#### Contents 3.2 CHT........ 3.3 Treap . . . . . . . . . . . . . . . . 3 1 Setups 4 Geometry 1.1 vimrc . . . . . . . . . . . . . . . . 4.1 Point . . . . . . . . . . . . 4.2 Convex Hull . . . . . . . . debug . . . . . . . . . . . . . 4.3 Minkowski sum . . . . . . 4 1.5 template . . . . . . . . . . 5 String 2 Graph 5.1 Suffix Array (SAIS) . . . . 2.1 Dominator Tree . . . . . . . 2.2 Incremental SCC . . . . . . 5.2 AC automaton . . . . . . 2.3 Block-Cut Tree . . . . . . 6 Math 6.1 module int . . . . . . . . . 6.2 FFT . . . . . . . . . . . . . . . 3 Data Structure 6.3 FWT . . . . . . . . . . . . 3.1 Li Chao Tree . . . . . . . . Setups 1.1 vimrc [6c9876] se nu ai rnu cin ts=4 sw=4 | sy on inoremap {<CR> {<CR>}<Esc>0 inoremap jk <Esc> 1.2 pbds [9f7c3e] #include <bits/stdc++.h> #include <bits/extc++.h> using namespace \_\_gnu\_pbds; using namespace std; template <typename T> using ordered\_set = tree<T,null\_type,less</pre> <T>,rb\_tree\_tag,tree\_order\_statistics\_node\_update>; int main(){ ordered\_set<int> st; st.insert(1); st.find\_by\_order(0);//iterator to 1 st.order\_of\_key(1);//returns 0 } **1.3 terminal** [46fc34] -- terminal --\$ setxkbmap -option caps:swapescape 1.4 debug [33c0d3] #ifdef MIKU string dbmc = "\033[1;38;2;57;197;187m", dbrs = \033[0m; #define debug (x...) cout << dbmc << "[" << #x << "] : ", dout(x) void dout() { cout << dbrs << endl; }</pre> template <typename T, typename ...U> #define debug(...) 39 #endif int main(){ int a = 49; char c = '8'; debug(a);// outputs "[a] : 49" debug(a, c); // outputs "[a, c] : 49, 8" debug("PCCORZ"); // outputs "["PCCORZ"] : PCCORZ" debug(); // outputs "[] : ' 1.5 template [5116af] #include <bits/stdc++.h> using namespace std; #define fs first #define sc second #define F first #define S second **#define** FOR(i, j, k) **for** (**int** i = j, Z = k; i < Z; i++) using ll = long long;

using lll = \_\_int128\_t;

typedef pair<ll,ll> pll

int main(){

typedef pair<int, int> pii;

typedef tuple <int,int,int> tiii;

```
2 Graph
```

#### 2.1 Dominator Tree [3b89c3]

```
struct DominatorTree{
  //1-indexed
  //not reachable from s -> not on tree
  int n:
  vector<vector<int>> G,rG;
  vector<int> pa,dfn,id;
  int dfnCnt;
  vector<int> semi,idom,best;
  vector<vector<int>> ret;
  void init(int _n){
    n = n;
    G = rG = ret = vector<vector<int>>(n+1);
    pa = dfn = id = vector < int > (n+1,-1);
    dfnCnt = 0:
    semi = idom = best = vector<int>(n+1,-1);
  void add_edge(int u,int v){
    G[u].push_back(v);
    rG[v].push_back(u);
  void dfs(int u){
    id[dfn[u]=++dfnCnt]=u;
    for(auto v:G[u]) if(!dfn[v]){
      dfs(v),pa[dfn[v]]=dfn[u];
  int find(int y,int x){
    if(y<=x)return y;</pre>
    int tmp=find(pa[y],x);
    if(semi[best[y]]>semi[best[pa[y]]])
      best[y]=best[pa[y]];
    return pa[y]=tmp;
  void tarjan(int root){
    dfnCnt=0;
    for(int i=1;i<=n;++i){</pre>
      dfn[i]=idom[i]=0;
      ret[i].clear();
      best[i]=semi[i]=i;
    dfs(root);
    for(int i=dfnCnt;i>1;--i){
      int u=id[i];
      for(auto v:rG[u]) if(v=dfn[v]){
        find(v,i);
        semi[i]=min(semi[i],semi[best[v]]);
      ret[semi[i]].push_back(i);
      for(auto v:ret[pa[i]]){
        find(v,pa[i]);
        idom[v
             ] = semi[best[v]]==pa[i] ? pa[i] : best[v];
      }
      ret[pa[i]].clear();
    for(int i=2; i<=dfnCnt; ++i){</pre>
      if(idom[i]!=semi[i]) idom[i]=idom[idom[i]];
      ret[id[idom[i]]].push_back(id[i]);
  }
  vector<vector<int>> solve(int s){
    tarjan(s);
    return ret;
};
```

