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Setups

1.1 vimrc [6c9876]

```
se nu ai rnu cin ts=4 sw=4 | sy on
inoremap {<CR> {<CR>}<Esc>0
inoremap jk <Esc>
```

1.2 pbds [9f7c3e]

```
#include <bits/stdc++.h>
#include <bits/extc++.h>
using namespace __gnu_pbds;
using namespace std;
template <typename T>
using ordered_set = tree<T,null_type,less</pre>
    <T>,rb_tree_tag,tree_order_statistics_node_update>;
int main(){
   ordered set < int > st:
    st.insert(1);
    st.find_by_order(0);//iterator to 1
    st.order_of_key(1);//returns 0
```

1.3 terminal [46fc34]

```
- terminal --
$ setxkbmap -option caps:swapescape
```

1.4 debug [33c0d3]

```
#ifdef MIKU
string
      dbmc = "\033[1;38;2;57;197;187m", dbrs = \033[0m;
#define debug
     (x...) cout << dbmc << "[" << #x << "] : ", dout(x)
void dout() { cout << dbrs << endl; }</pre>
template <typename T, typename ...U>
void dout(T t, U ...u) { cout
      << t << sizeof...(u) ? ", " : ""; dout(u...); }
#define debug(...) 39
#endif
int main(){
     int a = 49;
     char c = '8';
     debug(a);// outputs "[a] : 49"
debug(a, c); // outputs "[a, c] : 49, 8"
debug("PCCORZ"); // outputs "["PCCORZ"] : PCCORZ"
debug(); // outputs "[] : "
```

1.5 template [5116af]

```
#include <bits/stdc++.h>
using namespace std;
#define fs first
#define sc second
#define F first
#define S second
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++) | #define tiii tuple<int,int,int>
```

```
using ll = long long;
using lll = __int128_t;
typedef pair < int, int > pii;
typedef tuple < int, int, int > tiii;
typedef pair<ll,ll> pll
int main(){
```

Graph

2.1 Dominator Tree [3b89c3]

```
struct DominatorTree{
  //1-indexed
   //not reachable from s -> not on tree
  int n:
  vector < vector < int >> G.rG:
  vector<int> pa,dfn,id;
  int dfnCnt:
  vector<int> semi,idom,best;
  vector<vector<int>> ret;
  void init(int _n){
    n=_n;
    G = rG = ret = vector<vector<int>>(n+1);
    pa = dfn = id = vector < int > (n+1,-1);
    dfnCnt = 0;
     semi = idom = best = vector<int>(n+1,-1);
  void add_edge(int u,int v){
    G[u].push_back(v);
    rG[v].push_back(u);
  void dfs(int u){
    id[dfn[u]=++dfnCnt]=u;
    for(auto v:G[u]) if(!dfn[v]){
       dfs(v),pa[dfn[v]]=dfn[u];
  int find(int y,int x){
    if(y<=x)return y;</pre>
     int tmp=find(pa[y],x);
     if(semi[best[y]]>semi[best[pa[y]]])
       best[y]=best[pa[y]];
     return pa[y]=tmp;
  void tarjan(int root){
    dfnCnt=0;
    for(int i=1;i<=n;++i){</pre>
       dfn[i]=idom[i]=0;
       ret[i].clear();
       best[i]=semi[i]=i;
    dfs(root);
for(int i=dfnCnt;i>1;--i){
       int u=id[i];
       for(auto v:rG[u]) if(v=dfn[v]){
         find(v,i);
         semi[i]=min(semi[i],semi[best[v]]);
       ret[semi[i]].push_back(i);
       for(auto v:ret[pa[i]]){
         find(v,pa[i]);
         idom[v
             ] = semi[best[v]]==pa[i] ? pa[i] : best[v];
       ret[pa[i]].clear();
    for(int i=2; i<=dfnCnt; ++i){
  if(idom[i]!=semi[i]) idom[i]=idom[idom[i]];</pre>
       ret[id[idom[i]]].push_back(id[i]);
  vector<vector<int>> solve(int s){
    tarjan(s);
     return ret;
};
```

2.2 Incremental SCC [d8b556]

```
struct IncrementalSCC{
#define pii pair<int,int>
#define fs first
#define sc second
```

```
//if u == v : ans[i] = -1
//if not connected : ans[i] = m
//all 0-indexed
int n;
vector<int> ans;
int m;
vector<tiii> all:
vector<int> SCC(int n, vector<vector<int>>& paths){
  vector < int > scc_id(n,-1), idx(n,-1), low(n,-1), st;
  int cnt = 0,gcnt = 0;
  function < void(int) > dfs = [&](int now) -> void{
    low[now] = idx[now] = cnt++;
    st.push_back(now);
    for(auto nxt:paths[now]){
      if(scc_id[nxt] != -1)continue;
      if(idx[nxt] == -1){
        dfs(nxt);
        low[now] = min(low[now],low[nxt]);
        low[now] = min(low[now],idx[nxt]);
      }
    if(low[now] == idx[now]){
      int id = -1;
      while(id != now){
        id = st.back();
        st.pop_back();
        scc_id[id] = gcnt;
      qcnt++;
   }
  for(int i = 0;i<n;i++){</pre>
   if(scc_id[i] == -1)dfs(i);
  return scc_id;
vector<int> mapping;
void dc(int l,int r,vector<tiii> &edges){
 if(l == r){
    for(auto
         &[id,_,__]:edges)ans[id] = min(ans[id],l);
    return;
  int mid = (l+r)>>1;
  int cnt = 0;
  for(auto &[t,u,v]:edges){
    if(mapping[u] == -1)mapping[u] = cnt++;
    if(mapping[v] == -1)mapping[v] = cnt++;
 }
 n = cnt;
 vector<vector<int>> paths(n);
  vector<int> vv;
  for(auto &[t,u,v]:edges){
   vv.push_back(u);
    vv.push_back(v);
    u = mapping[u],v = mapping[v];
    if(t<=mid)paths[u].push_back(v);</pre>
  for(auto &i:vv)mapping[i] = -1;
  auto scc_id = SCC(n,paths);
  vector<tiii> vl,vr;
  for(auto &[t,u,v]:edges){
    if(scc_id[u] == scc_id[v]){
      ans[t] = min(ans[t],mid);
      vl.push_back(tiii(t,u,v));
    else{
      u = scc_id[u],v = scc_id[v];
      vr.push_back(tiii(t,u,v));
 vector < tiii > ().swap(edges);
 dc(l,mid,vl);
 dc(mid+1,r,vr);
 return;
void add edge(int u.int v){
 all.push_back(tiii(all.size(),u,v));
vector<tiii> solve(){//[time,u,v]
 m = all.size();
 vector<tiii> ret(m):
 for(auto [t,u,v]:all)ret[t] = tiii(m,u,v);
```

```
for(auto [t,u,v]:all)n = max({n,u,v});
    n++;
    ans = vector<int>(m,m);
    for(auto [t,u,v]:all){
      if(u == v)ans[t] = -1;
    mapping = vector<int>(n,-1);
    dc(0,m,all);
    for(int i = 0;i<m;i++)get<0>(ret[i]) = ans[i];
    return ret;
  IncrementalSCC(){
    ans.clear();
    n = m = 0;
#undef tiii
#undef pii
#undef fs
#undef sc
}:
```

