

Characterizing the Neurocognitive Mechanisms of Arithmetic

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CHARACTERIZING THE NEUROCOGNITIVE MECHANISMS OF ARITHMETIC

Pedro PINHEIRO-CHAGAS

Dissertation submitted for the degree of
Doctor of Philosophy

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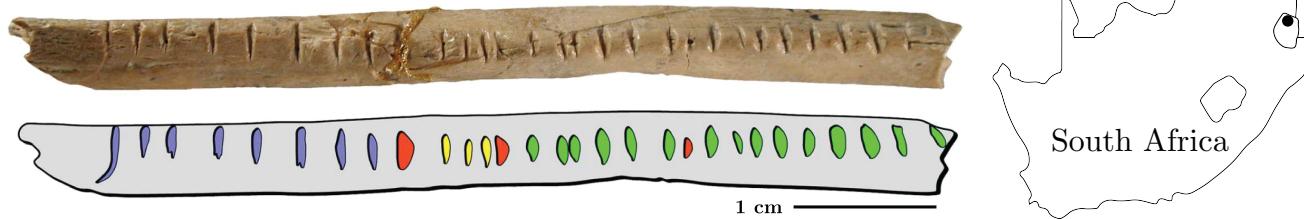
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Elizabeth SPELKE	Harvard University	Examiner
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Introduction

- **Mathematics:** a remarkable human invention.
- The fundamental language of science.
- Most elementary branch: **Arithmetic** – invented 50,000 years ago.

Tally sticks: store and transmit numerical information.



Central Market – Belo Horizonte



NeuroSpin



How are two numbers combined into a third?

$$3+5=8$$

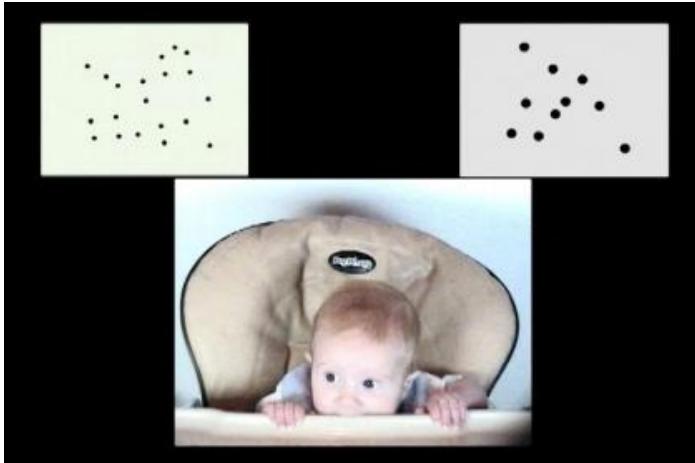
- Sophisticated abstract concepts & complex network of brain regions.
- My goal: characterize the neurocognitive mechanisms of arithmetic.
- Time-resolved: combining methods that allow for high temporal resolution of behavior/brain activity and high anatomical precision.
- Decompose the fast dynamics of the underlying processing stages.
 - Encoding of the operands, calculation *per se* and response.
- General overview of the state of the art: progress and limitations.

Foundations of arithmetic thinking

- **The Number Sense** (*Dantzig, 1967; Dehaene, 1999*)
 - Similar to the intuitions we have for time and space.
 - Spatially organized representation: *mental number line* (*Galton, 1881; Dehaene et al. 1993*).

Number discrimination in babies

(*Izard et al., 2009*)



Democratic decisions in baboons

(*Piantadosi & Cantlon, 2017*)

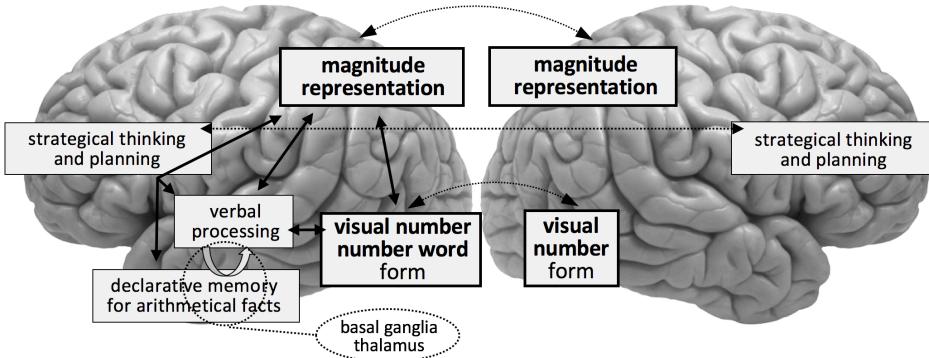


- **Evolutionary origin:** protect cubs, select preys, mating, etc.
- **Biological origin:** neurons tuned to numerosity in monkeys (*Nieder & Miller, 2004*).
Number network in monkeys and humans largely overlap in parietal and frontal areas.

Brain networks for arithmetic processing

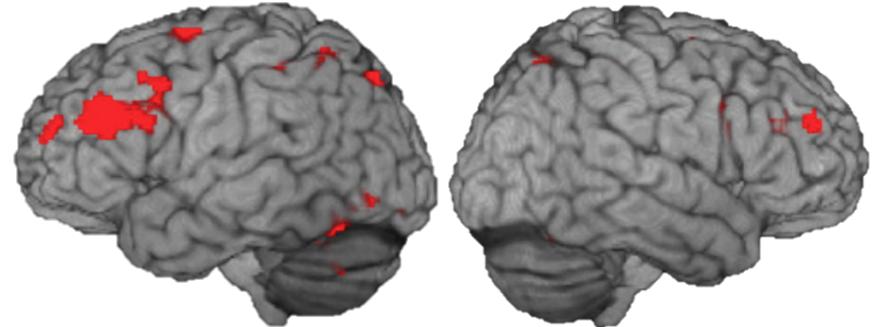
Putative network - neuropsychology

(Dehaene & Cohen, 1995)



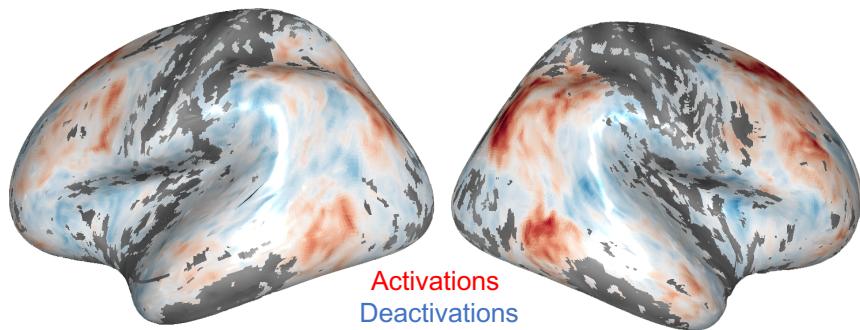
fMRI meta-analysis

(Arsalidou & Taylor, 2011)



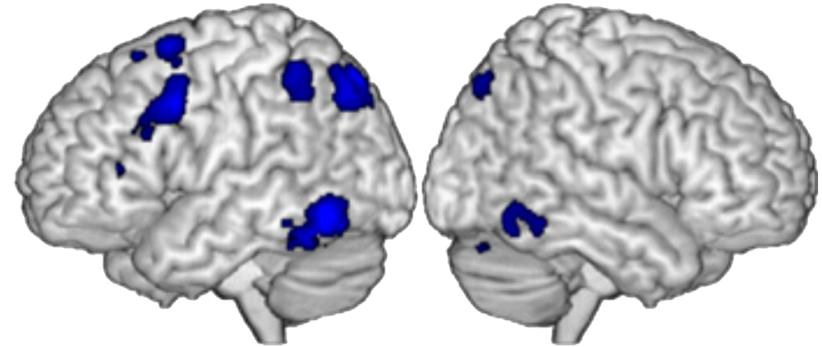
fMRI activations for number words in natural speech

(Huth et al., 2016)



Similar network engaged in high-level mathematics

(Amalric & Dehaene, 2016)



- Precise roles of each region and temporal dynamics still largely unknown.

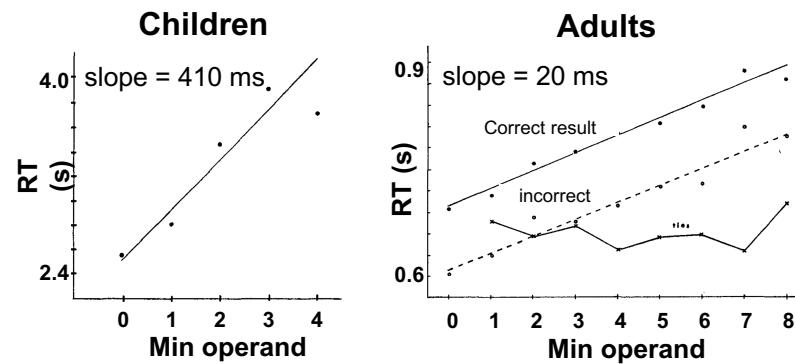
How does it work? Cognitive models of arithmetic:

- Problem-size effect: RTs increase as a function the size of the operands.

- The '*min*' counting model

(Groen & Parkman, 1972).

- *Min* operand best predictor of RT



- Fact retrieval models (Ashcraft, 1992, etc.)

- Commutativity - half of the table is memorized: L+S (Butterworth et al., 2001).

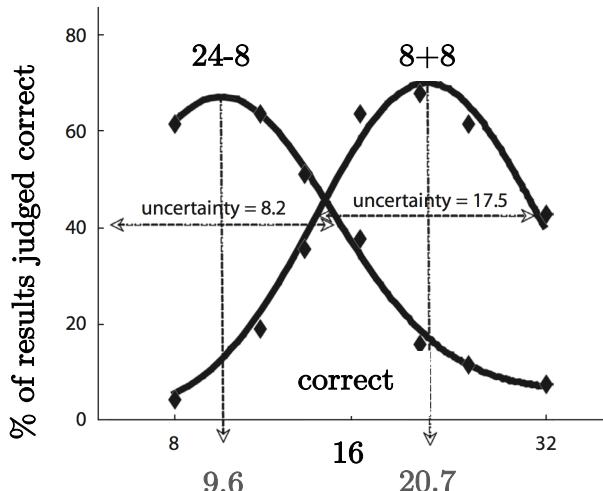
- Compact counting procedures

- Scrolling an ordered representation, such as the *mental number line*. (Barrouillet & Thevenot, 2013)

Calculation as '*movement*' along the mental number line

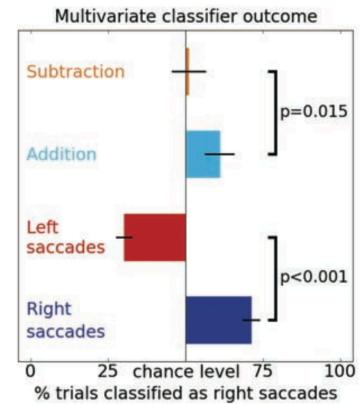
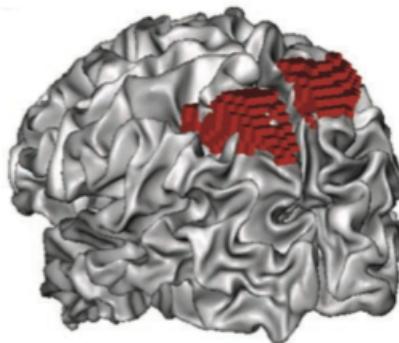
Operational Momentum effect

(McCrink et al., 2007)



- **Additions:** overestimated
- **Subtractions:** underestimated

Decoding left vs. right saccades generalizes to sub vs. add in pSPL
(Knops et al, 2009)



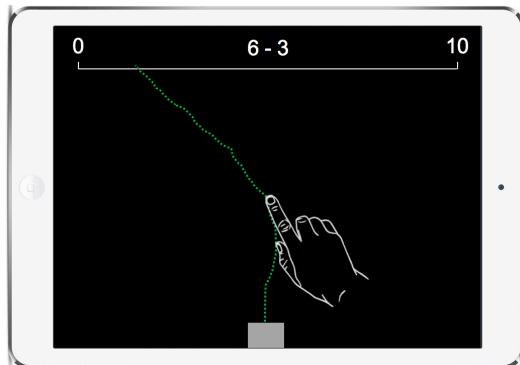
VIP-LIP vector addition for eye movement control
(Pouget, et al., 2002)

- Specific mechanism and temporal dynamics remain elusive.
During calculation or post-calculation?

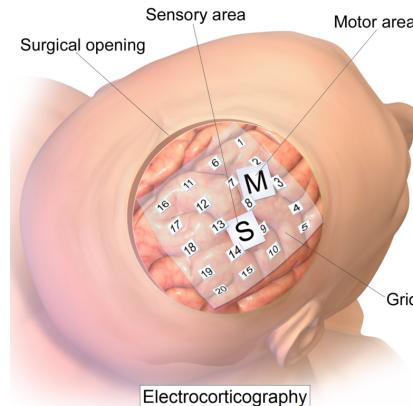
Experimental contributions

- Progress has been methodologically impeded by relying on:
Summary measures of the entire processing chain.
 - Mental chronometry: *blind to the absolute timing and order of the stages.*
 - fMRI: *low temporal resolution & relatively coarse functional specificity.*
- My approach, developed in 3 main studies:
 1. Dissect the covert stages of simple arithmetic.
 2. Re-evaluate the neural correlates of mental calculation.
 3. Decode the brain processes and underlying representational codes.

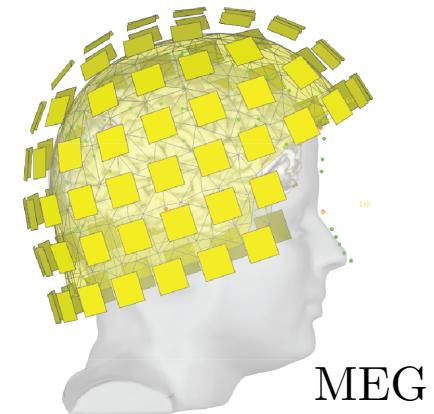
1. Finger-tracking



2. ECoG



3. Time-resolved MVPA



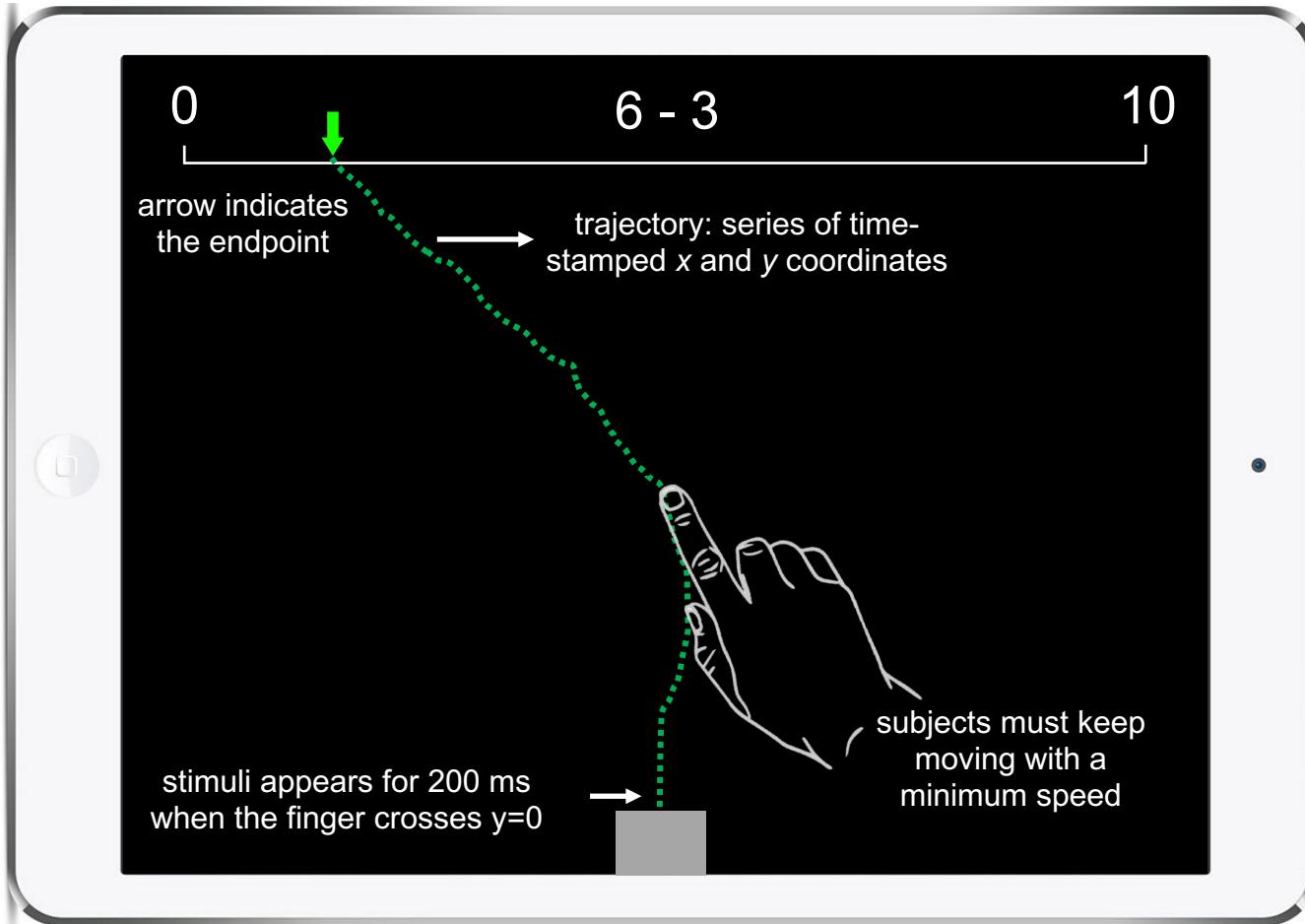
Chapter 2. Finger-tracking reveals the covert stages of mental arithmetic



Dror Dotan
Lecturer & finger-tracker
Tel Aviv University

Experimental Setup

30 adults, students, right-handed



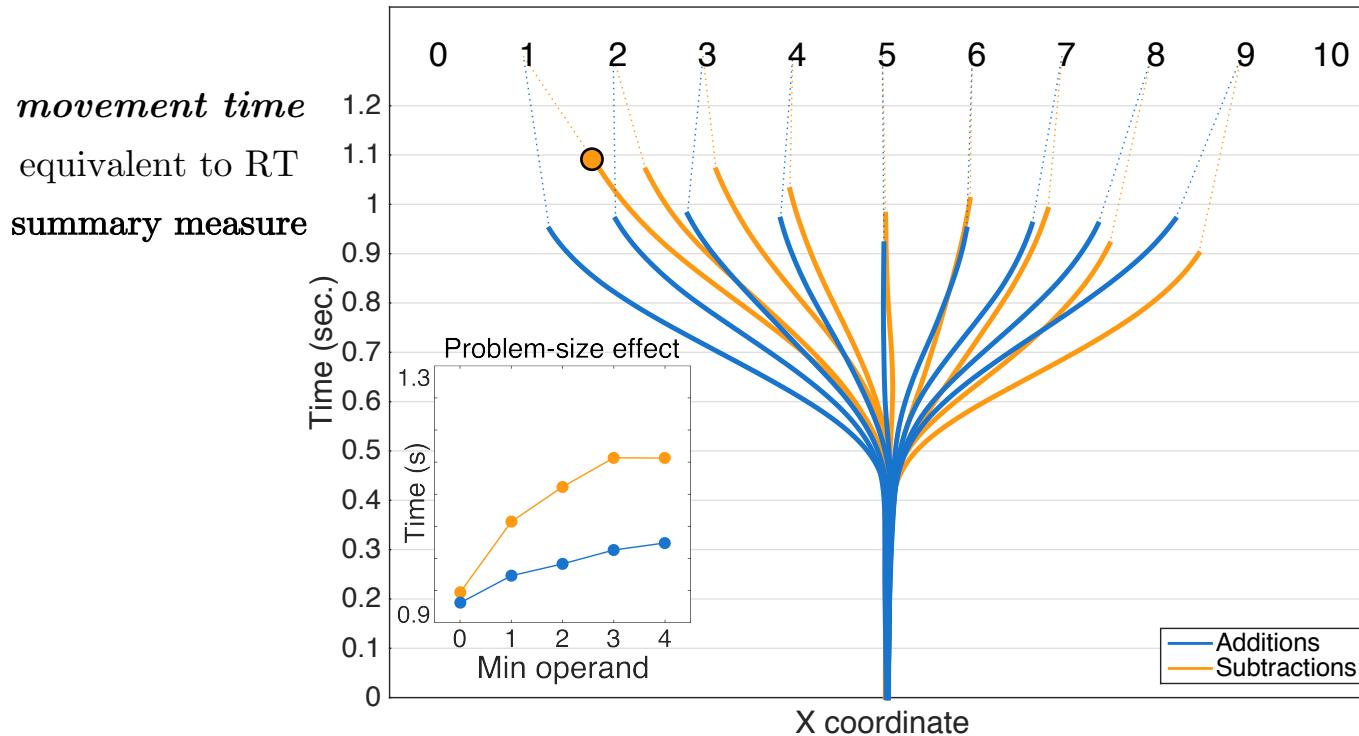
Assumption

*finger trajectories track the ongoing decision process
underlying a cognitive task*

Chapter 2. Finger-tracking reveals the covert stages of mental arithmetic

- Are the two operands processed serially or in parallel?
- Is there a stage whose duration increases linearly with the size of the numerical quantities, as implied by counting models?
- Can we determine the moment when the visuospatial biases underlying addition and subtraction occur?