#### 2.2 Incremental SCC [d8b556]

```
struct IncrementalSCC{
#define pii pair <int,int>
#define fs first
#define sc second
#define tiii tuple <int,int,int>
    //if u == v : ans[i] = -1
    //if not connected : ans[i] = m
    //all 0-indexed
    int n;
    vector <int> ans;
    int m;
    vector <tiii> all;
    vector <int> SCC(int n,vector <vector <int>>& paths){
        vector <int> scc_id(n,-1),idx(n,-1),low(n,-1),st;
        int cnt = 0,gcnt = 0;
```

```
function < void(int) > dfs = [&](int now) -> void{
    low[now] = idx[now] = cnt++;
    st.push_back(now);
    for(auto nxt:paths[now]){
      if(scc_id[nxt] != -1)continue;
      if(idx[nxt] == -1){
        dfs(nxt);
        low[now] = min(low[now],low[nxt]);
        low[now] = min(low[now],idx[nxt]);
    if(low[now] == idx[now]){
      int id = -1;
      while(id != now){
        id = st.back();
        st.pop_back();
        scc_id[id] = gcnt;
      gcnt++;
   }
  for(int i = 0;i<n;i++){</pre>
   if(scc_id[i] == -1)dfs(i);
  //cerr<<"SCC: "<<n<<"::";for(int
       i = 0;i<n;i++)cerr<<scc_id[i]<<',';cerr<<endl;</pre>
  return scc_id;
vector<int> mapping;
void dc(int l,int r,vector<tiii> &edges){
  //cerr<<l<<'
                '<<r<<":"<<endl;
  if(l == r){
    for(auto
        [id,_,_]:edges)ans[id] = min(ans[id],l);
    return;
  int mid = (l+r)>>1;
  int cnt = 0;
  for(auto &[t,u,v]:edges){
    if(mapping[u] == -1)mapping[u] = cnt++;
    if(mapping[v] == -1)mapping[v] = cnt++;
  n = cnt;
  vector<vector<int>> paths(n);
  vector<int> vv;
  for(auto &[t,u,v]:edges){
    vv.push_back(u);
    vv.push_back(v);
    u = mapping[u],v = mapping[v];
    if(t<=mid)paths[u].push_back(v);</pre>
  //for(auto &i:vv)cerr<<i<<',';cerr<<endl;
  for(auto &i:vv)mapping[i] = -1;
  auto scc_id = SCC(n,paths);
  //for(auto
       [t,u,v]:edges)cerr<<t<<','<<u<<','<<v<<endl;
  //cerr<<endl;
  vector<tiii> vl,vr;
  for(auto &[t,u,v]:edges){
    if(scc_id[u] == scc_id[v]){
      ans[t] = min(ans[t], mid);
      vl.push_back(tiii(t,u,v));
    else{
      u = scc_id[u],v = scc_id[v];
      vr.push_back(tiii(t,u,v));
    }
  }
  vector < tiii > ().swap(edges);
  dc(l,mid,vl);
  dc(mid+1,r,vr);
  return:
void add_edge(int u,int v){
  all.push_back(tiii(all.size(),u,v));
vector<tiii> solve(){//[time,u,v]
  m = all.size();
  vector<tiii> ret(m);
  for(auto [t,u,v]:all)ret[t] = tiii(m,u,v);
  for(auto [t,u,v]:all)n = max({n,u,v});
  n++:
  ans = vector<int>(m,m);
```

```
for(auto [t,u,v]:all){
    if(u == v)ans[t] = -1;
}
    mapping = vector<int>(n,-1);
    dc(0,m,all);
    for(int i = 0;i<m;i++)get<0>(ret[i]) = ans[i];
    return ret;
}
IncrementalSCC(){
    ans.clear();
    n = m = 0;
}
#undef tiii
#undef pii
#undef fs
#undef sc
};
```