2.3 Block-Cut Tree [f44682]

```
struct BlockCutTree{
  //0-indexed
  //returns a forest if the graph is not connected
  vector < vector < int >> g;
  vector<vector<int>> groups;
  vector<vector<int>> tr;
  vector < int > idx, low, st;
  int cnt,gcnt;
  int n;
  RoundSquareTree(int _n = 0){
    cnt = gcnt = 0;
    n = n;
    g = vector<vector<int>>(n);
  void add_edge(int a,int b){//adds bidirectional edges
    g[a].push_back(b);
    g[b].push_back(a);
  void dfs(int now){
    idx[now] = low[now] = cnt++;
    st.push_back(now);
    for(auto nxt:g[now]){
      if(idx[nxt] == -1){
         dfs(nxt);
         low[now] = min(low[now],low[nxt]);
         if(low[nxt] == idx[now]){
           int id = -1;
           tr.push_back(vector<int>());
           while(id != nxt){
             id = st.back();st.pop_back();
             groups[id].push_back(gcnt);
             tr[id].push_back(gcnt+n);
             tr[gcnt+n].push_back(id);
           groups[now].push_back(gcnt);
           tr[now].push_back(gcnt+n);
           tr[gcnt+n].push_back(now);
           gcnt++;
        }
      else idx[now] = min(idx[now],idx[nxt]);
    }
    return;
  }
  vector<vector<int>> solve(){//
       returns the tree (round vertices numbered [0,n))
    idx = low = vector<int>(n,-1);
    tr = vector<vector<int>>(n);
    for(int i = 0;i<n;i++){</pre>
      if(idx[i] == -1)dfs(i);
    return tr:
  }
};
```

2.4 **Euler Tour** [22e960]

```
#include <bits/stdc++.h>
using namespace std;

struct EulerTour{
   //undirected graph,0-indexed,fails if doesn't exist
   //returns the order of edges
   vector<vector<pii>>> g;
```

```
vector<int> ptr;
  vector<bool> vis;
  vector<int> re;
  int n,ecnt;
  void init(int _n){
   n = _n;
    ecnt = 0;
    g = vector<vector<pii>>>(n);
    ptr = vector<int>(n);
  void add_edge(int a,int b,int id = -1){
   if(id == -1)id = ecnt;
    g[a].push_back(pii(b,id));
    g[b].push_back(pii(a,id));
    ecnt++;
 }
  void dfs(int now){
    for(int &i = ptr[now];i<g[now].size();i++){</pre>
      auto [to,eid] = g[now][i];
      if(vis[eid])continue;
      vis[eid] = true;
      dfs(to);
      re.push_back(eid);
    return:
 }
  vector<int> solve(int s){
    re.clear();
    vis = vector<bool>(ecnt,0);
    dfs(s);
    reverse(re.begin(),re.end());
    return re;
 }
};
2.5 Dinic [360712]
struct Dinic{//0-indexed
 struct E{
    int t,f,c;
    E(int tt
```

```
= 0, int cc = 0, int ff = 0):t(tt),c(cc),f(ff){}
vector<vector<int>> paths;
vector<int> ptr,lvl;
vector<E> e;
queue<int> q;
Dinic(int _n = 0){
  paths = vector<vector<int>>(_n);
  ptr = lvl = vector<int>(_n);
void add_edge(int a,int b,int c,int d = 0){
  paths[a].push_back(e.size());
  e.push_back(E(b,c));
  paths[b].push_back(e.size());
  e.push_back(E(a,d));
bool bfs(int s,int t){
  fill(lvl.begin(),lvl.end(),-1);
  q.push(s);
  lvl[s] = 0:
  while(!q.empty()){
    auto now = q.front();q.pop();
    for(auto &eid:paths[now]){
      if(e[eid].f == e[eid].c)continue;
      if(lvl[e[eid].t] == -1){
   lvl[e[eid].t] = lvl[now]+1;
        q.push(e[eid].t);
    }
  return lvl[t] != -1;
int dfs(int now,int t,int flow){
  if(now == t)return flow;
  for(int &i = ptr[now];i<paths[now].size();i++){</pre>
    int eid = paths[now][i];
    if(e[eid].f == e[
        eid].c||lvl[e[eid].t] != lvl[now]+1)continue;
    if(int re =
        dfs(e[eid].t,t,min(flow,e[eid].c-e[eid].f))){
      e[eid].f += re;
      e[eid^1].f -=re;
      return re:
    }
  return 0;
```

```
int flow(int s,int t){
    int ans = 0;
    while(bfs(s,t)){
      fill(ptr.begin(),ptr.end(),0);
      while(auto re = dfs(s,t,INT_MAX)){
        ans += re;
      }
    }
    return ans;
  bool inScut(int k){
    return lvl[k] != -1;
};
```

