# **Contents**

```
3.5 Splay . . . . . . . . . . . . . . .
                                        3.6 Link-Cut Tree . . . . . . .
1 Setups
  1.1 vimrc . . . . . . . . . . . . . . . . .
                                     4 Geometry
  4.1 Point .
                                        4.2 Convex Hull . . . . . . . .
                                                                      6
       debug . . . . . . . . . . . .
                                        4.3 Minkowski sum . . . . . .
  1.5 template . . . . . . . . .
                                     5 String
2 Graph
                                        2.1 Dominator Tree . . . . . .
  2.2 Incremental SCC . . . . . .
                                        5.3 manacher . . .
                                                           . . . . . .
  2.3 Block-Cut Tree . . . . . .
                                        5.4 Suffix Array (SAIS) . . . .
  2.4 Euler Tour . . . . . . . .
                                        5.5 AC automaton . . . . . .
                   . . . . . . . .
  2.6 Gomory-Hu Tree . . . . .
  2.7 Min-Cost-Max-Flow . . . .
                                        6.1 FFT . . . . . . . . . . . . . . .
                                        6.2 FWT . . . . . . . . . . . . . . .
3 Data Structure
  3.1 Li Chao Tree . . .
                                        6.3 NTT........
  3.2 Dynamic Convex Hull . . . 4
                                        6.4 Chinese Remainder Theo-
```

3.4 quadrangle  $\dots$ 

# 1 Setups

### 1.1 vimrc [6c9876]

```
se nu ai rnu cin ts=4 sw=4 | sy on inoremap {<CR> {<CR>}<Esc>0 inoremap jk <Esc>
```

# 1.2 pbds [9f7c3e]

### 1.3 terminal [46fc34]

```
-- terminal --
|$ setxkbmap -option caps:swapescape
```

### 1.4 debug [33c0d3]

```
#ifdef MIKU
string
      dbmc = "\033[1;38;2;57;197;187m", dbrs = \033[0m;
#define debug
    (x...) cout << dbmc << "[" << #x << "] : ", dout(x)
void dout() { cout << dbrs << endl; }</pre>
template <typename T, typename ...U>
void dout(T t, U ...u) { cout
      << t << sizeof...(u) ? ", " : ""; dout(u...); }
#define debug(...) 39
#endif
int main(){
    int a = 49;
    char c = '8';
    debug(a);// outputs "[a] : 49"
debug(a, c); // outputs "[a, c] : 49, 8"
debug("PCCORZ"); // outputs "["PCCORZ"] : PCCORZ"
     debug(); // outputs "[] :
}
```

### 1.5 template [5116af]

```
#include <bits/stdc++.h>
using namespace std;
#define fs first
#define sc second
#define F first
#define S second
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
using ll = long long;</pre>
```

```
using lll = __int128_t;
typedef pair <int, int > pii;
typedef tuple <int,int,int > tiii;
typedef pair <ll,ll > pll

int main(){
}
```

# 2 Graph

# 2.1 Dominator Tree [3b89c3]

```
struct DominatorTree{
  //1-indexed
  //not reachable from s -> not on tree
  int n:
  vector<vector<int>> G,rG;
  vector<int> pa,dfn,id;
  int dfnCnt;
  vector<int> semi,idom,best;
  vector<vector<int>> ret;
  void init(int _n){
    n=_n;
    G = rG = ret = vector<vector<int>>(n+1);
    pa = dfn = id = vector < int > (n+1,-1);
    dfnCnt = 0;
    semi = idom = best = vector<int>(n+1,-1);
  void add_edge(int u,int v){
    G[u].push_back(v);
    rG[v].push_back(u);
  void dfs(int u){
    id[dfn[u]=++dfnCnt]=u;
    for(auto v:G[u]) if(!dfn[v]){
      dfs(v),pa[dfn[v]]=dfn[u];
  int find(int y,int x){
    if(y<=x)return y;</pre>
    int tmp=find(pa[y],x);
    if(semi[best[y]]>semi[best[pa[y]]])
      best[y]=best[pa[y]];
    return pa[y]=tmp;
  void tarjan(int root){
    dfnCnt=0;
    for(int i=1;i<=n;++i){</pre>
      dfn[i]=idom[i]=0;
      ret[i].clear():
      best[i]=semi[i]=i;
    dfs(root);
    for(int i=dfnCnt;i>1;--i){
      int u=id[i];
      for(auto v:rG[u]) if(v=dfn[v]){
         find(v,i);
         semi[i]=min(semi[i],semi[best[v]]);
      ret[semi[i]].push_back(i);
      for(auto v:ret[pa[i]]){
         find(v,pa[i]);
         idom[v
             ] = semi[best[v]]==pa[i] ? pa[i] : best[v];
      ret[pa[i]].clear();
    for(int i=2; i<=dfnCnt; ++i){
   if(idom[i]!=semi[i]) idom[i]=idom[idom[i]];</pre>
      ret[id[idom[i]]].push_back(id[i]);
  vector<vector<int>> solve(int s){
    tarian(s):
    return ret;
  }
};
```