#### 2.3 Block-Cut Tree [f44682]

```
struct BlockCutTree{
  //0-indexed
  //returns a forest if the graph is not connected
  vector<vector<int>> g;
  vector<vector<int>> groups;
  vector<vector<int>> tr;
  vector<int> idx,low,st;
  int cnt,gcnt;
  int n;
  RoundSquareTree(int _n = 0){
    cnt = gcnt = 0;
    n = _n;
    g = vector<vector<int>>(n);
  void add_edge(int a,int b){//adds bidirectional edges
    g[a].push_back(b);
    g[b].push_back(a);
  void dfs(int now){
    idx[now] = low[now] = cnt++;
    st.push_back(now);
    for(auto nxt:g[now]){
      if(idx[nxt] == -1){
        dfs(nxt);
        low[now] = min(low[now],low[nxt]);
        if(low[nxt] == idx[now]){
           int id = -1;
           tr.push_back(vector<int>());
          while(id != nxt){
            id = st.back();st.pop_back();
             groups[id].push_back(gcnt);
             tr[id].push_back(gcnt+n);
            tr[gcnt+n].push_back(id);
          groups[now].push_back(gcnt);
          tr[now].push_back(gcnt+n);
          tr[gcnt+n].push_back(now);
          qcnt++;
      else idx[now] = min(idx[now],idx[nxt]);
    }
    return:
  vector<vector<int>> solve(){//
       returns the tree (round vertices numbered [0,n))
    idx = low = vector<int>(n,-1);
    tr = vector<vector<int>>(n);
    for(int i = 0;i<n;i++){</pre>
      if(idx[i] == -1)dfs(i);
    return tr;
  }
};
```

#### 2.4 Euler Tour [a4ce3c]

```
#include <bits/stdc++.h>
using namespace std;

struct EulerTour{
   //undirected graph,0-indexed, fails if doesn't exist
   //returns the order of edges
#define pii pair <int,int>
   vector <vector <pii>> g;
   vector <int> ptr;
   vector <bool> vis;
```

```
vector<int> re:
  int n.ecnt:
  void init(int _n){
   n = _n;
   ecnt = 0;
   q = vector<vector<pii>>>(n);
    ptr = vector<int>(n);
  void add_edge(int a,int b,int id = -1){
    if(id == -1)id = ecnt;
    g[a].push_back(pii(b,id));
    g[b].push_back(pii(a,id));
    ecnt++;
  void dfs(int now){
    for(int &i = ptr[now];i<g[now].size();i++){</pre>
      auto [to,eid] = g[now][i];
      if(vis[eid])continue;
      vis[eid] = true;
      dfs(to);
      re.push_back(eid);
   }
    return;
  vector<int> solve(int s){
    re.clear();
    vis = vector<bool>(ecnt,0);
    dfs(s);
    return re;
#undef pii
```

## 3 Data Structure

### 3.1 Li Chao Tree [565209]

```
//range add line get min
//can even be used of modifies isn't range modify
#define ll long long
const ll SZ = 8e6+10;
const ll inf = 3e18;
vector<ll> all;
struct Line{
 ll m.b:
 Line(ll mm = 0, ll bb = 0):m(mm),b(bb){}
  ll operator()(ll k){
    return m*k+b;
struct LiChao{
#define ls now*2+1
#define rs now*2+2
#define mid ((l+r)>>1)
 Line seg[SZ];
 LiChao(){
    fill(seg,seg+SZ,Line(0,inf));
  void modify(int now,int l,int r,int s,int e,Line v){
    if(l == r){}
      if(seg[now](all[l])>v(all[l]))swap(seg[now],v);
      return:
    if(l>=s&&e>=r){
      if(seg
          [now](all[mid])>v(all[mid]))swap(seg[now],v);
      if(seg[now].m<v.m)modify(ls,l,mid,s,e,v);</pre>
      else modify(rs,mid+1,r,s,e,v);
      if(mid>=s)modify(ls,l,mid,s,e,v);
      if(mid<e)modify(rs,mid+1,r,s,e,v);</pre>
    return;
  ll getval(int now,int l,int r,int p){
    if(l == r)return seg[now](all[p]);
    if(mid>=p)return
         min(seg[now](all[p]),getval(ls,l,mid,p));
    else return
         min(seg[now](all[p]),getval(rs,mid+1,r,p));
  void add_line(int s,int e,Line v){
    modify(0,0,all.size()-1,s,e,v);
    return;
  ll getmin(int p){
```

```
return getval(0,0,all.size()-1,p);
 }
#undef ls
#undef rs
#undef mid
};
#undef ll long long
```