Averaged trajectories by result

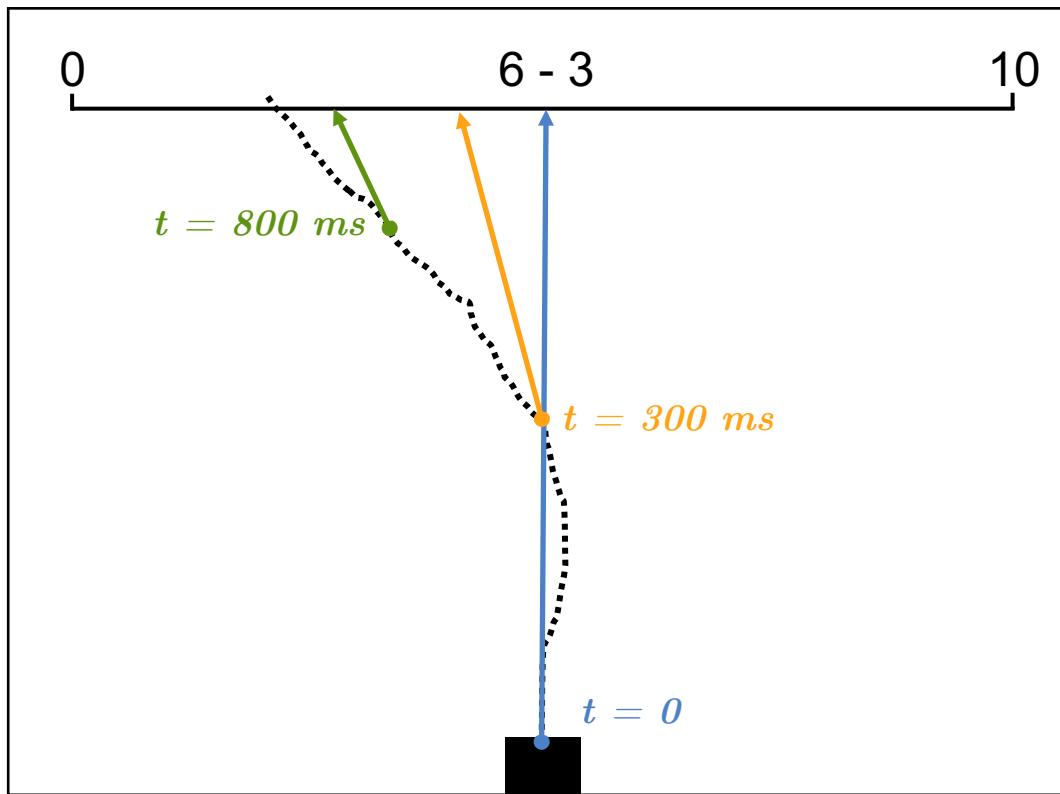


- The *min* operand is the best predictor of MT in additions & subtractions slope: 55 ms *sub*; 25 ms *add*; *Replicates Groen & Parkman (1972)*, etc.

Research in the past 40 years would stop at this stage to formulate cognitive models of arithmetic – problem-size effect

Decomposing the calculation task

Time-resolved multiple regression

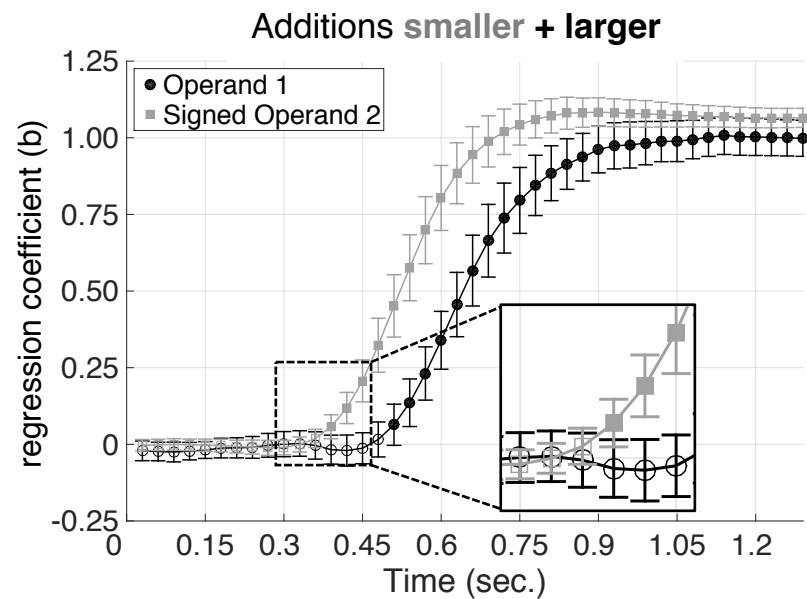
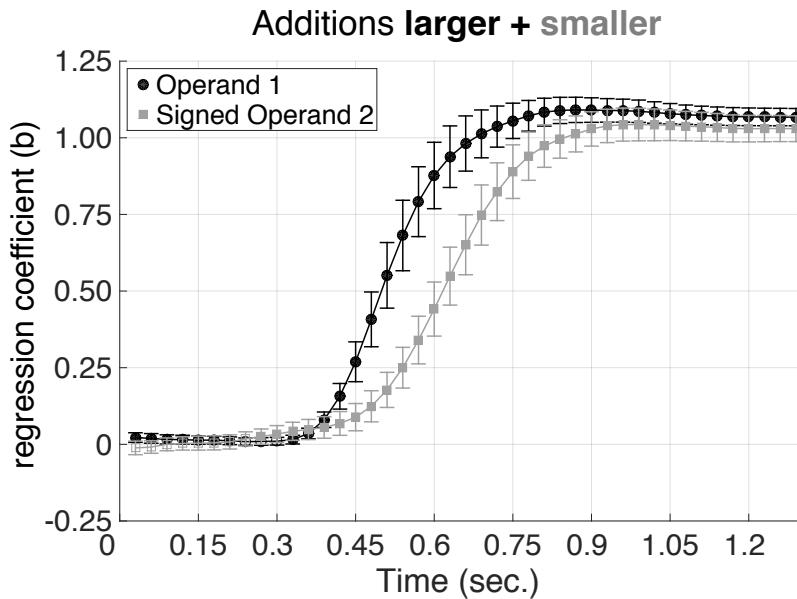


Implied endpoints: where the subject is aiming at each time t

- Multiple Regression at each time sample (30 ms), per subject.
 - *Dependent variable:* implied endpoint.
 - *Predictors:* operand 1, operand 2, operation, etc.

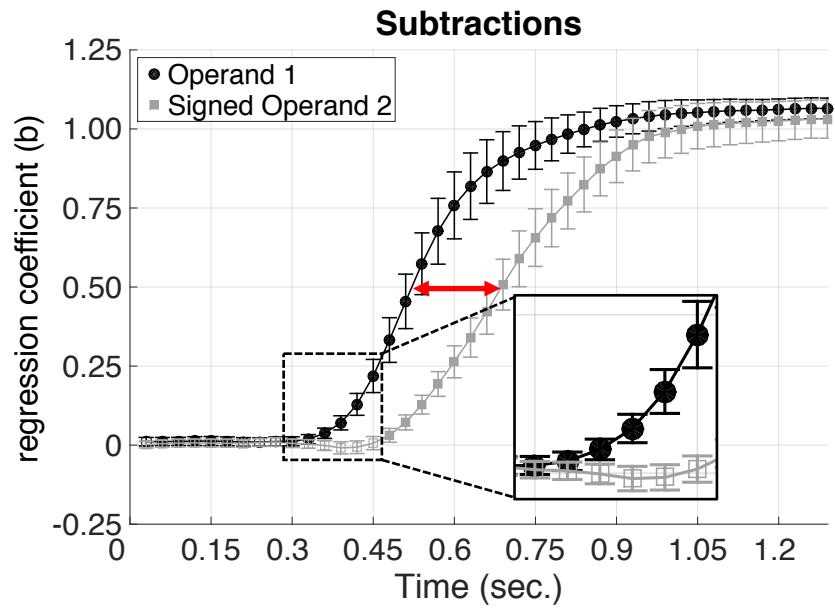
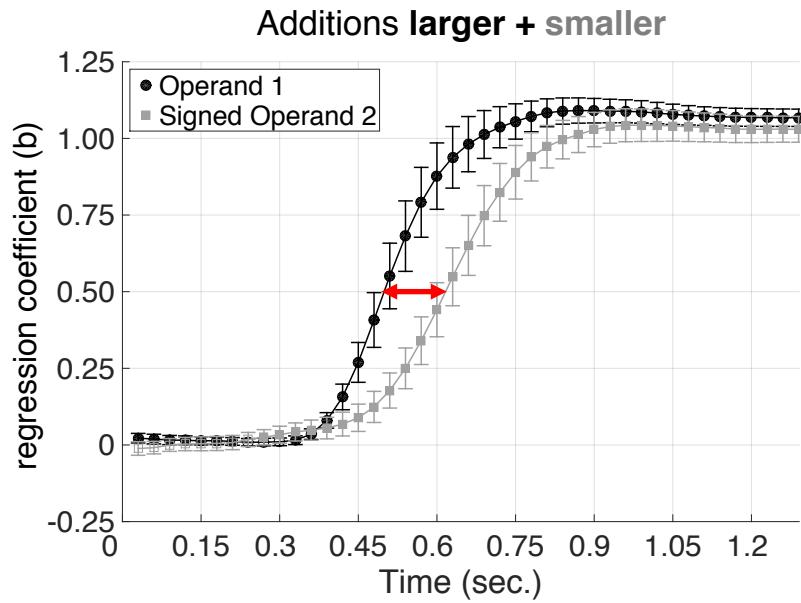
Are the operands processed
serially or in parallel?

Serial processing of the operands in additions

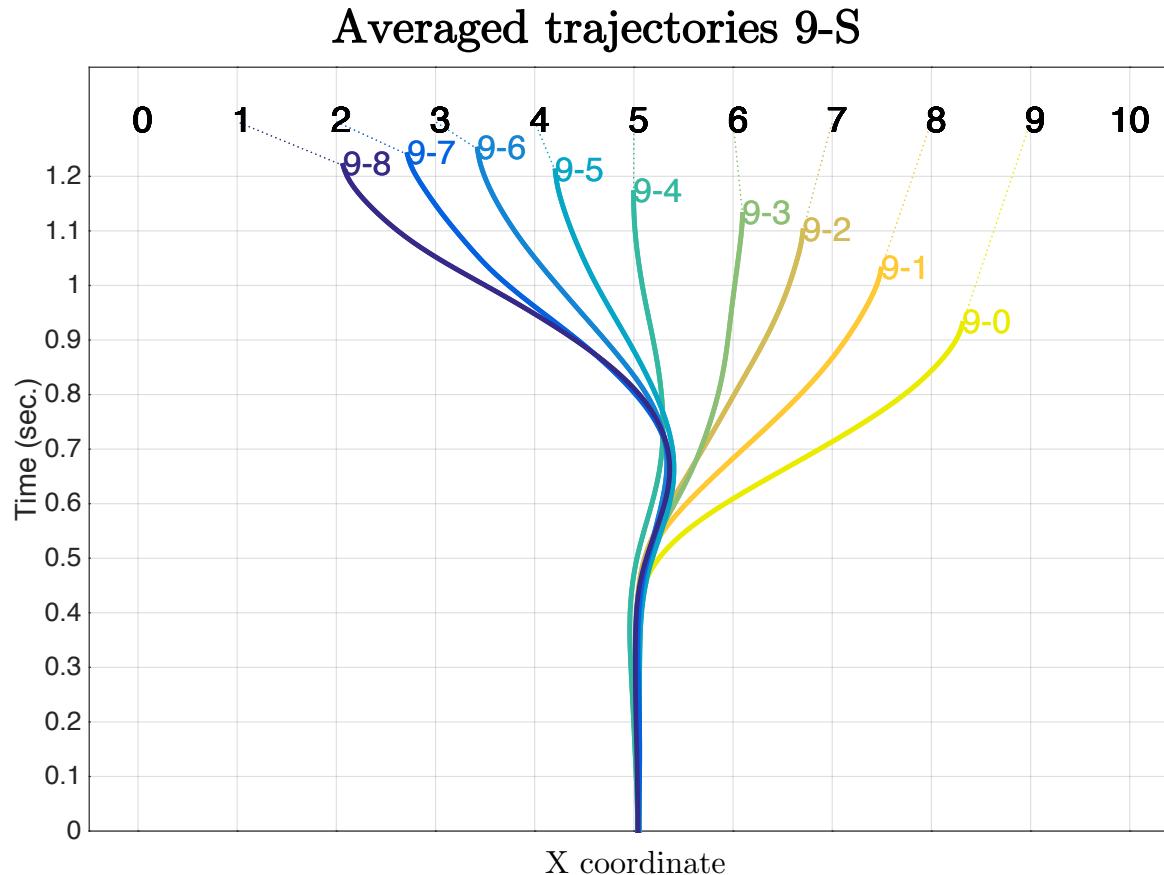


- **Reordering of the operands:** subjects first point to the larger operand irrespectively of the its location. *The effect is present in all 30 subjects.*
- Cost in MT of 14 ms on average. *Replicates (Butterworth et al., 2001).*

Higher serial processing of the operands in subtractions



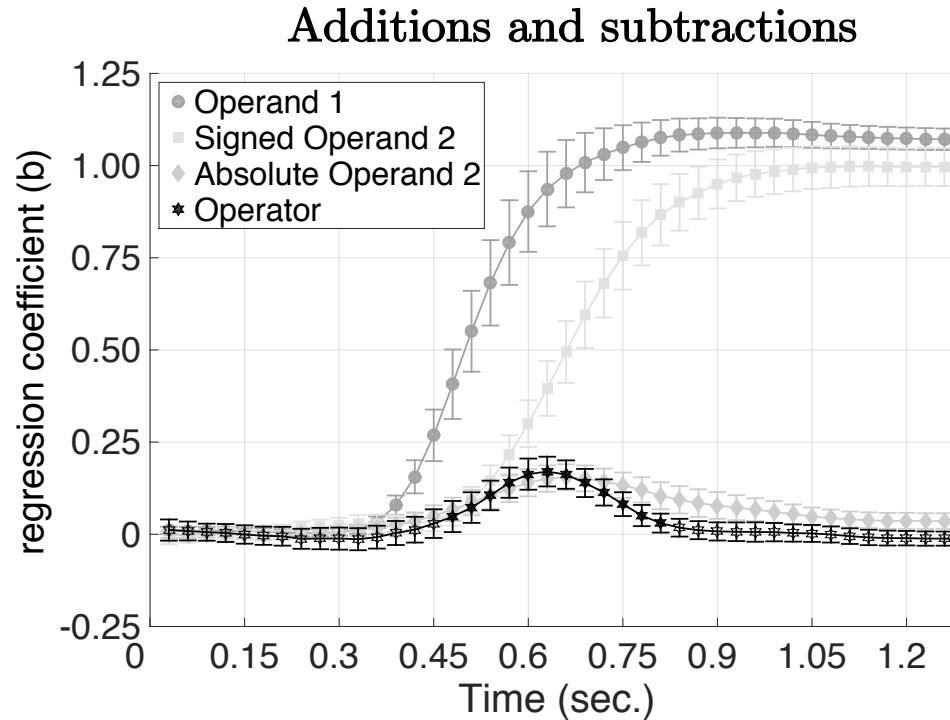
Direct visualization of the serial processing of the operands



- Subjects first point to the larger operand, then deviate to the correct result.
- Deviation unfolds **serially** and **proportionally** to the size of the *min* operand.
In both subtractions and additions (5-S, 5+S, etc.)
Passing through intermediate stages?

