

Heterogeneous LoRA for Federated Fine-tuning of On-Device Foundation Models

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Abstract

Foundation models (FMs) adapt well to specific domains or tasks with fine-tuning, and federated learning (FL) enables the potential for privacy-preserving fine-tuning of the FMs with on-device local data. For federated fine-tuning of FMs, we consider the FMs with small to medium parameter sizes of single digit billion at maximum, referred to as *on-device FMs (ODFMs)* that can be deployed on devices for inference but can only be fine-tuned with parameter efficient methods. In our work, we tackle the data and system heterogeneity problem of federated fine-tuning of ODFMs by proposing a novel method using heterogeneous low-rank approximations (LoRAs), namely HETLORA. First, we show that the naive approach of using homogeneous LoRA ranks across devices face a trade-off between overfitting and slow convergence, and thus propose HETLORA, which allows *heterogeneous ranks* across client devices and efficiently aggregates and distributes these heterogeneous LoRA modules. By applying rank self-pruning locally and sparsity-weighted aggregation at the server, HETLORA combines the advantages of high and low-rank LoRAs, which achieves improved convergence speed and final performance compared to homogeneous LoRA. Furthermore, HETLORA offers enhanced computation efficiency compared to full fine-tuning, making it suitable for federated fine-tuning across heterogeneous devices.

1 Introduction

The emerging foundation models (FMs) (Bommasani et al., 2022; Zhou et al., 2023; Radford et al., 2021; Devlin et al., 2019; OpenAI, 2023; Google, 2022; Touvron et al., 2023; Brown

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et al., 2020; Google, 2022; Driess et al., 2023; Google, 2023) have shown remarkable zero/few shot learning capabilities, performing well on a variety of tasks including text/image generation with prompts, language translation, solving math problems, and conversing in natural language. Standard FMs, however, demand costly resources for directly fine-tuning their entire parameter space. To tackle this issue, many recent works have proposed different parameter-efficient fine-tuning (PEFT) methods of FMs such as prompt tuning (Lester et al., 2021), utilizing adapters (Houlsby et al., 2019), or low-rank adaptation (LoRA) of the original model (Hu et al., 2021) which freezes the original pre-trained parameters of the FM and train additional, smaller number of parameters instead.

These PEFT methods, however, assume that i) FMs are deployed to and trained with the data of a *single* machine/client for adaptation to the downstream task and that ii) the client has enough resources to even fit a standard FM of hundred billion size for, at least, inference. In practice, there are frequently cases where we are interested in fine-tuning FMs for on-device private data that is distributed across multiple devices (clients). For instance, sensitive and private data such as medical information or law-related documents may be hard to collect centrally in a private manner and fine-tuning of the FMs may need to be done at the edge (Manoel et al., 2023; Shoham and Rappoport, 2023; Zhang et al., 2023c).

In our work, we focus on such federated fine-tuning scenarios, where we train a set of parameters collaboratively across clients to obtain a global set of parameters that can be plugged in to the FM for the targeted downstream task. Note that federated fine-tuning is orthogonal to personalization of FMs in federated learning (FL) (Guo et al., 2023), which

	Zero-Shot	Few-Shot	Full-Training
PaLM 2 XXS	2930.23	2541.86	23.71
PaLM 2 XS	2712.86	481.95	18.32

Table 1: Perplexity of PaLM 2 for zero-shot, few-shot (5 communication rounds), and full federated fine-tuning (200 communication rounds) for chat response on the multi-session chat data (further experimental details are in Section 4.)

aims to train parameters that perform well for individual clients rather than general downstream tasks. We also define *on-device FMs (ODFMs)* as models with few billion parameters at max that are able to fit into memory on limited capacity clients considering current hardwares.

Federated fine-tuning of ODFMs entails unique challenges non-present in either the standard PEFT of FMs or the standard federated training of models that are not FMs. First, FMs have their zero/few-shot learning capability often supported by their large parameter space that is trained on massive data. However, as we show in Table 1 and also presented by previous literature (Kojima et al., 2022), FMs’ performance deteriorates as their sizes get smaller and federated fine-tuning may not merely be useful but *inevitable* for ODFMs to perform well for downstream tasks on devices.

Moreover, devices have limited and heterogeneous system capabilities (Wang et al., 2019; Bonawitz et al., 2016) and data distributions (Sahu et al., 2020). A suitable PEFT method that flexibly adapts to such heterogeneity across devices should be investigated for federated fine-tuning of ODFMs. Previous work evaluated PEFT with FL via performing a general evaluation over different PEFT methods naïvely combined with FL (Guo et al., 2022; Zhang et al., 2023d; Chen et al., 2022; Wortsman et al., 2023; Yu et al., 2023). However, they do not consider the practical setting for ODFMs where PEFT methods are catered to the system and data heterogeneity of clients.

