Homomorphic Encryption: Evaluating its current uses

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Why Homomorphic Encryption?

Consumers are increasingly concerned about data privacy

How can businesses leverage on big data while being cautious of data privacy?



Why Homomorphic Encryption?

Homomorphic Encryption is a Privacy-Enhancing Technology that can achieve Data Privacy

History of Homomorphic Encryption

- Rather new technology; 30+ years since developed
- Limited commercial applications due to lack of specialist knowledge and standardisations
- In recent years, tech leaders (IBM, Google, Microsoft) are pushing for their widespread use

Homomorphic Encryption (HE)

- Based on Homomorphisms, a special type of mathematical function
- Fundamentally different from current encryption systems like RSA or AES
- Quantum-resistant: RSA is vulnerable is a post-quantum world, but Homomorphic Encryption is not

Homomorphisms

$$Enc(a) + Enc(b) = Enc(a + b)$$

"property-preserving" function

Homomorphisms

$$Enc(a) + Enc(b) = Enc(a + b)$$

Adding encrypted messages

Adding unencrypted messages

"property-preserving" function

Homomorphic Encryption (HE)

- Property-preserving encryption
- Able to run algorithms on encrypted data
- Results will be as if the algorithms were run on the raw, unencrypted data

A Common Scenario

- Client Company A: owns the raw data
- Server Company B: owns the software/ analytics ability

- Both parties are unwilling to share with each other

Solution: Homomorphic Encryption

- 1. Client encrypts raw data
- 2. Client sends encrypted data to server
- 3. Server computes on encrypted data
- 4. Server returns encrypted results to client
- 5. Client decrypts results

Result is as if server performed computations on raw data

Data is encrypted for the server

Pros & Cons of HE

Benefits	Disadvantages
Allows computations on encrypted data	Significantly slower than non-homomorphic encryption
Resolves the data privacy conflict between data owners and analytics companies	Lack of readily-available toolkits and standardisations (still in development!)
	Inherently not CCA-secure, which limits its applications

Key Applications of HE

Healthcare analytics

 Companies and governments holding sensitive data can outsource the analytics

Encrypted search

Search can be done by only indexing encrypted data

End-to-end verifiability in voting systems

Elections can be audited without revealing votes

Security Problems of Homomorphic Encryption

Adding any two ciphertexts A and B together will result in a **valid ciphertext** C. This property-preserving function of HE is known as ciphertext **malleability**.

Given the ciphertexts of A, B and C, attackers can discover that C = A + B. Attackers know the relationship between the ciphertexts.

Actual value of C is protected since actual values of A and B are not known.

However, what if the attacker can know A and B?

Then, the security of the HE scheme is compromised.

Data owners need to ensure that the raw data cannot be easily accessible.

However, applications can be very complex and include multi-party communication. Rich data flows could lead to inadvertent data leaks.

HE is still safe for pure outsourcing (one client one server) scenarios.

Secondly, HE does not provide integrity checks.

The attacker can simply double every data point using homomorphic operations, changing the entire database.

Currently, the only solution is to use canaries to detect these modifications.

Developing applications using Homomorphic Encryption

Types of HE

- HE is a broad class of encryption systems
- Partially HE: Some systems are only homomorphic for addition only or multiplication only, but not both
- Somewhat HE: Some systems only support a limited number of operations
- Fully HE: The most theoretically correct but also not practical to use

Common HE schemes

DGHV, BGV, BFV, CKKS (named after the researchers who developed them)

Decide on a scheme based on the data type and operations needed

 E.g. CKKS is an approximated-scheme that supports decimal operations

Brakerski/Fan-Vercauteren (BFV)

One of the more commonly-implemented HE schemes.

Based on the Ring Learning with Error (RLWE) problem that is computationally hard to solve.

Supports both public-key and symmetric encryption.

