

Isostatic constraint for 2D gravity inversion on passive rifted margins

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Running head: **Isostatic constraint for gravity inversion on passive margins**

ABSTRACT

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INTRODUCTION

Several methods have been proposed for using gravity and/or magnetic data to estimate the boundaries of juxtaposed sedimentary layers, the relief of basement under sedimentary basins and/or the Mohorovicic discontinuity (or simply Moho), which separates crust and mantle. These geophysical discontinuities represent, for such particular methods, density and/or magnetization contrasts in subsurface. All these methods suffer from the inherent ambiguity (Roy, 1962; Skeels, 1947) in determining the true physical property distribution that produces a discrete set of observed potential-field data. It is well known that, by using different density and/or magnetization contrasts, it is possible to find different surfaces producing the same potential-field data. To partially overcome this problem and obtain meaningful solutions, the interpreter must commonly use *a priori* information obtained from seismic data and/or boreholes in order to constrain the range of possible models.

There are methods that approximate the subsurface by a grid of juxtaposed cells with constant physical property. They estimate the physical property value of each cell and then interpret the estimated values to indirectly estimate the geometry of the geophysical discontinuities. Although very useful in geophysics, such methods are outside the scope of the present work. Here, we consider methods that represent discontinuities by surfaces separating layers with constant or depth-dependent physical property distribution (density and/or magnetization). In this case, the geometry of the geophysical discontinuities are directly determined by estimating the geometrical parameters describing the surfaces.

Different criteria can be used to classify the methods that directly estimate the geometry of geophysical discontinuities. Those applied over a sedimentary basin, for example, can be considered local scale methods, whereas those applied over a continent or country can be

considered regional scale methods and those applied over the whole globe can be considered global scale methods. They can also be classified according to the number of geophysical surfaces to be estimated.

By using these criteria, it is possible to define a first group of methods estimating the geometry of a single interface. In this group, there are local scale methods in space domain (e.g., Bott, 1960; Tanner, 1967; Cordell and Henderson, 1968; Dyrelus and Vogel, 1972; Pedersen, 1977; Pilkington and Crossley, 1986a; Richardson and MacInnes, 1989; Barbosa et al., 1997, 1999b,a; Silva et al., 2006; Pilkington, 2006; Chakravarthi and Sundararajan, 2007; Martins et al., 2010; Silva et al., 2010; Lima et al., 2011; Martins et al., 2011; Barnes and Barraud, 2012; Silva et al., 2014; Silva and Santos, 2017), and Fourier domain (e.g., Oldenburg, 1974; Granser, 1987; Reamer and Ferguson, 1989; Guspí, 1993). Most of these methods were applied to estimate the relief of basement under a sedimentary basin. There are also regional scale methods for estimating a single interface representing the Moho in spaced domain (e.g., Shin et al., 2009; Bagherbandi and Eshagh, 2012; Barzaghi and Biagi, 2014; Sampietro, 2015; Uieda and Barbosa, 2017) and in Fourier domain (e.g., Braitenberg et al., 1997; Braitenberg and Zadro, 1999; van der Meijde et al., 2013). Additionally, there are some global scale methods for estimating the Moho in spaced domain (e.g., Sünkel, 1985; Sjöberg, 2009).

The second group of methods is formed by those estimating multiple surfaces separating layers with constant or depth-dependent physical properties (e.g., Pilkington and Crossley, 1986b; Gallardo et al., 2005; Camacho et al., 2011; Salem et al., 2014). All these methods have been applied at local scale, to characterize a single sedimentary basin. The number of methods forming this group is significantly lower than that in the first one. Additionally, the methods forming the second group suffer from a greater ambiguity and, as a consequence,

they require more priori information to decrease the number of possible solutions.

Among those directly estimating the geometry of the surfaces, there are some regional and global scale methods in space domain that impose some degree of isostatic equilibrium to the estimated models (e.g., Süinkel, 1985; Sjöberg, 2009; Bagherbandi and Eshagh, 2012; Sampietro, 2015) or analyze their deviations from a perfect isostatic equilibrium (e.g., Shin et al., 2009). Salem et al. (2014) presented one of the few local scale methods in space domain that simultaneously estimates the basement and Moho reliefs by imposing isostatic equilibrium. They imposed a perfect isostatic equilibrium according to the Airy’s local compensation model (Turcotte and Schubert, 2002), which describes well the transition from continental to oceanic crust at rifted margins (Worzel, 1968; Watts and Moore, 2017).

Here, we present a new local scale method for simultaneously estimating the geometries of basement and Moho along a profile on a passive rifted margin. Our method is formulated, in space domain, as a non-linear gravity inversion. In order to produce stable solutions and introduce priori information, we use different constraints imposing smoothness and lower/upper bounds on basement and Moho depths, as well as proximity between estimated and known depths at some points along the profile. We also use a constraint (which we conveniently call as *isostatic constraint*) imposing smoothness on the lithostatic stress exerted on a planar surface located at depth, below which we assume that there is no lateral density variations. We considered that no vertical forces are acting on the lateral surfaces of each column forming the lithosphere. Notice that, by imposing smoothness on the lithostatic stress, our method does not estimate a model in perfect isostatic equilibrium, but a model as close as possible to the isostatic equilibrium. Tests with synthetic data show the performance of our method in simultaneously retrieving the geometry of basement and Moho of different models. We also analyze the influence of the isostatic constraint on the

estimated surfaces at regions showing abrupt crustal thinning, which is typically shown in volcanic passive margins (Geoffroy, 2005). Finally, we illustrate the performance of our method by inverting satellite gravity data on a profile over the Pelotas basin (Stica et al., 2014), which is located at the southern of Brazil and is considered a classical example of volcanic passive margin.

METHODOLOGY

Forward problem

Let \mathbf{d}^o be the observed data vector, whose i -th element d_i^o , $i = 1, \dots, N$, represent the observed gravity disturbance at the point (x_i, y_i, z_i) , on a profile located over a rifted passive margin. The coordinates are referred to a topocentric Cartesian system, with z axis pointing downward, y -axis along the profile and x -axis perpendicular to the profile. We assume that the actual mass distribution in a rifted passive margin can be schematically represented according to Figure 1. In this model, the subsurface is formed by four layers. The first and shallowest one represents a water layer with constant density $\rho^{(w)}$. The second layer is formed by Q vertically adjacent parts representing sediments, salt or volcanic rocks. In our example, this layer is formed by two parts with constant densities $\rho^{(q)}$, $q = 1, 2$. Different models can be created by changing the number Q . The third layer of our model represents the crust. For simplicity, we presume that the crust density may be equal to $\rho^{(cc)}$, which represents the continental crust, or equal to $\rho^{(oc)}$, which represents the oceanic crust. The deepest layer represents a homogeneous mantle with constant density $\rho^{(m)}$. The interface separating the second and third layers defines the basement relief whereas that separating the third and fourth layers defines the Moho. These surfaces are represented by dashed-

white lines in Figure 1. We also presume the existence of an isostatic compensation depth at S_0 (represented as a continuous white line in Figure 1), below which there is no lateral variations in the mass distribution.