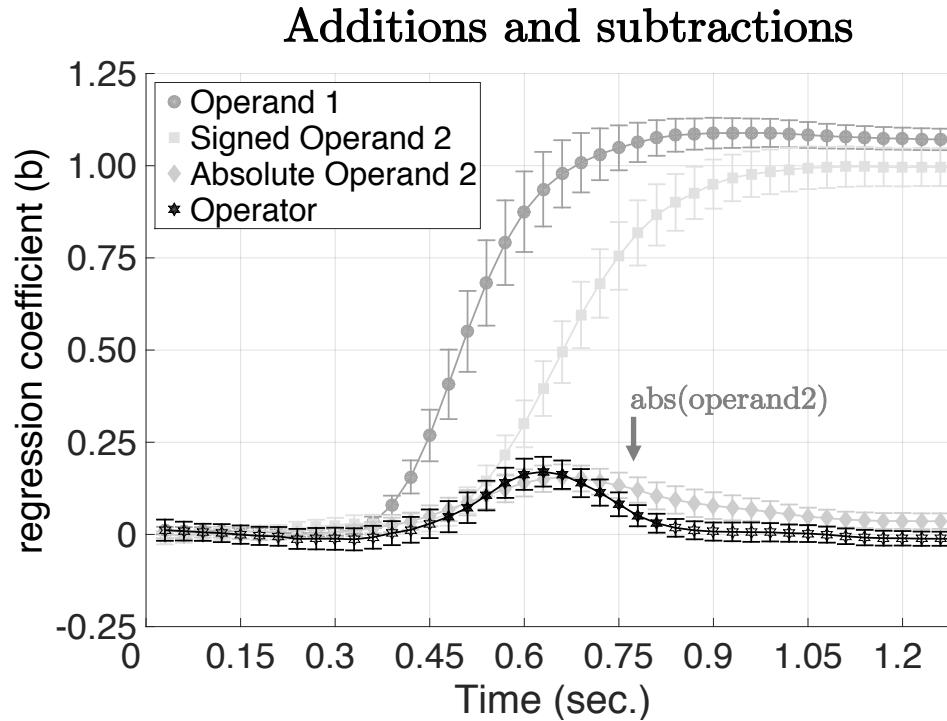
**What is the time-course of the visuospatial
biases in addition and subtraction?**

Transient OM effect at the time of processing the *min* operand



- + and – signs distort the finger to the right & left sides (larger & smaller numbers).
- *During calculation, not post-calculation.*

Transient activation of the absolute value of the subtrahend



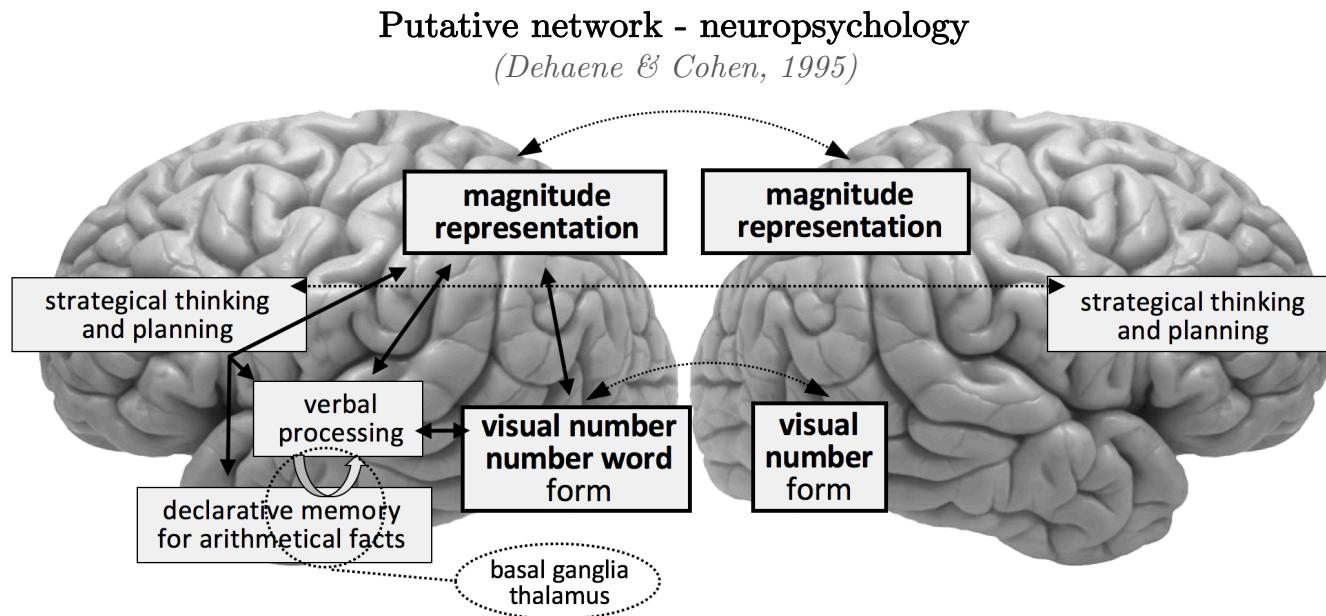
- Additional stage in subtraction: discard the absolute value of the *min.*

Chapter 2. Discussion and conclusions

- The **operands** are processed **serially**: larger operand first independent of its location: **direct visualization** of the **reordering effect** for additions S+L.
- The deviation from the larger operand to the correct result unfolds serially and **proportionally** to the **size** of the *min* operand (intermediate stages?).
- **Transient OM effect** at the time of the **integration of the min**: visuospatial attention system recruited during the calculation.
- Support for a model in which single-digit additions and subtractions are computed by a stepwise displacement on the mental number line.
Compatible with compact counting procedures & retrieval by tabular search.

What are the neural correlates?

Traditional view

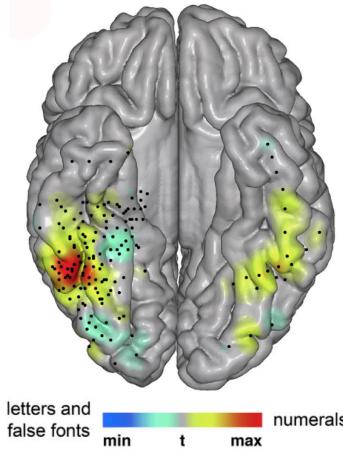


- **Lateral parietal cortex:** main hubs for magnitude processing and calculation. BOLD activity in the IPS and SPL increase as a function of problem-size.
(Dehaene et al., 1999; Kanjlia et al., 2016, etc.)
- **Ventral temporal cortex:** visual recognition of numerals ...

Arithmetic processing in the *ventral stream*

'Number Form Area' in the pITG

(Shum et al. 2013)

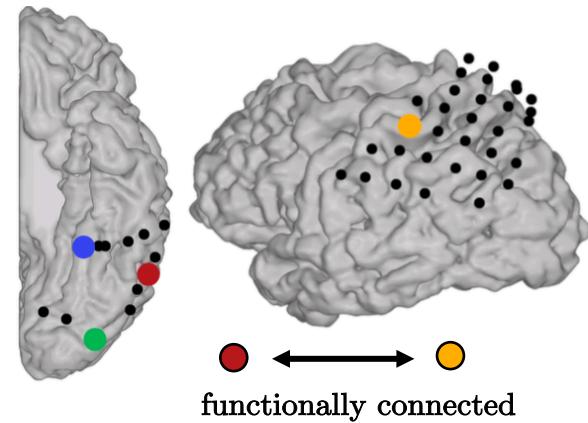
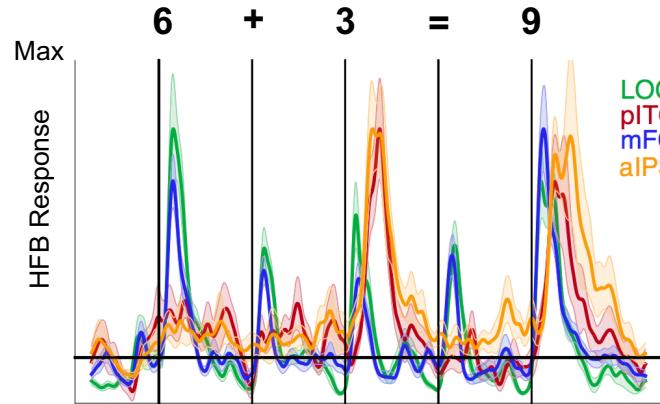
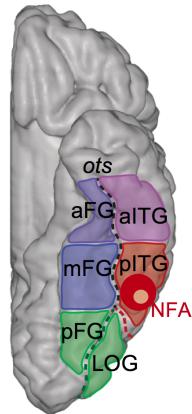


Two distinct neuronal populations in the pITG

(Daitch et al., 2016)

NFA: response to numerals
is *context independent*

Adjacent population – pITG_{math}:
response to numerals depends on *calculation*



Chapter 3. Brain mechanisms of arithmetic: a crucial role for ventral temporal cortex



Josef Parvizi



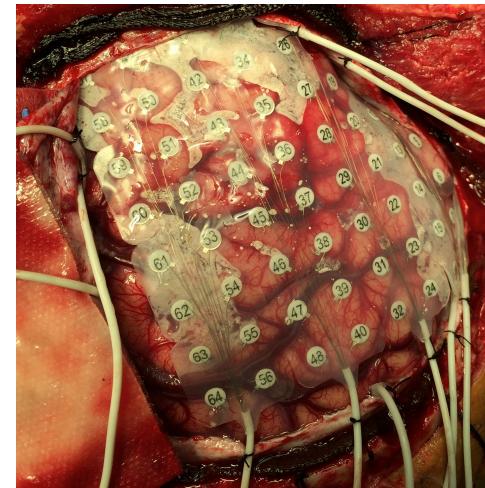
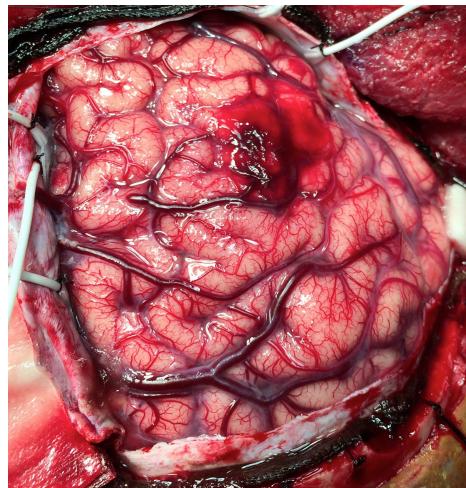
Amy Daitch



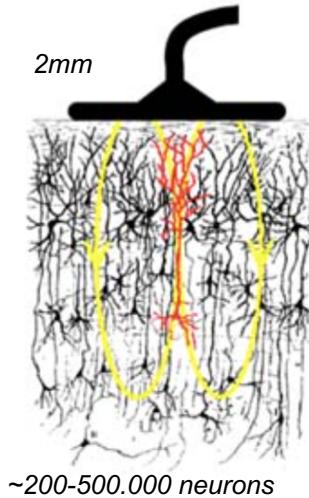
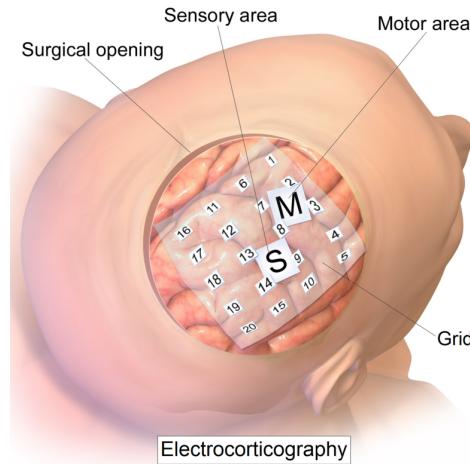
Chapter 3. Brain mechanisms of arithmetic: a crucial role for ventral temporal cortex

- Test if, how and when numerical features (*problem-size*) modulate the activity in calculation-selective neuronal populations in the LPC and VTC.
- Predictions:
 - IPS: parametrically increase of the activity with problem-size.
 - pITG: ?
 - If digit recognition only: early burst, constant for all problems.
 - If top-down attentional modulation– increase with problem-size.
 - Unpredicted role in calculation?

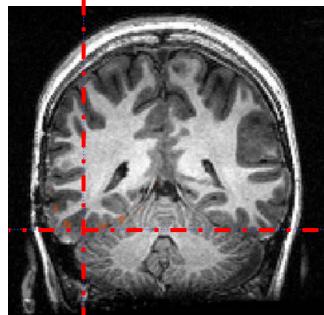
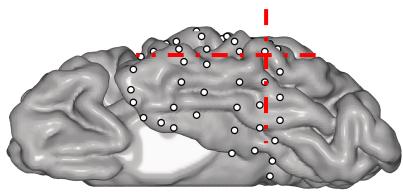
Electrocorticography (ECoG)



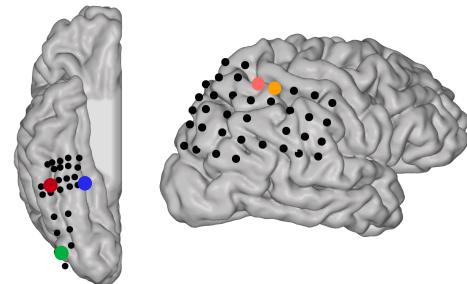
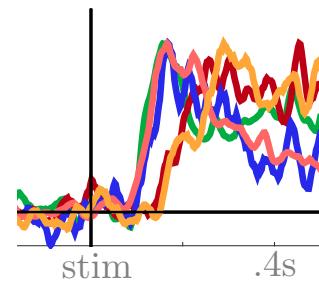
EEG (Electrocorticography)



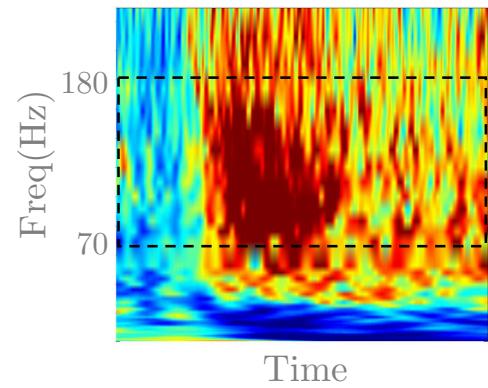
High spatial precision



High temporal resolution

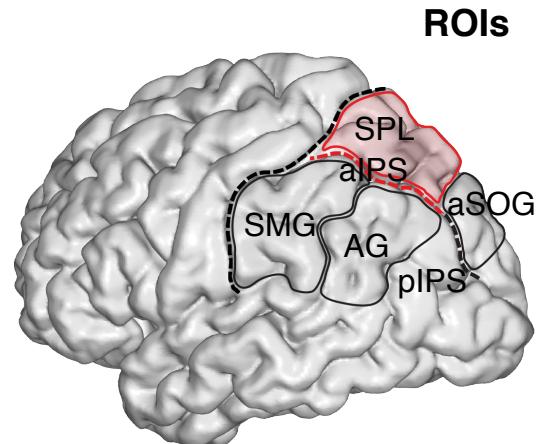


Rich frequency content

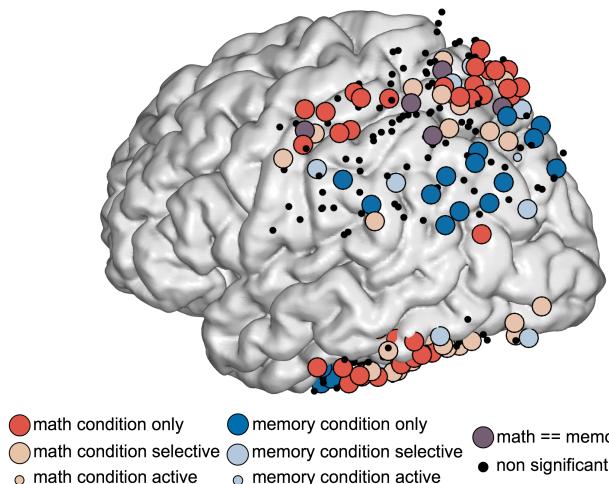


Task, ROIs, selectivity and problem-size effect

10 subjects with coverage in VTC and LPC



Channel selectivity



All sites from all subjects projected into a single left hemisphere

Math

$$13+5=17$$

80 trials
Min op: 1:9
Max op: 10:87

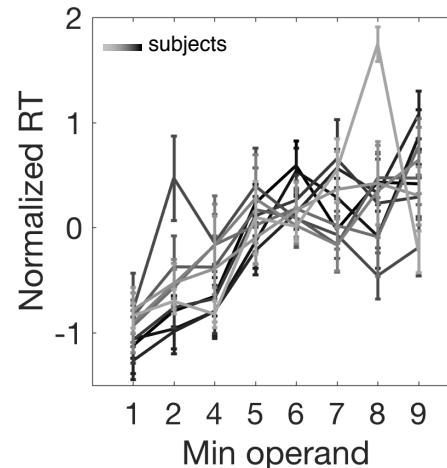
Memory

$$\text{I ate fruit today}$$

control
sentence comprehension
50 trials

◆-----◆ RT
Self-paced
ITI 200 ms

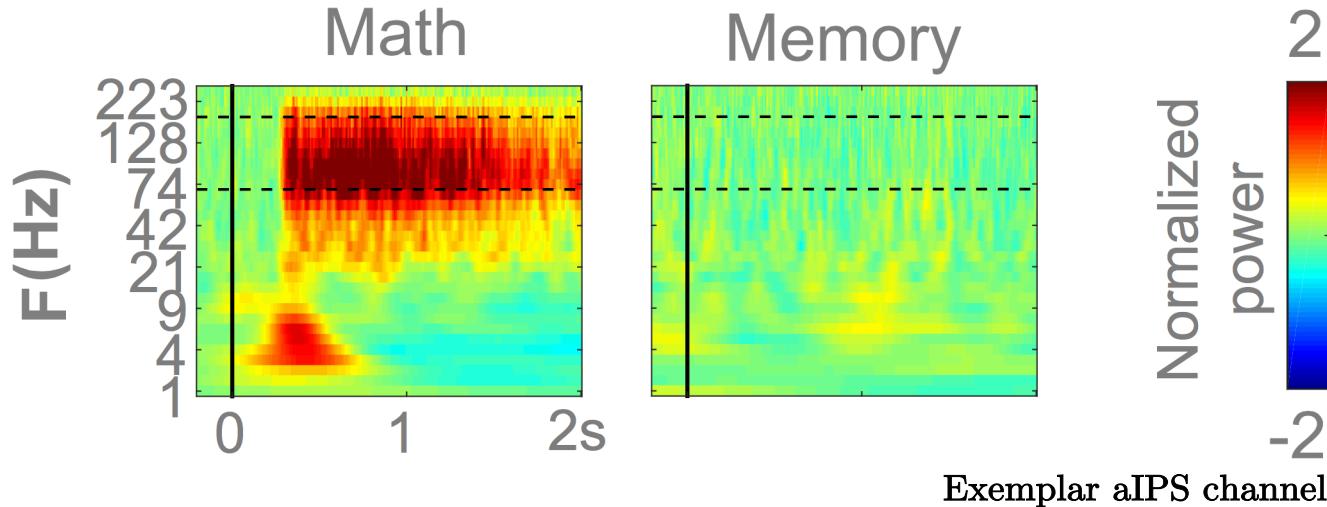
Problem-size effect



Best predictor of RT in 9/10 subjects

High frequency broadband (HFB): 70–180 Hz

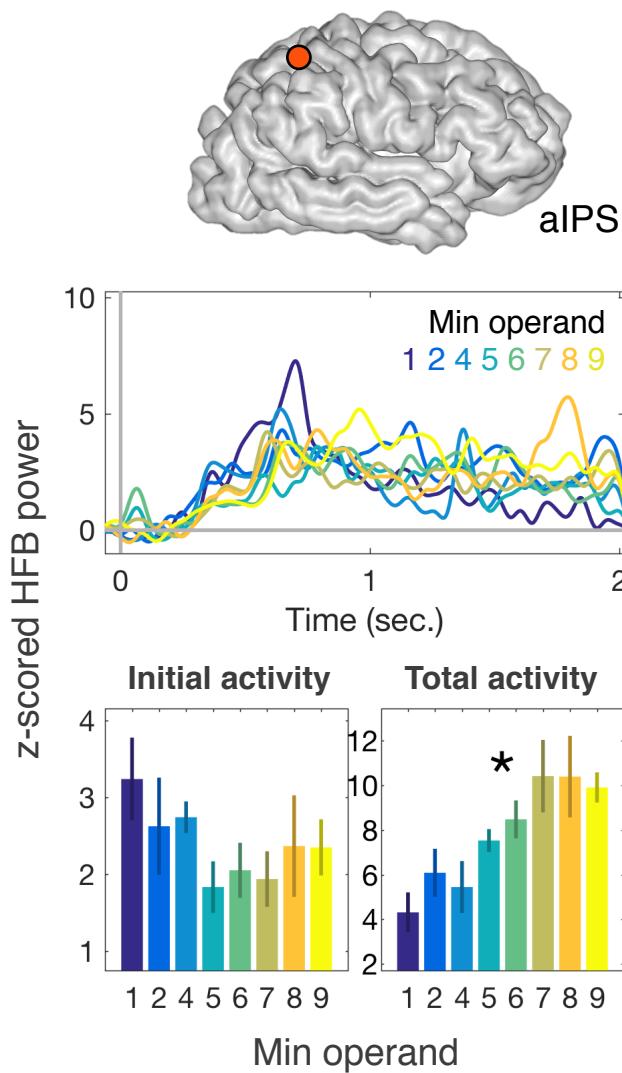
high correlations with local spiking activity and the fMRI BOLD signal