### 2.2 Incremental SCC [d8b556]

```
struct IncrementalSCC{
    #define pii pair < int , int >
    #define fs first
    #define sc second
#define tiii tuple < int , int , int >
    // if u == v : ans[i] = -1
```

```
//if not connected : ans[i] = m
//all 0-indexed
int n;
vector<int> ans;
int m;
vector<tiii> all;
vector<int> SCC(int n, vector<vector<int>>& paths){
  vector < int > scc_id(n,-1), idx(n,-1), low(n,-1), st;
  int cnt = 0,gcnt = 0;
  function < void(int) > dfs = [&](int now) -> void{
    low[now] = idx[now] = cnt++;
    st.push_back(now);
    for(auto nxt:paths[now]){
      if(scc_id[nxt] != -1)continue;
      if(idx[nxt] == -1){
        dfs(nxt);
        low[now] = min(low[now],low[nxt]);
        low[now] = min(low[now],idx[nxt]);
      }
    if(low[now] == idx[now]){
      int id = -1;
      while(id != now){
        id = st.back();
        st.pop_back();
        scc_id[id] = gcnt;
      qcnt++;
   }
  for(int i = 0;i<n;i++){</pre>
    if(scc_id[i] == -1)dfs(i);
  return scc id;
}
vector<int> mapping;
void dc(int l,int r,vector<tiii> &edges){
  if(l == r){
    for(auto
         [id,_,_]:edges)ans[id] = min(ans[id],l);
  int mid = (l+r)>>1;
  int cnt = 0;
  for(auto &[t,u,v]:edges){
    if(mapping[u] == -1)mapping[u] = cnt++;
    if(mapping[v] == -1)mapping[v] = cnt++;
  }
  n = cnt;
  vector<vector<int>> paths(n);
  vector<int> vv;
  for(auto &[t,u,v]:edges){
    vv.push_back(u);
    vv.push_back(v);
    u = mapping[u],v = mapping[v];
    if(t<=mid)paths[u].push_back(v);</pre>
  for(auto &i:vv)mapping[i] = -1;
  auto scc_id = SCC(n,paths);
  vector<tiii> vl,vr;
  for(auto &[t,u,v]:edges){
    if(scc_id[u] == scc_id[v]){
      ans[t] = min(ans[t], mid);
      vl.push_back(tiii(t,u,v));
    else{
      u = scc_id[u],v = scc_id[v];
      vr.push_back(tiii(t,u,v));
  vector < tiii > ().swap(edges);
  dc(l,mid,vl);
  dc(mid+1,r,vr);
  return:
void add_edge(int u,int v){
 all.push_back(tiii(all.size(),u,v));
vector<tiii> solve(){//[time,u,v]
 m = all.size();
  vector<tiii> ret(m);
  for(auto [t,u,v]:all)ret[t] = tiii(m,u,v);
  for(auto [t,u,v]:all)n = max({n,u,v});
```

```
n++;
    ans = vector < int > (m, m);
    for (auto [t, u, v]: all) {
        if (u == v) ans[t] = -1;
    }
    mapping = vector < int > (n, -1);
    dc(0, m, all);
    for (int i = 0; i < m; i + +) get < 0 > (ret[i]) = ans[i];
    return ret;
}
Incremental SCC() {
    ans.clear();
    n = m = 0;
}
#undef tiii
#undef pii
#undef fs
#undef sc
};
```

### 2.3 Block-Cut Tree [f44682]

```
struct BlockCutTree{
  //0-indexed
  //returns a forest if the graph is not connected
  vector<vector<int>> g;
  vector<vector<int>> groups;
  vector<vector<int>> tr;
  vector<int> idx,low,st;
  int cnt,gcnt;
  int n;
  RoundSquareTree(int _n = 0){
    cnt = gcnt = 0;
    n = _n;
    g = vector<vector<int>>(n);
  void add_edge(int a,int b){//adds bidirectional edges
    g[a].push_back(b);
    g[b].push_back(a);
  void dfs(int now){
    idx[now] = low[now] = cnt++;
    st.push_back(now);
    for(auto nxt:g[now]){
      if(idx[nxt] == -1){
        dfs(nxt);
        low[now] = min(low[now],low[nxt]);
        if(low[nxt] == idx[now]){
           int id = -1;
           tr.push_back(vector<int>());
          while(id != nxt){
            id = st.back();st.pop_back();
             groups[id].push_back(gcnt);
             tr[id].push_back(gcnt+n);
            tr[gcnt+n].push_back(id);
           groups[now].push_back(gcnt);
          tr[now].push_back(gcnt+n);
          tr[gcnt+n].push_back(now);
          qcnt++;
        }
      else idx[now] = min(idx[now],idx[nxt]);
    return:
  }
  vector<vector<int>> solve(){//
       returns the tree (round vertices numbered [0,n))
    idx = low = vector<int>(n,-1);
    tr = vector<vector<int>>(n);
    for(int i = 0;i<n;i++){</pre>
      if(idx[i] == -1)dfs(i);
    return tr:
  }
};
```

# 2.4 Euler Tour [a4ce3c]

```
#include <bits/stdc++.h>
using namespace std;

struct EulerTour{
   //undirected graph,0-indexed,fails if doesn't exist
   //returns the order of edges
#define pii pair<int,int>
   vector<vector<pii>>> g;
```

return re:

}

return 0;

```
vector<int> ptr;
  vector<bool> vis;
                                                               int flow(int s,int t){
  vector<int> re;
                                                                 int ans = 0;
                                                                 while(bfs(s,t)){
  int n,ecnt;
                                                                   fill(ptr.begin(),ptr.end(),0);
  void init(int _n){
   n = _n;
                                                                   while(auto re = dfs(s,t,INT_MAX)){
    ecnt = 0;
                                                                     ans += re;
                                                                   }
    g = vector<vector<pii>>>(n);
    ptr = vector<int>(n);
                                                                 }
                                                                 return ans;
  void add_edge(int a,int b,int id = -1){
   if(id == -1)id = ecnt;
                                                               bool inScut(int k){
    g[a].push_back(pii(b,id));
                                                                 return lvl[k] != -1;
    g[b].push_back(pii(a,id));
    ecnt++;
                                                            };
 }
                                                             2.6 Gomory-Hu Tree [3ab29a]
  void dfs(int now){
    for(int &i = ptr[now];i<g[now].size();i++){</pre>
                                                             struct GomoryHuTree{//0-indexed
      auto [to,eid] = g[now][i];
                                                             #define pii pair<int,int>
      if(vis[eid])continue;
                                                            #define tiii tuple<int,int,int>
      vis[eid] = true;
                                                               vector<tiii> edges;
      dfs(to);
                                                               vector<vector<pii>> tr;
      re.push_back(eid);
                                                               vector<int> p;
                                                               int n;
    return:
                                                               GomoryHuTree(int _n = 0){
 }
                                                                 n = _n;
  vector<int> solve(int s){
                                                                 p = vector<int>(_n,0);
    re.clear();
                                                                 tr = vector<vector<pii>>(_n);
    vis = vector<bool>(ecnt,0);
    dfs(s);
                                                               void add edge(int a,int b,int c){
    return re;
                                                                 edges.push_back(tiii(a,b,c));
 }
#undef pii
                                                               vector<vector<pii>>> make_tree(){
                                                                 fill(p.begin(),p.end(),0);
2.5 Dinic [360712]
                                                                 tr = vector<vector<pii>>>(n);
                                                                 for(int i = 1;i<p.size();i++){</pre>
struct Dinic{//0-indexed
                                                                   Dinic din(n);
  struct E{
                                                                   for(auto &[a,b,w]:edges){
    int t,f,c;
                                                                     din.add_edge(a,b,w,w);
    E(int tt
         = 0, int cc = 0, int ff = 0):t(tt),c(cc),f(ff){}
                                                                   int w = din.flow(i,p[i]);
                                                                   tr[i].push_back(pii(p[i],w));
  vector<vector<int>> paths;
                                                                   tr[p[i]].push_back(pii(i,w));
 vector<int> ptr,lvl;
                                                                   for(int j = i+1;j<n;j++){</pre>
 vector<E> e;
                                                                     if(p[j] == p[i]&&din.inScut(j))p[j] = i;
  queue<int> q;
 Dinic(int _n = 0){
    paths = vector<vector<int>>(_n);
                                                                 return tr;
    ptr = lvl = vector<int>(_n);
                                                              }
                                                            #undef pii
  void add_edge(int a,int b,int c,int d = 0){
                                                            #undef tiii
    paths[a].push_back(e.size());
                                                            };
    e.push_back(E(b,c));
    paths[b].push_back(e.size());
                                                            2.7 Min-Cost-Max-Flow [80eed6]
    e.push back(E(a.d)):
                                                            #define T ll
 bool bfs(int s,int t){
                                                            const T inf = 1e12;
    fill(lvl.begin(),lvl.end(),-1);
                                                             struct MCMF{//TC:0(VEF)
    q.push(s);
                                                               struct E{
    lvl[s] = 0:
                                                                 int t.f:
    while(!q.empty()){
                                                                 T c,w;
      auto now = q.front();q.pop();
                                                                 E(int tt,T cap,T wei):t(tt),c(cap),w(wei),f(0){}
      for(auto &eid:paths[now]){
        if(e[eid].f == e[eid].c)continue;
                                                               vector < E > e;
        if(lvl[e[eid].t] == -1){
   lvl[e[eid].t] = lvl[now]+1;
                                                               vector<vector<int>> paths:
                                                               vector<T> dis:
                                                               vector<int> pre;
          q.push(e[eid].t);
                                                               vector<bool> inq;
     }
                                                               queue<int> q;
                                                               int n:
    return lvl[t] != -1;
                                                               MCMF(int _n = 0){
                                                                 n = _n;
                                                                 paths = vector<vector<int>>(n);
  int dfs(int now,int t,int flow){
    if(now == t)return flow;
                                                                 e.clear();
    for(int &i = ptr[now];i<paths[now].size();i++){</pre>
                                                                 pre = vector<int>(n);
      int eid = paths[now][i];
                                                                 dis = vector<T>(n);
      if(e[eid].f == e[
                                                                 inq = vector<bool>(n);
          eid].c||lvl[e[eid].t] != lvl[now]+1)continue;
                                                               void add_edge
      if(int re =
          dfs(e[eid].t,t,min(flow,e[eid].c-e[eid].f))){
                                                                   (int a,int b,int c,int d){//from,to,cap,wei
        e[eid].f += re;
                                                                 paths[a].push_back(e.size());
        e[eid^1].f -=re;
                                                                 e.push_back(E(b,c,d));
```

paths[b].push\_back(e.size());

e.push back(E(a,0,-d));

bool SPFA(int s,int t){

```
fill(dis.begin(),dis.end(),inf);
    fill(pre.begin(),pre.end(),-1);
    dis[s] = 0;
    q.push(s);inq[s] = true;
    while(!q.empty()){
      auto now = q.front();q.pop();
inq[now] = false;
      //assert(dis[now]>=0);
      for(auto &eid:paths[now]){
        if(e[eid].f == e[eid].c)continue;
        int nxt = e[eid].t;
        if(dis[nxt]>dis[now]+e[eid].w){
          pre[nxt] = eid;
          dis[nxt] = dis[now]+e[eid].w;
          if(!inq[nxt]){
            inq[nxt] = true;
            q.push(nxt);
          }
        }
      }
    }
    return dis[t] != inf;
  T flow(int s,int
      t, int cnt = INT_MAX){//cnt is the number of flows
    T ans = 0;
    while(cnt--&&SPFA(s,t)){
      ans += dis[t];
      int now = t;
      while(pre[now] != -1){
        int eid = pre[now];
        e[eid].f++;
        e[eid^1].f--
        now = e[eid^1].t;
     }
    return ans;
 }
};
#undef T
```