In order to define the anomalous mass distribution producing the observed gravity disturbance, we presume a reference mass distribution formed by two layers (not shown). The shallowest layer represents a homogeneous crust with constant density $\rho^{(r)}$. The deepest layer in the reference mass distribution represents a homogeneous mantle with constant density $\rho^{(m)}$. Notice that the mantle in the reference mass distribution has the same density as the mantle in our rifted margin model (Figure 1). The interface separating the crust and mantle in the reference mass distribution is conveniently called *reference Moho* (represented as a continuous white line in Figure 1). The reference model can be thought of as the outer layers of a concentric mass distribution producing the normal gravity field.

We consider that the anomalous mass distribution producing the observed data is defined as the difference between the rifted margin model (Figure 1) and the reference mass distribution (not shown). As a consequence, the anomalous mass distribution is characterized by regions with constant density contrast. This anomalous distribution is approximated by an interpretation model formed by N columns of vertically stacked prisms (Figure 2). For convenience, we presume that there is an observed gravity disturbance over the center of each column. We consider that the prisms in the extremities of the interpretation model extend to infinity along the y axis in order to prevent edge effects in the forward calculations. The i -th column is formed by four vertically adjacent layers, which in turn are composed of vertically adjacent prisms having infinite length along the x -axis.

The first and shallowest layer represents water, is formed by a single prism, has thickness

$t_i^{(w)}$ and a constant density contrast $\Delta\rho^{(w)} = \rho^{(w)} - \rho^{(r)}$. The second layer forming the i -th column of the interpretation model is defined by the interpreter, according to the geological environment to be studied and the a priori information availability. As a general rule, this layer can be defined by a set of Q vertically adjacent prisms, each one with thickness $t_i^{(q)}$ and constant density contrast $\Delta\rho^{(q)} = \rho^{(q)} - \rho^{(r)}$, $q = 1, \dots, Q$. The third layer represents the crust, it is also formed by a single prism, has thickness $t_i^{(c)}$ and density contrast $\Delta\rho_i^{(c)} = \rho^{(c)} - \rho^{(r)}$, with ρ^c being the crust density. According to our rifted margin model (Figure 1), the crust density $\rho_i^{(c)}$ may assume two possible values, depending on its position with respect to the y_{COT} (Figure 2). As a consequence, the prisms forming the third layer of the interpretation model may have two possible density contrasts: $\Delta\rho_i^{(c)} = \rho^{(cc)} - \rho^{(r)}$, for $y_i \leq y_{COT}$, or $\Delta\rho_i^{(c)} = \rho^{(oc)} - \rho^{(r)}$, for $y_i > y_{COT}$. The top of this layer defines the basement relief and its bottom the relief of the Moho. The fourth layer represents the mantle, it is divided into two parts, each one formed by a single prism having a constant density contrast $\Delta\rho^{(m)} = \rho^{(m)} - \rho^{(r)}$. The shallowest portion of this layer has thickness $t_i^{(m)}$. Its top and bottom define, respectively, the depths of Moho and the planar isostatic compensation layer S_0 . The deepest portion of the fourth layer has thickness ΔS_0 , top at the surface S_0 and bottom at the planar surface $S_0 + \Delta S_0$, which defines the reference Moho.

Given the density contrasts, the COT position y_{COT} , the isostatic compensation depth S_0 , the thickness of the water layer and of the $Q - 1$ prisms forming the shallowest portion of the second layer, it is possible to describe the interpretation model in terms of an $M \times 1$

parameter vector \mathbf{p} , $M = 2N + 1$, defined as follows:

$$\mathbf{p} = \begin{bmatrix} \mathbf{t}^Q \\ \mathbf{t}^m \\ \Delta S_0 \end{bmatrix}, \quad (1)$$

where \mathbf{t}^Q and \mathbf{t}^m are $N \times 1$ vectors whose i -th elements t_i^Q and t_i^m represent, respectively, the thickness of the prism forming the deepest portion of the second layer and the thickness of the prism forming the shallowest portion of the fourth layer of the interpretation model. In this case, the gravity disturbance produced by the interpretation model (the predicted gravity disturbance) at the position (x_i, y_i, z_i) can be written as the sum of the vertical component of the gravitational attraction exerted by the L prisms forming the interpretation model as follows:

$$d_i(\mathbf{p}) = k_g G \sum_{j=1}^L f_{ij}(\mathbf{p}), \quad (2)$$

where $f_{ij}(\mathbf{p})$ represents an integral over the volume of the j -th prism. Here, these volume integrals are computed with the expressions proposed by Nagy et al. (2000), by using the open-source Python package *Fatiando a Terra* (Uieda et al., 2013).

Inverse problem

Let $\mathbf{d}(\mathbf{p})$ be the predicted data vector, whose i -th element $d_i(\mathbf{p})$ is defined by Equation 2. Estimating the particular parameter vector $\mathbf{p} = \hat{\mathbf{p}}$ producing a predicted data vector $\mathbf{d}(\mathbf{p})$ as close as possible to the observed data vector \mathbf{d}^o can be formulated as the problem of minimizing the goal function

$$\Gamma(\mathbf{p}) = \Phi(\mathbf{p}) + \mu \sum_{\ell=0}^3 \alpha_\ell \Psi_\ell(\mathbf{p}), \quad (3)$$

subject to

$$p_j^{min} < p_j < p_j^{max}, \quad j = 1, \dots, M, \quad (4)$$

where p_j^{min} and p_j^{max} define, respectively, lower and upper bounds for the j -th element of \mathbf{p} . The goal function is minimized by using the Levenberg-Marquardt method (Aster et al., 2005) and the inequality constraint (equation 4) is incorporated by using the same strategy employed by Barbosa et al. (1999b). In Equation 3, μ represents the regularizing parameter, $\Phi(\mathbf{p})$ represents the misfit function given by

$$\Phi(\mathbf{p}) = \frac{1}{N} \|\mathbf{d}^o - \mathbf{d}(\mathbf{p})\|_2^2, \quad (5)$$

where $\|\cdot\|_2^2$ represents the squared Euclidean norm, α_ℓ represent the weights assigned to the regularizing functions $\Psi_\ell(\mathbf{p})$, which define the constraints on the parameters to be estimated, $\ell = 0, 1, 2, 3$. All the derivatives of the misfit function $\Phi(\mathbf{p})$ with respect to the parameters as computed by using a central finite difference approximation. Finally, the weights α_ℓ (equation 3) are defined as follows:

$$\alpha_\ell = \tilde{\alpha}_\ell f_\ell, \quad \ell = 0, 1, 2, 3, \quad (6)$$

where $\tilde{\alpha}_\ell$ is a positive scalar, $f_\ell = \frac{E_\Phi}{E_\ell}$, E_ℓ is the median of the elements forming the main diagonal of the Hessian matrix of the ℓ -th constraining function $\Psi_\ell(\mathbf{p})$ (equations 16, 17, 19 and 20) and E_Φ is the median of the elements forming the main diagonal of the Hessian matrix of the misfit function $\Phi(\mathbf{p})$ (equation 5) produced by the initial approximation for \mathbf{p} . Notice that, in fact, the interpreter defines the weights α_ℓ indirectly from the previously assigned values for the positive scalars $\tilde{\alpha}_\ell$ (equation 6).