2.6 Gomory-Hu Tree [3ab29a]

```
struct GomoryHuTree{//0-indexed
#define pii pair<int,int>
#define tiii tuple<int,int,int>
  vector<tiii> edges;
  vector<vector<pii>> tr;
  vector<int> p;
  int n;
  GomoryHuTree(int _n = 0){
    n = _n;
    p = vector<int>(_n,0);
    tr = vector<vector<pii>>(_n);
  void add edge(int a,int b,int c){
    edges.push_back(tiii(a,b,c));
  vector<vector<pii>> make_tree(){
    fill(p.begin(),p.end(),0);
    tr = vector<vector<pii>>>(n);
    for(int i = 1;i<p.size();i++){</pre>
      Dinic din(n);
      for(auto &[a,b,w]:edges){
        din.add_edge(a,b,w,w);
      int w = din.flow(i,p[i]);
      tr[i].push_back(pii(p[i],w));
      tr[p[i]].push_back(pii(i,w));
      for(int j = i+1;j<n;j++){</pre>
        if(p[j] == p[i]&&din.inScut(j))p[j] = i;
    return tr;
  }
#undef pii
#undef tiii
};
```

2.7 Min-Cost-Max-Flow [80eed6]

```
#define T ll
const T inf = 1e12;
struct MCMF{//TC:0(VEF)
  struct E{
    int t.f:
    T c,w;
    E(int tt,T cap,T wei):t(tt),c(cap),w(wei),f(0){}
  vector < E > e;
  vector<vector<int>> paths:
  vector<T> dis:
  vector<int> pre;
  vector < bool > inq;
  queue<int> q;
  int n:
  MCMF(int _n = 0){
    n = _n;
    paths = vector<vector<int>>(n);
    e.clear();
    pre = vector<int>(n);
    dis = vector<T>(n);
    inq = vector<bool>(n);
  void add_edge
      (int a,int b,int c,int d){//from,to,cap,wei
    paths[a].push_back(e.size());
    e.push_back(E(b,c,d));
    paths[b].push_back(e.size());
    e.push back(E(a,0,-d));
  bool SPFA(int s,int t){
```

```
fill(dis.begin(),dis.end(),inf);
    fill(pre.begin(),pre.end(),-1);
    dis[s] = 0;
    q.push(s);inq[s] = true;
    while(!q.empty()){
      auto now = q.front();q.pop();
inq[now] = false;
      //assert(dis[now]>=0);
      for(auto &eid:paths[now]){
        if(e[eid].f == e[eid].c)continue;
        int nxt = e[eid].t;
        if(dis[nxt]>dis[now]+e[eid].w){
          pre[nxt] = eid;
          dis[nxt] = dis[now]+e[eid].w;
          if(!inq[nxt]){
            ing[nxt] = true;
            q.push(nxt);
          }
        }
      }
    }
    return dis[t] != inf;
  T flow(int s,int
      t, int cnt = INT_MAX){//cnt is the number of flows
    T ans = 0;
    while(cnt--&&SPFA(s,t)){
      ans += dis[t];
      int now = t;
      while(pre[now] != -1){
        int eid = pre[now];
        e[eid].f++;
        e[eid^1].f--;
        now = e[eid^1].t;
    return ans;
  }
};
#undef T
2.8 KM [2bf044]
```

```
// Kuhn-Munkres :
    Bipartite matching with "maximum" weight in O(n^3)
struct KM{
    const static int
        M = 500; // modify maximum number of vertices
    int n;
   ll ans = 0;
   // 0-base
   vector
   vector<ll> lx, ly, slack;
   bitset<M> visx, visy; // initialize with all zero
    // abbr
# define forx for(int x=0; x<n; x++)</pre>
 define fory for(int y=0; y<n; y++)</pre>
# define z match[y]
    bool dfs(int x){
       visx[x] = 1;
        fory{
           if(visy[y]) continue;
           ll d = lx[x]+ly[y]-w[x][y];
           if(!d){
               visy[y] = 1;
               if(z==-1 || (!visx[z] && dfs(z))){
                   z = x;
                   return 1:
               }
           else if(d<slack[y]) slack[y] = d;</pre>
       return 0;
   }
    bool augment(){
       fory if(!visy[y] && !slack[y]){
           visy[y] = 1;
           if(z==-1) return 1;
           else if(!visx[z] && dfs(z)){
               z = -1;
               return 1;
           }
```

```
return 0:
    void relabel(){
        ll d = INT64_MAX;
        fory if(!visy[y]) d = min(d, slack[y]);
        forx if(visx[x]) lx[x] -= d;
            if(visy[y]) ly[y] += d;
            else slack[y] -= d;
        }
    }
    KM(vector<vector<ll>>
        &W): n(W.size()), w(W) { // input edges' weight
        //initialize
        slack.resize(n);
        match.assign(n, -1);
        lx.assign(n, INT64_MIN);
        ly.assign(n, ⊖);
        forx fory lx[x] = max(lx[x], w[x][y]);
        //matching
        forx{
            visx.reset();
            visv.reset();
            visx[x] = 1;
            fory slack[y] = lx[x]+ly[y]-w[x][y];
            while(!augment()) relabel();
            visx.reset();
            visy.reset();
            dfs(x);
        //summing
        forx ans += lx[x];
        fory ans += ly[y];
    }
# undef forx
# undef fory
# undef z
};
```

