

Homework 2

[1] A uniform plane wavefunction has the instantaneous expression

$$\Phi(x,t) = 5 \sin(200\pi t + 0.4\pi x + 30^\circ).$$

Identify or calculate the following:

- i) the radian frequency ω of the wave in rad/s
- ii) the frequency f in Hz of the wave
- iii) the direction of propagation of the wave
- iv) the wavelength λ in m of the wave
- v) the amplitude A of the wave, and
- vi) the phase velocity v_{ph} in m/s of the wave.

[2] A uniform plane scalar wave represented by the function $\Phi(x,t)$ is specified as having the following properties:

The wave propagates in the $-x$ direction

Wave amplitude = 10

Wave frequency = 500 Hz

Wave's phase velocity = 100 m/s

The wavefunction $\Phi(0,0)$ at $x = 0$ and $t = 0$ has the value $\Phi(0,0) = 5$.

Find the expression $\Phi(x,t)$ of the wave function.

[3] Consider two scalar UPW's of the same amplitude which have incrementally different frequencies and thus incrementally different wavelengths. Both waves are given to be propagating in the $+z$ direction. Show that the effect of interference between the two UPW's is to generate an amplitude-modulated carrier wave (cw) signal moving in the $+z$ direction such that the cw component of the signal propagates with phase velocity $v_p = \omega/k$ while the envelope signal propagates with group velocity $v_g = d\omega/dk$.