

systems

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$v_1(x, y, t) = u(x, y, t)\hat{i} + v(x, y, t)\hat{j}$ is the baroclinic velocity. T is temperature (in energy units). Q is an unknown radiation parameter. The rest of the quantities are known constants.

System 1

$$\begin{aligned}\partial_t u - fv + \epsilon_1 u &= -\kappa \frac{\partial T}{\partial x} \\ \partial_t v - fu + \epsilon_1 v &= -\kappa \frac{\partial T}{\partial y} \\ \hat{A}_1 \partial_t T + M_{s1} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) &= Q\end{aligned}$$

System 2

$$\begin{aligned}\partial_t u - fv + \epsilon_1 u &= -\kappa \frac{\partial T}{\partial x} \\ \partial_t v - fu + \epsilon_1 v &= -\kappa \frac{\partial T}{\partial y} \\ \hat{A}_1 \partial_t T + a_T v \frac{\partial T}{\partial y} + M_{s1} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) &= Q\end{aligned}$$

Initial conditions for systems 1,2

$$\begin{aligned}u(x, y, 0) &= \cos(x + y) \\ v(x, y, 0) &= \cos(x) + \cos(y) \\ T(x, y, 0) &= \sin(x + y)\end{aligned}$$

System 3

$$\begin{aligned}\partial_t v + \epsilon_1 v &= -\kappa \frac{\partial T}{\partial y} \\ \hat{A}_1 \partial_t T + a_T v \frac{\partial T}{\partial y} + M_{s1} \frac{\partial v}{\partial y} &= Q\end{aligned}$$

Initial conditions for system 3

$$v(x, 0) = x, \quad T(x, 0) = \cos(x)$$