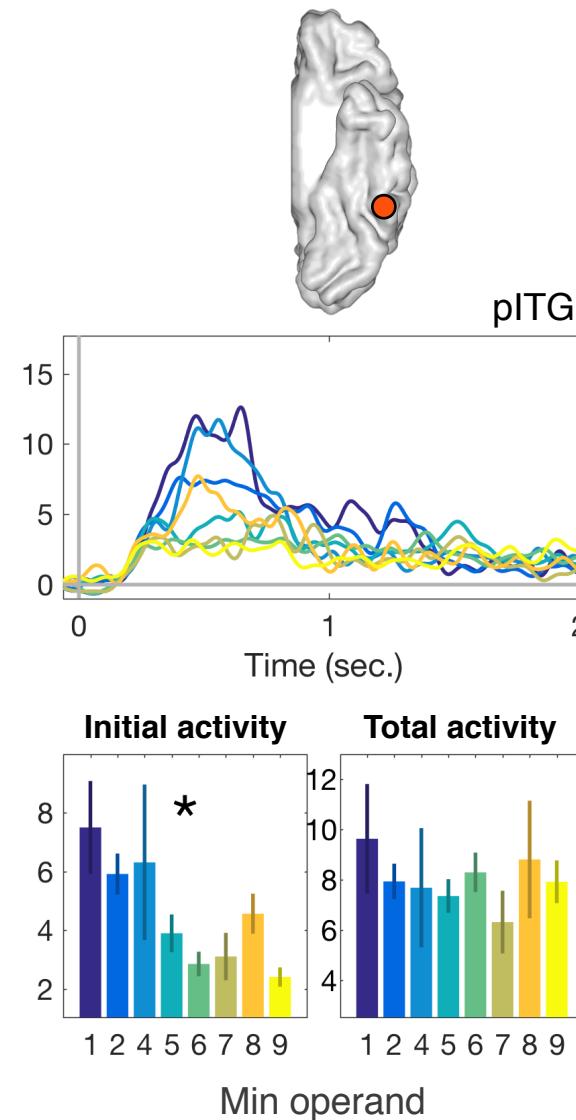
Two time windows:

- **initial activity : 1st second**
averaged over the 1st second, when greatest increase in activity occurs.
- **total activity: integral**
integral of the activity from trial onset to response: equivalent to BOLD.

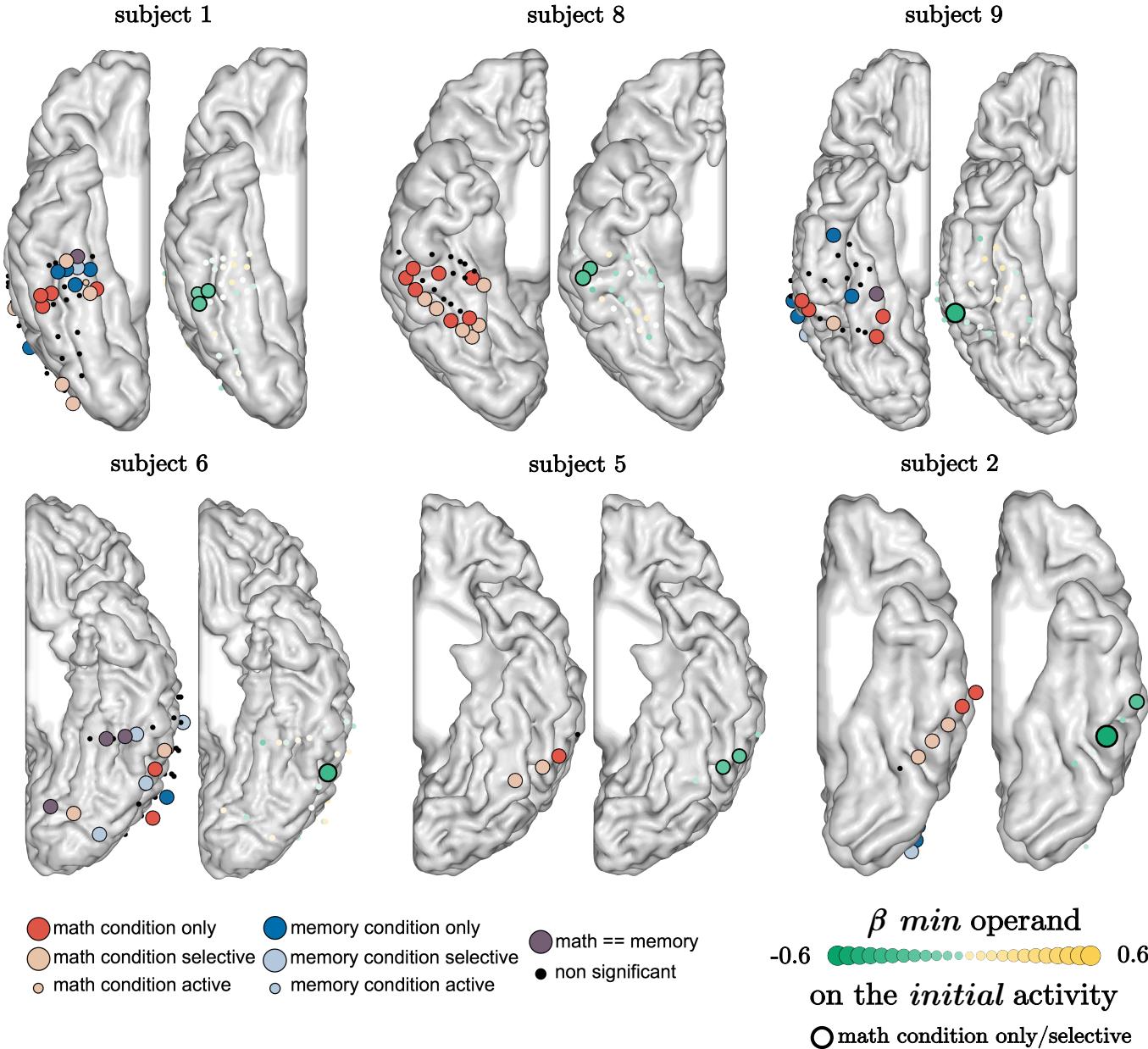
**Increased *total* activity by
min operand in aIPS and SPL**



**Decreased *initial* activity by
min operand in pITG**

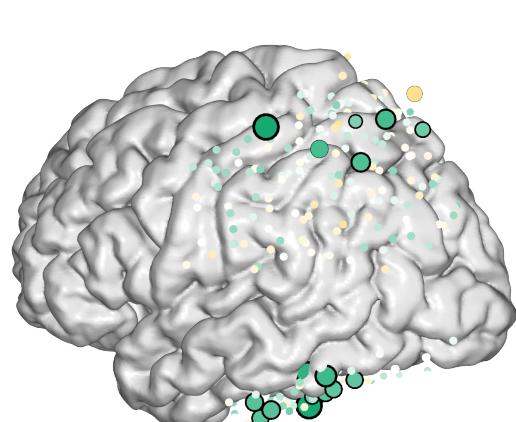


Anatomical and functional precision of the pITG modulation

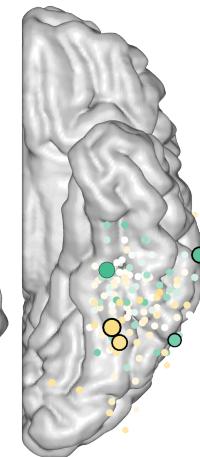
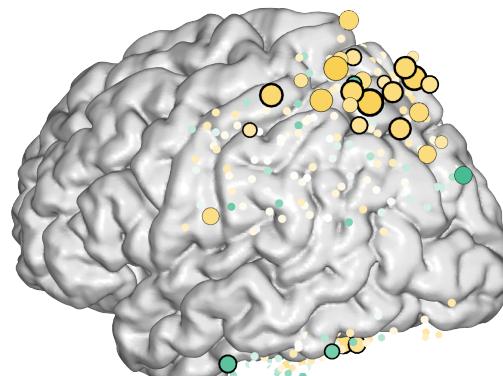
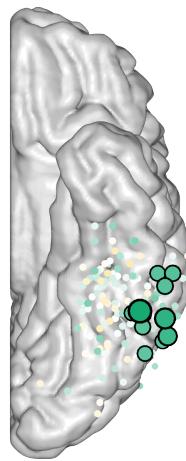


Effect of the *min* operand on the:

initial activity



total activity



increase
0.6

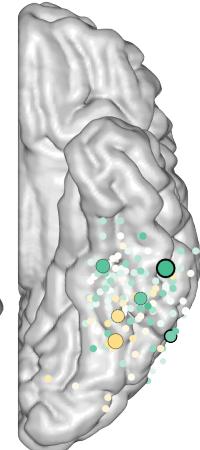
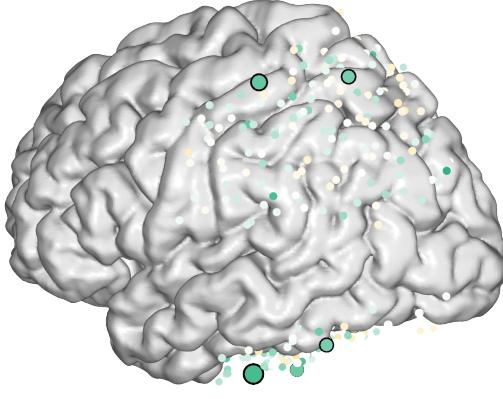
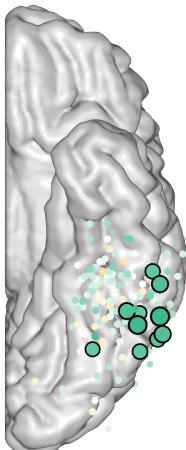
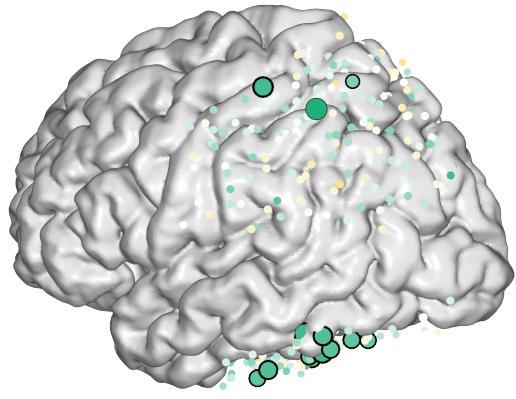
β

-0.6
decrease

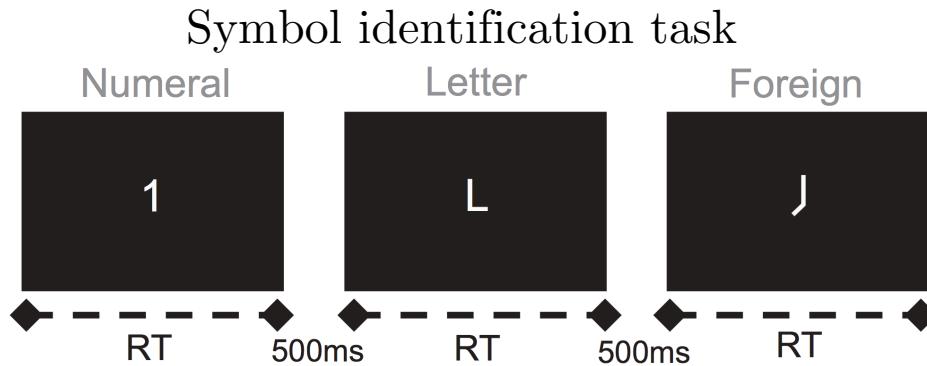
○ math selective

pITG 10 sites
6 subjects

Effect of min operand controlled by RT



Modulation of pITG does not reflect tuning to digits



Subject	Hemi	Region	Numeral active	Numeral selective	Modulation by numeral
S1	R	pITG	✓	-	-
S1	R	pITG	✓	-	-
S1	R	pITG	-	-	-
S2	L	pITG	✓	-	-
S2	L	aITG	-	-	-
S5	L	pITG	✓	-	-
S5	L	pITG	✓	-	-
S6	L	pITG	-	-	-
S8	R	pITG	✓	✓	-
S8	R	pITG	✓	-	-
S9	R	pITG	-	-	-

- 9/10 pITG sites are **not NFA**.
- pITG modulation is exclusive to the **calculation task**.

Chapter 3. Discussion and conclusions

- Modulation of aIPS and SPL corroborates previous fMRI findings.
Increased total activity as a function of problem-size.
Constant initial activity; Slow and sustained – highly correlated with RT.
Calculation and accumulation of evidence to achieve a decision.
- Surprising role of pITG in mental arithmetic beyond digit recognition.
Decreased initial activity as a function of problem-size.
Constant total activity: blind to fMRI.; Fast - not correlated with RT.
Early identification of problem difficulty (amount of semantic evidence?).
- Re-evaluation of neurocognitive models of arithmetic and dyscalculia.
pITG as an **important hub** for **calculation**.
- **Expands the classical view of the VTC:** contains regions specifically involved in sophisticated symbolic forms of reasoning, such as mental arithmetic.

Chapter 4. Decoding the processing stages of mental arithmetic with MEG

- Lacking a comprehensive picture of the organization of the brain processes.
- Time-resolved multivariate pattern analysis applied to MEG.
- Can we decode the identity of the operands? Representational codes?
- Can we track in time the emergence of the internally computed result?
- Are the brain processes completely serial or do they partially overlap in a form of a cascade of computations that can be simultaneously decoded?

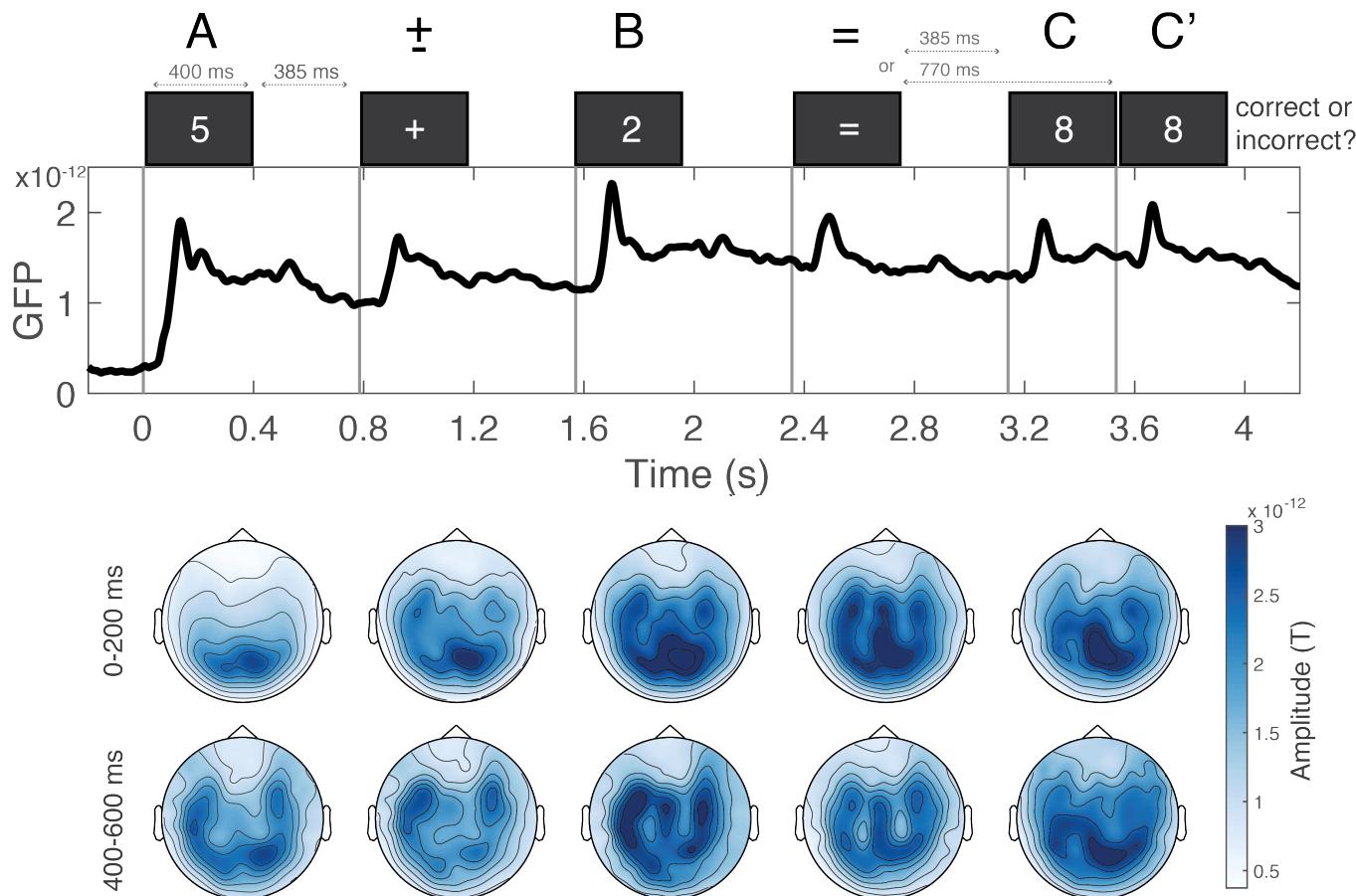
Experimental Design

20 adults, students, right-handed



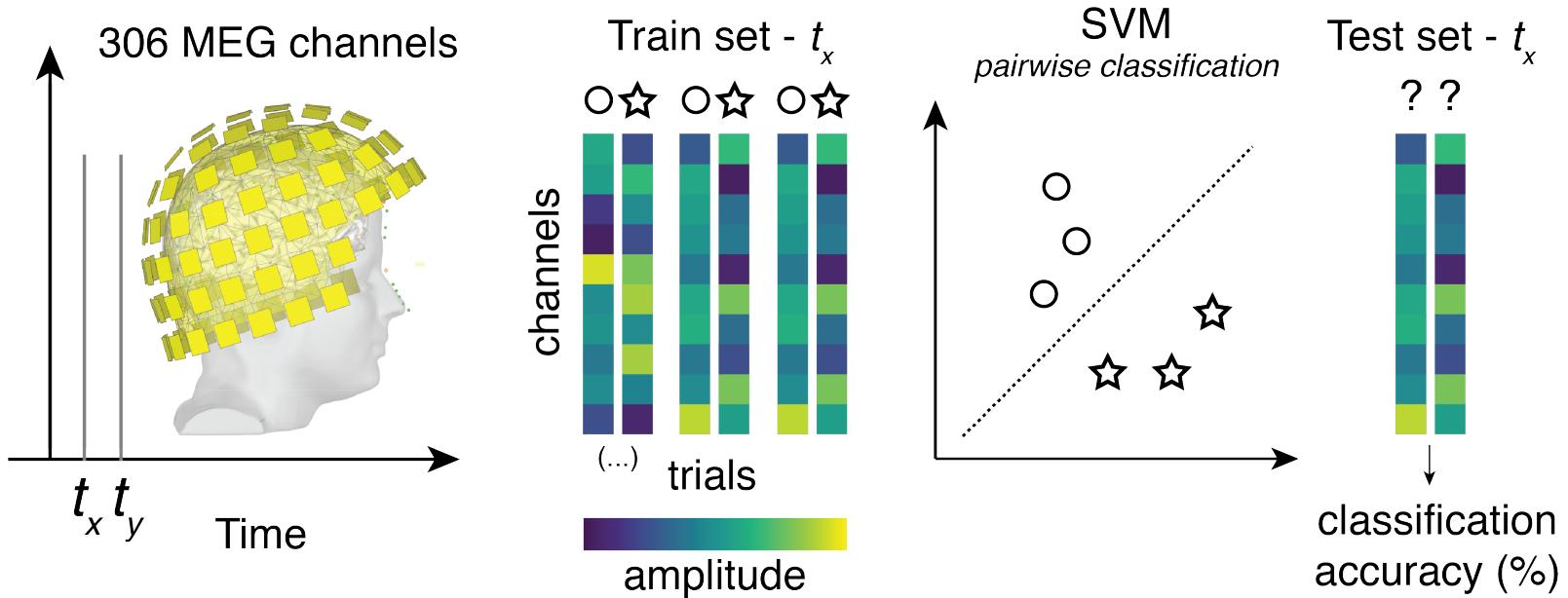
- A - max operand = 3, 4, 5, 6
- B - min operand = 0, 1, 2, 3
- Result = 0 – 9 (3, 4, 5, 6 - 50 trials each)
- C – proposed result = 0 – 9
50% incorrect (absolute distance: 1, 2, 3, 4)