# 3 Data Structure

# 3.1 Li Chao Tree [565209]

```
//range add line get min
//can even be used if modifies aren't range modify
#define ll long long
const ll SZ = 8e6+10;
const ll inf = 3e18;
vector<ll> all;
struct Line{
  ll m,b;
  Line(ll mm = 0,ll bb = 0):m(mm),b(bb){}
  ll operator()(ll k){
   return m*k+b;
 }
struct LiChao{
#define ls now*2+1
#define rs now*2+2
#define mid ((l+r)>>1)
  Line seg[SZ];
  LiChao(){
    fill(seg,seg+SZ,Line(0,inf));
  void modify(int now,int l,int r,int s,int e,Line v){
    if(l == r){
      if(seg[now](all[l])>v(all[l]))swap(seg[now],v);
      return;
    if(l>=s&&e>=r){
          [now](all[mid])>v(all[mid]))swap(seg[now],v);
      if(seg[now].m<v.m)modify(ls,l,mid,s,e,v);</pre>
      else modify(rs,mid+1,r,s,e,v);
    else{
      if(mid>=s)modify(ls,l,mid,s,e,v);
      if(mid<e)modify(rs,mid+1,r,s,e,v);</pre>
    return;
  ll getval(int now,int l,int r,int p){
    if(l == r)return seg[now](all[p]);
    if(mid>=p)return
         min(seg[now](all[p]),getval(ls,l,mid,p));
```

### 3.2 Dynamic Convex Hull [98f67f]

```
//reference : 8BCube
#define ll long long
// only works for integer coordinates!! maintain max
struct Line {
   mutable ll a, b, p;
  bool operator
       <(const Line &rhs) const { return a < rhs.a; }
  bool operator<(ll x) const { return p < x; }</pre>
struct CHT : multiset<Line, less<>>> {
  static const ll kInf = 1e18;
  ll Div(ll a,
        ll b) { return a / b - ((a ^ b) < 0 && a % b); }
  bool isect(iterator x, iterator y) {
     if (y == end()) { x->p = kInf; return 0; }
     if (x
         ->a == y->a) x->p = x->b > y->b ? kInf : -kInf;
    else x->p = Div(y->b - x->b, x->a - y->a);
     return x->p >= y->p;
  void addline(ll a, ll b) {
    auto z = insert({a, b, \theta}), y = z++, x = y;
     while (isect(y, z)) z = erase(z);
    if (x != begin
         () && isect(--x, y)) isect(x, y = erase(y));
     while ((y = x) != begin
         () && (--x)->p >= y->p) isect(x, erase(y));
  ll query(ll x) {
     auto l = *lower_bound(x);
     return l.a * x + l.b;
  }
};
```