In our work, we focus on one of the most prominent PEFT methods, LoRA (Hu et al., 2021) which proposes to train low-rank approximations of the original model. Using LoRA, the number of trainable parameters is greatly reduced to at most 0.02% of the original ODFM size (see Table 2). The simplest way to apply LoRA to federated fine-tuning is training with homogeneous rank r across the clients as one would train any global model with FL. However, this does not cater to the heterogeneity in FL, where it is even difficult to choose the

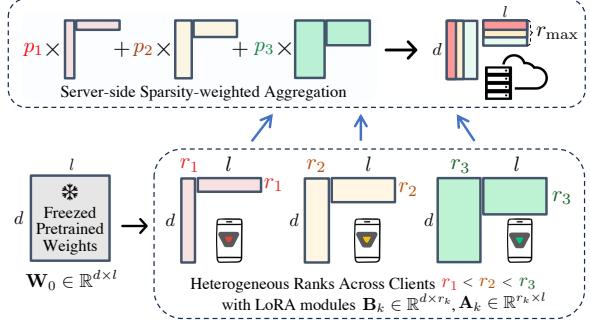


Figure 1: Overview of heterogeneous rank deployment of LoRA: the pretrained weights \mathbf{W}_0 are stored on-device and heterogeneous ranks are assigned to different clients with $r_{\min} = r_1 < r_2 < r_3 = r_{\max}$. In our proposed HETLORA, the server receives the trained heterogeneous LoRA modules and aggregates them with sparsity-weighted aggregation to update the global LoRA module.

right LoRA rank for resource limited mobile devices with natural system and data heterogeneity.

To this end, we propose heterogeneous LoRA, namely HETLORA in short, for federated fine-tuning to cater to system and data heterogeneity and outperform the naïve combination of LoRA and federated fine-tuning where homogeneous ranks are applied across clients. We show the performance of PaLM 2 (Google, 2023) of XXS and XS size for chat responses on the multi-session chat data (Xu et al., 2021) and text summarization for the Reddit data (Völske et al., 2017), both which are real world data from clients. Our contributions can be summarized as follows:

- We propose HETLORA that can apply different rank LoRA modules to different clients to cater to the heterogeneous system capabilities and data complexities of the clients, via utilizing rank self-pruning and sparsity-weighted aggregation.
- We show the performance of naïvely applying LoRA with homogeneous ranks across clients for federated fine-tuning, and show that while large ranks help in speeding-up training, they lead to faster overfitting while smaller ranks are slower in training but does not suffer from overfitting.
- We then evaluate HETLORA to show that it outperforms naïvely applying homogeneous ranks across clients in terms of both training speed, communication/computation efficiency, and final performance, gaining the best of both worlds of homogeneous LoRA with high and low ranks.

	$r = 1$	$r = 5$	$r = 10$	$r = 20$	$r = 50$	$r = 100$	$r = 150$	$r = 200$
PaLM 2 XXS, PaLM 2 XS	0.02%	0.11%	0.21%	0.42%	1.05%	2.10%	3.14%	4.19%

Table 2: Percentage of the LoRA parameters’ size for different ranks r compared to the original pre-trained ODFM’s parameter size. Even for large ranks such as $r = 200$ the trainable LoRA parameters’ size compared to the original pre-trained ODFM size is less than 5% for both PaLM 2-XS and PaLM 2-XXS.

2 Related Work

Parameter-Efficient Fine Tuning. There has been a plethora of recent work on PEFT which either trains a subset of parameters within the existing FM whilst other parameters are freezed or introduces an additional set of trainable parameters whilst keeping the original FM freezed. For the former, methods such as head or bias fine-tuning (Wei et al., 2021; Bu et al., 2022; Lee et al., 2019; Zaken et al., 2021) has been explored, while for the latter, methods such as adapters (Houlsby et al., 2019), prompt (Lester et al., 2021) or prefix-tuning (Li and Liang, 2021), and low-rank approximation (Hu et al., 2021) has been proposed. While these number of methods has been proven to perform as well as full model fine-tuning with just a few number of parameters for the centralized setting, it has not been thoroughly explored how these methods perform for a much smaller FM such as ODFMs, in the decentralized setting where clients’ system-capacities can be heterogeneous and much limited.

Federated Fine-Tuning. Recently, interest in the intersection of FMs and FL has notably increased (Zhou et al., 2023; Yu et al., 2023). Many recent work has proposed to combine the PEFT methods devised for the centralized setting to FL such as training prompts or adapters collaboratively with FL (Guo et al., 2022; Chen et al., 2022; Zhang et al., 2023a; Shysheya et al., 2023; Legate et al., 2023). Another line of work has proposed to perform a few-shot or nearly zero-shot training of FMs with FL for improved communication-efficiency (Wortsman et al., 2023; Zhang et al., 2023d). However, these work either overlooks that most devices do not have the resource to fit a general FM (Touvron et al., 2023; Brown et al., 2020) (>8 B parameters) even for inference or does not consider the heterogeneous system capacities of the clients. It is detrimental to consider these factors since FMs that actually fits to the devices in FL are much smaller, making them weaker in the general intelligence capabilities, and also hetero-

geneous system capacities may prohibit deploying same sized PEFT parameters across clients.