3.2 CHT [98f67f]

```
//reference : 8BCube
#define ll long long
// only works for integer coordinates!! maintain max
struct Line {
  mutable ll a, b, p;
  bool operator
       <(const Line &rhs) const { return a < rhs.a; }</pre>
  bool operator<(ll x) const { return p < x; }</pre>
};
struct CHT : multiset<Line, less<>> {
   static const ll kInf = 1e18;
  ll Div(ll a,
        ll b) { return a / b - ((a ^ b) < 0 && a % b); }
  bool isect(iterator x, iterator y) {
     if (y == end()) { x->p = kInf; return 0; }
     if (x
         ->a == y->a) x->p = x->b > y->b ? kInf : -kInf;
     else x - > p = Div(y - > b - x - > b, x - > a - y - > a);
     return x->p >= y->p;
  void addline(ll a, ll b) {
     auto z = insert({a, b, 0}), y = z++, x = y;
     while (isect(y, z)) z = erase(z);
     if (x != begin
         () && isect(--x, y)) isect(x, y = erase(y));
     while ((y = x) != begin
         () && (--x)->p >= y->p) isect(x, erase(y));
  ll query(ll x) {
     auto l = *lower_bound(x);
     return l.a * x + l.b;
  }
};
```

```
3.3 Treap [ff4001]
#define ll long long
//range reverse range add range sum
//need to push before using the info on node
struct node{
  int pri;
  int pl,pr;
  ll sum,tag,val;
  int sz;
  int rev:
  node(){
    pl = pr = sum = tag = 0;
    sz = 0;
    rev = 0:
    pri = rand():
 }
};
const int SZ = 2e5+10;
struct Treap{
  node nd[SZ];
  int cnt =
  Treap(){
    cnt = 0;
  int newnode(){
    cnt++:
    nd[cnt].sz = 1;
    return cnt;
  void pull(int now){
    if(!now)return;
    nd[now].sz = nd[nd[now].pr].sz+nd[nd[now].pl].sz+1;
    ll ls = nd[nd[now
        ].pl].sum+nd[nd[now].pl].tag*nd[nd[now].pl].sz;
    ll rs = nd[nd[now
        ].pr].sum+nd[nd[now].pr].tag*nd[nd[now].pr].sz;
    nd[now].sum = nd[now].val+ls+rs;
    return;
  void push(int now){
```

```
if(!now)return:
    if(nd[now].rev){
      swap(nd[now].pl,nd[now].pr);
      if(nd[now].pl)nd[nd[now].pl].rev ^= 1;
      if(nd[now].pr)nd[nd[now].pr].rev ^= 1;
      nd[now].rev = 0;
    int tl = nd[now].pl,tr = nd[now].pr;
    nd[now].val += nd[now].tag;
    if(tl)nd[tl].tag += nd[now].tag;
    if(tr)nd[tr].tag += nd[now].tag;
    nd[now].tag = 0;
    pull(now);
  int merge(int a,int b){
    if(!a)return b;
    if(!b)return a:
    if(nd[a].pri>nd[b].pri){
      push(a);
      nd[a].pr = merge(nd[a].pr,b);
      pull(a);
      return a;
      push(b);
      nd[b].pl = merge(a,nd[b].pl);
      pull(b);
      return b;
  void split(int now,int &a,int &b,int tar){
    if(!now){
      a = b = 0;
      return;
    push(now);
    if(nd[nd[now].pl].sz+1<=tar){</pre>
      a = now;
      split(nd[now
          ].pr,nd[a].pr,b,tar-(nd[nd[now].pl].sz+1));
    else{
      b = now;
      split(nd[now].pl,a,nd[b].pl,tar);
    pull(a):
    pull(b);
    return:
 }
};
Treap T;
```