2.9 Max Clique [0de041]

```
constexpr size_t kN = 150; using bits = bitset<kN>;
#define _all(T) T.begin(),T.end()
struct MaxClique {
  bits G[kN], cs[kN];
  int ans, sol[kN], q, cur[kN], d[kN], n;
void init(int _n) {
    n = _n;
    for (int i = 0; i < n; ++i) G[i].reset();</pre>
      add_edge(int u, int v) { G[u][v] = G[v][u] = 1; }
  void pre_dfs(vector<int> &v, int i, bits mask) {
    if (i < 4) {
      for (
           int x : v) d[x] = (int)(G[x] \& mask).count();
      sort(_all(v), [&](int x, int y) {
  return d[x] > d[y]; });
    vector<int> c(v.size());
    cs[1].reset(), cs[2].reset();
    int l = max(ans - q + 1, 1), r = 2, tp = 0, k;
    for (int p : v) {
      for (k = 1; (cs[k] \& G[p]).any(); ++k);
      if (k >= r) cs[++r].reset();
      cs[k][p] = 1;
      if (k < l) v[tp++] = p;
    for (k = l; k < r; ++k)</pre>
      for (auto p = cs[k]._Find_first();
          p < kN; p = cs[k]._Find_next(p))</pre>
        v[tp] = (int)p, c[tp] = k, ++tp;
    dfs(v, c, i + 1, mask);
  void dfs(vector<int> &v, vector<int> &c,
      int i, bits mask) {
    while (!v.empty()) {
      int p = v.back(); v.pop_back(); mask[p] = 0;
      if (q + c.back() <= ans) return;</pre>
      cur[q++] = p;
      vector<int> nr;
      for (int x : v) if (G[p][x]) nr.push_back(x);
      if (!nr.empty()) pre_dfs(nr, i, mask & G[p]);
```

```
else if (q > ans) ans = q, copy_n(cur, q, sol);
    c.pop_back(); --q;
}
int solve() {
    vector < int > v(n); iota(_all(v), 0);
    ans = q = 0; pre_dfs(v, 0, bits(string(n, '1')));
    return ans; // sol[0 ~ ans -1]
}
};
```

3 Data Structure

3.1 Li Chao Tree [565209]

```
//range add line get min
//can even be used if modifies aren't range modify \mbox{\tt \#define} ll \mbox{\tt long} \mbox{\tt long}
const ll SZ = 8e6+10;
const ll inf = 3e18;
vector<ll> all:
struct Line{
  ll m,b;
  Line(ll mm = 0,ll bb = 0):m(mm),b(bb){}
  ll operator()(ll k){
    return m*k+b;
struct LiChao{
#define ls now*2+1
#define rs now*2+2
#define mid ((l+r)>>1)
  Line seg[SZ];
  LiChao(){
    fill(seg,seg+SZ,Line(0,inf));
  void modify(int now,int l,int r,int s,int e,Line v){
      if(seg[now](all[l])>v(all[l]))swap(seg[now],v);
      return:
    if(l>=s&&e>=r){
      if(seg
           [now](all[mid])>v(all[mid]))swap(seg[now],v);
      if(seg[now].m<v.m)modify(ls,l,mid,s,e,v);</pre>
      else modify(rs,mid+1,r,s,e,v);
    else{
      if(mid>=s)modify(ls,l,mid,s,e,v);
      if(mid<e)modify(rs,mid+1,r,s,e,v);</pre>
    return:
  ll getval(int now,int l,int r,int p){
    if(l == r)return seg[now](all[p]);
    if(mid>=p)return
          min(seg[now](all[p]),getval(ls,l,mid,p));
    else return
         min(seg[now](all[p]),getval(rs,mid+1,r,p));
  void add_line(int s,int e,Line v){
    modify(0,0,all.size()-1,s,e,v);
    return:
  ll getmin(int p){
    return getval(0,0,all.size()-1,p);
#undef ls
#undef rs
#undef mid
#undef ll long long
```

3.2 Dynamic Convex Hull [98f67f]

```
ll Div(ll a.
        ll b) { return a / b - ((a ^ b) < 0 && a % b); }
  bool isect(iterator x, iterator y) {
    if (y == end()) { x->p = kInf; return 0; }
    if (x
    ->a == y->a) x->p = x->b > y->b ? kInf : -kInf; else x->p = Div(y->b - x->b, x->a - y->a);
    return x->p >= y->p;
  void addline(ll a, ll b) {
    auto z = insert({a, b, 0}), y = z++, x = y;
    while (isect(y, z)) z = erase(z);
    if (x != begin
         () && isect(--x, y)) isect(x, y = erase(y));
    while ((y = x) != begin
         () && (--x)->p >= y->p) isect(x, erase(y));
  ll query(ll x) {
    auto l = *lower_bound(x);
    return l.a * x + l.b;
  }
};
3.3 Treap [ff4001]
#define ll long long
//range reverse range add range sum
```

```
//need to push before using the info on node
struct node{
  int pri;
  int pl,pr;
  ll sum,tag,val;
  int sz;
  int rev;
  node(){
    pl = pr = sum = tag = 0;
    sz = 0;
    rev = 0;
    pri = rand();
}:
const int SZ = 2e5+10;
struct Treap{
  node nd[SZ];
  int cnt = 0;
  Treap(){
    cnt = 0;
  int newnode(){
    cnt++:
    nd[cnt].sz = 1;
    return cnt;
  void pull(int now){
    if(!now)return:
    nd[now].sz = nd[nd[now].pr].sz+nd[nd[now].pl].sz+1;
    ll ls = nd[nd[now]]
        ].pl].sum+nd[nd[now].pl].tag*nd[nd[now].pl].sz;
    ll rs = nd[nd[now
        ].pr].sum+nd[nd[now].pr].tag*nd[nd[now].pr].sz;
    nd[now].sum = nd[now].val+ls+rs;
    return;
  void push(int now){
    if(!now)return:
    if(nd[now].rev){
      swap(nd[now].pl,nd[now].pr);
      if(nd[now].pl)nd[nd[now].pl].rev ^= 1;
      if(nd[now].pr)nd[nd[now].pr].rev ^= 1;
      nd[now].rev = 0;
    int tl = nd[now].pl,tr = nd[now].pr;
    nd[now].val += nd[now].tag;
    if(tl)nd[tl].tag += nd[now].tag;
    if(tr)nd[tr].tag += nd[now].tag;
    nd[now].tag = 0;
    pull(now);
  int merge(int a,int b){
    if(!a)return b;
    if(!b)return a;
    if(nd[a].pri>nd[b].pri){
      push(a);
      nd[a].pr = merge(nd[a].pr,b);
      pull(a);
      return a;
```

```
else{
      push(b);
      nd[b].pl = merge(a,nd[b].pl);
      pull(b);
      return b;
  void split(int now,int &a,int &b,int tar){
    if(!now){
      a = b = 0;
      return;
    push(now);
    if(nd[nd[now].pl].sz+1<=tar){</pre>
      a = now;
      split(nd[now
          ].pr,nd[a].pr,b,tar-(nd[nd[now].pl].sz+1));
    else{
      b = now;
      split(nd[now].pl,a,nd[b].pl,tar);
    pull(a);
    pull(b);
    return:
 }
Treap T;
```