# 3.3 Treap [ff4001]

```
#define ll long long
//range reverse range add range sum
//need to push before using the info on node
struct node{
  int pri;
  int pl,pr;
  ll sum,tag,val;
  int sz;
  int rev;
  node(){
    pl = pr = sum = tag = 0;
    S7 = 0:
    rev = 0;
    pri = rand();
 }
};
const int SZ = 2e5+10;
struct Treap{
 node nd[SZ];
  int cnt = 0:
  Treap(){
    cnt = 0;
  int newnode(){
    cnt++:
    nd[cnt].sz = 1;
    return cnt;
  void pull(int now){
    if(!now)return;
    nd[now].sz = nd[nd[now].pr].sz+nd[nd[now].pl].sz+1;
```

```
ll ls = nd[nd[now
        ].pl].sum+nd[nd[now].pl].tag*nd[nd[now].pl].sz;
    ll rs = nd[nd[now
        ].pr].sum+nd[nd[now].pr].tag*nd[nd[now].pr].sz;
    nd[now].sum = nd[now].val+ls+rs;
    return:
  void push(int now){
    if(!now)return;
    if(nd[now].rev){
      swap(nd[now].pl,nd[now].pr);
      if(nd[now].pl)nd[nd[now].pl].rev ^= 1;
      if(nd[now].pr)nd[nd[now].pr].rev ^= 1;
      nd[now].rev = 0;
    int tl = nd[now].pl,tr = nd[now].pr;
nd[now].val += nd[now].tag;
    if(tl)nd[tl].tag += nd[now].tag;
    if(tr)nd[tr].tag += nd[now].tag;
    nd[now].tag = 0;
    pull(now);
  int merge(int a,int b){
    if(!a)return b;
    if(!b)return a;
    if(nd[a].pri>nd[b].pri){
      push(a);
      nd[a].pr = merge(nd[a].pr,b);
      pull(a);
      return a;
    else{
      push(b);
      nd[b].pl = merge(a,nd[b].pl);
      pull(b);
      return b;
    }
  void split(int now,int &a,int &b,int tar){
    if(!now){
      a = b = 0;
      return;
    push(now);
    if(nd[nd[now].pl].sz+1<=tar){</pre>
      a = now;
      split(nd[now
          ].pr,nd[a].pr,b,tar-(nd[nd[now].pl].sz+1));
    else{
      b = now:
      split(nd[now].pl,a,nd[b].pl,tar);
    pull(a);
    pull(b);
    return;
 }
Treap T;
3.4 quadrangle [1d61e6]
struct QUADRANGLE {
    struct TUPLE {
```

```
int l, r,
    TUPLE() {}
    TUPLE(int _l,
        int _r, int _id) : l(_l), r(_r), id(_id) {}
int n, now;
deque<TUPLE> dq;
int calc_dp(int id, int i) {
    // ...
bool cmp(int cid, int pid, int i) {
void init(int _n) {
   n = _n;
now = 1;
    dq.clear();
void kill_head() {
    now++;
    if (dq
        .front().l == dq.front().r) dq.pop_front();
```

```
else dq.front().l++;
    void push(int id) {
         while (dq.size()) {
             TUPLE tl = dq.back();
             dq.pop_back();
             if (cmp(id, tl.id, tl.l)) {
                 continue:
             int l = tl.l, r = tl.r + 1;
             while (l + 1 < r) {
   int mid = (l + r) >> 1;
                 (cmp(id, tl.id, mid) ? r : l) = mid;
             dq.push_back(TUPLE(tl.l, l, tl.id));
             if (r <= n) dq.push_back(TUPLE(r, n, id));</pre>
             return:
         dq.push_back(TUPLE(now, n, id));
    int determine(int id) {
         return calc_dp(dq.front().id, id);
};
3.5 Splay [977ab6]
#include <bits/stdc++.h>
using namespace std;
#define ll long long
const int SZ = 2e5+10;
//1-indexed,0 used for nullptr
//range reverse range sum
struct Splay{
#define ls ch[now][0]
#define rs ch[now][1]
  ll val[SZ];
  ll sum[SZ];
  int ch[SZ][2],fa[SZ],cnt,rev[SZ],sz[SZ];
  void pull(int now){
    if(!now)return
    sum[now] = sum[ls]+sum[rs]+val[now];
    sz[now] = sz[ls]+sz[rs]+1;
    return:
  void push(int now){
    if(!now)return;
    if(rev[now]){
      swap(ls,rs);
      rev[ls] ^= 1;
rev[rs] ^= 1;
      rev[now] = 0;
    pull(now);
    return:
  Splay(){
    fill(sz+1,sz+SZ,1);
    return;
  int newnode(){
    return ++cnt;
  int dir(int now){//is ls or rs
    return ch[fa[now]][1] == now;
  bool isroot(int k){//for LCT
    return !fa[k]||ch[fa[k]][dir(k)] != k;
  void rot(int now){
    assert(now):
    assert(fa[now]);
    int p = fa[now];
    int g = fa[p];
    push(g);
    push(p);
    push(now);
    int d = dir(now);
    if(!isroot(p))ch[g][dir(p)] = now;
    fa[ch[now][d^1]] = p;
```

 $ch[p][d] = ch[now][d^1];$ 

fa[now] = g;

fa[p] = now; ch[now][d^1] = p;

pull(p);

pull(now);

```
return:
  void splay(int now){
    if(!now)return;
    while(!isroot(now)){
      push(fa[fa[now]]);
      push(fa[now]);
      push(now);
      if(!isroot(fa[now])){
        if(dir(fa[now]) == dir(now))rot(fa[now]);
        else rot(now);
      rot(now);
    push(now);
    return:
  int get_sz(int now,int tar){
    push(now);
    while(now&&sz[ls]+1 != tar){
      if(sz[ls]>=tar)now = ls;
      else{
        tar -= sz[ls]+1;
        now = rs;
      push(now);
    }
    return now;
  void merge(int a,int b){
    if(!a||!b)return;
    splay(a); splay(b);
    a = get_sz(a,sz[a]);
    b = get_sz(b,1);
    splay(a); splay(b);
    ch[a][1] = b;
    fa[b] = a;
    pull(a);
    return:
  pair<int,int> split(int a,int tar){
    splay(a);
    if(!tar)return make_pair(0,a);
    int b = get_sz(a,tar);
    splay(b);
    pair<int,int> re;
    re.first = b;
    re.second = ch[b][1];
    fa[ch[b][1]] = 0;
    ch[b][1] = 0;
    pull(b);
    return re;
#undef ls
#undef rs
};
3.6 Link-Cut Tree [085466]
```

```
#define ll long long
//needs splay
//vertex add paths sum link-cut
struct LCT{
 Splay sp;
  void access(int x){
    sp.splay(x);
    sp.ch[x][1] =
    sp.pull(x);
    while(sp.fa[x]){
     int u = sp.fa[x];
      sp.splay(u);
      sp.push(u);
      sp.ch[u][1] = x;
      sp.pull(u);
      sp.splay(x);
   }
  void makeroot(int x){
    access(x);sp.splay(x);
    sp.rev[x] ^= 1;
  void link(int u,int v){
    makeroot(u);
    sp.splay(u);
    sp.fa[u] = v;
  void cut(int u,int v){
```

```
makeroot(u):
     access(v):
     sp.splay(v);
     int lc = sp.ch[v][0];
     sp.fa[lc] = 0;
     sp.ch[v][0] = 0;
     sp.pull(v);
  ll path_sum(int u,int v){
    makeroot(u);
     access(v);
     sp.splav(v);
     return sp.sum[v];
  void addval(int u,int val){
     sp.splay(u);
     sp.val[u] += val;
     sp.pull(u);
     return:
  int find(int p){
     access(p);
     return sp.get_sz(p,1);
};
```