Sustained activation from posterior to anterior sensors



- Apply time-resolved MPVA over the entire trial.

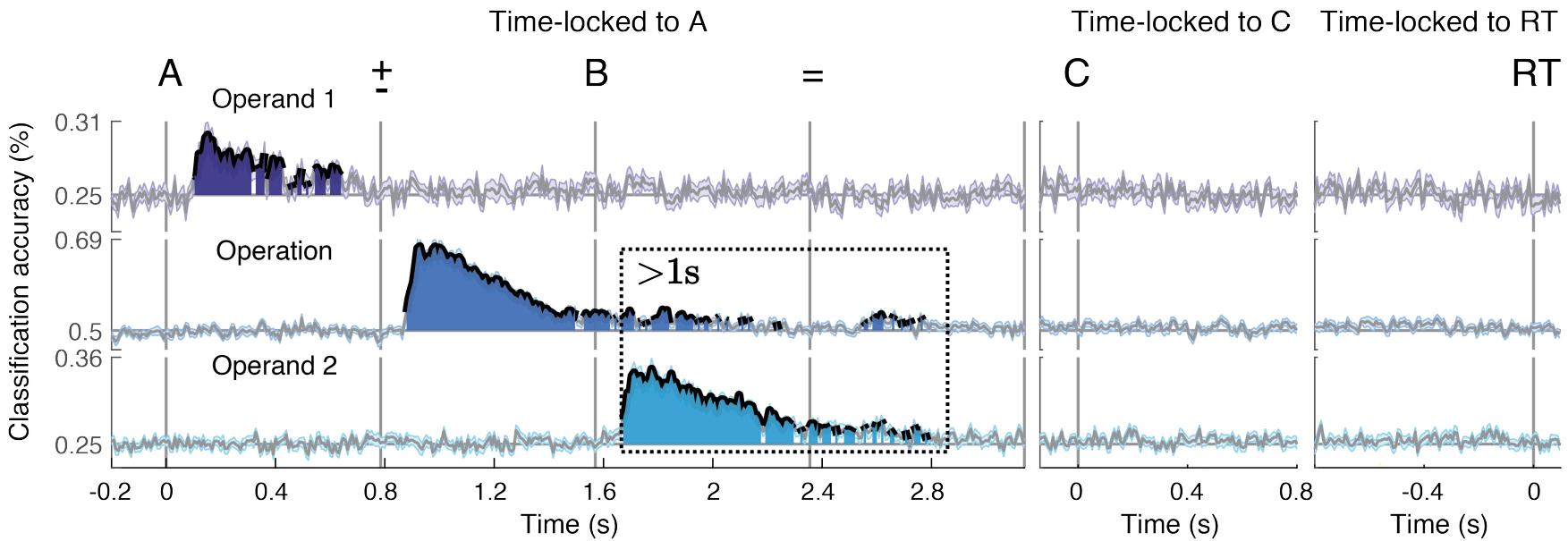
Time-resolved decoding



- The classifier is applied at each time sample t_x , t_y ... , per subject.
- Generalization across time - can the classifier trained at t_x generalize to t_y ?
Test how stable in time are the underlying codes.
- Generalization across conditions.
Test the existence of possible common codes.

(King & Dehaene, 2014)

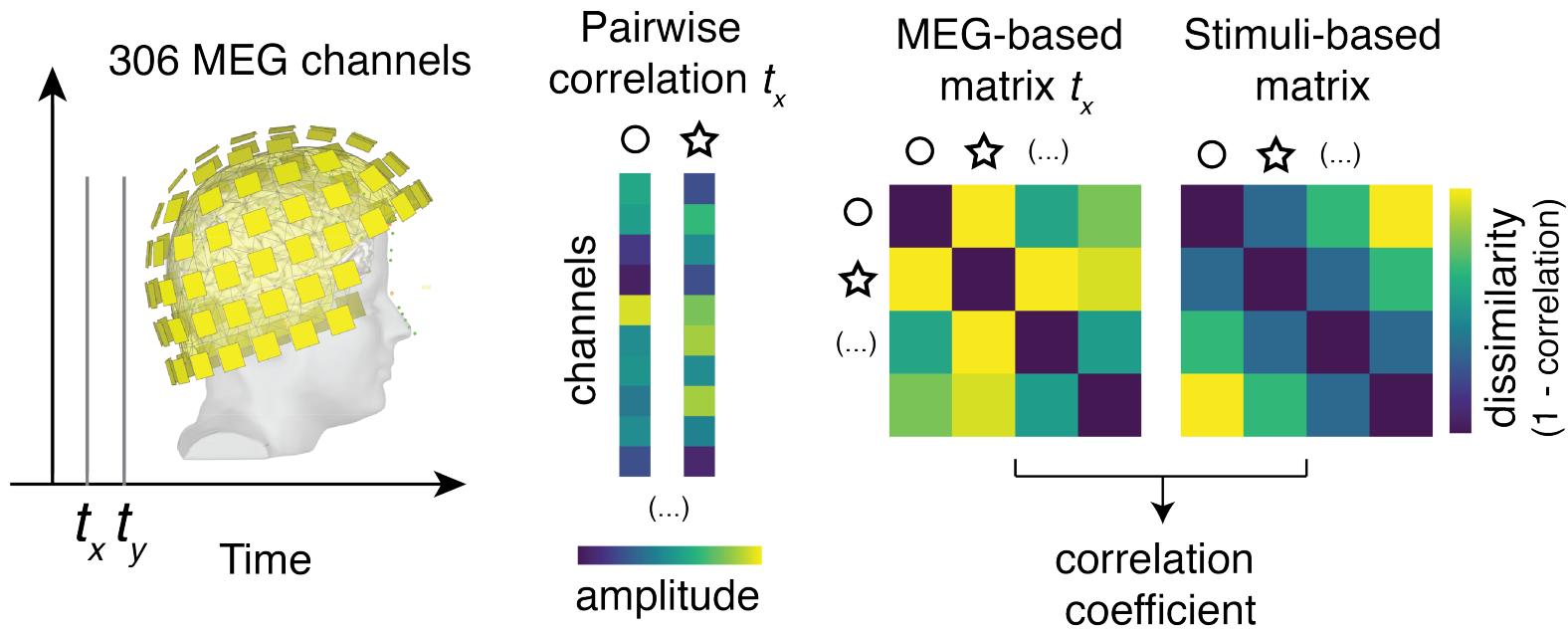
Decoding operands and operation



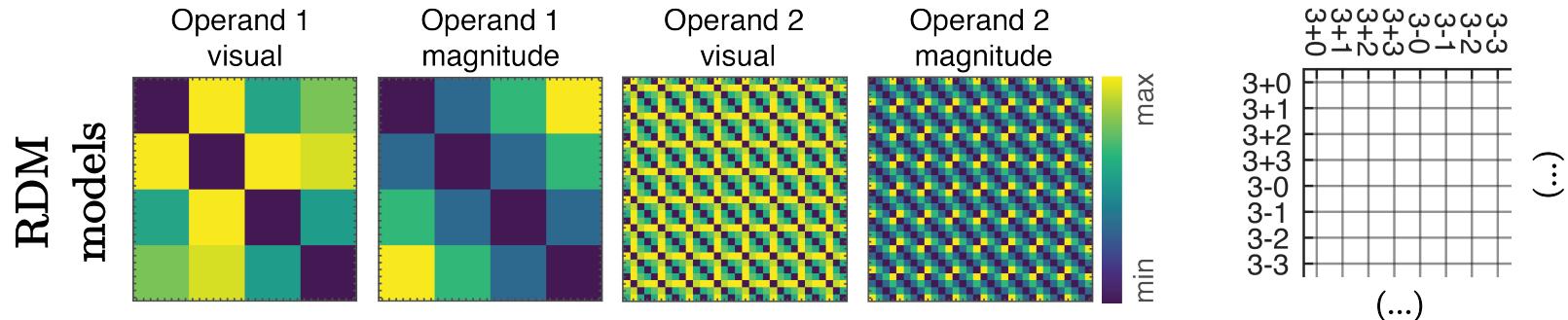
- **Operand 1:** transient, rapidly decreases after stim offset.
- **Operand 2:** higher accuracy and for a **longer** period – 1s.
- **Operation (*sub* vs. *add*):** sustained for 2s, rebound after equal sign.
- Long overlap between **operation** and **operand 2** – 1s.

Temporal dynamics of the representational codes?

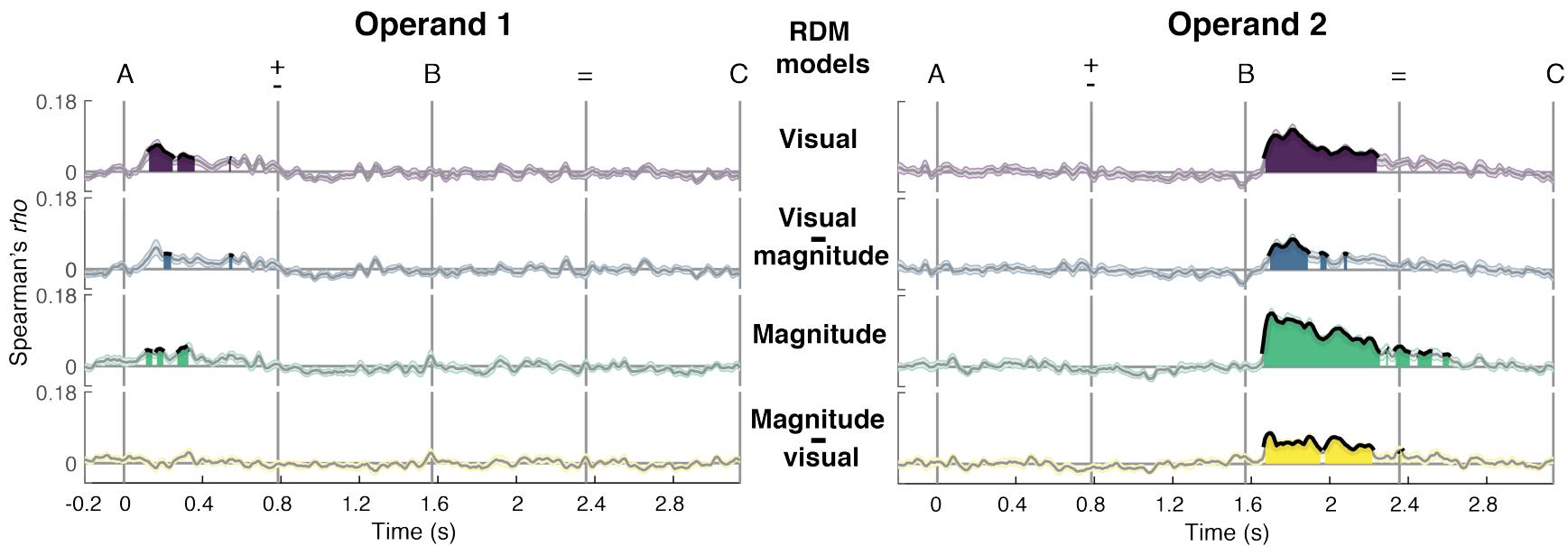
Time-resolved Representational Similarity Analysis



- The RSA is computed at each time sample $t_x, t_y \dots$, per subject.
- Simultaneously test the effect of different stimuli-based models.

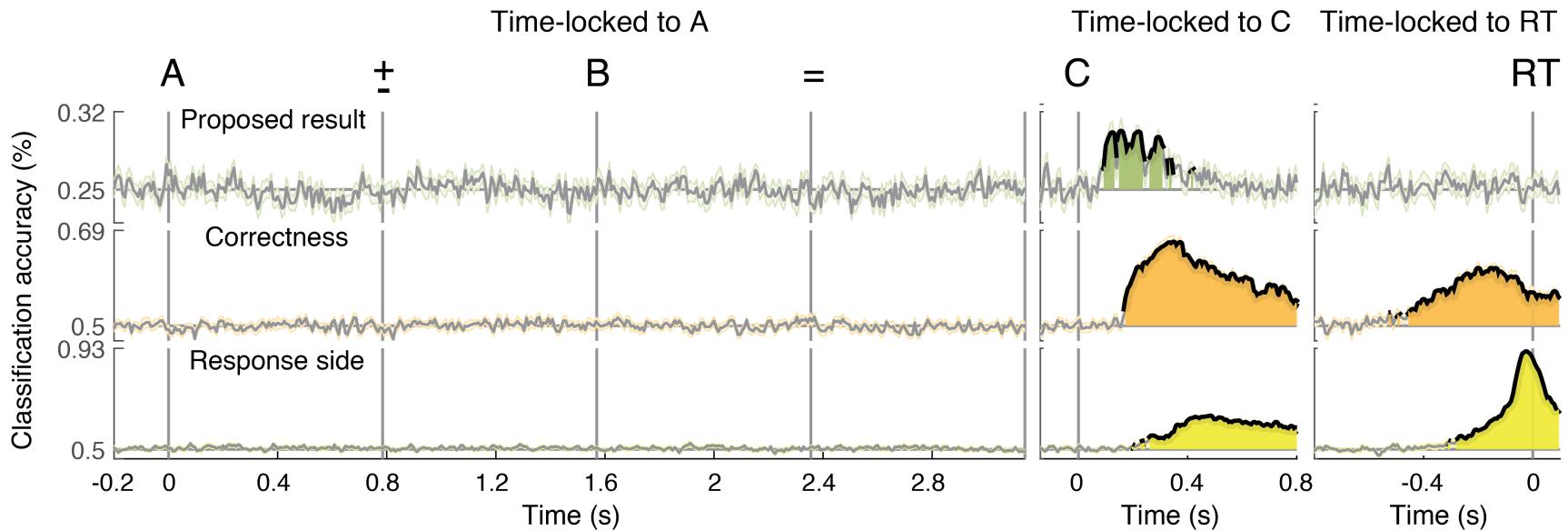


Representational geometries of the operands



- **Operand 1:** visual dimension is dominant.
- **Operand 2:** both visual and magnitude dimensions, **magnitude** dominant.
No precedence of the visual dimension.

