅								S ₁₄				
820		S ₁₆₂₂											
9	λ ₈		λ ₈		λ ₈								
10	λ ₄												
11									λ ₂				
12	λ ₁₀		λ ₁₀		λ ₁₀								
13	λ ₄		λ ₄		λ ₄								
14	λ ₇		λ ₇		λ ₇						17		
1622	λ ₁		λ ₁		λ ₁					λ ₁			
17	λ ₁₁		λ ₁₁		λ ₁₁								
21	λ ₂		λ ₂	λ ₂	λ ₂	λ ₂							