Only a few number of recent work has looked in to using LoRA for FL. For instance, in (Babakniya et al., 2023), the importance of the initialization for the LoRA modules is evaluated where they propose to train the LoRA modules with FL and then perform singular value decomposition (SVD) to gain a good initialization of the LoRA modules. However, the training process of LoRA itself is not altered to adapt to heterogeneous system capabilieis of devices. Another recent work (Yi et al., 2023) has evaluated LoRA in the context of personalized FL, but other than applying LoRA to personalization, the LoRA method itself is, again, not changed. Our work proposes heterogeneous LoRA for federated fine-tuning where heterogeneous ranks are deployed and trained across clients by a new algorithm that includes rank self-pruning and sparsity weighted aggregation.

3 Federated Fine-Tuning with LoRA

3.1 Preliminaries

Formally, we define the pre-trained ODFM as $\mathbf{W}_0 \in \mathbb{R}^{d \times l}$ and the trainable low-rank decomposed matrix as $\Delta\mathbf{W} \in \mathbb{R}^{d \times l}$. In standard LoRA (Hu et al., 2021) under the centralized setting, the low-rank decomposition of $\Delta\mathbf{W}$ is constructed such that $\Delta\mathbf{W} = \mathbf{B}\mathbf{A}$ where $\mathbf{B} \in \mathbb{R}^{d \times r}$ and $\mathbf{A} \in \mathbb{R}^{r \times l}$ are the low rank decomposition of $\Delta\mathbf{W}$ with identical rank r . Now, let us consider LoRA for federated fine-tuning where there are M total clients. Each client $k \in [M]$ has private data \mathcal{B}_k and its corresponding local empirical loss function $F_k(\mathbf{W}) = \frac{1}{|\mathcal{B}_k|} \sum_{\xi \in \mathcal{B}_k} \ell(\mathbf{W}, \xi)$, where $\ell(\mathbf{W}, \xi)$ is the loss for model \mathbf{W} at data sample ξ . The optimization task for federated fine-tuning is to collaboratively find the global parameters which we define as $\bar{\mathbf{B}}$ and $\bar{\mathbf{A}}$, given the pretrained knowledge \mathbf{W}_0 that can minimize the global objective $F(\bar{\mathbf{W}}) = \frac{1}{M} \sum_{k=1}^M F_k(\bar{\mathbf{W}})$ where $\bar{\mathbf{W}} = \mathbf{W}_0 + \bar{\mathbf{B}} \bar{\mathbf{A}}$. Later in the paper, when

introducing heterogeneous LoRA we truncate the LoRA modules' rank dimension, for example from $\mathbf{B} \in \mathbb{R}^{d \times r}$, $\mathbf{A} \in \mathbb{R}^{r \times l}$ to $\mathbf{B}' \in \mathbb{R}^{d \times r'}$, $\mathbf{A}' \in \mathbb{R}^{r' \times l}$ where $r' < r$. Throughout the paper, we denote such truncation of a matrix with the $:$ symbol for each row and column at the subscript. For instance, for truncation to $r' < r$ at the column for the matrix $\mathbf{B} \in \mathbb{R}^{d \times r}$, we keep all the columns until r' and omit the last $r - r'$ columns and denote the resulting matrix it as $\mathbf{B}_{:,r'}$.

3.2 Naïve Case: Homogeneous LoRA

A straightforward way to perform federated fine-tuning with LoRA is to train the LoRA modules \mathbf{B} , \mathbf{A} with homogeneous rank r across all clients with standard FL (McMahan et al., 2017). Specifically, first the clients have the pre-trained ODFM weights \mathbf{W}_0 stored in their devices prior to training for the forward pass when training the LoRA modules. Then, the server sends the global LoRA modules $\bar{\mathbf{B}}^{(t)}$, $\bar{\mathbf{A}}^{(t)}$ to the set of m selected clients $\mathcal{S}^{(t)}$ per communication round t . Each selected client $k \in \mathcal{S}^{(t)}$ trains the LoRA modules on their local data for a few local iterations (usually with mini-batch SGD) and send the updated modules $\mathbf{B}_k^{(t)}$, $\mathbf{A}_k^{(t)}$ back to the server. The server then updates the global LoRA modules accordingly to $\bar{\mathbf{B}}^{(t+1)} = \sum_{k \in \mathcal{S}^{(t)}} \mathbf{B}_k^{(t)} / m$, $\bar{\mathbf{A}}^{(t+1)} = \sum_{k \in \mathcal{S}^{(t)}} \mathbf{A}_k^{(t)} / m$ and sends back to the next set of selected clients for the next communication round. This training process is nearly identical to the standard FL algorithm (McMahan et al., 2017) except that the pretrained weights \mathbf{W}_0 are freezed and locally stored in the clients' devices and only the LoRA moduels are trained and communicated.

Instead of such homogeneous rank deployment across all clients, it is not only possible but more practical to use heterogeneous rank deployment for federated fine-tuning. This involves training LoRA modules with varying ranks on different clients, based on their system capabilities. Such setting is motivated and often required from the system constraints of the clients (Wang et al., 2021) where most of the clients are only capable of having smaller ranks while a few can handle larger ranks. However, this approach poses challenges in aggregating and redistributing the LoRA modules. To address these challenges, we introduce a solution called HETLORA, which pushes the limits

beyond homogeneous LoRA deployment.