BFV

Encryption adds **noise** to the messages

 Without the key, it is difficult to decrypt the noisy messages

Noise grows during computation process

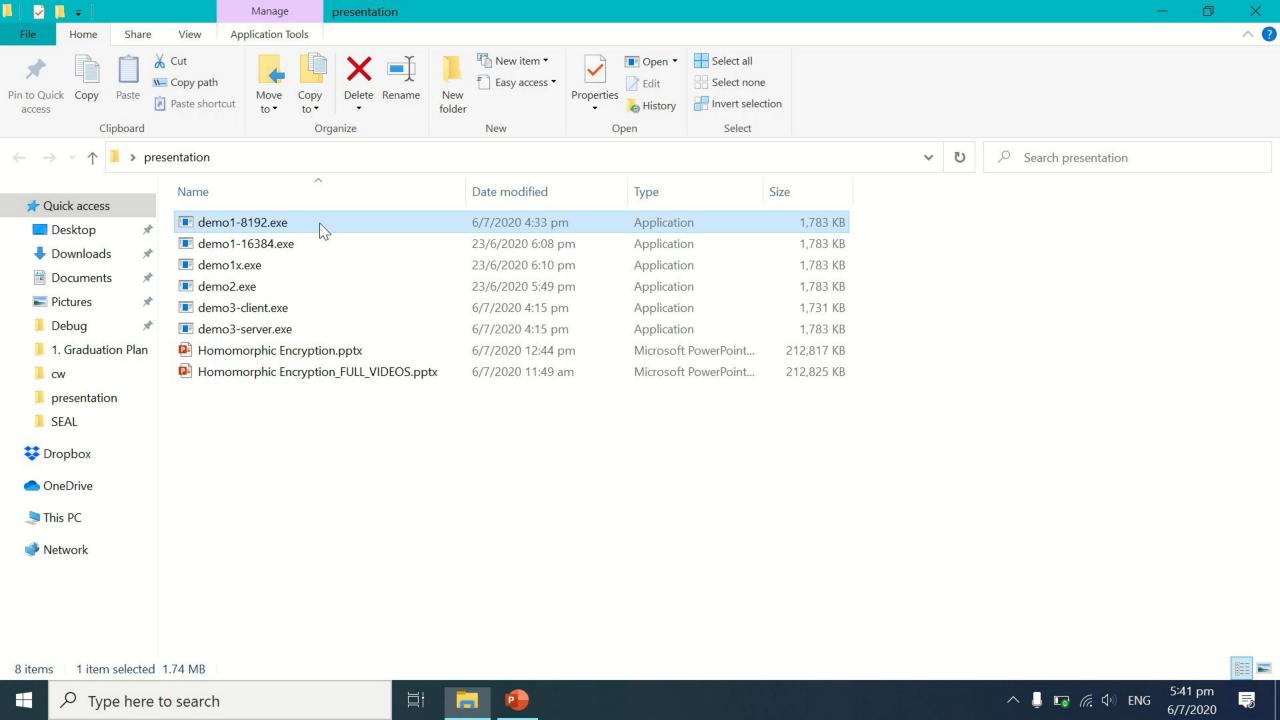
- Adding two ciphertexts: negligible growth
- Multiplying two ciphertexts: noise almost doubles

BFV

Once noise exceeds threshold, it is not possible to decrypt the message correctly

Able to "reset" the noise by bootstrapping

- Decrypt and re-encrypt the messages
- Very expensive operation (HE is slow)



```
C:\Users\Joyce\Desktop\presentation\demo1-8192.exe
Microsoft SEAL version: 3.5.3
         Demo 1: Noise growth in BFV encryption
  Encryption parameters :
    scheme: BFV
   poly_modulus_degree: 8192
    coeff modulus size: 218 (43 + 43 + 44 + 44 + 44) bits
    plain modulus: 2048
Parameter validation (success): valid
\sim\sim\sim\sim Calculate (x^4+1) for x = 6 \sim\sim\sim\sim
STEP 1 -->
Express x = 6 as a hexadecimal plaintext polynomial 0x6.
STEP 2 -->
Encrypt the plaintext.
   + number of polynomials (size) of freshly encrypted x: 2
   + noise budget in freshly encrypted x: 155 bits
STEP 3 -->
First, compute x_{square}(x^2).
   + number of polynomials (size) of x square: 3
   + noise budget in x square: 132 bits
STEP 4 -->
Then, compute x fourth (x^4).
   + number of polynomials (size) of x_fourth: 5
   + noise budget in x_fourth: 101 bits
   + multiplication roughly doubles the size of the ciphertext
STEP 5 -->
Next, add 1 to the result (x^4 + 1).
   + number of polynomials (size) of x fourth plus one: 5
   + noise budget in x_fourth_plus_one: 101 bits
   + addition is a negligible operation and does not have a large effect on the noise
STEP 6 -->
    + decryption of encrypted result: 0x511 ..... expected was 0x511
```