### Geometry 4

# 4.1 Point [47044e]

```
template < typename T = int>
struct Pt{
  T x,y;
  Pt (T xx = (T)(0), T yy = (T)(0)):x(xx),y(yy){}
  Pt operator+(Pt b)const{return Pt(x+b.x,y+b.y);}
  Pt operator-(Pt b)const{return Pt(x-b.x,y-b.y);}
  T operator*(Pt b)const{return x*b.x+y*b.y;}
  T operator^(Pt b)const{return x*b.y-y*b.x;}
  T operator/(Pt b)const{return x*b.y-y*b.x;}
  bool operator
      <(Pt b)const{return x == b.x?y<b.y:x<b.x;}
  friend int dir(Pt a,Pt b){//returns sign(a ^ b)
    auto re = a ^ b;
    return re<0?-1:re>0?1:0;
  friend bool onseg(Pt x,Pt s,Pt e){
    if(((e-x)^(s-x)) != 0)return false;
    else if((s-x)*(e-x)>0)return false;
    return true:
  friend int
       intersect(Pt s1,Pt e1,Pt s2,Pt e2){//returns 0
       if doesn't intersect,1 if intersect,2 if on line
    if(onseg(s1,s2,e2)||onseg(e1,s2,
        e2)||onseg(s2,s1,e1)||onseg(e2,s1,e1))return 2;
    if(dir(s1-s2,e2-s2)*dir(e1-s2,e2-s2)<0&&
        dir(s2-s1,e1-s1)*dir(e2-s1,e1-s1)<0)return 1;</pre>
    return 0:
  }
};
```

### 4.2 Convex Hull [2a54da]

```
//needs Point.cpp
template < typename T = int>
struct ConvexHull{//returns in clockwise direction
  vector<Pt<T>> solve(vector<Pt<T>> v){
    sort(v.begin(),v.end());
    vector<Pt<T>> u,d;
    for(auto &i:v){
      while(u.size()>1&&((i-u.end()[-1])
          ^(u.end()[-2]-u.end()[-1]))>=0)u.pop_back();
      while(d.size()>1&&((i-d.end()[-1])
          ^(d.end()[-2]-d.end()[-1]))<=0)d.pop_back();
      u.push_back(i);
      d.push_back(i);
    for(int i =
         1;i+1<d.size();i++)u.push_back(d.end()[-1-i]);
    return u;
  }
};
```

### 4.3 Minkowski sum [9db95e]

```
//needs Point template
template <typename T>
vector<Pt
    <T>> minkowski(vector<Pt<T>> va, vector<Pt<T>> vb){
  deque<Pt<T>> a,b;
  for(auto &i:va)a.push_back(i);
  for(auto &i:vb)b.push_back(i);
  Pt head = *min_element(a.begin(),a.end());
  while(a[0].x != head.x||a[0].y != head.y){
    a.push_back(a[0]);
    a.pop_front();
  head = *min element(b.begin(),b.end());
  while (b[0].x != head.x||b[0].y != head.y){
    b.push_back(b[0]);
    b.pop_front();
  a.push back(a[0]);
  b.push_back(b[0]);
  int p1 = 0, p2 = 0;
  vector<Pt<T>> re;
  while(p1 < a.size()&&p2 < b.size()){</pre>
    //cerr<<a
        .size()<<','<<b.size()<<":"<<p1<<' '<<p2<<endl;
    int dir = 0;
    re.push_back(a[p1]+b[p2]);
    if(p1+1 == a.size())dir = 1;
    else if(p2+1 == b.size())dir = 0;
    else
        if(((a[p1+1]-a[p1])^(b[p2+1]-b[p2]))>0)dir = 0;
    else dir =
    if(dir == 0)p1++;
    else p2++:
 }
  return re;
}
```

# 5 String

### 5.1 KMP [bb2a1b]

```
template <typename T>
struct KMP {
    void operator()(T a, int n, int *pi) {
        pi[0] = -1, pi[1] = 0;
        for (int i = 1; i < n; i++) {
            int j = pi[i];
            while (j >= 0 && a[i] != a[j]) j = pi[j];
            pi[i + 1] = j + 1;
        }
    }
};
```

### 5.2 Zalgorithm [6a03da]

```
template <typename T>
struct Z_alg {
    void operator()(T *a, int n, int *z) {
        fill(z, z + n + 1, 0);
        int l = 0;
        for (int i = 1; i <= n; i++) {</pre>
            if (i >= l + z[l]) {
                while (i + z[i] < n
                      && a[i + z[i]] == a[z[i]]) z[i]++;
                l = i;
                continue;
            int i_ = i - l;
            if (i_ + z[i_] == z[l]) {
                z[i] = z[i_];
                 while (i + z[i] < n
                      && a[i + z[i]] == a[z[i]]) z[i]++;
                 l = i;
                 continue;
            z[i] = (
                 i_+ z[i_-] < z[l] ? z[i_-] : z[l] - i_-);
        }
    }
};
```