3.3 Proposed Method: Heterogeneous LoRA

Overview. Our proposed heterogeneous LoRA method, namely HETLORA, is not restricted to any specific method to assign the ranks to the clients and the clients can decide their respective ranks themselves. For formality, in our paper, we formulate that each client has a rank denoted as r_k , within a range of $r_k \in [r_{\min}, r_{\max}]$, $\forall k$ (see Fig. 1). HETLORA comprises three steps: 1) Distribution via Truncation, 2) Local Training with Rank Self-Pruning, and 3) Sparsity-Weighted Aggregation of the LoRA modules. These steps are detailed further in the subsequent paragraphs. An overview of HETLORA is illustrated in Fig. 2.

1) Distribution via Truncation. At the beginning of each communication round t , the server holds initial global LoRA modules $\bar{\mathbf{B}}^{(t)}$, $\bar{\mathbf{A}}^{(t)}$ with a global rank $r^{(t)}$. The value of the global rank $r^{(t)}$ depends on how we aggregate the heterogeneous rank LoRA modules which is elaborated on in step 3). The server then distributes these global LoRA modules to a subset of selected set of clients $\mathcal{S}^{(t)}$ with heterogeneous ranks $r_k^{(t)}, k \in \mathcal{S}^{(t)}$ for local training¹. With the given global LoRA modules, we consider a simple and intuitive method of *truncation* where the server sends $\bar{\mathbf{B}}_{:,r_k}^{(t)}$, $\bar{\mathbf{A}}_{:,r_k}^{(t)}$ to each client k with rank $r_k^{(t)}$ for local training where we omitted the superscript for r_k for simplicity.

2) Local Training with Rank Self-Pruning. After receiving LoRA modules from the server as $\mathbf{B}_k^{(t,0)} = \bar{\mathbf{B}}_{:,r_k}^{(t)}$, $\mathbf{A}_k^{(t,0)} = \bar{\mathbf{A}}_{:,r_k}^{(t)}$, each client $k \in \mathcal{S}^{(t)}$ performs τ local iterations of mini-batch SGD on their local data to minimize the local objective $\frac{1}{|\mathcal{B}_k|} \sum_{\xi \in \mathcal{B}_k} \ell((\mathbf{B}_k, \mathbf{A}_k), \xi | \mathbf{W}_0)$, and sends back the updated LoRA modules $\mathbf{B}_k^{(t,\tau)} \in \mathbb{R}^{d \times r_k^{(t)}}$ and $\mathbf{A}_k^{(t,\tau)} \in \mathbb{R}^{r_k^{(t)} \times l}$ to the server. This is the same process as the standard local training step in vanilla FedAvg (McMahan et al., 2017). However, we improve this vanilla local training step by adding a rank self-pruning mechanism where clients self-prune their respective ranks depending on the magnitude of the model parameters.

¹There is a superscript t for the ranks $r_k^{(t)}$ across clients which indicates that in HETLORA these heterogeneous ranks can be changed over the communication rounds via self-pruning explained in step 2).

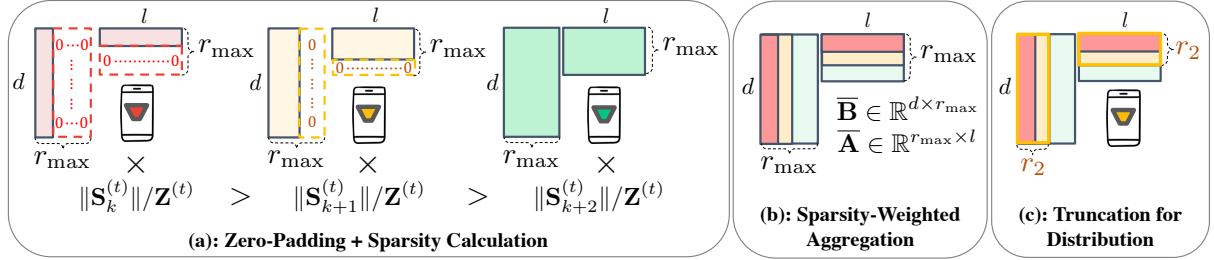


Figure 2: Overview of the zero-padding, sparsity-weighted aggregation, and truncation method for HETLORA; (a): Zero-pad LoRA modules with smaller ranks to r_{\max} (clients with rank r_{\max} does not need padding) and calculate their sparsity by calculating the Frobenius norm of the reconstructed model $\Delta \mathbf{W}_k^{(t)} = \mathbf{B}_k^{(t)} \mathbf{A}_k^{(t)}$; (b): After padding, aggregate all of the clients' LoRA modules with the weights $\|\mathbf{S}_k^{(t)}\|/\mathbf{Z}^{(t)}$ calculated by $\Delta \mathbf{W}_k^{(t)}$ to get the global LoRA modules; (c): Truncate the global LoRA modules for the specific rank of the next selected client (example for client with rank r_2).