# 4 Geometry

#### 4.1 Point [d6339e]

```
template < typename T = int>
struct Pt{
 T x, y;
  Pt (T xx = T(),T yy = T()):x(xx),y(yy){}
 Pt operator+(Pt b)const{return Pt(x+b.x,y+b.y);}
 Pt operator - (Pt b) const{return Pt(x-b.x,y-b.y);}
 T operator*(Pt b)const{return x*b.x+y*b.y;}
 T operator^(Pt b)const{return x*b.y-y*b.x;}
  T operator/(Pt b)const{return x*b.y-y*b.x;}
 bool operator
      <(Pt b)const{return x == b.x?y<b.y:x<b.x;}
  friend int dir(Pt a,Pt b){//returns sign(a ^ b)
   auto re = a ^ b;
    return re<0?-1:re>0?1:0;
  friend bool onseg(Pt x,Pt s,Pt e){
    if(((e-x)^(s-x)) != 0)return false;
    else if((s-x)*(e-x)>0)return false;
    return true;
  friend int
       intersect(Pt s1,Pt e1,Pt s2,Pt e2){//returns 0
       if doesn't intersect,1 if intersect,2 if on line
    if(onseg(s1,s2,e2)||onseg(e1,s2,
        e2)||onseg(s2,s1,e1)||onseg(e2,s1,e1))return 2;
    if(dir(s1-s2,e2-s2)*dir(e1-s2,e2-s2)<0&&</pre>
        dir(s2-s1,e1-s1)*dir(e2-s1,e1-s1)<0)return 1;</pre>
    return 0;
```

## 4.2 Convex Hull [2a54da]

**}**;

```
//needs Point.cpp
template < typename T = int>
struct ConvexHull{//returns in clockwise direction
  vector<Pt<T>> solve(vector<Pt<T>> v){
    sort(v.begin(),v.end());
    vector<Pt<T>> u,d;
    for(auto &i:v){
      while(u.size()>1&&((i-u.end()[-1])
          ^(u.end()[-2]-u.end()[-1]))>=0)u.pop_back();
      while(d.size()>1&&((i-d.end()[-1])
          ^(d.end()[-2]-d.end()[-1]))<=0)d.pop_back();
      u.push back(i);
      d.push_back(i);
    for(int i =
         1; i+1 < d. size(); i++)u.push back(d.end()[-1-i]);
    return u;
 }
};
```

#### 4.3 Minkowski sum [9db95e]

```
//needs Point template
template <typename T>
vector<Pt
    <T>> minkowski(vector<Pt<T>> va, vector<Pt<T>> vb){
  deque<Pt<T>> a,b;
  for(auto &i:va)a.push_back(i);
  for(auto &i:vb)b.push_back(i);
  Pt head = *min_element(a.begin(),a.end());
  while (a[0].x != head.x | |a[0].y != head.y){
    a.push_back(a[0]);
    a.pop_front();
  head = *min_element(b.begin(),b.end());
  while(b[0].x != head.x||b[0].y != head.y){
    b.push_back(b[0]);
    b.pop_front();
  a.push_back(a[0]);
  b.push_back(b[0]);
  int p1 = 0, p2 = 0;
  vector<Pt<T>> re;
  while(p1 < a.size()&&p2 < b.size()){</pre>
    //cerr<<a
         .size()<<','<<b.size()<<":"<<p1<<' '<<p2<<endl;
    int dir = 0;
    re.push_back(a[p1]+b[p2]);
    if(p1+1 == a.size())dir = 1;
    else if(p2+1 == b.size())dir = 0;
        if(((a[p1+1]-a[p1])^(b[p2+1]-b[p2]))>0)dir = 0;
    else dir = 1;
    if(dir == 0)p1++;
    else p2++;
  return re;
```