### 5.3 manacher [c7bcd5]

```
template <typename T>
struct MANACHER {
    void operator()(T a, int n, int *mn) {
```

```
fill(mn, mn + n, 0);
         int l = 0;
         for (int i = 1; i < n; i++) {</pre>
             if (i > l + mn[l]) {
                 while (i - mn[i] - 1 >= 0
                      && i + mn[i] + 1 < n && a[i - mn[i]]
                       - 1] == a[i + mn[i] + 1]) mn[i]++;
                 1 = i
                 continue;
             int i_ = 2 * l - i;
if (i_ - mn[i_] == l - mn[l]) {
                 mn[i] = mn[i_];
                 while (i - mn[i] - 1 >= 0
                      && i + mn[i] + 1 < n && a[i - mn[i]
                       - 1] == a[i + mn[i] + 1]) mn[i]++;
                 l = i:
                 continue;
             mn[i] = (i_ - mn[i_]
                 > l - mn[l] ? mn[i_] : i_ - l + mn[l]);
        }
    }
};
```

### 5.4 Suffix Array (SAIS) [a683f1]

```
int SA[MXN * 2], H[MXN], RA[MXN];
namespace SAIS {
    bool _t[MXN * 2];
    int _s[MXN *
    2], _c[MXN * 2], x[MXN], _p[MXN], _q[MXN * 2]; void pre(int *sa, int *c, int n, int z) {
         fill_n(sa, n, 0);
         copy_n(c, z, x);
    void induce(int
          *sa, int *c, int *s, bool *t, int n, int z) {
         copy_n(c, z - 1, x + 1);
         FOR(i, 0, n) {
             if (sa[i] && !t[sa[i] - 1]) {
                  sa[x[s[sa[i] - 1]]++] = sa[i] - 1;
             }
         copy_n(c, z, x);
for (int i = n - 1; i >= 0; i--) {
   if (sa[i] && t[sa[i] - 1]) {
                  sa[--x[s[sa[i] - 1]]] = sa[i] - 1;
         }
    void sais(int *s, int *sa, int
    *p, int *q, bool *t, int *c, int n, int z) {
         bool uniq = t[n - 1] = true;
         int nn = 0, nmxz =
               -1, *nsa = sa + n, *ns = s + n, last = -1;
         fill_n(c, z, 0);
         FOR(i, \theta, n) uniq &= ++c[s[i]] < 2;
         partial_sum(c, c + z, c);
         if (uniq) {
             FOR(i, \theta, n) sa[--c[s[i]]] = i;
             return:
         for (int i = n - 2; i >= 0; i--) {
             t[i] = (s[i] ==
                  s[i + 1] ? t[i + 1] : s[i] < s[i + 1]);
         pre(sa, c, n, z);
FOR(i, 1, n) {
             if (t[i] && !t[i - 1]) {
                  sa[--x[s[i]]] = p[q[i] = nn++] = i;
             }
         induce(sa, c, s, t, n, z);
         FOR(i, 0, n) {
             if (sa[i] && t[sa[i]] && !t[sa[i] - 1]) {
                  bool neq = last < 0 || !equal(s + sa[</pre>
                       i], s + p[q[sa[i]] + 1], s + last);
                  ns[q[last = sa[i]]] = nmxz += neq;
             }
         }
         sais(ns, nsa,
             p + nn, q + n, t + n, c + z, nn, nmxz + 1);
         pre(sa, c, n, z);
         for (int i = nn - 1; i >= 0; i--) {
             sa[--x[s[p[nsa[i]]]]] = p[nsa[i]];
```

### 5.5 AC automaton [c073c7]

```
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
struct AC {
    int nc;
    char c[MXN];
    int pi[MXN], p[MXN], nxt[MXN][MXC];
    void init() {
         fill(nxt[0], nxt[0] + MXC, 1);
         fill(nxt[1], nxt[1] + MXC, -1);
    int add node(int par, char c) {
         c[nc] = _c;
         p[nc] = par;
         fill(nxt[nc], nxt[nc] + MXC, -1);
         return nc++;
    int push(string &s) {
         int now = 1;
         for (auto &i : s) {
             if (nxt[now][i - 'a'] == -1)
    nxt[now][i - 'a'] = add_node(now, i);
             now = nxt[now][i - 'a'];
         }
         return now;
    void build() {
         queue < int > q;
         pi[1] = 0;
         FOR(i, 0, MXC) {
             if (nxt[1][
                 i] == -1) nxt[1][i] = nxt[pi[1]][i];
             else q.push(nxt[1][i]);
         while (q.size()) {
             int id = q.front();
             q.pop();
             pi[id] = nxt[pi[p[id]]][c[id] - 'a'];
FOR(i, 0, MXC) {
    if (nxt[id][i]
                      == -1) nxt[id][i] = nxt[pi[id]][i];
                  else q.push(nxt[id][i]);
             }
        }
    }
};
```