3.4 quadrangle [1d61e6]

```
struct QUADRANGLE
    struct TUPLE {
        int l, r,
                   id;
        TUPLE() {}
        TUPLE(int _l,
             int _r, int _id) : l(_l), r(_r), id(_id) {}
    int n, now;
    deque<TUPLE> dq;
    int calc_dp(int id, int i) {
        // ...
    bool cmp(int cid, int pid, int i) {
        // ...
    void init(int _n) {
        n = _n;
now = 1;
        dq.clear();
    void kill_head() {
        now++;
        if (dq
             .front().l == dq.front().r) dq.pop_front();
        else dq.front().l++;
    void push(int id) {
        while (dq.size()) {
            TUPLE tl = dq.back();
             dq.pop_back();
            if (cmp(id, tl.id, tl.l)) {
                 continue:
            int l = tl.l, r = tl.r + 1;
            while (l + 1 < r) {
                 int mid = (l + r) >> 1;
                 (cmp(id, tl.id, mid) ? r : l) = mid;
            dq.push_back(TUPLE(tl.l, l, tl.id));
            if (r <= n) dq.push_back(TUPLE(r, n, id));</pre>
        dq.push_back(TUPLE(now, n, id));
    int determine(int id) {
        return calc_dp(dq.front().id, id);
    }
};
```

3.5 Splay [977ab6]

```
#include <bits/stdc++.h>
using namespace std;
```

```
#define ll long long
const int SZ = 2e5+10;
//1-indexed,0 used for nullptr
//range reverse range sum
struct Splay{
#define ls ch[now][0]
#define rs ch[now][1]
  ll val[SZ];
  ll sum[SZ];
  int ch[SZ][2],fa[SZ],cnt,rev[SZ],sz[SZ];
  void pull(int now){
    if(!now)return;
    sum[now] = sum[ls]+sum[rs]+val[now];
    sz[now] = sz[ls]+sz[rs]+1;
    return;
  void push(int now){
    if(!now)return;
    if(rev[now]){
      swap(ls,rs);
      rev[ls] ^= 1;
rev[rs] ^= 1;
      rev[now] = 0;
    pull(now);
    return:
  Splay(){
    fill(sz+1,sz+SZ,1);
    return:
  int newnode(){
    return ++cnt;
  int dir(int now){//is ls or rs
    return ch[fa[now]][1] == now;
  bool isroot(int k){//for LCT
    return !fa[k]||ch[fa[k]][dir(k)] != k;
  void rot(int now){
    assert(now);
    assert(fa[now]);
    int p = fa[now];
    int g = fa[p];
    push(g);
    push(p);
    push(now);
    int d = dir(now);
    if(!isroot(p))ch[g][dir(p)] = now;
    fa[ch[now][d^1]] = p;
    ch[p][d] = ch[now][d^1];
    fa[now] = g;
    fa[p] = now;
    ch[now][d^1] = p;
    pull(p);
    pull(now);
    return:
  void splay(int now){
    if(!now)return;
    while(!isroot(now)){
      push(fa[fa[now]]);
      push(fa[now]);
      push(now):
      if(!isroot(fa[now])){
        if(dir(fa[now]) == dir(now))rot(fa[now]);
        else rot(now);
      rot(now);
    push(now);
    return;
  int get_sz(int now,int tar){
    push(now);
    while(now&&sz[ls]+1 != tar){
      if(sz[ls]>=tar)now = ls;
      else{
        tar -= sz[ls]+1;
        now = rs;
      push(now);
    return now:
  }
```

```
void merge(int a,int b){
    if(!a||!b)return;
    splay(a); splay(b);
    a = get_sz(a,sz[a]);
    b = get_sz(b,1);
    splay(a); splay(b);
    ch[a][1] = b;
    fa[b] = a;
    pull(a);
    return;
  }
  pair < int , int > split(int a , int tar){
    splay(a);
    if(!tar)return make_pair(0,a);
    int b = get_sz(a,tar);
    splay(b);
    pair<int,int> re;
    re.first = b;
    re.second = ch[b][1];
    fa[ch[b][1]] = 0;
    ch[b][1] = 0;
    pull(b);
    return re;
#undef ls
#undef rs
};
```

3.6 Link-Cut Tree [085466]

```
#define ll long long
//needs splay
//vertex add paths sum link-cut
struct LCT{
  Splay sp;
  void access(int x){
    sp.splay(x);
    sp.ch[x][1] = 0;
    sp.pull(x);
    while(sp.fa[x]){
      int u = sp.fa[x];
      sp.splay(u);
      sp.push(u);
      sp.ch[u][1] = x;
      sp.pull(u);
      sp.splay(x);
   }
  void makeroot(int x){
    access(x);sp.splay(x);
    sp.rev[x] ^= 1;
  void link(int u,int v){
    makeroot(u);
    sp.splay(u);
    sp.fa[u] = v;
  void cut(int u,int v){
    makeroot(u);
    access(v):
    sp.splay(v);
    int lc = sp.ch[v][0];
    sp.fa[lc] = 0;
    sp.ch[v][0] = 0;
    sp.pull(v);
  ll path_sum(int u,int v){
    makeroot(u);
    access(v);
    sp.splay(v);
    return sp.sum[v];
  void addval(int u,int val){
    sp.splay(u);
    sp.val[u] += val;
    sp.pull(u);
    return;
  int find(int p){
    access(p);
    return sp.get_sz(p,1);
};
```