# 5 String

#### 5.1 Suffix Array (SAIS) [a683f1]

```
int SA[MXN * 2], H[MXN], RA[MXN];
namespace SAIS {
    bool _t[MXN * 2];
    int _s[MXN *
              _c[MXN * 2], x[MXN], _p[MXN], _q[MXN * 2];
         2],
    void pre(int *sa, int *c, int n, int z) {
        fill_n(sa, n, 0);
        copy_n(c, z, x);
    void induce(int
         *sa, int *c, int *s, bool *t, int n, int z) {
        copy_n(c, z - 1, x + 1);
        FOR(i, 0, n) {
            if (sa[i] && !t[sa[i] - 1]) {
                 sa[x[s[sa[i] - 1]]++] = sa[i] - 1;
        copy_n(c, z, x);
for (int i = n - 1; i >= 0; i--) {
            if (sa[i] && t[sa[i] - 1]) {
```

```
sa[--x[s[sa[i] - 1]]] = sa[i] - 1;
        }
    void sais(int *s, int *sa, int
    *p, int *q, bool *t, int *c, int n, int z) {
    bool uniq = t[n - 1] = true;
         int nn = 0, nmxz =
               -1, *nsa = sa + n, *ns = s + n, last = -1;
         fill_n(c, z, 0);
         FOR(i, 0, n) uniq &= ++c[s[i]] < 2;
         partial_sum(c, c + z, c);
         if (uniq) {
             FOR(i, 0, n) sa[--c[s[i]]] = i;
             return:
         for (int i = n - 2; i >= 0; i--) {
             t[i] = (s[i] ==
                  s[i + 1] ? t[i + 1] : s[i] < s[i + 1]);
         pre(sa, c, n, z);
FOR(i, 1, n) {
             if (t[i] && !t[i - 1]) {
                 sa[--x[s[i]]] = p[q[i] = nn++] = i;
             }
         induce(sa, c, s, t, n, z);
         FOR(i, 0, n) {
   if (sa[i] && t[sa[i]] && !t[sa[i] - 1]) {
                  bool neq = last < 0 || !equal(s + sa[</pre>
                      i], s + p[q[sa[i]] + 1], s + last);
                  ns[q[last = sa[i]]] = nmxz += neq;
             }
         sais(ns, nsa,
             p + nn, q + n, t + n, c + z, nn, nmxz + 1);
         pre(sa, c, n, z);
         for (int i = nn - 1; i >= 0; i--) {
             sa[--x[s[p[nsa[i]]]] = p[nsa[i]];
         induce(sa, c, s, t, n, z);
    void mkhei(int n) {
         for (int i = 0, j = 0; i < n; i++) {</pre>
             if (RA[i]) {
                  for (; i + j < n
                  }
        }
    void build(int *s, int n, int mxc) {
        copy_n(s, n, _s), _s[n] = 0;
sais(_s, SA, _p, _q, _t, _c, n + 1, mxc);
copy_n(SA + 1, n, SA);
         FOR(i, 0, n) RA[SA[i]] = i;
         mkhei(n);
         copy(H + 1, H + n, H);
    }
}
```

#### 5.2 AC automaton [c073c7]

```
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
struct AC {
    int nc;
    char c[MXN];
    int pi[MXN], p[MXN], nxt[MXN][MXC];
    void init() {
        fill(nxt[0], nxt[0] + MXC, 1);
        fill(nxt[1], nxt[1] + MXC, -1);
    int add_node(int par, char _c) {
        c[nc] = _c;
        p[nc] = par;
        fill(nxt[nc], nxt[nc] + MXC, -1);
        return nc++;
    int push(string &s) {
        int now = 1;
        for (auto &i : s) {
            if (nxt[now][i - 'a'] == -1)
                 nxt[now][i - 'a'] = add_node(now, i);
            now = nxt[now][i - 'a'];
```

```
return now;
     void build() {
         queue<int> q;
         pi[1] = 0;
         FOR(i, 0, MXC) {
             if (nxt[1][
    i] == -1) nxt[1][i] = nxt[pi[1]][i];
             else q.push(nxt[1][i]);
         while (q.size()) {
             int id = q.front();
             q.pop();
             pi[id] = nxt[pi[p[id]]][c[id] - 'a'];
             FOR(i, 0, MXC)
                 if (nxt[id][i]
                      == -1) nxt[id][i] = nxt[pi[id]][i];
                  else q.push(nxt[id][i]);
             }
         }
     }
};
```

#### 6 Math

#### module int [a4a56c] 6.1

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
template <int mod = 998244353>
struct mint {
    int x;
    mint() : x(0) {}
mint(int _x) : x((_x % mod + mod) % mod) {}
operator int() const {
        return x;
    template <typename T>
    mint operator+(T t) {
        mint o = mint(t);
        int y = x + o.x;
        y = (y > mod ? mod : 0);
        return mint(y);
    template <typename T>
    mint &operator+=(T t) {
        return (*this = operator+(t));
    template <typename T>
    mint operator - (T t) {
        mint o = mint(t);
        int y = x - o.x;
        y += (y < \theta ? mod : \theta);
        return mint(y);
    template <typename T>
    mint &operator -=(T t) {
        return (*this = operator-(t));
    template <typename T>
    mint operator*(T t) {
        mint o = mint(t);
        return mint((ll) x + o.x % mod);
    template <typename T>
    mint &operator*=(T t) {
        return (*this = operator*(t));
    template <typename T>
    mint POW(T t) {
        int b = int(t);
        mint a(x), ans(1);
        while (b) {
    if (b & 1) ans *= a;
             b >>= 1;
             a *= a;
        }
        return ans;
    template <typename T>
    mint inv()
        return POW(mod - 2);
    template <typename T>
```