Isostatic constraint

Consider that the interpretation model (Figure 2) is in isostatic equilibrium (Turcotte and Schubert, 2002; Hofmann-Wellenhof and Moritz, 2005; Lowrie, 2007) so that the lithostatic stress (pressure) is constant on the isostatic compensation surface S_0 . The ratio of the lithostatic stress to gravity exerted by the i -th column of the model on S_0 is given by:

$$t_i^{(w)} \rho^{(w)} + t_i^{(1)} \rho_i^{(1)} + \dots + t_i^{(Q)} \rho_i^{(Q)} + t_i^{(c)} \rho_i^{(c)} + t_i^{(m)} \rho^{(m)} = \sigma_0, \quad (7)$$

where σ_0 is an arbitrary positive constant. Here, we considered that no vertical forces are acting on the lateral surfaces of each column forming the model. By rearranging terms in Equation 7 and using the relation

$$S_0 = t_i^{(w)} + t_i^{(1)} + \dots + t_i^{(Q)} + t_i^{(c)} + t_i^{(m)}, \quad (8)$$

it is possible to show that:

$$\Delta \tilde{\rho}_i^{(Q)} t_i^{(Q)} + \Delta \tilde{\rho}_i^{(m)} t_i^{(m)} + \Delta \tilde{\rho}_i^{(w)} t_i^{(w)} + \Delta \tilde{\rho}_i^{(1)} t_i^{(1)} + \dots + \Delta \tilde{\rho}_i^{(Q-1)} t_i^{(Q-1)} + \rho_i^{(c)} S_0 = \sigma_0, \quad (9)$$

where $\Delta \tilde{\rho}_i^{(\alpha)} = \rho_i^{(\alpha)} - \rho_i^{(c)}$, $\alpha = w, 1, \dots, Q-1, Q, m$. In order to describe the lithostatic stress exerted by all columns forming the interpretation model on the surface S_0 , Equation 9 can be written, in matrix notation, as follows:

$$\mathbf{M}^{(Q)} \mathbf{t}^{(Q)} + \mathbf{M}^{(m)} \mathbf{t}^{(m)} + \mathbf{M}^{(w)} \mathbf{t}^{(w)} + \mathbf{M}^{(1)} \mathbf{t}^{(1)} + \dots + \mathbf{M}^{(Q-1)} \mathbf{t}^{(Q-1)} + \boldsymbol{\rho}^{(c)} S_0 = \sigma_0 \mathbf{1}, \quad (10)$$

where $\mathbf{1}$ is an $N \times 1$ vector with all elements equal to one, $\mathbf{t}^{(\alpha)}$, $\alpha = w, 1, \dots, Q-1, Q, m$, are $N \times 1$ vectors with i -th element defined by the thickness $t_i^{(\alpha)}$ of a prism forming the i -th column, $\mathbf{M}^{(\alpha)}$ are $N \times N$ diagonal matrices with elements ii of main diagonal defined by the density contrasts $\Delta \tilde{\rho}_i^{(\alpha)}$, respectively, and $\boldsymbol{\rho}^{(c)}$ is an $N \times 1$ vector containing the densities of the prisms representing the crust. By applying the first-order Tikhonov regularization

(Aster et al., 2005) to the constant vector $\sigma_0 \mathbf{1}$, we obtain the following expression:

$$\mathbf{R}(\mathbf{C}\mathbf{p} + \mathbf{D}\mathbf{t}) = \mathbf{0}, \quad (11)$$

where $\mathbf{0}$ is a vector with null elements and the remaining terms are given by:

$$\mathbf{C} = \begin{bmatrix} \mathbf{M}^{(Q)} & \mathbf{M}^{(m)} & \mathbf{0} \end{bmatrix}_{N \times M}, \quad (12)$$

$$\mathbf{D} = \begin{bmatrix} \mathbf{M}^{(w)} & \mathbf{M}^{(1)} & \dots & \mathbf{M}^{(Q-1)} & \boldsymbol{\rho}^{(c)} \end{bmatrix}_{N \times (QN+1)}, \quad (13)$$

$$\mathbf{t} = \begin{bmatrix} \mathbf{t}^{(w)} \\ \mathbf{t}^{(1)} \\ \vdots \\ \mathbf{t}^{(Q-1)} \\ S_0 \end{bmatrix}_{(QN+1) \times 1}, \quad (14)$$

\mathbf{p} is the parameter vector (Equation 1) and \mathbf{R} is an $(N-1) \times N$ matrix, whose element ij is defined as follows:

$$[\mathbf{R}]_{ij} = \begin{cases} 1 & , \quad j = i \\ -1 & , \quad j = i + 1 \\ 0 & , \quad \text{otherwise} \end{cases}. \quad (15)$$

Finally, from Equation 11, it is possible to define the regularizing function $\Psi_0(\mathbf{p})$ (Equation 3):

$$\Psi_0(\mathbf{p}) = \|\mathbf{R}(\mathbf{C}\mathbf{p} + \mathbf{D}\mathbf{t})\|_2^2. \quad (16)$$

We conveniently call this function as *Isostatic constraint*. Notice that minimizing this function imposes smoothness on the pressure exerted by the interpretation model on the isostatic compensation surface S_0 . Consequently, it imposes an interpretation model as close as possible of an isostatic equilibrium.

Smoothness constraint

This constraint imposes smoothness on the adjacent thickness of the prisms forming the deepest portion of the second layer and the shallowest part of the fourth layer of the interpretation model by applying the first-order Tikhonov regularization (Aster et al., 2005) to the vectors $\mathbf{t}^{(Q)}$ and $\mathbf{t}^{(m)}$ (Equation 1). Mathematically, this constraint is represented by the regularizing function $\Psi_1(\mathbf{p})$ (Equation 3):

$$\Psi_1(\mathbf{p}) = \|\mathbf{S}\mathbf{p}\|_2^2, \quad (17)$$

where \mathbf{S} is an $(N - 1) \times M$ matrix given by:

$$\mathbf{S} = \begin{bmatrix} \mathbf{R} & \mathbf{R} & \mathbf{0} \end{bmatrix}, \quad (18)$$

where \mathbf{R} is defined by Equation 15 and $\mathbf{0}$ is a vector with all elements equal to zero.