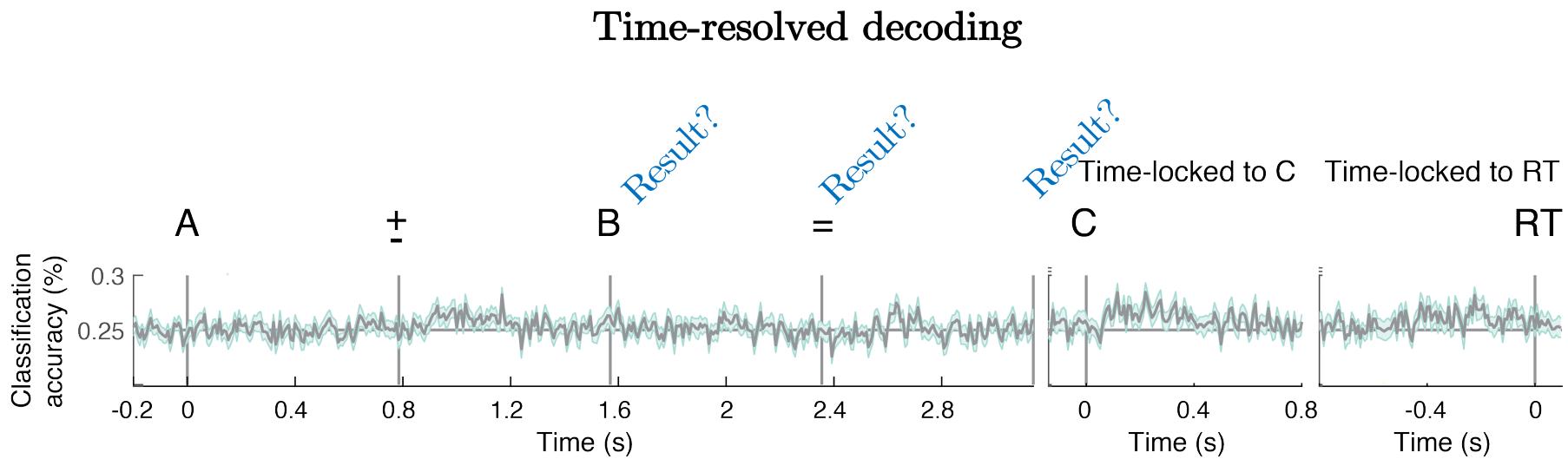
Highly overlapping dynamics at the decision stage



1. Identify the proposed result.
2. Judge whether it is correct or incorrect.
3. Press the response button.

Searching for a neural signature of the internally computed result

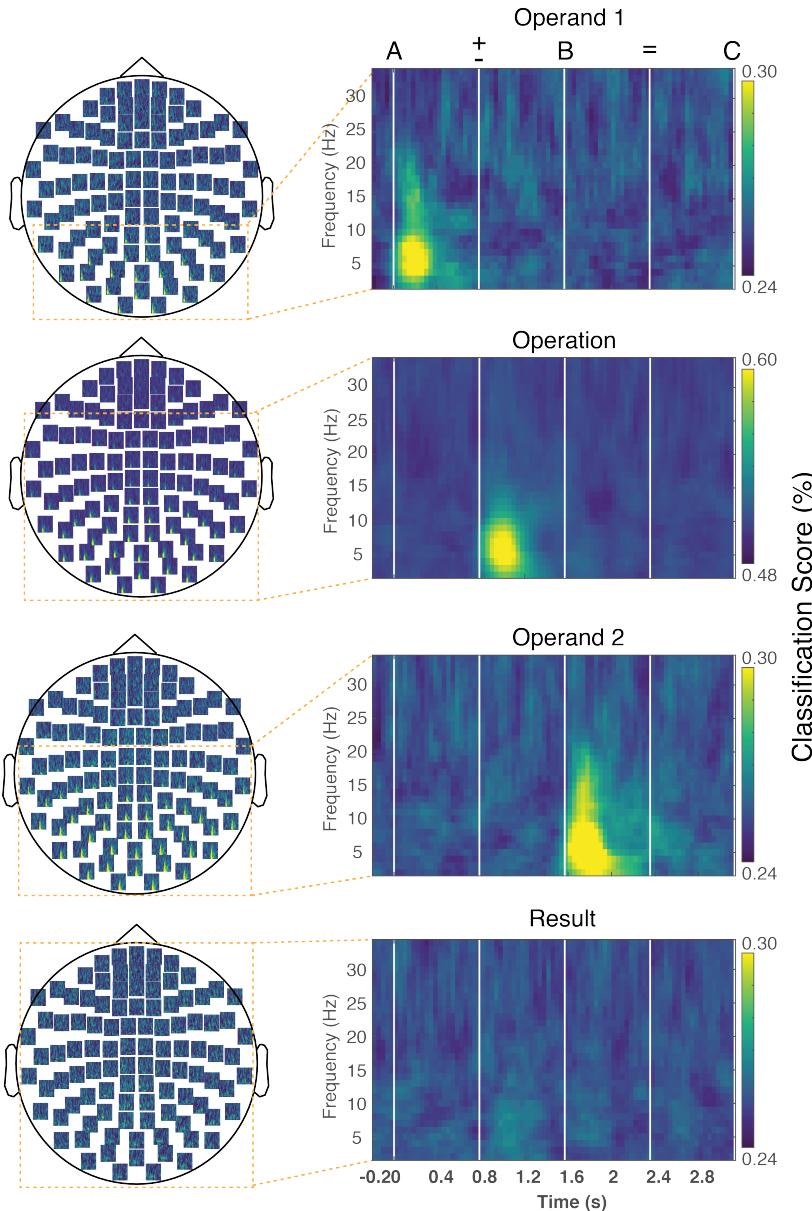
Several attempts, no success



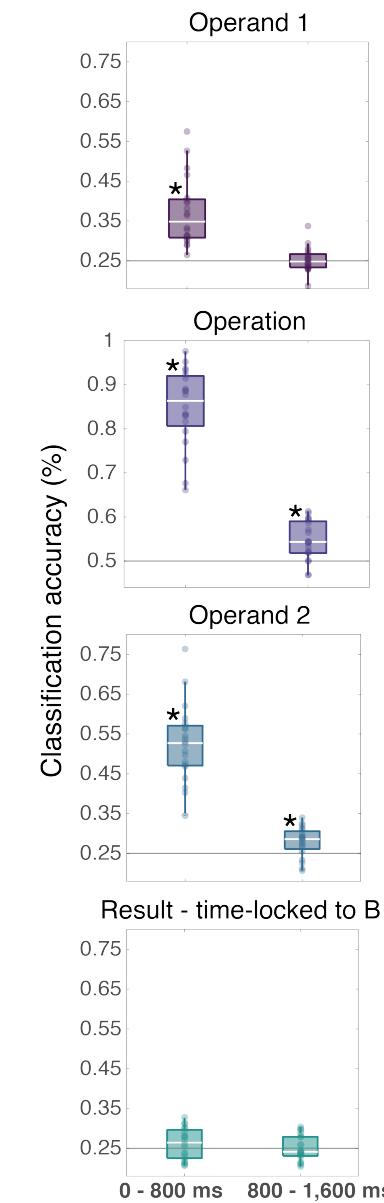
Searching for a neural signature of the internally computed result

Several attempts, no success

Searchlight LDA (sensor, time and frequency)



Riemannian Geometry (integrated over time)



Chapter 4. Discussion and conclusions

- First comprehensive picture of the unfolding processing stages underlying arithmetic calculations at a single-trial level.
- Decoding of **operand 1**: low, transient - **visual dimension**.
- Decoding **operand 2 (*min*)**: high, sustained - visual and **magnitude dimensions**; *Additional neuronal populations recruited in the VTC and LPC?*
- **Fast and highly overlapping dynamics** at the **decision stage**:
 1. Identify the proposed result.
 2. Judge whether it is correct or incorrect.
 3. Press the response button.
- **Inability to decode the internally computed result**
 - Externally and internally generated codes have different neural substrates.
 - Internally generated: rare gamma bursts, sparse code, '*silent states*'? *Hard to capture with MEG.*
 - Limitations of the design (n_{trials} , no time-stamping, etc.).

General conclusions and future directions

General conclusions and future directions

- Single-digit addition and subtraction rely on quantity manipulation:
 - Operands are processed serially: larger $>$ smaller.
 - Stepwise displacement on the mental number line.
 - *Precise mechanisms of the serial processing and learning?*
- Arithmetic is implemented in the dorsal and ventral pathways:
 - IPS and SPL: arithmetic computations and decision-making.
 - pITG: beyond digit recognition: **early identification of problem difficulty**.
 - *How do they interact? IPS integrates the activity of pITG? PFC?*
- Decoding the processing stages of mental calculation:
 - Cascade of highly dynamic and partially overlapping brain states.
 - Operand 1: visual; **Operand 2 (min)**: visual and **magnitude codes**.
 - *Temporal evolution from symbol to quantity?*
- Searching for neural signatures of the internally computed result:
 - Inability to decode with MEG.
 - *When and where is it generated?*
- Beyond numbers: the syntactic structure of arithmetic expressions

Stay tuned for the next articles

Pinheiro-Chagas, P., Dotan, D., Piazza, M., Dehaene, S. (*in preparation*).
Decomposing the syntactic structure of arithmetic expressions.

Dotan, D., Pinheiro-Chagas, P., Dehaene, S. (*in preparation*) Track it to crack it:
revealing the succession of processing stages with pointing trajectories.

Baek, S., Daitch, A., Pinheiro-Chagas, P., Parvizi, J. (*under revision*). Neuronal
population responses in the human ventral temporal and lateral parietal cortex during
arithmetic processing with digits and number words.

Other articles produced during the dissertation

Dresler, T., Bugden, S., Gouet, C., Lallier, M., Oliveira, D., **Pinheiro-Chagas, P.**, Pires, A., Wang, Y., Zugarramurdi, C., Weissheimer, J. (*under review*). Translational research in learning disabilities: the place of neuroimaging.

Borghesani*, V., de Hevia*, L., Viarouge*, A., **Pinheiro-Chagas, P.**, Eger, E., Piazza, M. (*under review*). Processing number and length in the parietal cortex: sharing resources, not a common code.

Pinheiro-Chagas, P.*, Dinino, D.*., Haase, V. G., Wood, G., Knops, A. (*in preparation*) The developmental trajectory of the operational momentum effect.

Borghesani*, V., de Hevia*, L., Viarouge*, A., **Pinheiro-Chagas, P.**, Eger, E., Piazza, M. (2016). Comparing magnitudes across dimensions: a univariate and multivariate approach. International Workshop on Pattern Recognition in Neuroimaging, 1-4.

Pinheiro-Chagas, P. Wood, G., Knops, A., Krinzinger, H., Lonnemann, J., Starling-Alves, I., Willmes, K., Haase, V. G. (2014). In how many ways is the approximate number system associated with exact calculation? *PLoS One*, 19, 9(11), e111155.

Carvalho, M. R., Vianna, G., Oliveira, L., Costa, A. J., **Pinheiro-Chagas, P.**, Sturzenecker, R., Zen, P. R., Rosa, R. F., de Aguiar, M. J., Haase, V. G. (2014). Are 22q11.2 distal deletions associated with math difficulties? *American Journal of Medical Genetics Part A*, 164A(9), 2256-62.

Haase, V. G., Júlio-Costa, A., Lopes-Silva, J. B., Starling-Alves, I., Antunes, A. M., **Pinheiro-Chagas, P.**, Wood, G. (2014). Contributions from specific and general factors to unique deficits: two cases of mathematics learning difficulties. *Frontiers in Psychology*, 13, 5-102.

Moura, R., Wood, G., **Pinheiro-Chagas, P.**, Lonnemann, J., Krinzinger, H., Willmes, K., Haase, V. G. (2013). Transcoding abilities in typical and atypical mathematics achievers: the role of working memory and procedural and lexical competencies. *Journal of Experimental Child Psychology*, 116(3), 707-27

* The authors equally contributed to the work

TrajTracker: track it to crack it

Platform for trajectory tracking experiments & data analysis

Home

Experiment

Paradigms

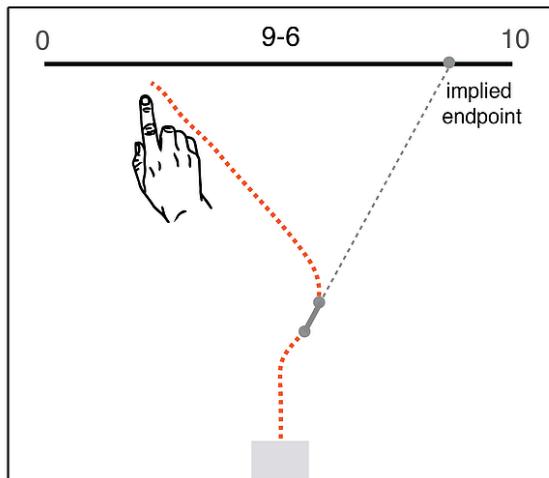
Analyze

About

TrajTracker Experiment 1.0 (beta version) is now released!

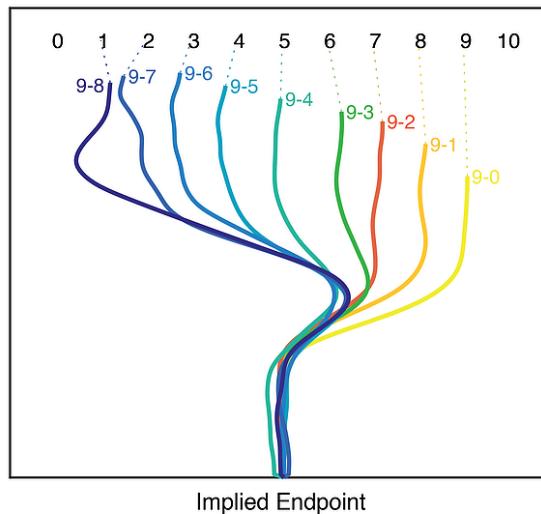
Android support will be available with the next release of [Expyriment](#) for Android.

Number-to-position mapping



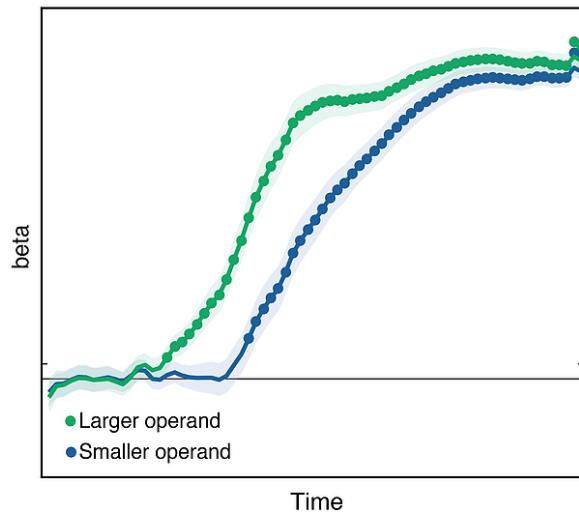
Point to the correct result on the number line

Averaged trajectories



Implied Endpoint

Time-resolved multiple regression



Time

tracking mental calculation online



TrajTracker is a software package for running and analyzing psychology experiments, focused on mouse/finger tracking experiments. New to trajectory tracking? Read about it [here](#).



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BETTENCOURT
SCHUELLER
FOUNDATION



Stan Dehaene
Collège de France; NeuroSpin



Manuela Piazza
University of Trento



Dror Dotan
Tel Aviv University



Amy Daitch
Stanford University



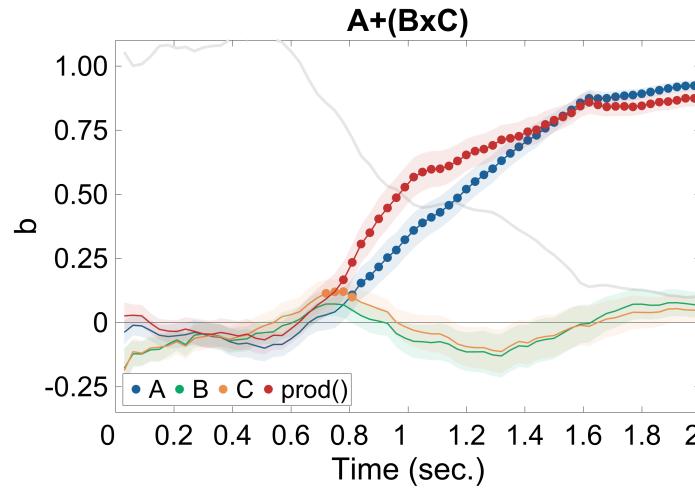
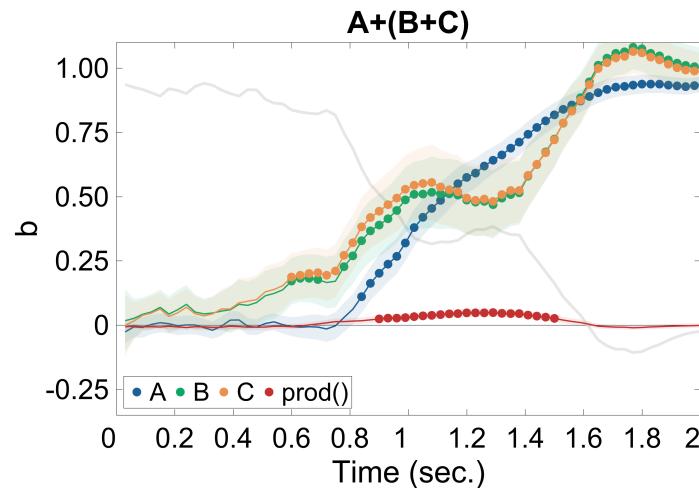
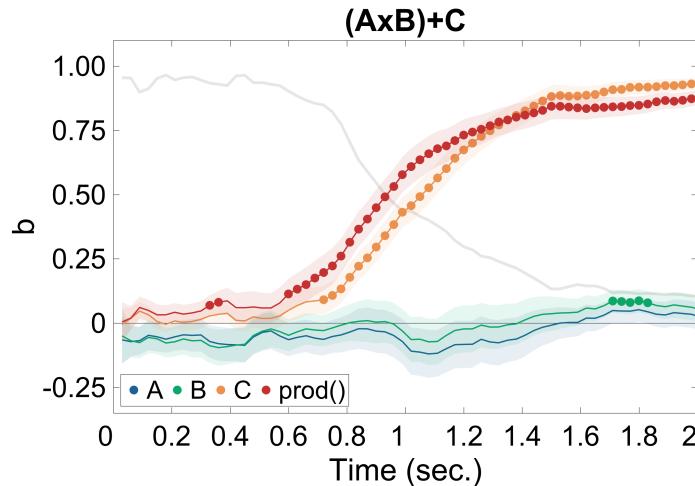
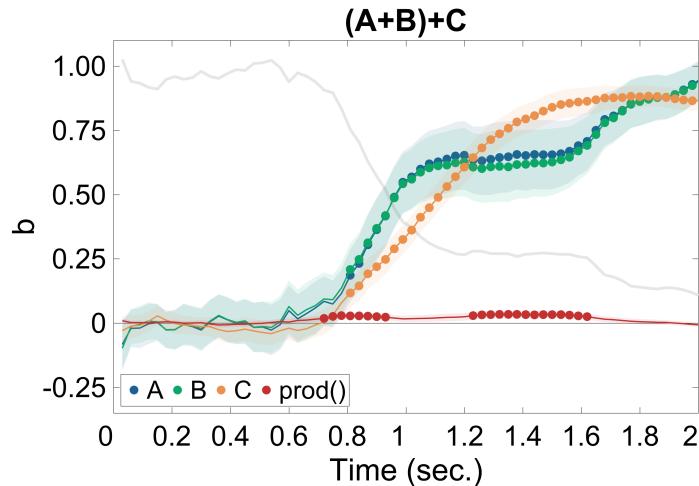
Josef Parvizi
Stanford University



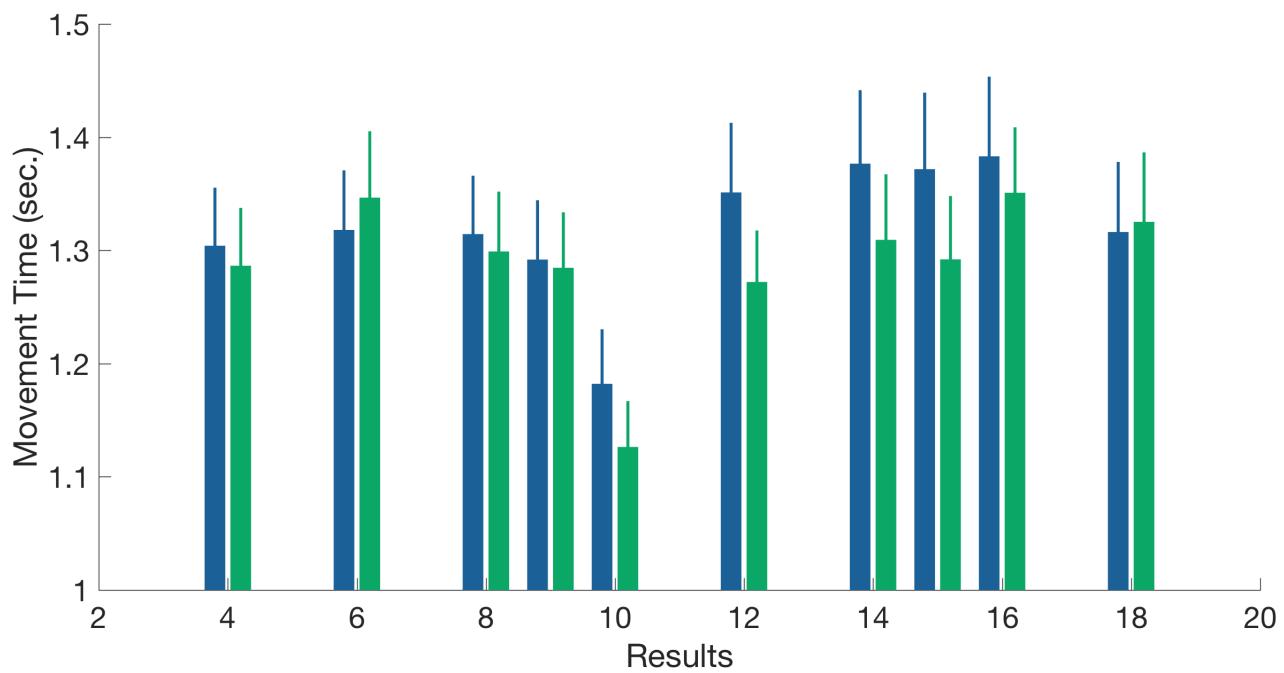
Marietta Ren

Supplementary Slides

Serial processing of arithmetic expressions



- Parenthesis first, irrespective of its location.
- Multiplication does not rely on quantity manipulation (product directly).