4 Geometry

4.1 Point [47044e]

```
template < typename T = int>
struct Pt{
  T x,y;
  Pt (T xx = (T)(0), T yy = (T)(0)):x(xx),y(yy){}
  Pt operator+(Pt b)const{return Pt(x+b.x,y+b.y);}
  Pt operator-(Pt b)const{return Pt(x-b.x,y-b.y);}
  T operator*(Pt b)const{return x*b.x+y*b.y;}
  T operator^(Pt b)const{return x*b.y-y*b.x;}
  T operator/(Pt b)const{return x*b.y-y*b.x;}
  bool operator
      <(Pt b)const{return x == b.x?y<b.y:x<b.x;}
  friend int dir(Pt a,Pt b){//returns sign(a ^ b)
    auto re = a ^ b;
    return re<0?-1:re>0?1:0;
  friend bool onseg(Pt x,Pt s,Pt e){
    if(((e-x)^(s-x)) != 0)return false;
    else if((s-x)*(e-x)>0)return false;
    return true;
  friend int
       intersect(Pt s1,Pt e1,Pt s2,Pt e2){//returns 0
        if doesn't intersect,1 if intersect,2 if on line
    if(onseg(s1,s2,e2)||onseg(e1,s2,
        e2)||onseg(s2,s1,e1)||onseg(e2,s1,e1))return 2;
    if(dir(s1-s2,e2-s2)*dir(e1-s2,e2-s2)<0&&</pre>
        dir(s2-s1,e1-s1)*dir(e2-s1,e1-s1)<0)return 1;</pre>
    return 0:
  }
};
```

4.2 Convex Hull [2a54da]

```
//needs Point.cpp
template < typename T = int>
struct ConvexHull{//returns in clockwise direction
  vector<Pt<T>> solve(vector<Pt<T>> v){
     sort(v.begin(),v.end());
     vector<Pt<T>> u,d;
     for(auto &i:v){
       while(u.size()>1&&((i-u.end()[-1])
           ^(u.end()[-2]-u.end()[-1]))>=0)u.pop_back();
       while(d.size()>1&&((i-d.end()[-1])
           ^(d.end()[-2]-d.end()[-1]))<=0)d.pop_back();
      u.push_back(i);
      d.push_back(i);
     for(int i =
          1;i+1<d.size();i++)u.push_back(d.end()[-1-i]);
     return u;
  }
};
```

4.3 Minkowski sum [9db95e]

```
//needs Point template
template <typename T>
vector<Pt
    <T>> minkowski(vector<Pt<T>> va.vector<Pt<T>> vb){
  deque<Pt<T>> a.b:
  for(auto &i:va)a.push_back(i);
  for(auto &i:vb)b.push_back(i);
  Pt head = *min_element(a.begin(),a.end());
  while (a[\theta].x != head.x||a[\theta].y != head.y){
    a.push_back(a[0]);
    a.pop_front();
  head = *min_element(b.begin(),b.end());
  while(b[0].x != head.x||b[0].y != head.y){
    b.push_back(b[0]);
    b.pop_front();
  a.push_back(a[0]);
  b.push_back(b[0]);
  int p1 = 0, p2 = 0;
  vector<Pt<T>> re;
  while(p1 < a.size()&&p2 < b.size()){</pre>
   //cerr<<a
         .size()<<','<<b.size()<<":"<<p1<<' '<<p2<<endl;
    int dir = 0;
    re.push_back(a[p1]+b[p2]);
    if(p1+1
            == a.size())dir :
    else if(p2+1 == b.size())dir = 0;
    else
        if(((a[p1+1]-a[p1])^(b[p2+1]-b[p2]))>0)dir = 0;
```

```
else dir = 1;
  if(dir == 0)p1++;
  else p2++;
return re;
```

String 5

5.1 KMP [bb2a1b]

```
template <tvpename T>
struct KMP {
    void operator()(T a, int n, int *pi) {
        pi[0] = -1, pi[1] = 0;
        for (int i = 1; i < n; i++) {</pre>
            int j = pi[i];
            while (j >= 0 && a[i] != a[j]) j = pi[j];
            pi[i + 1] = j + 1;
        }
    }
};
```

5.2 Zalgorithm [6a03da]

```
template <typename T>
struct Z_alg {
    void operator()(T *a, int n, int *z) {
        fill(z, z + n + 1, 0);
         int l = 0;
         for (int i = 1; i <= n; i++) {</pre>
             if (i >= l + z[l]) {
                 while (i + z[i] < n
                      && a[i + z[i]] == a[z[i]]) z[i]++;
                 l = i;
                 continue;
             int i_ = i - l;
if (i_ + z[i_] == z[l]) {
                 z[i] = z[i_];
                 while (i + z[i] < n
                      && a[i + z[i]] == a[z[i]]) z[i]++;
                 l = i;
                 continue:
             z[i] = (
                  i_ + z[i_] < z[l] ? z[i_] : z[l] - i_);</pre>
        }
    }
};
```

5.3 manacher [c7bcd5]

```
template <typename T>
struct MANACHER {
    void operator()(T a, int n, int *mn) {
         fill(mn, mn + n, \theta);
         int l = 0;
         for (int i = 1; i < n; i++) {</pre>
             if (i > l + mn[l]) {
                  while (i - mn[i] - 1 >= 0
     && i + mn[i] + 1 < n && a[i - mn[i]</pre>
                        - 1] == a[i + mn[i] + 1]) mn[i]++;
                  l = i;
                  continue;
             int i_ = 2 * l - i;
             if (i_ - mn[i_] == l - mn[l]) {
                  mn[i] = mn[i_];
                  while (i - mn[i] - 1 >= 0
                      && i + mn[i] + 1 < n && a[i - mn[i]]
                        - 1] == a[i + mn[i] + 1]) mn[i]++;
                  l = i;
                  continue;
             mn[i] = (i_ - mn[i_]
                  > l - mn[l] ? mn[i_] : i_ - l + mn[l]);
        }
    }
};
```