Specifically, we add a regularization term to the original local objective to get $\min_{\mathbf{B}_k, \mathbf{A}_k} \frac{1}{|\mathcal{B}_k|} \sum_{\xi \in \mathcal{B}_k} \ell((\mathbf{B}_k, \mathbf{A}_k), \xi | \mathbf{W}_0) + \lambda \|\mathbf{B}_{k,:r_k \gamma:r_k}\| \|\mathbf{A}_{k,r_k \gamma:r_k,:}\|$ where $\gamma < 1$ is a decay-factor that determines how aggressively we want to prune the ranks to a smaller value. The regularization term aims to minimize the norm of the last few ranks, which will become smaller if the first loss term $\frac{1}{|\mathcal{B}_k|} \sum_{\xi \in \mathcal{B}_k} \ell((\mathbf{B}_k, \mathbf{A}_k), \xi | \mathbf{W}_0)$ is not very large. After training with the new local objective we compare the norm of the updated LoRA modules' last few layers $\|\mathbf{B}_{k,:r_k \gamma:r_k}\| \|\mathbf{A}_{k,r_k \gamma:r_k,:}\|$ with the ones from the initially received LoRA modules. If the former is smaller we prune the last few layers (pruning intensity is determined by γ) and send back the LoRA modules with a smaller rank. This means that for the LoRA modules which incurs a small local loss, i.e., well-trained on the clients' local data, the LoRA modules are more likely to be pruned to a smaller rank.

Such pruning allows HETLORA to reduce the noise in the LoRA modules introduced by clients having a larger rank than the actual rank that their data complexity requires, and also reduces the complexity of the LoRA modules to improve generalization and prevent overfitting (see Table 4). Once the rank is pruned for a client, the client saves the updated rank and uses it as the starting rank if selected for future communication rounds. The client then sends back their updated and possibly rank-pruned LoRA modules to the server for the modules to be processed in the next server-side aggregation step.

3) Sparsity-Weighted Aggregation. Finally, the last step of HETLORA is aggregating the received heterogeneous LoRA modules

$\mathbf{B}_k^{(t,\tau)}, \mathbf{A}_k^{(t,\tau)}, k \in \mathcal{S}^{(t)}$. A straightforward way to aggregate the heterogeneous LoRA modules is using *zero-padding* to all the received LoRA modules with $r_i^{(t)} < \max\{r_k^{(t)} | k \in \mathcal{S}^{(t)}\}$ and then perform simple averaging over the modules. However, such naive aggregation can lead to biasing the model towards higher rank clients even when these clients may not hold valuable training information, i.e., having low data complexity, giving noisy updates.

In an ideal scenario where we can deploy any rank to any client, deploying higher ranks to the clients with higher data complexity or larger local datasets can retrieve more informative and less sparse updates from the clients. Conversely if we assign higher ranks to the clients whose data complexity is low, the actual rank of the full model from the reconstructed LoRA modules can be smaller than the assigned rank. Thus the higher rank client's update may be unnecessarily over-emphasized in the naive zero padding method.

Based on this insight we propose a sparsity-weighted aggregation scheme where the server reconstructs these LoRA modules to the full model as $\Delta \mathbf{W}_k^{(t)} = \mathbf{B}_k^{(t)} \mathbf{A}_k^{(t)}$ and gets the norm of the singular value vectors from the full models denoted as $\mathbf{S}_k^{(t)}$ by calculating $\|\Delta \mathbf{W}_k^{(t)}\|_F$. Note that the costly process of performing SVD for each of the full model $\Delta \mathbf{W}_k^{(t)}$ can be avoided by simply calculating the Frobenius norm of $\Delta \mathbf{W}_k^{(t)}$ (see Lemma 1.2 in (Guruswami and Kannan, 2012)). The server then weighs the LoRA modules with aggregation weight $p_k^{(t)}$ which is proportional to the norm of the singular value vectors. Formally, we have the the global LoRA modules updated as $\bar{\mathbf{B}}^{(t+1)} = \sum_{k \in \mathcal{S}^{(t)}} p_k^{(t)} \mathbf{B}_k^{(t)}, \bar{\mathbf{A}}^{(t+1)} = \sum_{k \in \mathcal{S}^{(t)}} p_k^{(t)} \mathbf{A}_k^{(t)}$ where $p_k^{(t)} := \|\mathbf{S}_k^{(t)}\|/\mathbf{Z}^{(t)}$ with

normalizing factor $\mathbf{Z}^{(t)} := \sum_{k' \in S^{(t)}} \|\mathbf{S}_{k'}^{(t)}\|$. This way, we can de-emphasize the larger rank assigned clients that have rather less informative updates, and more emphasize the smaller rank assigned clients that have more informative ones.

3.4 Why not Simply Reconstruct First, then Redistribute the LoRA modules?

One might ask why not simply reconstruct each of the LoRA modules to the full matrix and aggregate them. Here we show that reconstructing the LoRA modules and aggregating them to get the full model results in a different full model compared to when we aggregate the LoRA modules first and then reconstruct the final model. In Section 4 we also empirically show that reconstructing the LoRA modules to the full model and redistributing them after truncated SVD to the corresponding rank of the clients results in an underwhelming performance compared to HETLoRA.