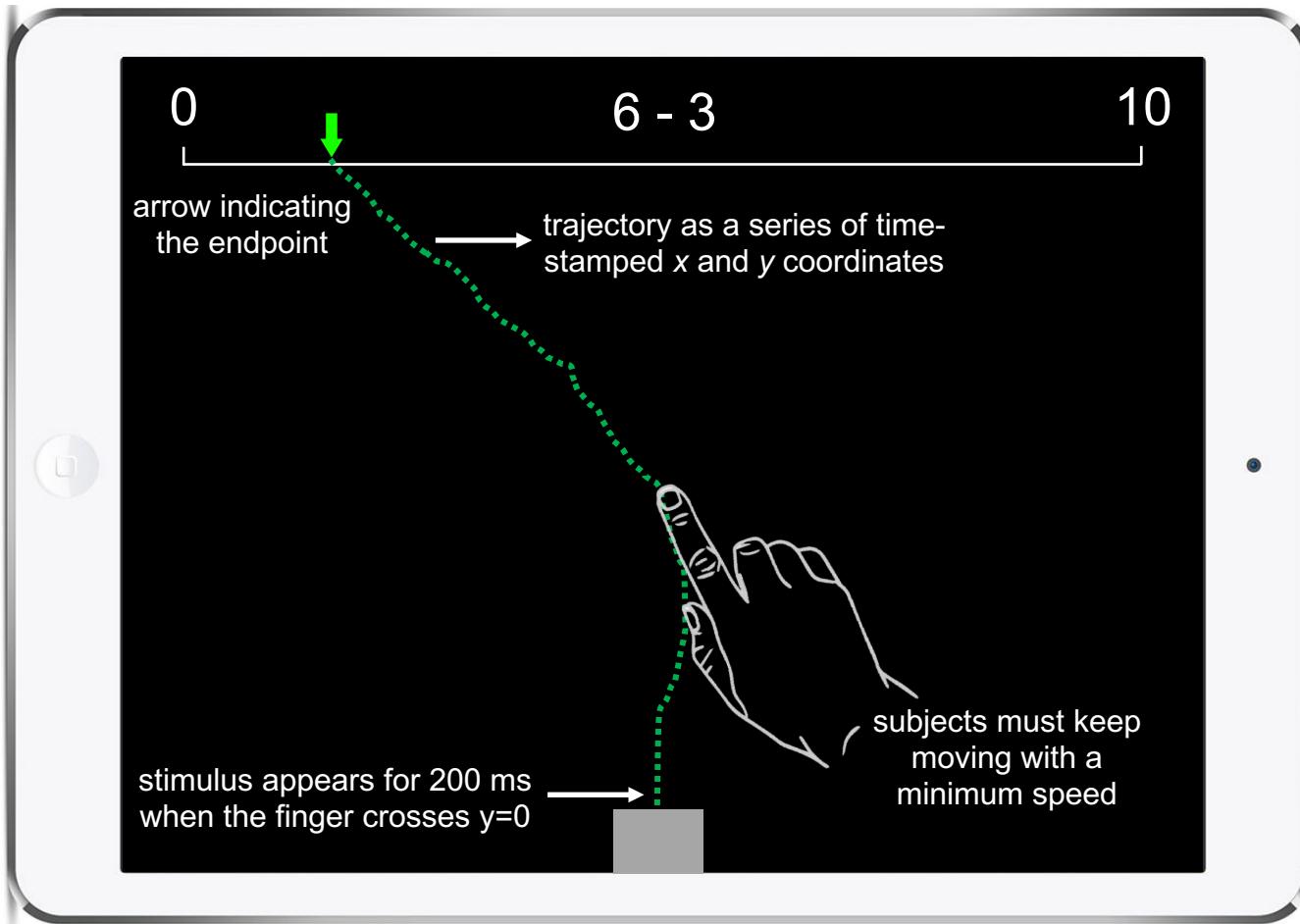


(Pinheiro-Chagas, Dotan, Manuela & Dehaene, in preparation)

Chapter 2. Finger-tracking reveals the covert stages of mental arithmetic

Experimental Setup

30 adults, students, right-handed

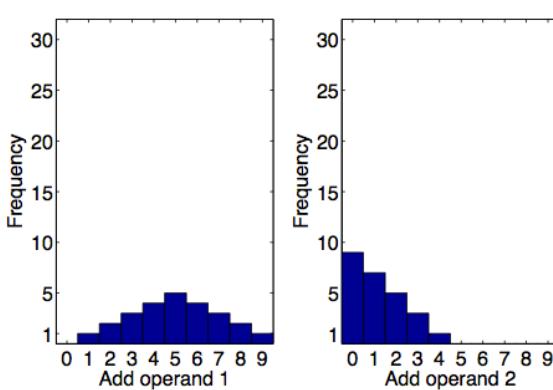


Block1 – Matched Operands
All problems $x+y$ and $x-y$
with results between 1:9

Block2 – Matched Results
All results 1:9 are equally likely
for both addition and subtraction

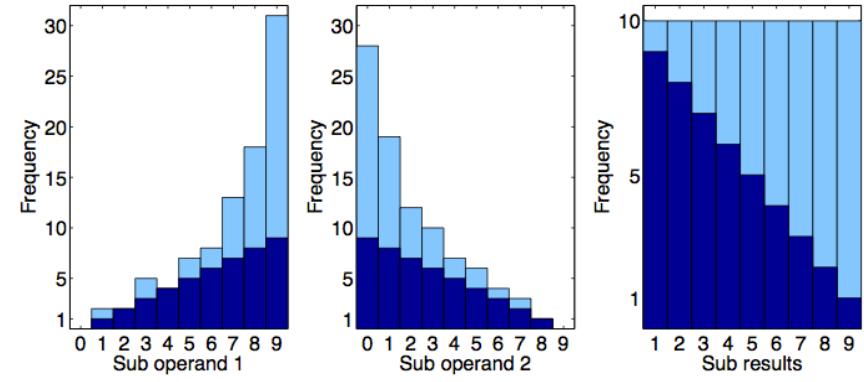
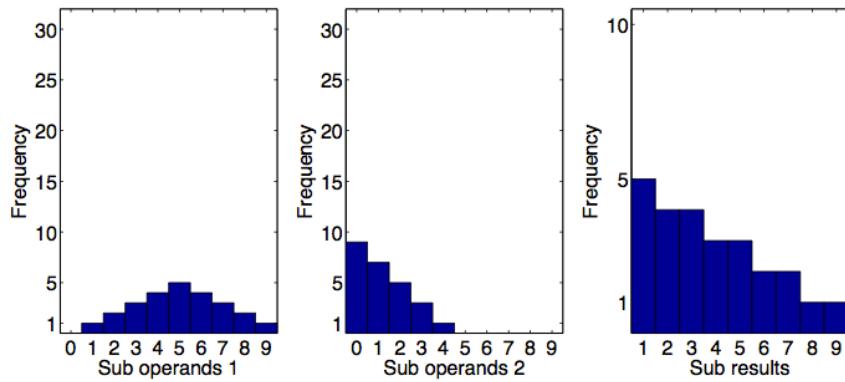
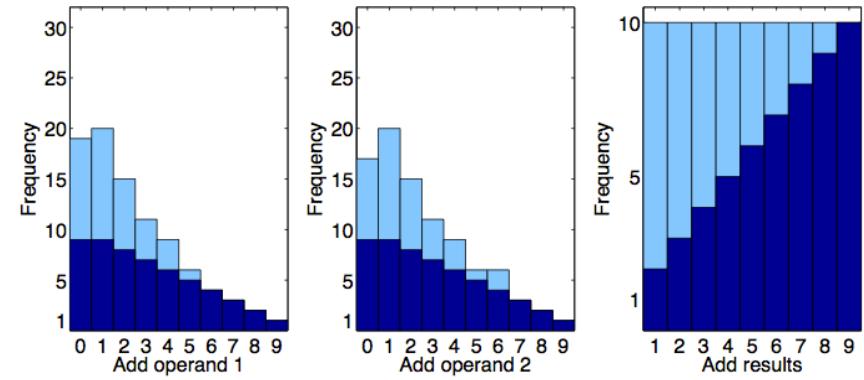
List of stimuli for the experiment

Block1 – Matched Operands



Block2 – Matched Results

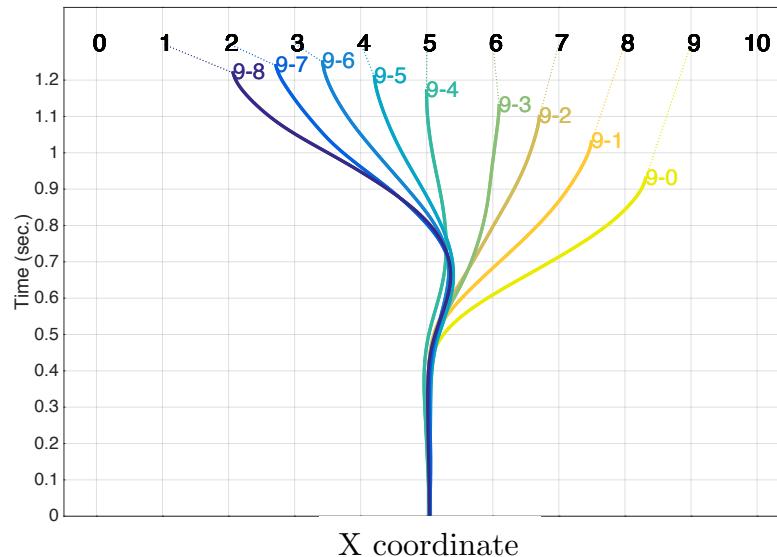
Distributions of operands and results



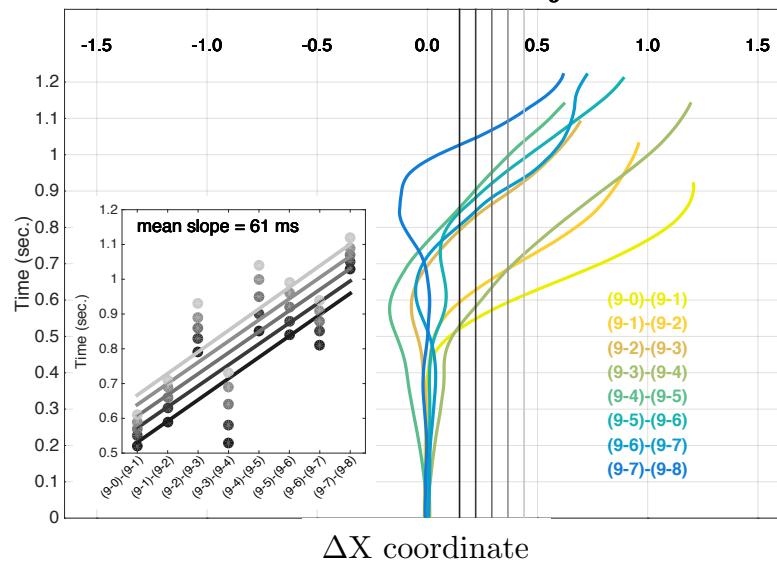
Direct visualization of the serial processing of the operands

Participants first point to the larger operand and then deviate to the correct result

Averaged trajectories 9-S



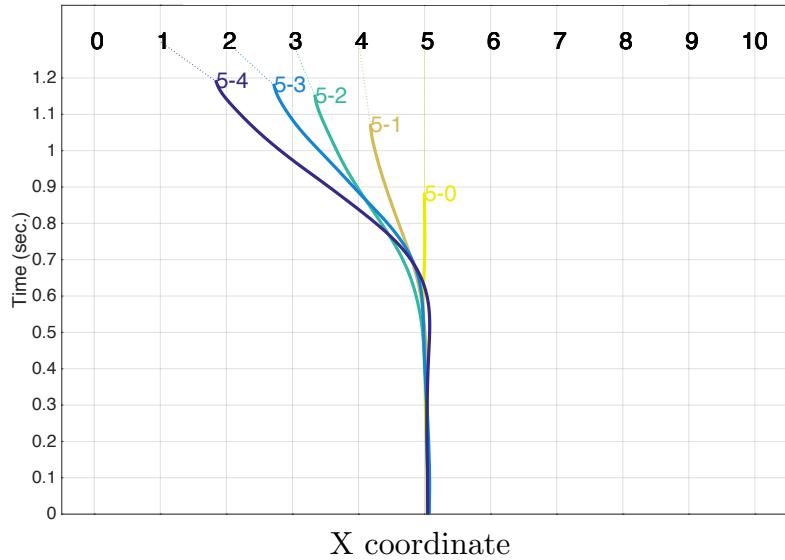
Subtracted consecutive trajectories 9-S



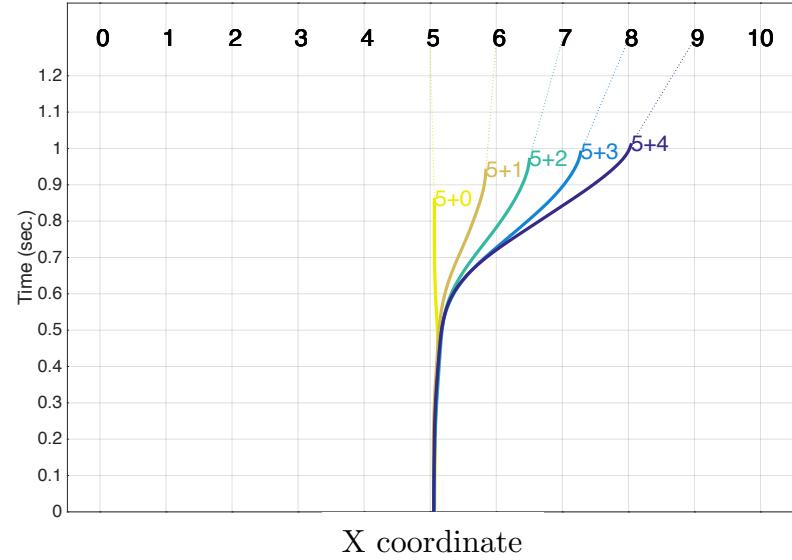
Direct visualization of the serial processing of the operands

The deviation unfolds serially and proportionally to the size of the smaller operand