Equality constraint

Equality constraint on basement depths

Let \mathbf{a} be a vector whose k -th element a_k , $k = 1, \dots, A$, is the known basement depth at the horizontal coordinate y_k^A of the profile. These known basement depth values are used to define the regularizing function $\Psi_2(\mathbf{p})$ (Equation 3):

$$\Psi_2(\mathbf{p}) = \|\mathbf{A}\mathbf{p} - \mathbf{a}\|_2^2, \quad (19)$$

where \mathbf{A} is an $A \times M$ matrix whose k -th line has one element equal to one and all the remaining elements equal to zero. The location of the single non-null element in the k -th line of \mathbf{A} depends on the coordinate y_k^A of the known basement depth a_k . Let us consider, for example, an interpretation model formed by $N = 10$ columns. Consider also that the

basement depth at the coordinates $y_1^A = y_4$ and $y_2^A = y_9$ of the profile are equal to 25 and 35.7 km, respectively. In this case, $A = 2$, \mathbf{a} is a 2×1 vector with elements $a_1 = 25$ and $a_2 = 35.7$ and \mathbf{A} is a $2 \times M$ matrix ($M = 2N + 1 = 21$). The element 4 of the first line and the element 9 of the second line of \mathbf{A} are equal to 1 and all its remaining elements are equal to zero.

Equality constraint on Moho depths

Let \mathbf{b} be a vector whose k -th element b_k , $k = 1, \dots, B$, is the difference between the isostatic compensation depth S_0 and the known Moho depth at the horizontal coordinate y_k^B of the profile. These differences, which must be positive, are used to define the regularizing function $\Psi_3(\mathbf{p})$ (Equation 3):

$$\Psi_3(\mathbf{p}) = \|\mathbf{B}\mathbf{p} - \mathbf{b}\|_2^2, \quad (20)$$

where \mathbf{B} is a $B \times M$ matrix whose k -th line has one element equal to one and all the remaining elements equal to zero. This matrix is defined in the same way as matrix \mathbf{A} (Equation 19).

Practical procedures

Describe a brief recipe for choosing the weights $\tilde{\alpha}_\ell$ (equation 6) based on the convergence of the inverse problem, estimated model, etc.

APPLICATIONS TO SYNTHETIC DATA

Simple models

We have simulated two simple models (I and II) formed by four layers: water, sediments, crust (continental and oceanic) and mantle. The only differences between them are the geometries of basement and Moho. For both models, the reference density $\rho^{(r)}$ is equal to that of the continental crust. Figure 3 shows the result obtained by applying our method to invert the synthetic gravity disturbance produced by the simple model I, as well as the initial guess and known depths used in the inversion. This result was obtained by using all but the isostatic constraint. The weights α_ℓ (equation 3) were defined by using $\tilde{\alpha}_\ell$ (equation 6) given by: $\tilde{\alpha}_0 = 0$, $\tilde{\alpha}_1 = 10^1$, $\tilde{\alpha}_2 = 10^2$ and $\tilde{\alpha}_3 = 10^2$. Notice that, without using the isostatic constraint, our method was able to estimate a model that fits the simulated gravity disturbance and lithostatic stress curve, as well as shows basement and Moho reliefs very close to the true ones. In this case, both basement and Moho are smooth. However, the lithostatic stress curve shows a pronounced discontinuity over the COT. This feature breaks the smoothness of the lithostatic stress curve and is not compatible with the a priori information imposed by the isostatic constraint (equation 16).

Figure 4 shows the result obtained by using all the constraints (including the isostatic constraint). In this case, the weights α_ℓ (equation 3) were defined by using different values for the positive scalars $\tilde{\alpha}_\ell$ (equation 6): $\tilde{\alpha}_0 = 10^2$, $\tilde{\alpha}_1 = 10^1$, $\tilde{\alpha}_2 = 10^2$ and $\tilde{\alpha}_3 = 10^2$. By using the isostatic constraint, we obtain a predicted lithostatic stress curve that is smoother than that shown in Figure 3. However, differently from the previous result, there is a significant discrepancy between the estimated and true reliefs of basement and Moho. The larger differences occur on the region close to COT, where the true lithostatic stress

curve shows that steep slope. These results illustrate a situation in which the a priori information imposed by the isostatic constraint is not compatible with the true model.

Figures 5 and 6 show an example in which the isostatic constraint imposes the correct a priori information. These results were obtained by applying our method to invert the synthetic gravity disturbance produced by the simple model II. The result shown in the first figure was obtained by using all but the isostatic constraint. The weights α_ℓ (equation 3) were defined by using $\tilde{\alpha}_\ell$ (equation 6) given by: $\tilde{\alpha}_0 = 0$, $\tilde{\alpha}_1 = 10^{-1}$, $\tilde{\alpha}_2 = 10^0$ and $\tilde{\alpha}_3 = 10^0$. The result shown in Figure 6 was obtained by using all constraints. The weights α_ℓ (equation 3) were defined by using $\tilde{\alpha}_\ell$ (equation 6) given by: $\tilde{\alpha}_0 = 10^0$, $\tilde{\alpha}_1 = 10^{-1}$, $\tilde{\alpha}_2 = 10^0$ and $\tilde{\alpha}_3 = 10^0$. In this example, the results obtained with and without the isostatic constraint produced practically the same data fit. However, there are significant differences on the lithostatic stress curves and the geometry of the estimated models. We can see that the isostatic constraint produces a smoother lithostatic stress curve, which is in perfect agreement with the a priori information imposed by the regularizing function $\Psi_0(\mathbf{p})$ (equation 16). The isostatic constraint also produces an estimated Moho which is closer to the true one along the entire profile. The main differences in the estimated basement, however, occur at the first ≈ 60 km, on the region coincident with the abrupt crustal thinning in the simple model II. It is worth noting that, on this region, the true lithostatic stress curve is relatively smooth and the basement presents steep slopes. These slopes cannot be properly retrieved without using the isostatic constraint, as shown in Figure 5. Differently from the results shown in Figure 3 and 4, those shown in Figures 5 and 6 exemplify a case in which the isostatic constraint contributes to better estimating the geometries of basement and Moho.