demo1: Summary of Steps

- 1. Encrypt plaintext x to get Enc(x)
- 2. $Enc(x^2) = Enc(x) * Enc(x)$
- 3. $Enc(x^4) = Enc(x^2) * Enc(x^2)$
- 4. $Enc(x^4 + 1) = Enc(x^4) + Enc(1)$
- 5. Get a ciphertext representing $Enc(x^4 + 1)$
- 6. Decrypt the ciphertext to get $x^4 + 1$

demo1: Summary of Steps

1. Encrypt plaintext x to get Enc(x)

2.
$$\operatorname{Enc}(x^2) = \operatorname{Enc}(x) * \operatorname{Enc}(x)$$

- 3. $\operatorname{Enc}(x^4) = \operatorname{Enc}(x^2) * \operatorname{Enc}(x^2)$
- 4. $Enc(x^4 + 1) = Enc(x^4) + Enc(1)$

Homomorphic operations

- 5. Get a ciphertext representing $Enc(x^4 + 1)$
- 6. Decrypt the ciphertext to get $x^4 + 1$

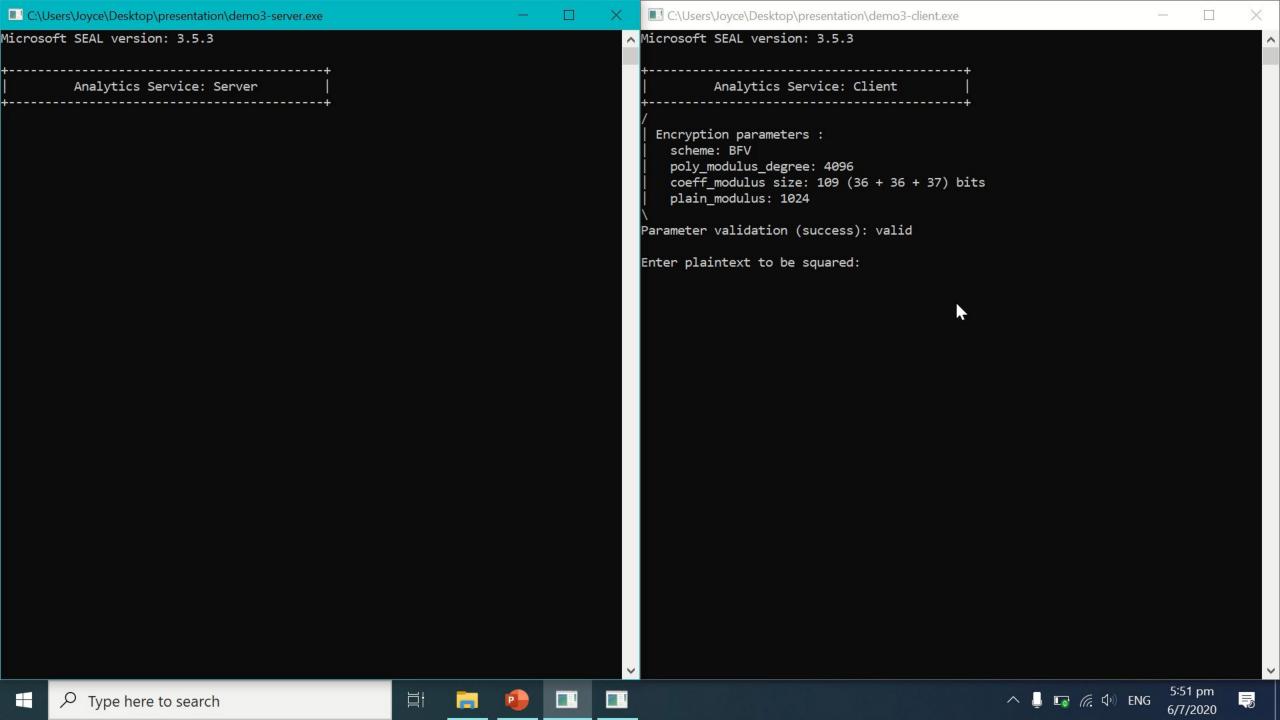
demo1: Size and noise budget changes

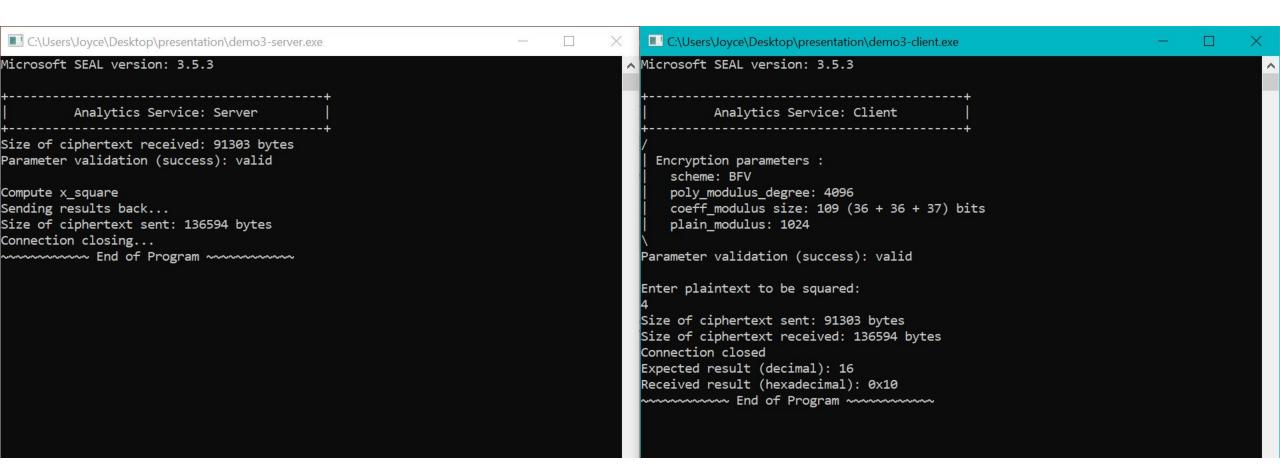
Ciphertext	Size (number of polynomials)	Noise budget (Remaining noise space)
X	2	54
x^2	3	31
x ⁴	5	2
$x^4 + 1$	5	2

demo: client-server model

Client encrypts raw data, and holds encryption key

Server does not have access to raw data and encryption keys





demo: Space consumption of data

Large increase in space consumption

- Unencrypted integers = 4 bytes
- After encryption, 100 000 bytes
- Not very scalable for large data sets

Problems with SEAL::BFV

Limited practical use

- Lack of functionality Only primitive operations are available (addition, multiplication)
- Encryption and decryption takes up data owner's resources

Trade-off between spending resources on encryption vs spending resources on computation and analytics

Problems with SEAL::BFV

A rather low-level library working with polynomial operations

- Developers need to have an understanding of how to represent the data in polynomials
- To select the BFV parameters, there is a need to estimate the computations results beforehand
- Difficult to adapt existing machine learning models to HE libraries

Moving Forward with HE

Still a research-level technique.

Have to solve fundamental issues like **making basic operations faster**.

Ultimately, the goal is to create data-agnostic software with generic analytics capabilities.

More about the Development Environment

Done using native C++ on Windows

SEAL library with BFV encryption

Homomorphic for addition and multiplication

Server is on only localhost, and communicates with Client via WinSock

For Developers

Libraries:

- PALISADE (a collaboration by various universities)
- **SEAL** (Microsoft)
- HELib (IBM)
- Private Join and Compute (Google)

Thank You!