Let us consider a simple case where there are 2 clients with heterogeneous rank lora modules $\mathbf{B}_1 \in \mathbb{R}^{d \times 1}$, $\mathbf{A}_1 \in \mathbb{R}^{1 \times l}$ and $\mathbf{B}_2 \in \mathbb{R}^{d \times 1}$, $\mathbf{A}_2 \in \mathbb{R}^{2 \times l}$ respectively for client 1 and client 2 where the former has rank 1 and latter has rank 2. We set the notation for the LoRA modules’ i^{th} row and j^{th} column value for \mathbf{B}_k and \mathbf{A}_k as $b_{k,ij}$ and $a_{k,ij}$ respectively. Then with $d = 3$, $l = 2$, when we reconstruct each of the LoRA modules first and then aggregate the full model we have its i^{th} row and j^{th} column as $(\sum_{k=1}^2 b_{k,i0} a_{k,0j}) + b_{2,i1} a_{2,1j}$ and aggregating the LoRA modules first and then reconstructing the model has the full model’s i^{th} row and j^{th} column as $(\sum_{k=1}^2 b_{k,i0})(\sum_{k=1}^2 a_{k,0j}) + b_{2,i1} a_{2,1j}$.

One can observe that the difference between the two models are the cross-terms between the left and right module of different client 1 and 2, i.e., $b_{1,i0} a_{2,0j} + b_{2,i0} a_{1,0j}$ for the i^{th} row and j^{th} column. In other words, when we reconstruct the LoRA modules first and then aggregate them to get the full model, each term in the full model are cross-products between the left and right module of each client and not the cross-products between clients. Thus, reconstructing the LoRA modules loses information on the cross-relation across clients, only retaining the knowledge on the cross-relation between the LoRA modules \mathbf{B} and \mathbf{A} . Such observation is also corroborated by the *reconstruction first*’s underwhelming performance in Table 3.

4 Experiments

In this section, we present results for HETLoRA and its baselines in terms of the performance on training speed, computation/communication efficiency, and final achieved performance. First, we show the performance of homogeneous LoRA to show how LoRA in general performs for low and high rank values. Second, we demonstrate HETLoRA’s performance for different r_{min} and r_{max} values comparing them with full fine-tuning, homogeneous LoRA, and the reconstruction-first method elaborated in Section 3.4. We also conduct an ablation study on HETLoRA with varying decay factor γ for the rank self-pruning step. The rank distribution across clients for HETLoRA, unless mentioned otherwise, is set to a truncated power-law distribution with $\alpha = 0.1$ in the range between $[r_{min}, r_{max}]$ (inclusively), where the small α value makes the distribution skewed towards smaller ranks. All experiments were ran with 3 different random seeds and their average is shown along with the standard deviation.

Model. We use the Transformer-based language model PaLM 2 (Google, 2023) of size XXS and XS for our experiments which are lightweight enough to fit in to the category of ODFMs (Google DeepMind, 2023) compared to standard FMs. The LoRA modules are applied to only the self-attention layers as proposed in the original LoRA paper (Hu et al., 2021), and their relative number of parameters compared to the original model are shown in Table 2.

Tasks. The tasks we consider are the chat dialogue from the multi-session chat (MSC) dataset (Xu et al., 2021) and the text summarization task from the Reddit dataset (Völske et al., 2017). The MSC data is a collection of human-human interactions comprising numerous extended chat sessions, and we use perplexity (Zhang et al., 2018) as the metric which has been used to show the quality of chat responses from generative models from previous literature (Sedoc et al., 2019). We sample 100 users uniformly at random and partition their data for training and evaluation by each `previous_dialogs` and `dialog`. The Reddit text summarization data consists of real users’ reddit posts and their summarization, and we use RougeL (Lin, 2004) as the metric. We use 298 users from Reddit that have at least 100 data sam-

	Reddit (RougeL)		Multi-Session Chat (Perplexity)	
	PaLM 2-XXS	PaLM 2-XS	PaLM 2-XXS	PaLM 2-XS
Full	94.56 (±0.01)	94.87 (±0.04)	32.70 (±0.17)	23.40 (±0.36)
HOMLoRA $r = 5$	92.57(±1.56), $\times 0.001$	92.89(±0.96)	80.51(±8.32), $\times 0.001$	64.59(±9.31)
HOMLoRA $r = 50$	70.57(±2.13), $\times 0.01$	84.95(±1.59)	307.96(±11.43), $\times 0.01$	167.46(±1.72)
Recon+SVD	63.28(±1.92), $\times 0.003$	75.17(±1.25)	323.89(±20.57), $\times 0.002$	215.63(±15.38)
HETLoRA $\gamma = 0.99$	94.23 (±0.03), $\times 0.003$	94.41 (±0.05)	53.93 (±1.57), $\times 0.002$	38.76 (±0.52)

Table 3: Final RougeL score for Reddit text summarization and perplexity for multi-session chat for different federated fine-tuning methods. The blue text indicates the ratio of trained number of parameters compared to the full fine-tuning case. HETLoRA outperforms both HOMLoRA and Recon+SVD method, but slightly underperforms the full fine-tuning case. However, compared to full fine-tuning the number of trained parameter is significantly smaller.