Volcanic margin model

We have simulated a simple volcanic margin model formed by four layers: water, sediments + seaward dipping reflectors, crust (continental and oceanic) and mantle. The reference density $\rho^{(r)}$ is equal to that of the continental crust. Similarly to the simple model II (Figures 5 and 6), our volcanic margin model shows a significant crustal thinning at the first part of the profile. Figures 7 and 8 show the results obtained, respectively, by using and not using the isostatic constraint to estimate the geometries of basement and Moho. The weights α_ℓ (equation 3) used to obtain the result shown in the first figure were defined with $\tilde{\alpha}_\ell$ (equation 6) equal to: $\tilde{\alpha}_0 = 0$, $\tilde{\alpha}_1 = 10^{-1}$, $\tilde{\alpha}_2 = 10^0$ and $\tilde{\alpha}_3 = 10^0$. The $\tilde{\alpha}_\ell$ (equation 6) used to obtain the result shown in Figure 8 are given by: $\tilde{\alpha}_0 = 10^0$, $\tilde{\alpha}_1 = 10^{-1}$, $\tilde{\alpha}_2 = 10^0$ and $\tilde{\alpha}_3 = 10^0$.

We can see that, without using the isostatic constraint, our method could not retrieve the pronounced crustal thinning located at the first part of our volcanic margin model. As shown in Figure 7, the difference between the estimated and true basement reach ≈ 10 km at the position ≈ 75 km on the profile. On the other hand, as in the previous test with the simple model II, the isostatic constraint was able to produce an estimated basement very close to the true one (Figure 8).

APPLICATION TO REAL DATA

We applied our method to interpret a gravity profile over the Pelotas basin (Stica et al., 2014), located at the southern of Brazil. This basin is considered a classical example of volcanic margin (Geoffroy, 2005) showing ...

CONCLUSIONS

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quat lorem. Sed lacinia nulla vitae enim. Pellentesque tincidunt purus vel magna. Integer non enim. Praesent euismod nunc eu purus. Donec bibendum quam in tellus. Nullam cursus pulvinar lectus. Donec et mi. Nam vulputate metus eu enim. Vestibulum pellentesque felis eu massa.

ACKNOWLEDGMENTS

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LIST OF FIGURES

1 Rifted margin model formed by four layers. The first one represents a water layer with constant density $\rho^{(w)}$. The second layer is formed by $Q = 2$ vertically adjacent parts. They represent sediments, salt or volcanic rocks and have constant densities $\rho^{(q)}$, $q = 1, \dots, Q$. The third layer represents the crust, which is divided into the continental crust, with a constant density $\rho^{(cc)}$, and the oceanic crust, with a constant density $\rho^{(oc)}$. We presume an abrupt Crust-Ocean Transition (COT). Finally, the fourth layer of our model represents a homogeneous mantle with constant density $\rho^{(m)}$. Basement and Moho are represented by the dashed-white lines. The continuous white lines represent the isostatic compensation depth at S_0 and the reference Moho at $S_0 + \Delta S$.

2 Interpretation model formed by N columns of vertically stacked prisms. Each column is formed by four layers of prisms and locally approximates the four layers of the rifted margin model (Figure 1). Each prism has a constant density contrast defined as the difference between its corresponding density at the rifted margin model (Figure 1) and the constant density $\rho^{(r)}$ of the shallowest layer forming the reference density distribution (see text). Basement and Moho are represented by the dashed-white lines. The continuous white line represents the isostatic compensation depth at S_0 . The base of the interpretation model coincides with the reference Moho located at $S_0 + \Delta S$.

3 Application to synthetic data produced by the simple model I. The numbers in the legend represent the density values in kg/m^3 . The bottom panel shows the estimated and true surfaces, the initial basement and Moho used in the inversion (initial guess surfaces), as well as the known depths at basement (blue triangles) and Moho (green diamonds). The middle panel shows the true and estimated lithostatic stress curves computed by using equation 7. The values are multiplied by a constant gravity value equal to 9.81 m/s^2 . The

upper panel shows the true gravity disturbance data produced by the simple model I (simulated data), as well as the data produced by the estimated model (predicted data) and that produced by the model used as initial guess in the inversion (initial guess data). The estimated model was obtained by using all but the isostatic constraint. For simplicity, the contour of the prisms forming the interpretation model were omitted.

4 Application to synthetic data produced by the simple model I. The difference with respect to Figure 3 is that the estimated model was obtained by using all constraints.

5 Application to synthetic data produced by the simple model II. The numbers in the legend represent the density values in kg/m^3 . The bottom panel shows the estimated and true surfaces, the initial basement and Moho used in the inversion (initial guess surfaces), as well as the known depths at basement (blue triangles) and Moho (green diamonds). The middle panel shows the true and estimated lithostatic stress curves computed by using equation 7. The values are multiplied by a constant gravity value equal to 9.81 m/s^2 . The upper panel shows the true gravity disturbance data produced by the simple model II (simulated data), as well as the data produced by the estimated model (predicted data) and that produced by the model used as initial guess in the inversion (initial guess data). The estimated model was obtained by using all but the isostatic constraint. For simplicity, the contour of the prisms forming the interpretation model were omitted.

6 Application to synthetic data produced by the simple model II. The difference with respect to Figure 5 is that the estimated model was obtained by using all constraints.

7 Application to synthetic data produced by the volcanic margin model. The numbers in the legend represent the density values in kg/m^3 . The bottom panel shows the estimated and true surfaces, the initial basement and Moho used in the inversion (initial guess surfaces), as well as the known depths at basement (blue triangles) and Moho (green

diamonds). The middle panel shows the true and estimated lithostatic stress curves computed by using equation 7. The values are multiplied by a constant gravity value equal to 9.81 m/s^2 . The upper panel shows the true gravity disturbance data produced by the volcanic margin model (simulated data), as well as the data produced by the estimated model (predicted data) and that produced by the model used as initial guess in the inversion (initial guess data). The estimated model was obtained by using all but the isostatic constraint. For simplicity, the contour of the prisms forming the interpretation model were omitted.

8 Application to synthetic data produced by the volcanic margin model. The difference with respect to Figure 7 is that the estimated model was obtained by using all constraints.