5.4 Suffix Array (SAIS) [a683f1]

```
int SA[MXN * 2], H[MXN], RA[MXN];
namespace SAIS {
    bool _t[MXN * 2];
    int _s[MXN *
         2], _c[MXN * 2], x[MXN], _p[MXN], _q[MXN * 2];
```

```
void pre(int *sa, int *c, int n, int z) {
    fill_n(sa, n, 0);
    copy_n(c, z, x);
void induce(int
    *sa, int *c, int *s, bool *t, int n, int z) {
copy_n(c, z - 1, x + 1);
copy_n(c, z - 2, x + 1);
    FOR(i, 0, n) {
    if (sa[i] && !t[sa[i] - 1]) {
              sa[x[s[sa[i] - 1]]++] = sa[i] - 1;
    }
    copy_n(c, z, x);
for (int i = n - 1; i >= 0; i--) {
         if (sa[i] && t[sa[i] - 1]) {
              sa[--x[s[sa[i] - 1]]] = sa[i] - 1;
    }
void sais(int *s, int *sa, int
     *p, int *q, bool *t, int *c, int n, int z) {
    bool uniq = t[n - 1] = true;
    int nn = 0, nmxz =
           -1, *nsa = sa + n, *ns = s + n, last = -1;
    fill_n(c, z, 0);
    FOR(i, 0, n) uniq &= ++c[s[i]] < 2;
    partial_sum(c, c + z, c);
    if (uniq) {
         FOR(i, 0, n) sa[--c[s[i]]] = i;
         return:
    for (int i = n - 2; i >= 0; i--) {
         t[i] = (s[i] ==
              s[i + 1] ? t[i + 1] : s[i] < s[i + 1]);
    pre(sa, c, n, z);
    FOR(i, 1, n) {
         if (t[i] && !t[i - 1]) {
              sa[--x[s[i]]] = p[q[i] = nn++] = i;
         }
    induce(sa, c, s, t, n, z);
    FOR(i, 0, n) {
         if (sa[i] && t[sa[i]] && !t[sa[i] - 1]) {
              bool neq = last < 0 || !equal(s + sa[</pre>
                   i], s + p[q[sa[i]] + 1], s + last);
              ns[q[last = sa[i]]] = nmxz += neq;
    }
    sais(ns, nsa,
         p + nn, q + n, t + n, c + z, nn, nmxz + 1);
    pre(sa, c, n, z);
    for (int i = nn - 1; i >= 0; i--) {
         sa[--x[s[p[nsa[i]]]]] = p[nsa[i]];
    induce(sa, c, s, t, n, z);
void mkhei(int n) {
    for (int i = 0, j = 0; i < n; i++) {</pre>
         if (RA[i]) {
              for (; i + j < n</pre>
                    && SA[RA[i] - 1] + j < n && _s[i +
              j] == _s[SA[RA[i] - 1] + j]; ++j);
H[RA[i]] = j, j = max(0, j - 1);
         }
    }
void build(int *s, int n, int mxc) {
    copy_n(s, n, _s), _s[n] = 0;
sais(_s, SA, _p, _q, _t, _c, n + 1, mxc);
copy_n(SA + 1, n, SA);
    FOR(i, 0, n) RA[SA[i]] = i;
    mkhei(n);
    copy(H + 1, H + n, H);
```

5.5 AC automaton [c073c7]

```
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
struct AC {
    int nc;
    char c[MXN];
    int pi[MXN], p[MXN], nxt[MXN][MXC];
    void init() {
        nc = 2;
```

```
fill(nxt[0], nxt[0] + MXC, 1);
fill(nxt[1], nxt[1] + MXC, -1);
     int add_node(int par, char _c) {
         c[nc] = _c;
         p[nc] = par;
         fill(nxt[nc], nxt[nc] + MXC, -1);
         return nc++;
     int push(string &s) {
         int now = 1;
         for (auto &i : s) {
             return now;
     void build() {
         queue < int > q;
         pi[1] = 0;
         FOR(i, 0, MXC) {
             if (nxt[1][
    i] == -1) nxt[1][i] = nxt[pi[1]][i];
             else q.push(nxt[1][i]);
         while (q.size()) {
             int id = q.front();
             q.pop();
             pi[id] = nxt[pi[p[id]]][c[id] - 'a'];
             FOR(i, 0, MXC) {
    if (nxt[id][i]
                     == -1) nxt[id][i] = nxt[pi[id]][i];
                 else q.push(nxt[id][i]);
             }
         }
    }
};
```

6 Math

6.1 FFT [9ff2a9]

```
#define TYPE double
typedef complex < TYPE > cd;
#undef TYPE
struct FFT {
     const double pi = acos(-1);
     cd cis(double theta) {
         return cd(cos(theta), sin(theta));
     cd OMEGA(int n, int k) {
    return cis(pi * 2 * k / n);
     void operator()(cd *a, int N, bool inv) {
   auto REV = [&](int x) -> int {
              int ans = 0;
              for (int i = 1; i < N; i <<= 1) {</pre>
                   ans <<= 1;
                   if (i & x) ans |= 1;
              return ans;
          FOR(i, 0, N) {
              int r = REV(i);
              if (i < r) swap(a[i], a[r]);</pre>
         for (int w = 1; w < N; w <<= 1) {</pre>
              int on = w << 1;</pre>
              for (int ok = 0; ok < w; ok++) {
                   cd omega
                         = OMEGA(on, (inv ? -1 : 1) * ok);
                   for (int s = 0; s < N; s += on) {</pre>
                       cd &L =
                             a[s + ok], &R = a[s + ok + w];
                       cd l = L, r = omega * R;
                       L = l + r;
                       R = l - r;
                   }
              }
         if (inv) {
              for (int i = 0; i < N; i++) a[i] /= N;</pre>
} fft;
```