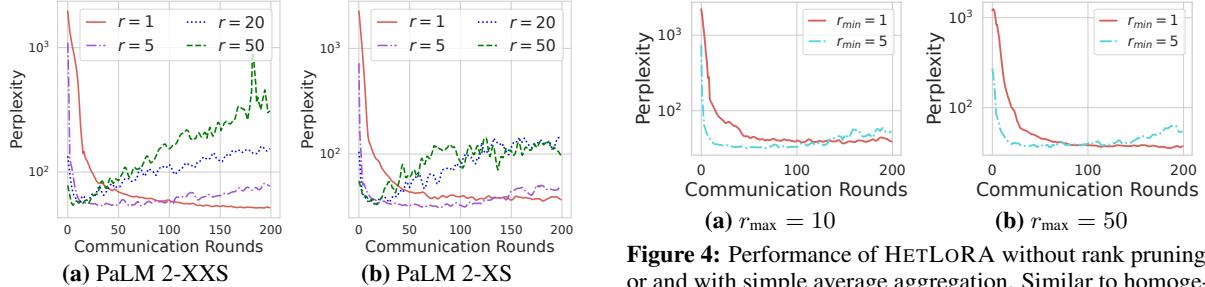


Figure 3: Performance of homogeneous LoRA for different rank r . Higher ranks achieve better performance with fewer communication rounds than the lower ranks, but they overfit quickly. Conversely, the lowest rank $r = 1$ achieves low perplexity slower than higher ranks, but without overfitting.

ples as the training clients and use another 100 users with at least 100 data samples for evaluation.

Local Training. We use mini-batch size 8 and number of local iterations $\tau = 5$ with the feature length set to 1024. For the learning rate we perform grid search in $\eta = \{0.1, 0.01, 0.001, 0.0001\}$. For each MSC and Reddit task, we select 5 and 10 clients per communication round respectively.

4.1 Experiment Results

Homogeneous LoRA and the Effect of Ranks r . First, we evaluate the performance of federated fine-tuning of the LoRA modules with homogeneous LoRA deployment across clients in Fig. 3 for different ranks $r \in [1, 5, 20, 50]$. We observe that a higher rank r for homogeneous LoRA achieves better perplexity floor with fewer communication rounds than the lower ranks but quickly overfits resulting in worse performance compared to the lower ranks after more communication rounds. On the other hand, while the lower rank cases need more communication rounds to achieve good performance, it does not have the problem of overfitting as the higher ranks. Hence for homogeneous LoRA, there is a trade-off to consider between low and high ranks, in terms of faster performance achievement and overfitting. Note that these ob-

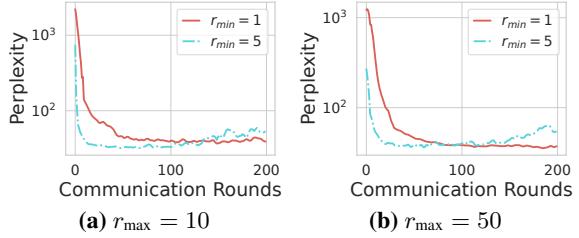


Figure 4: Performance of HETLoRA without rank pruning or with simple average aggregation. Similar to homogeneous LoRA, larger r_{\min} leads to overfitting for heterogeneous LoRA, but it is not as severe as homogeneous LoRA even for larger maximum rank $r_{\max} = 50$ showing that the smaller rank LoRA modules act as a regularizer for HETLoRA.

servations are consistent with previous literature in the centralized setting where a higher rank does not necessarily yields the best performance (Hu et al., 2021; Zhang et al., 2023b). Next, we show that HETLoRA achieves good performance quickly without this overfitting issue, showing better performance than the homogeneous LoRA case.

Naïve Heterogeneous LoRA and the Effect of r_{\min} and r_{\max} .

First, we show the performance of *naïve* heterogeneous LoRA *without* self rank-pruning and with only average aggregation instead of the sparsity-weighted aggregation in Fig. 4. We can see similar observations to those from homogeneous LoRA where a smaller minimum rank $r_{\min} = 1$ leads to slower training but better performance while a larger maximum rank leads to faster training but worse performance. However, compared to homogeneous LoRA the overfitting does not get as severe for heterogeneous LoRA even with much larger ranks such as $r_{\max} = 50$. We can imply from this result that the smaller rank LoRA modules act as a regularizer in heterogeneous LoRA. Next, we show that by adding the self rank-pruning and sparsity-weighted aggregation, even with $r_{\min} = 5$ we are able to prevent overfitting issues and achieve better training speed and final performance than other baselines.

	Reddit (RougeL)		Multi-Session Chat (Perplexity)	
	PaLM 2-XXS	PaLM 2-XS	PaLM 2-XXS	PaLM 2-XS
HETLoRA, $\gamma = 1$	92.17 (± 0.08)	91.95 (± 0.03)	55.07 (± 0.81)	40.92 (± 0.58)
HETLoRA, $\gamma = 0.99$	94.23 (± 0.03)	94.41 (± 0.05)	53.93 (± 1.57)	38.76 (± 0.52)
HETLoRA, $\gamma = 0.95$	89.62 (± 1.33)	83.19 (± 1.70)	71.10 (± 1.39)	46.39 (± 0.87)
HETLoRA, $\gamma = 0.85$	60.31 (± 3.04)	53.28 (± 2.47)	120.72 (± 10.93)	59.67 (± 1.98)

Table 4: Ablation study on the effect of the decaying factor γ for HETLoRA’s self-rank pruning in the local training step. While aggressive pruning can be harmful to HETLoRA’s performance, pruning ($\gamma = 0.99$) can outperform the case when there is no pruning at all ($\gamma = 1$) by reducing the noise introduced by large rank clients with low data complexity.