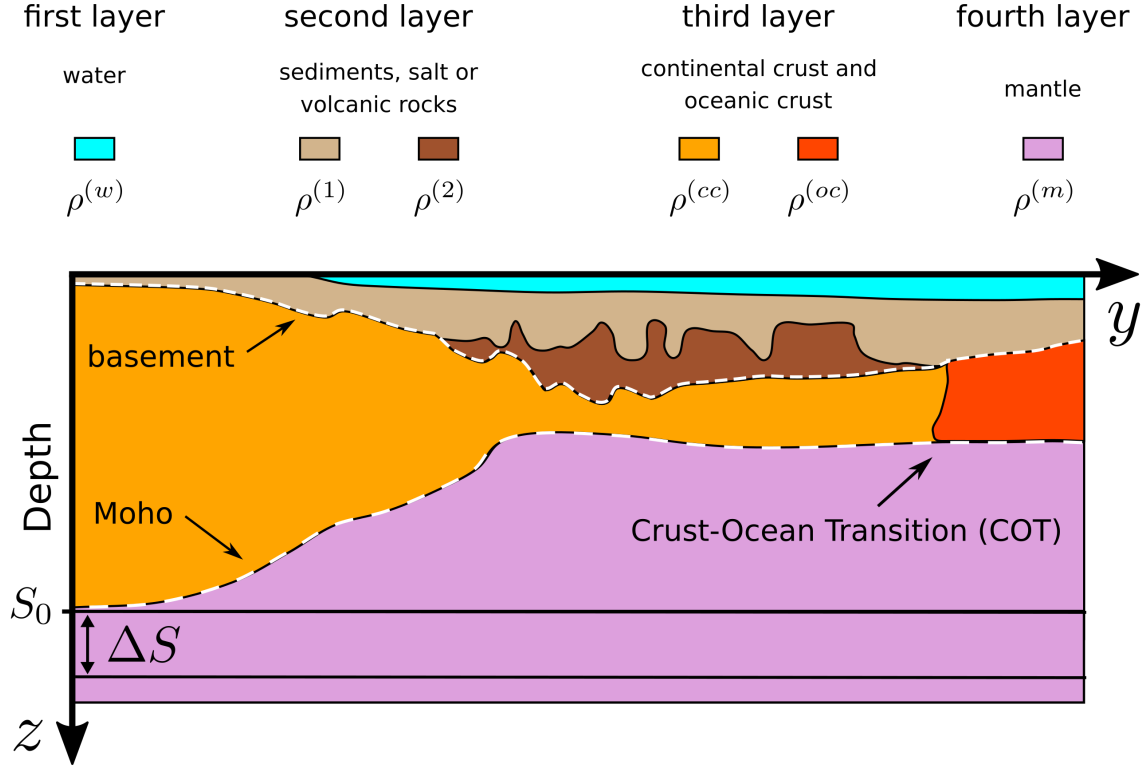


Figure 1: Rifted margin model formed by four layers. The first one represents a water layer with constant density $\rho^{(w)}$. The second layer is formed by $Q = 2$ vertically adjacent parts. They represent sediments, salt or volcanic rocks and have constant densities $\rho^{(q)}$, $q = 1, \dots, Q$. The third layer represents the crust, which is divided into the continental crust, with a constant density $\rho^{(cc)}$, and the oceanic crust, with a constant density $\rho^{(oc)}$. We presume an abrupt Crust-Ocean Transition (COT). Finally, the fourth layer of our model represents a homogeneous mantle with constant density $\rho^{(m)}$. Basement and Moho are represented by the dashed-white lines. The continuous white lines represent the isostatic compensation depth at S_0 and the reference Moho at $S_0 + \Delta S$.

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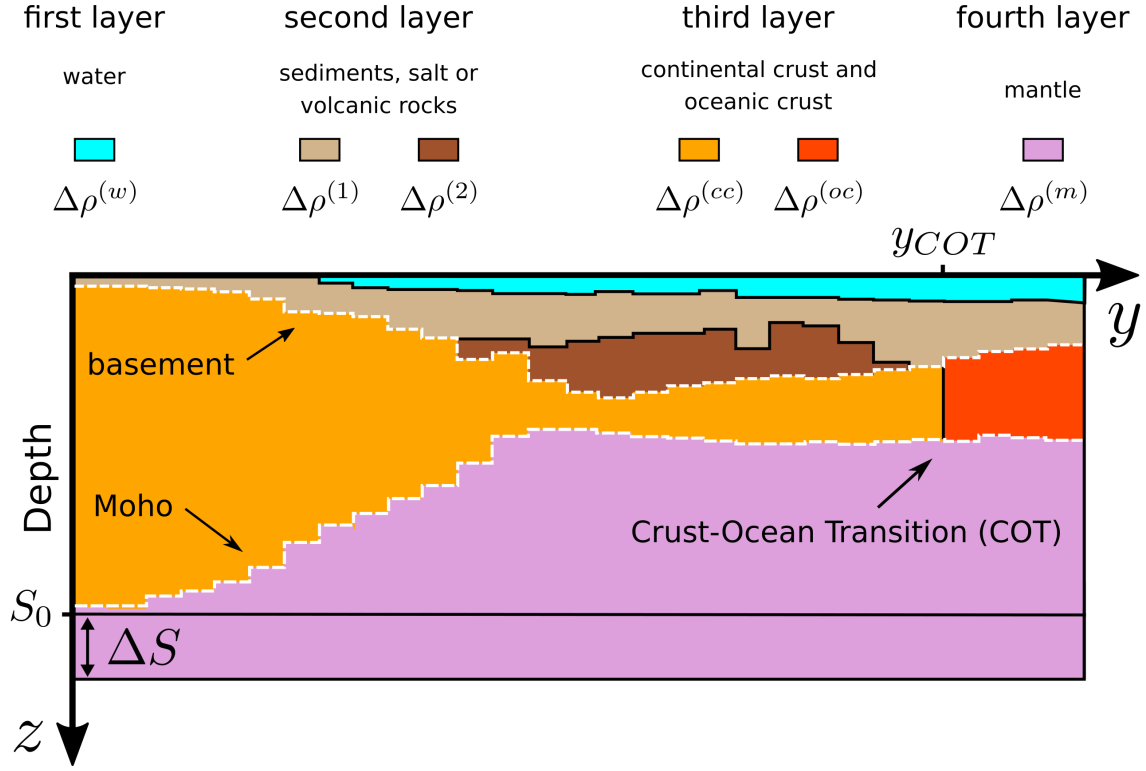


Figure 2: Interpretation model formed by N columns of vertically stacked prisms. Each column is formed by four layers of prisms and locally approximates the four layers of the rifted margin model (Figure 1). Each prism has a constant density contrast defined as the difference between its corresponding density at the rifted margin model (Figure 1) and the constant density $\rho^{(r)}$ of the shallowest layer forming the reference density distribution (see text). Basement and Moho are represented by the dashed-white lines. The continuous white line represents the isostatic compensation depth at S_0 . The base of the interpretation model coincides with the reference Moho located at $S_0 + \Delta S$.