```
int b = mod - 2, a = x;
    mint operator/(T t) {
         mint o = mint(t);
                                                                           int ans = 1:
         return operator*(o.inv());
                                                                           while (b) {
                                                                               if (b & 1) ans = (ll) ans * a % mod;
    template <typename T>
                                                                               b >>= 1;
    mint & operator /= (T t) {
                                                                               a = (ll) a * a % mod;
         return (*this = operator/(t));
                                                                           return mint(ans);
};
                                                                      }
                                                                 };
6.2 FFT [263d47]
                                                                  template <typename T = int>
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
                                                                  struct FWT {
template <typename T>
                                                                      enum FWT_TYPE {
struct FFT {
                                                                           AND,
    const T pi = acos(-1);
                                                                           OR,
    complex < T > cis(T theta) {
                                                                           XOR
         return complex < T > (cos(theta), sin(theta));
                                                                      };
                                                                      const MAT mat[3] = {
    complex <T > OMEGA(int n, int k) {
    return cis(pi * 2 * k / n);
                                                                           {{1, 1}, {0, 1}}, {{1, 1}},
                                                                           \{\{1, 1\}, \{1, -1\}\}\
    void apply(complex<T> *a, int N, bool inv) {
                                                                      };
         auto REVERSE = [&](int x) -> int {
                                                                      const MAT tam[3] = {
             int ans = 0;
                                                                           {{1, -1}, {0, 1}}, {{1, 0}, {-1, 1}}, {{1, 1}, {1, -1}}
             for (int i = 1; i < N; i <<= 1) {</pre>
                  ans <<= 1;
                  if (i & x) ans |=1;
                                                                      FWT() {}
             return ans;
                                                                      void btf(T &L, T &R, MAT &m) {
                                                                           T l = L, r = R;
         FOR(i, 0, N) {
                                                                           L = l * m.fs.fs + r * m.fs.sc;
             int r = REVERSE(i);
                                                                           R = l * m.sc.fs + r * m.sc.sc;
             if (i < r) swap(a[i], a[r]);</pre>
                                                                      void apply(T *a, int n, bool inv, FWT_TYPE tp) {
         for (int w = 1; w < N; w <<= 1) {
                                                                           MAT m = (inv ? tam : mat)[tp];
             int omega_n = w << 1;</pre>
                                                                           for (int w = 1; w < n; w <<= 1) {</pre>
             for (int
                                                                               FOR(i, 0, n) if (i & w) {
                   omega_k = \theta; omega_k < w; omega_k++) {
                                                                                    btf(a[i - w], a[i], m);
                  complex < T > omega = OMEGA(
                  omega_n, (inv ? -1 : 1) * omega_k);
for (int s = 0; s < N; s += omega_n) {</pre>
                                                                           if (tp == FWT_TYPE::XOR && inv) {
                       complex < T > \&L = a[s + omega\_k]
                                                                               T n_ = T(n).inv();
                           ], &R = a[s + omega_k + w];
                                                                               FOR(i, 0, n) a[i] = a[i] * n_;
                      complex < T > l = L, r = omega * R;
                                                                           }
                      L = l + r;
                                                                      }
                      R = l - r;
                                                                 };
                  }
             }
         if (inv) {
             FOR(i, 0, N) a[i] /= N;
    }
};
#undef FOR
6.3 FWT [a168b9]
```

```
#include <bits/stdc++.h>
using namespace std:
#define fs first
#define sc second
#define FOR(i, j, k) for (int i = j, Z = k; i < Z; i++)
using ll = long long;
typedef pair<int, int> pii;
typedef pair<pii, pii> MAT;
template <int mod = 998244353>
struct mint {
    int x;
    mint() : x(0) \{
    mint(int _x) : x(_x) \{ \}
    mint operator+(mint o) {
        int y = x + o.x;
        y -= (y >= mod ? mod : 0);
        return mint(y);
    mint operator*(int y) {
        y += (y < 0 ? mod : 0);
        return mint((ll) x * y % mod);
    mint operator*(mint o) {
        return mint((ll) x * o.x % mod);
    mint inv() {
```