# 6 Math

### **6.1 FFT** [9ff2a9]

```
#define TYPE double
typedef complex<TYPE> cd;
#undef TYPE

struct FFT {
    const double pi = acos(-1);
    cd cis(double theta) {
        return cd(cos(theta), sin(theta));
    }
    cd OMEGA(int n, int k) {
        return cis(pi * 2 * k / n);
    }
}
```

```
void operator()(cd *a, int N, bool inv) {
         auto REV = [\&](int x) \rightarrow int {
             int ans = 0;
             for (int i = 1; i < N; i <<= 1) {</pre>
                  ans <<= 1;
                  if (i & x) ans |= 1;
             return ans;
         FOR(i, 0, N) {
             int r = REV(i);
             if (i < r) swap(a[i], a[r]);</pre>
         for (int w = 1; w < N; w <<= 1) {</pre>
             int on = w << 1;
             for (int ok = 0; ok < w; ok++) {
                  cd omega
                       = OMEGA(on, (inv ? -1 : 1) * ok);
                  for (int s = 0; s < N; s += on) {</pre>
                      cd &L =
                           a[s + ok], &R = a[s + ok + w];
                      cd l = L, r = omega * R;
                      L = l + r;
                      R = l - r;
                  }
             }
         if (inv) {
             for (int i = 0; i < N; i++) a[i] /= N;</pre>
         }
} fft;
6.2 FWT [a168b9]
#include <bits/stdc++.h>
using namespace std;
#define fs first
#define sc second
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
using ll = long long;
typedef pair<int, int> pii;
typedef pair<pii, pii> MAT;
template <int mod = 998244353>
struct mint {
    int x;
     mint() : x(0) {}
     mint(int _x) : x(_x) \{ \}
     mint operator+(mint o) {
         int y = x + o.x;
         y -= (y >= mod ? mod : 0);
         return mint(y);
    mint operator*(int y) {
    y += (y < 0 ? mod : 0);
         return mint((ll) x * y % mod);
     mint operator*(mint o) {
         return mint((ll) x * o.x % mod);
     mint inv() {
         int b = mod - 2, a = x;
         int ans = 1;
         while (b) {
   if (b & 1) ans = (ll) ans * a % mod;
             b >>= 1;
             a = (ll) a * a % mod;
         return mint(ans);
    }
};
template <typename T = int>
struct FWT {
     enum FWT_TYPE {
         AND,
         OR.
         XOR
    };
```

const MAT mat[3] = {  $\{\{1, 1\}, \{0, 1\}\}, \{\{1, 0\}, \{1, 1\}\},$ 

const MAT tam[3] = {

}:

 $\{\{1, 1\}, \{1, -1\}\}$ 

```
{{1, -1}, {0, 1}},
{{1, 0}, {-1, 1}},
{{1, 1}, {1, -1}}
    FWT() {}
    void btf(T &L, T &R, MAT &m) {
        T l = L, \Gamma = R;
        L = l * m.fs.fs + r * m.fs.sc;
        R = l * m.sc.fs + r * m.sc.sc;
    void apply(T *a, int n, bool inv, FWT_TYPE tp) {
    MAT m = (inv ? tam : mat)[tp];
        for (int w = 1; w < n; w <<= 1)
             FOR(i, 0, n) if (i & w) {
                 btf(a[i - w], a[i], m);
         if (tp == FWT_TYPE::XOR && inv) {
             T n_ = T(n).inv();
             FOR(i, 0, n) a[i] = a[i] * n_;
    }
};
6.3 NTT [13fd5f]
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
    const static int LG = 20;
    int mod;
    int o[(1 << LG) + 1];</pre>
    int ADD(int a, int b) {
        // help yourself
    int SUB(int a, int b) {
        // help yourself
    int MUL(int a, int b) {
        // help yourself
    int POW(int a, int b) {
        // help yourself
    NTT(int g, int gap, int _mod) {
        mod = _mod;
o[0] = 1;
         int pp = POW(g, gap);
         FOR(i,
             1, (1 << LG) + 1) o[i] = MUL(o[i - 1], pp);
    void operator()(int *a, int n, bool inv) {
        auto REV = [&](int x) -> int {
             int ans = 0;
             for (int w = 1; w < n; w <<= 1) {</pre>
                 ans = (ans << 1) | (x & 1);
                 x >>= 1;
             return ans;
        FOR(i, 0, n) {
             int j = REV(i);
             if (i < j) swap(a[i], a[j]);</pre>
         for (int w = 1; w < n; w <<= 1) {
             int owo = 1 << (LG - __lg(w) - 1), oid = 0;
             FOR(i, 0, w) {
                 int omega
                       = o[inv ? (1 << LG) - oid : oid];
                 for (int s = 0; s < n; s += (w << 1)) {
                      int &L
                           = a[s + i], &R = a[s + w + i];
                      int l = L, r = MUL(omega, R);
                      L = ADD(l, r);
                      R = SUB(l, r);
                 oid += owo;
             }
        if (inv) {
             int x = POW(n, mod - 2);
             FOR(i, 0, n) a[i] = MUL(a[i], x);
        }
    }
};
NTT ntt1(3, 952, 998244353);
```

```
NTT ntt2(3, 100, 104857601);
NTT ntt3(3, 160, 167772161);
```

### 6.4 Chinese Remainder Theorem [6fdd6f]

```
using lll = __int128_t;
struct ICRT {
    lll p1, p2, p3;
     lll c1, c2, c3;
     ICRT() {}
     ICRT(lll _p1,
          lll _p2, lll _p3) : p1(_p1), p2(_p2), p3(_p3) {
          auto POW = [&](lll a, lll b, lll mod) -> lll {
              lll ans = 1;
              while (b) {
                   if (b & 1) ans = ans * a % mod;
                   b >>= 1;
                   a = a * a % mod;
              }
              return ans:
         };
         c1 = POW(p2 * p3 % p1, p1 - 2, p1) * p2 * p3;
c2 = POW(p3 * p1 % p2, p2 - 2, p2) * p3 * p1;
c3 = POW(p1 * p2 % p3, p3 - 2, p3) * p1 * p2;
     ill operator()(int r1, int r2, int r3) {
         return (c1
              * r1 + c2 * r2 + c3 * r3) % (p1 * p2 * p3);
    }
};
ICRT icrt(998244353, 104857601, 167772161);
```