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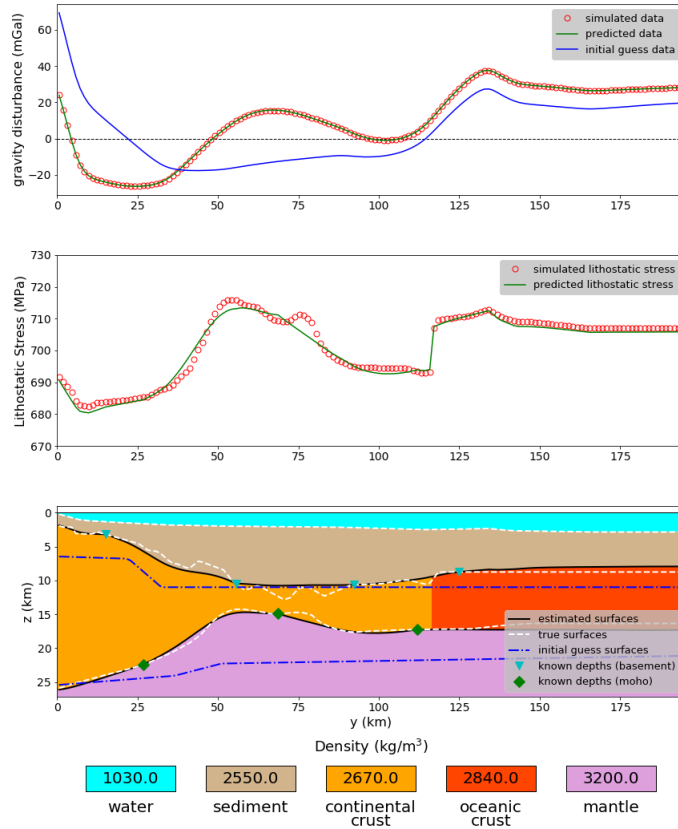


Figure 3: Application to synthetic data produced by the simple model I. The numbers in the legend represent the density values in kg/m^3 . The bottom panel shows the estimated and true surfaces, the initial basement and Moho used in the inversion (initial guess surfaces), as well as the known depths at basement (blue triangles) and Moho (green diamonds). The middle panel shows the true and estimated lithostatic stress curves computed by using equation 7. The values are multiplied by a constant gravity value equal to 9.81 m/s^2 . The upper panel shows the true gravity disturbance data produced by the simple model I (simulated data), as well as the data produced by the estimated model (predicted data) and that produced by the model used as initial guess in the inversion (initial guess data). The estimated model was obtained by using all but the isostatic constraint. For simplicity, the contour of the prisms forming the interpretation model were omitted.

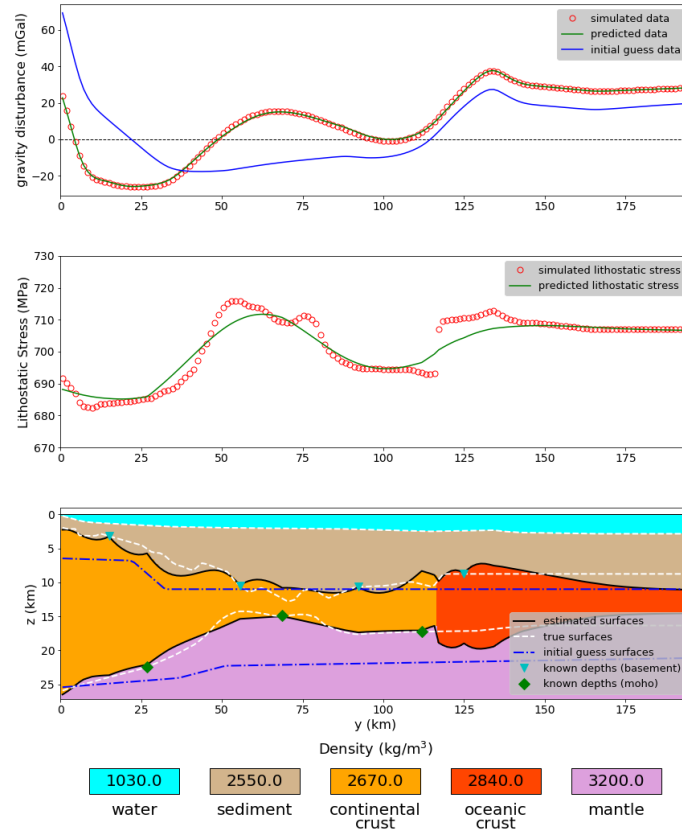


Figure 4: Application to synthetic data produced by the simple model I. The difference with respect to Figure 3 is that the estimated model was obtained by using all constraints.

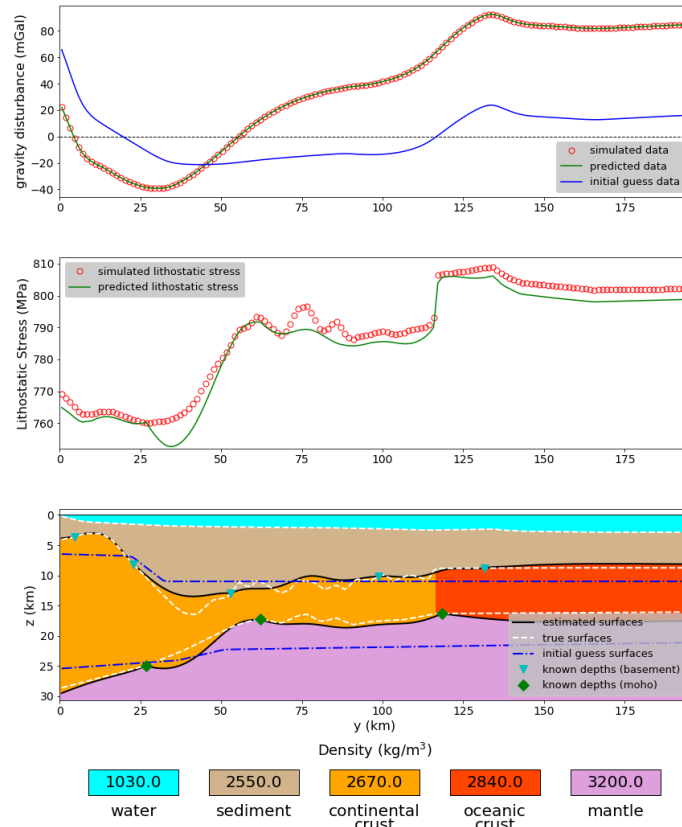


Figure 5: Application to synthetic data produced by the simple model II. The numbers in the legend represent the density values in kg/m^3 . The bottom panel shows the estimated and true surfaces, the initial basement and Moho used in the inversion (initial guess surfaces), as well as the known depths at basement (blue triangles) and Moho (green diamonds). The middle panel shows the true and estimated lithostatic stress curves computed by using equation 7. The values are multiplied by a constant gravity value equal to 9.81 m/s^2 . The upper panel shows the true gravity disturbance data produced by the simple model II (simulated data), as well as the data produced by the estimated model (predicted data) and that produced by the model used as initial guess in the inversion (initial guess data). The estimated model was obtained by using all but the isostatic constraint. For simplicity, the contour of the prisms forming the interpretation model were omitted.