6.2 FWT [a168b9]

```
#include <bits/stdc++.h>
 using namespace std;
#define fs first
#define sc second
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
using ll = long long;
typedef pair<int, int> pii;
 typedef pair < pii, pii > MAT;
 template <int mod = 998244353>
 struct mint {
     int x;
     mint() : x(0) \{
     mint(int _x) : x(_x) {}
     mint operator+(mint o) {
         int y = x + o.x;
         y -= (y >= mod ? mod : 0);
         return mint(y);
     mint operator*(int y) {
         y += (y < 0 ? mod : 0);
         return mint((ll) x * y % mod);
     mint operator*(mint o) {
         return mint((ll) x * o.x % mod);
     mint inv() {
         int b = mod - 2, a = x;
         int ans = 1;
         while (b) {
              if (b & 1) ans = (ll) ans * a % mod;
              b >>= 1:
              a = (ll) a * a % mod;
         return mint(ans);
     }
};
 template <typename T = int>
 struct FWT {
     enum FWT_TYPE {
         AND,
         OR,
         XOR
     };
     const MAT mat[3] = {
         {{1, 1}, {0, 1}}, {{1, 1}},
         {{1, 1}, {1, -1}}
     };
     const MAT tam[3] = {
         {{1, -1}, {0, 1}}, {{1, 0}, {-1, 1}}, {{1, 1}, {1, -1}}
     };
     FWT() {}
     void btf(T &L, T &R, MAT &m) {
         Tl = L, r = R;
         L = l * m.fs.fs + r * m.fs.sc;
         R = l * m.sc.fs + r * m.sc.sc;
     void apply(T *a, int n, bool inv, FWT_TYPE tp) {
    MAT m = (inv ? tam : mat)[tp];
         for (int w = 1; w < n; w <<= 1) {</pre>
              FOR(i, 0, n) if (i & w) {
                  btf(a[i - w], a[i], m);
              }
         if (tp == FWT_TYPE::XOR && inv) {
              T n_{-} = T(n).inv();
              FOR(i, 0, n) a[i] = a[i] * n_;
         }
     }
};
6.3 NTT [13fd5f]
```

```
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
struct NTT {
    const static int LG = 20;
    int mod;
    int o[(1 << LG) + 1];
    int ADD(int a, int b) {</pre>
```

```
// help yourself
    int SUB(int a, int b) {
        // help yourself
    int MUL(int a, int b) {
        // help yourself
    int POW(int a, int b) {
        // help yourself
    NTT(int g, int gap, int _mod) {
        mod = _{mod};
        o[0] = 1;
        int pp = POW(g, gap);
        FOR(i,
             1, (1 \ll LG) + 1) o[i] = MUL(o[i - 1], pp);
    void operator()(int *a, int n, bool inv) {
        auto REV = [\&](int x) \rightarrow int {
             int ans = 0;
             for (int w = 1; w < n; w <<= 1) {</pre>
                 ans = (ans << 1) | (x & 1);
             return ans;
        FOR(i, 0, n) {
             int j = REV(i);
             if (i < j) swap(a[i], a[j]);</pre>
        for (int w = 1; w < n; w <<= 1) {</pre>
             int owo = 1 << (LG - __lg(w) - 1), oid = 0;
             FOR(i, 0, w) {
                 int omega
                 = o[inv ? (1 << LG) - oid : oid];
for (int s = 0; s < n; s += (w << 1)) {
                     int &L
                           = a[s + i], &R = a[s + w + i];
                     int l = L, r = MUL(omega, R);
                     L = ADD(l, r);
                     R = SUB(l, r);
                 oid += owo;
            }
        if (inv) {
             int x = POW(n, mod - 2);
             FOR(i, 0, n) a[i] = MUL(a[i], x);
        }
    }
};
NTT ntt1(3, 952, 998244353);
NTT ntt2(3, 100, 104857601);
NTT ntt3(3, 160, 167772161);
```

6.4 Chinese Remainder Theorem [6fdd6f]

```
using lll = __int128_t;
struct ICRT {
     lll p1, p2, p3;
     lll c1, c2, c3;
     ICRT() {}
     ICRT(Ill _p1,
lll _p2, lll
                          _p3) : p1(_p1), p2(_p2), p3(_p3) {
          auto POW = [&](lil a, lil b, lil mod) -> lil {
               lll ans = 1;
               while (b) {
                    if (b & 1) ans = ans * a % mod;
                   b >>= 1;
                    a = a * a % mod;
               return ans;
          };
         c1 = POW(p2 * p3 % p1, p1 - 2, p1) * p2 * p3;
c2 = POW(p3 * p1 % p2, p2 - 2, p2) * p3 * p1;
c3 = POW(p1 * p2 % p3, p3 - 2, p3) * p1 * p2;
     lll operator()(int r1, int r2, int r3) {
          return (c1
               * r1 + c2 * r2 + c3 * r3) % (p1 * p2 * p3);
};
ICRT icrt(998244353, 104857601, 167772161);
```

6.5 Pollard Rho [b24d9c]

```
//needs mad, mub, mul, pw with changable mod
//!!!use int128 for pw and mul
bool isprime(ll x) {
  if (x <= 2 || ~x & 1) return x == 2;</pre>
  auto witn = [&](ll a, int t) {
    for (ll a2; t-- && (a2 = mul(a, a, x)); a = a2)
     if (a2 == 1 && a != 1 && a != x - 1) return true;
    return a > 1;
  int t = __builtin_ctzll(x-1); ll odd = (x-1) >> t;
  for (ll m:
      {2, 325,
           9375, 28178, 450775, 9780504, 1795265022})
  if (witn(pw(m % x, odd, x), t)) return false;
  return true;
ll pollard_rho(ll n) {
  static mt19937_64 rnd(120821011);
  if (!(n & 1)) return 2;
  ll y = 2, z = y, c = rnd() % n, p = 1, i = 0, t; auto f = [&](ll x) {
    return mad(mul(x, x, n), c, n); };
  do {
    p = mul(mub(z = f(f(z)), y = f(y), n), p, n);
    if (++i &= 63) if (i == (i & -i)) t = gcd(p, n);
  } while (t == 1);
  return t == n ? pollard_rho(n) : t;
vector<ll> factorize(ll k){
  if(k == 1)return {};
  else if(isprime(k))return {k};
    vector<ll> re;
    function < void(ll) > dc = [&](ll k){
      if(isprime(k)){
        re.push_back(k);
        return:
      ll x = pollard_rho(k);
      dc(x);dc(k/x);
    sort(re.begin(),re.end());
    return re;
  }
}
```