Heterogeneous LoRA compared to Baselines.

Finally, we compare our proposed HETLoRA with other baselines in Table 3 and Fig. 5. We see that HETLoRA with $r_{\min} = 5$ and $r_{\max} = 50$ achieves faster training as well as better performance than homogeneous LoRA cases with both edge cases of the ranks $r \in \{5, 50\}$ and reconstruction+SVD which was explained in Section 3.4. This implies that HETLoRA is not only practical in the sense that clients are allowed to have their own rank values, it can also outperform the limited case of homogeneous LoRA where all clients have $r = r_{\min}$ or the impractical case where all clients have $r = r_{\max}$. We also observe that HETLoRA achieves slightly lower performance than full fine-tuning. However, as shown in the blue text in Table 3 that shows the number of trained parameters compared to the full fine-tuning case, full fine-tuning requires to train a much larger number of parameters compared to HETLoRA, making it infeasible to train with ODFMs in practice. We also show in Fig. 6 that to achieve the targeted performance for both Reddit and MSC task, HETLoRA requires significantly less number of parameters to be trained and communicated compared to full fine-tuning. Although for Reddit, HOMLoRA has a slightly less number of parameters to be trained, the final achieved RougeL is outperformed by HETLoRA as shown in Table 3.

Effect of the Decaying Factor γ . Lastly, we conduct an ablation study on the effect of the decaying factor γ of HETLoRA’s local training step with self-rank pruning in Table 4. We observed that aggressive pruning hurts the performance where $\gamma = 0.85$ shows the worse performance across the varying γ values. On the other hand, no pruning at all ($\gamma = 1$) underperforms the case when there is pruning ($\gamma = 0.99$), showing that reducing the noise introduced by large rank clients which data complexity is actually not that high indeed improves the performance.

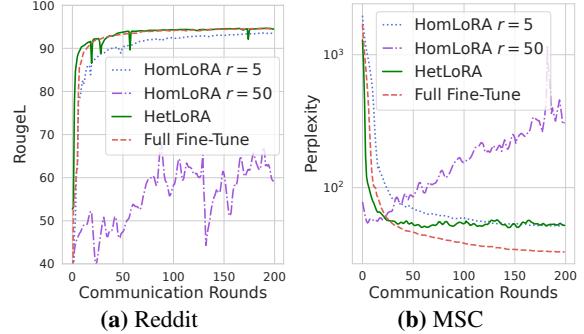


Figure 5: Comparison of the performance across homogeneous LoRA, heterogeneous LoRA, and full fine-tuning. Heterogeneous LoRA achieves better performance than homogeneous LoRA with fewer number of communication rounds.

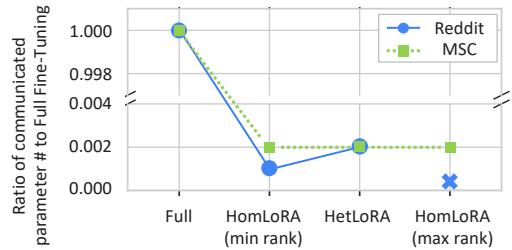


Figure 6: Ratio of communicated number of parameters for different PEFT methods to full fine-tuning to achieve the target value for the metric where it is RougeL 80 for Reddit text summarization task and perplexity 150 for the multi-session chat response task. The ‘X’ means that the target metric is not achieved even after convergence.

5 Discussions and Concluding Remarks

In our work, we investigated federated fine-tuning for ODFMs that cater to device system and data heterogeneity with our proposed HETLoRA. We show that HETLoRA is not only practical but also achieves better training speed, communication/computation efficiency, and final performance compared to homogeneous LoRA. We also show interesting findings consistent with previous literature (Hu et al., 2021; Zhang et al., 2023b) that increasing ranks does not always help for homogeneous LoRA. Our findings in this work opens up several questions worth investigating. For instance, if the settings allow us to assign specific ranks to

clients what will be the effective way to assign the ranks across clients for better convergence and performance? Another important next step of our work includes pursuing the theoretical convergence and generalization of heterogeneous LoRA.

6 Limitations

In this work, we address tackling system and data heterogeneity in federated fine-tuning of on-device foundation models. Our work is motivated by clients being able to carry different ranks for the LoRA fine-tuning method depending on their available resources, and thus exploiting this characteristic to improve federated fine-tuning with heterogeneous LoRA. However, our work assumes that the rank distribution across clients (which is analogous to how system resources are distributed across clients) is independent to the data distribution. There can be scenarios in which this is not necessarily the case where the rank and data distribution can be correlated. For instance, more affluent populations can have better off devices with larger resource capacity, and may have data distributions different to that of less affluent populations. Such correlation should be explored for future work to better understand the implications of heterogeneous LoRA.

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