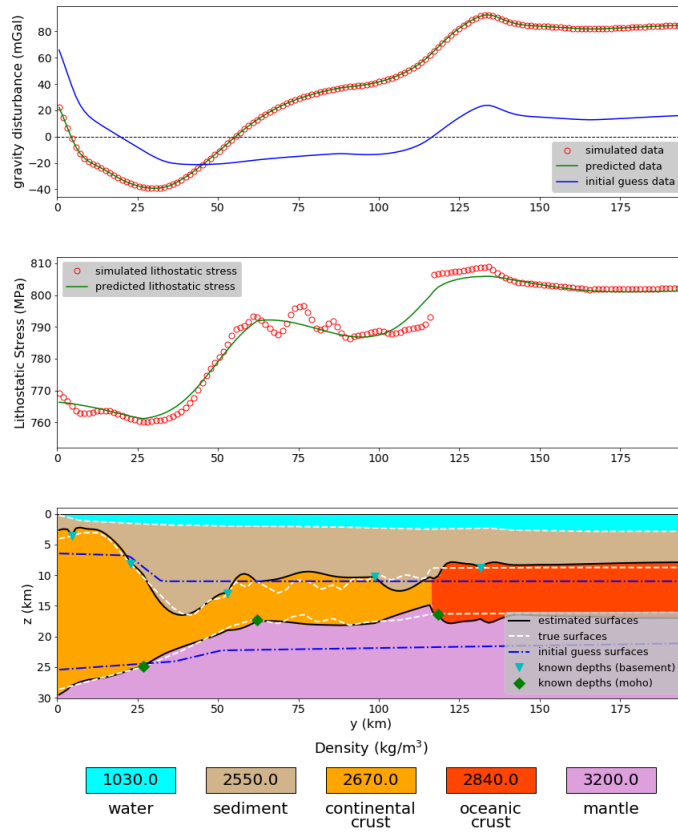


Figure 6: Application to synthetic data produced by the simple model II. The difference with respect to Figure 5 is that the estimated model was obtained by using all constraints.

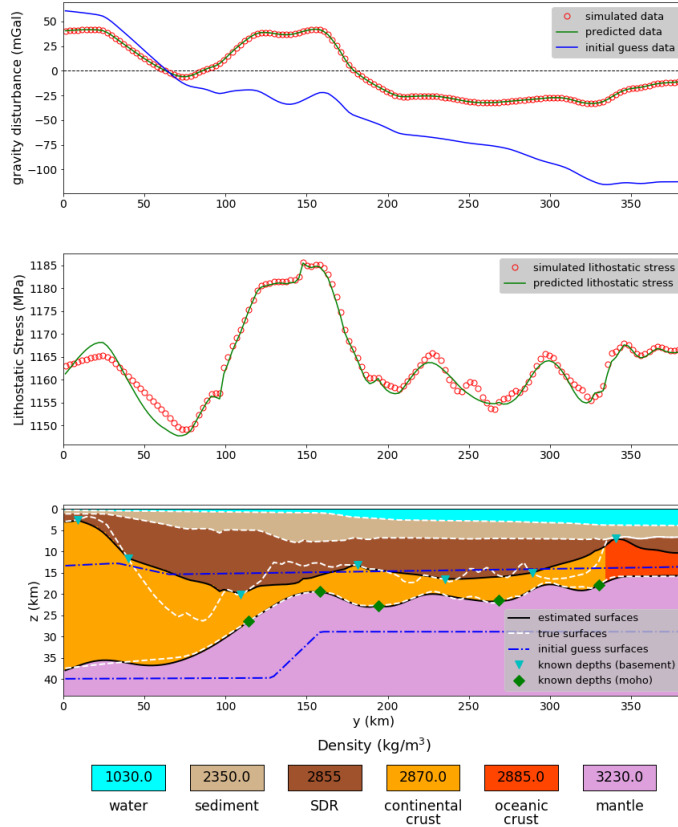


Figure 7: Application to synthetic data produced by the volcanic margin model. The numbers in the legend represent the density values in kg/m^3 . The bottom panel shows the estimated and true surfaces, the initial basement and Moho used in the inversion (initial guess surfaces), as well as the known depths at basement (blue triangles) and Moho (green diamonds). The middle panel shows the true and estimated lithostatic stress curves computed by using equation 7. The values are multiplied by a constant gravity value equal to 9.81 m/s^2 . The upper panel shows the true gravity disturbance data produced by the volcanic margin model (simulated data), as well as the data produced by the estimated model (predicted data) and that produced by the model used as initial guess in the inversion (initial guess data). The estimated model was obtained by using all but the isostatic constraint. For simplicity, the contour of the prisms forming the interpretation model were omitted.

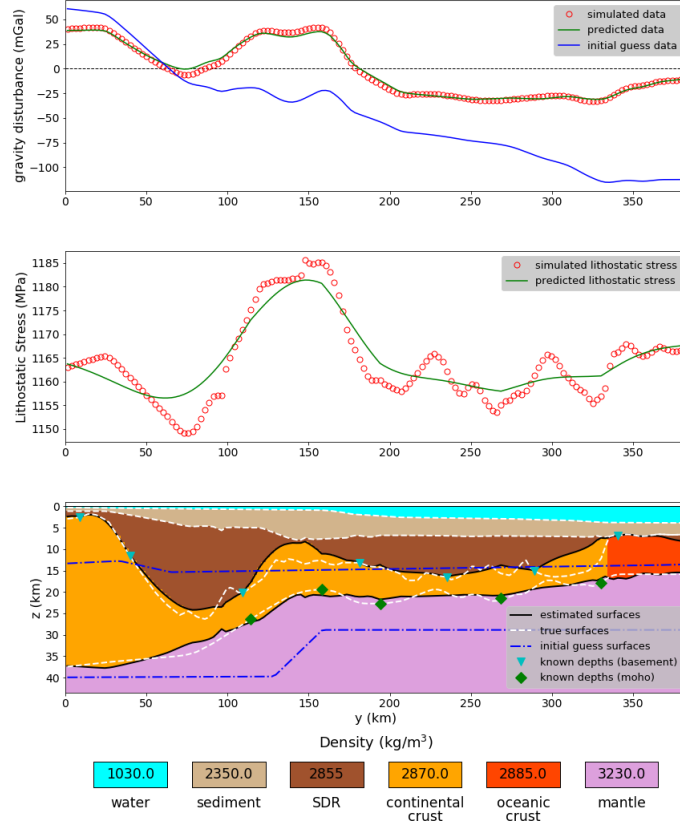


Figure 8: Application to synthetic data produced by the volcanic margin model. The difference with respect to Figure 7 is that the estimated model was obtained by using all constraints.

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