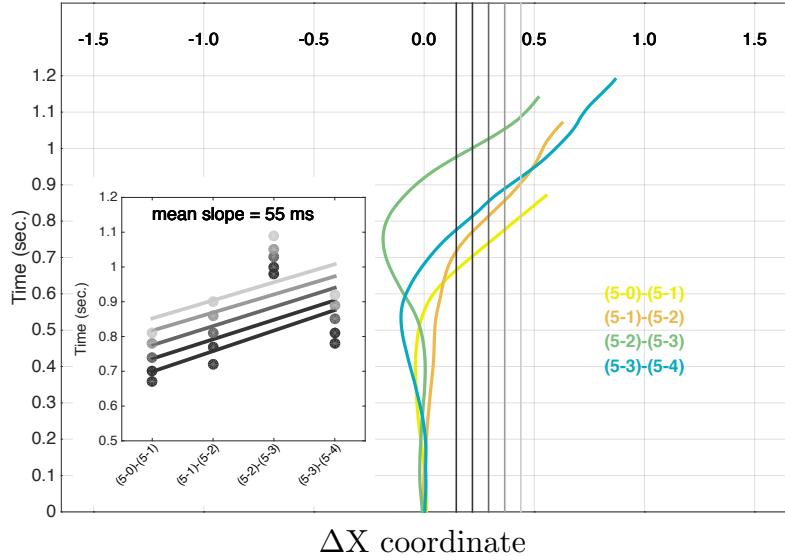
Averaged trajectories 5-S



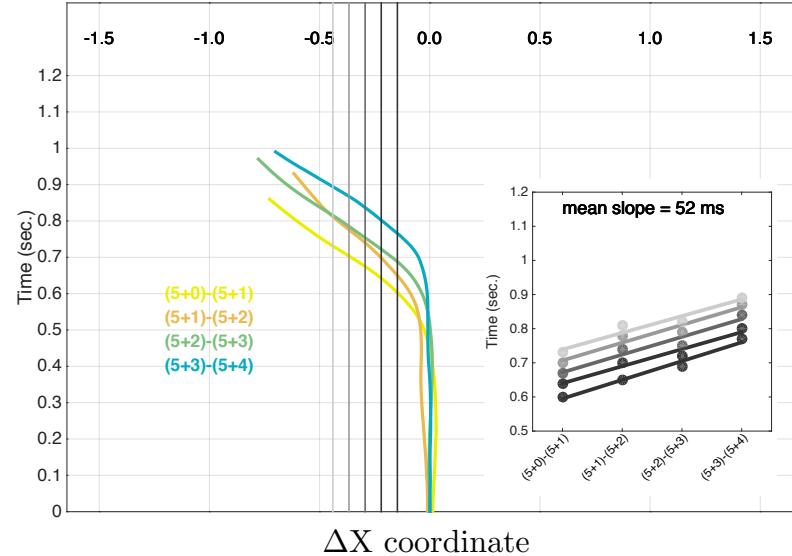
Averaged trajectories 5+S



Subtracted consecutive trajectories 5-S

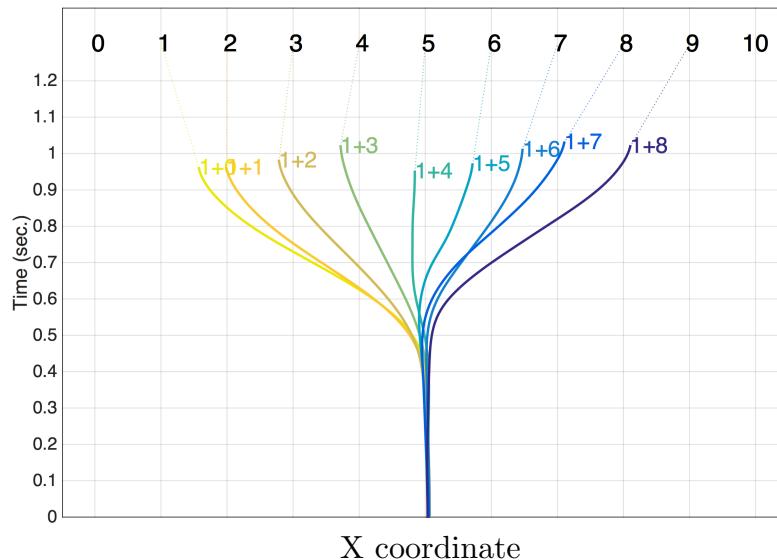


Subtracted consecutive trajectories 5+S

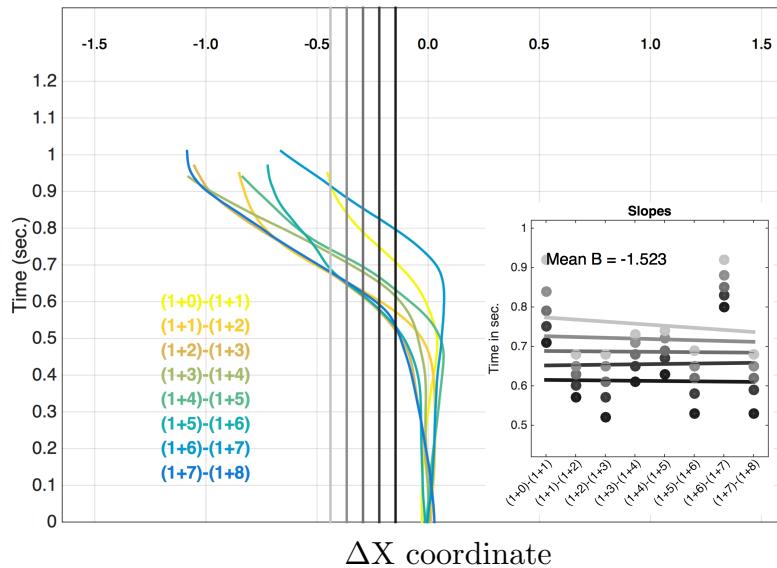


Not a by-product of the geometrical and motor constraints

Averaged trajectories 1+L

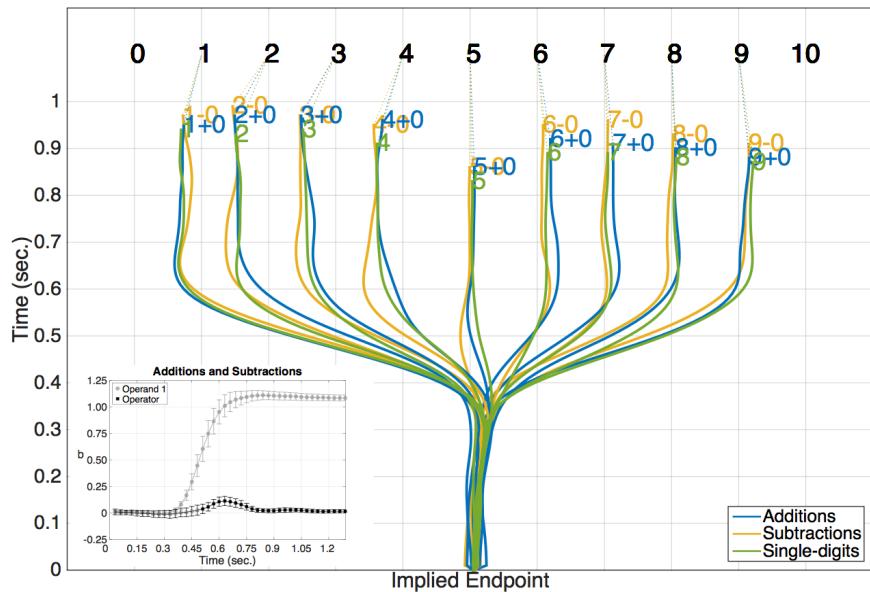


Subtracted consecutive trajectories 1+L

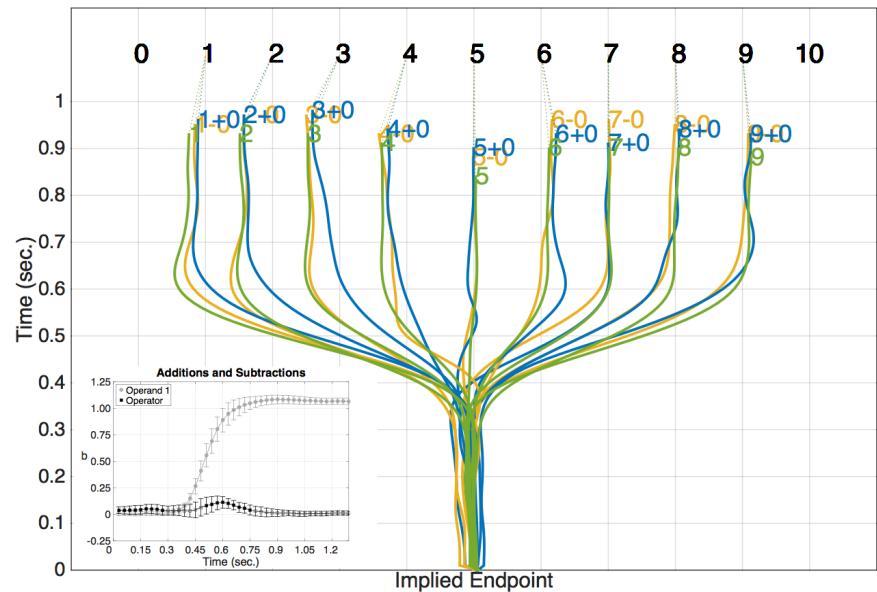


OM in zero problems

Block 1 – Matched Operands

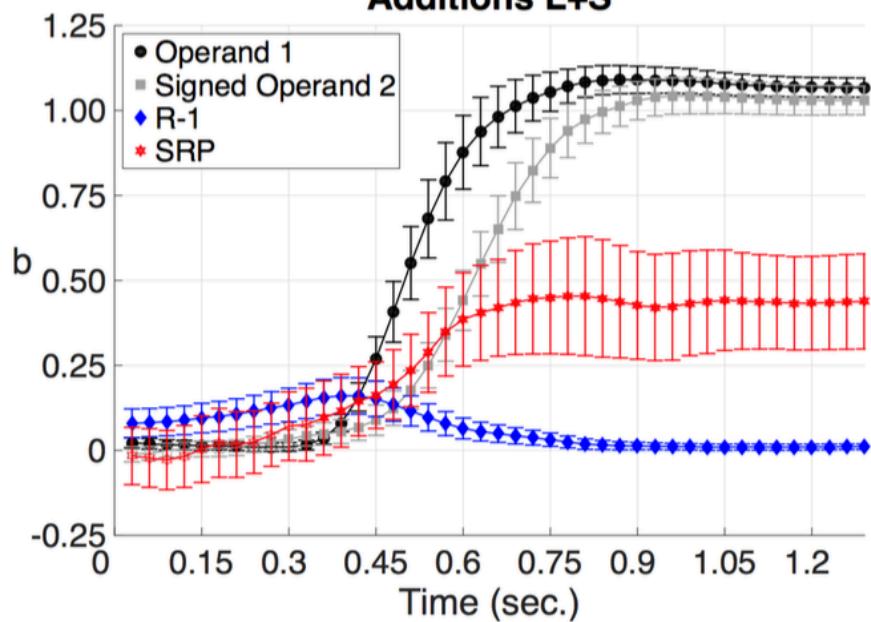


Block 2 – Matched Results

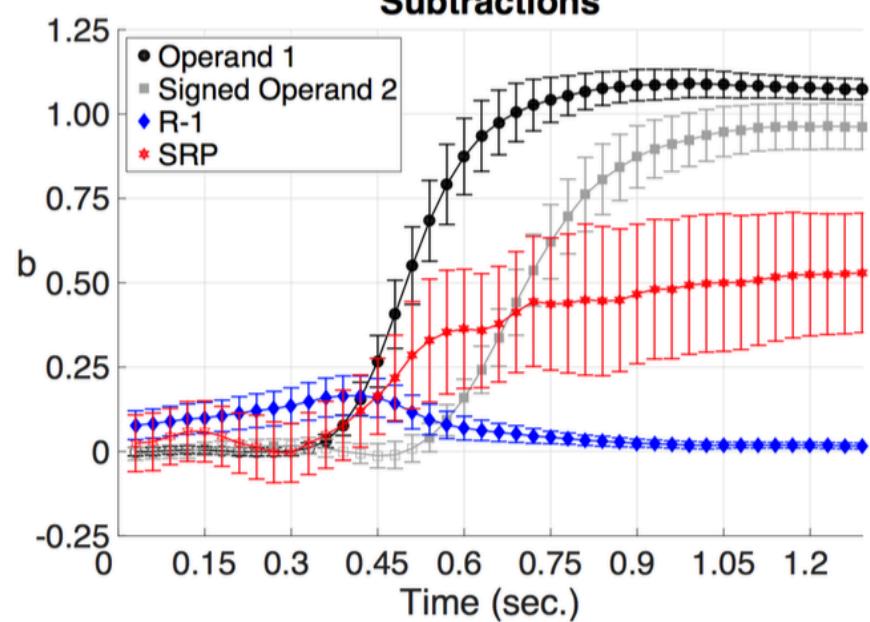


Block 1 – Matched Operands

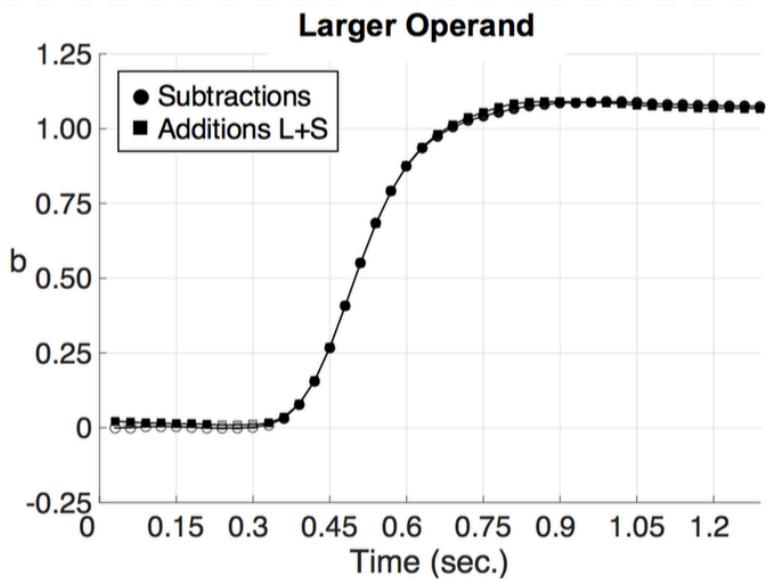
Additions L+S



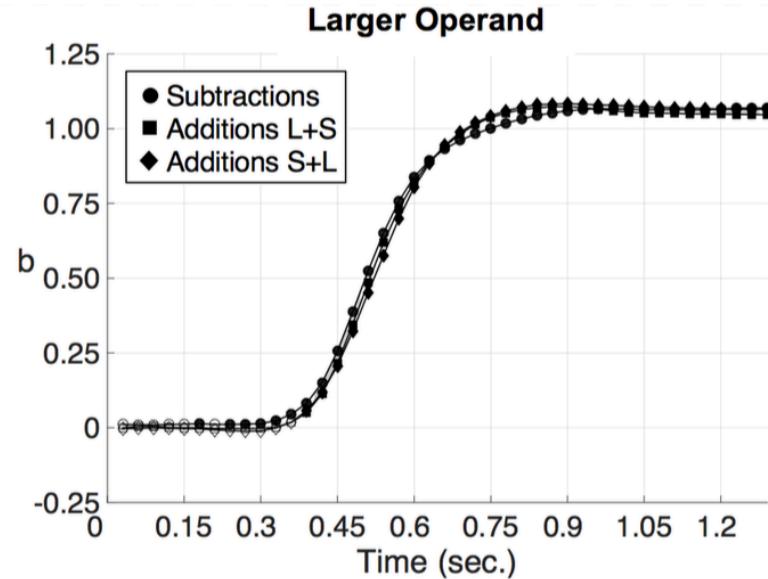
Subtractions



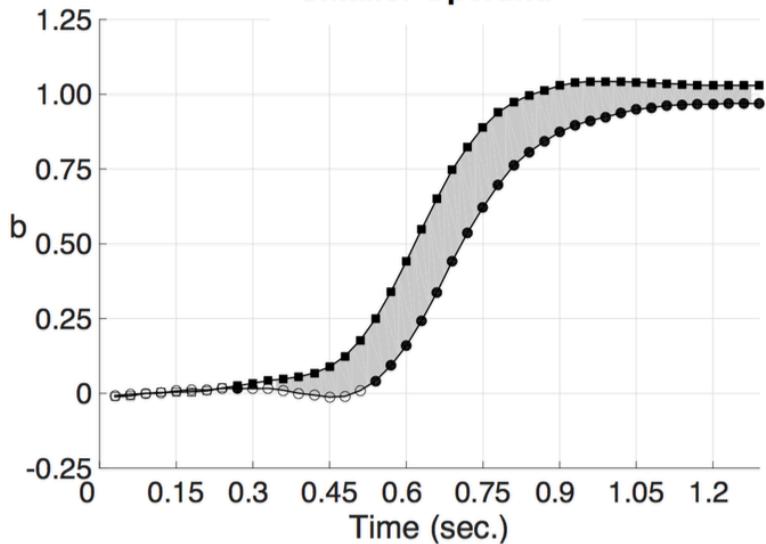
Block 1 – Matched operands



Block 2 – Matched Results



Smaller Operand



Smaller Operand

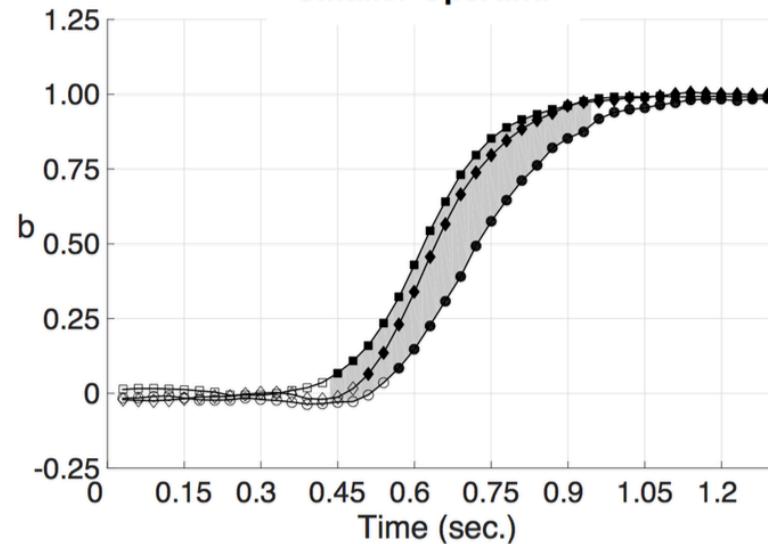
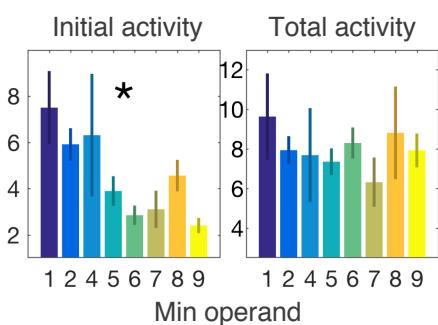
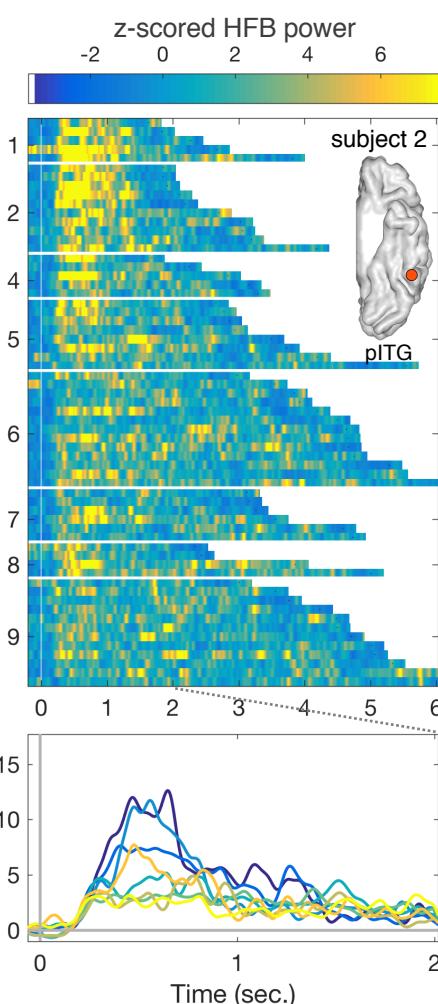
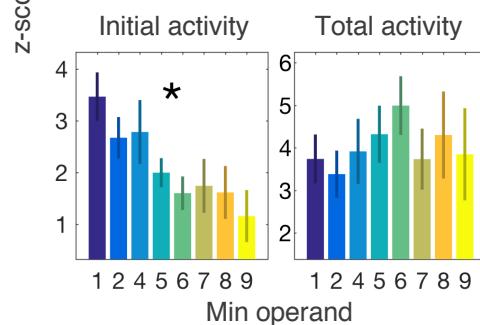
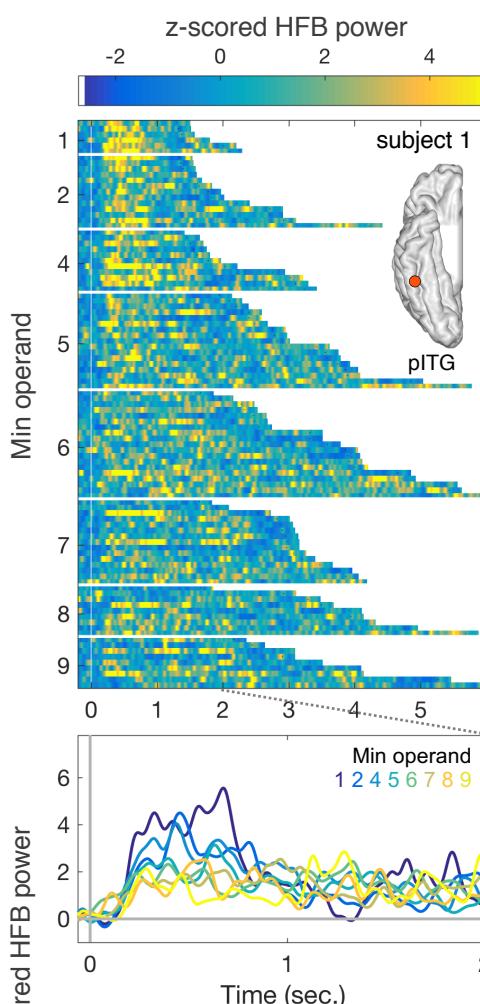
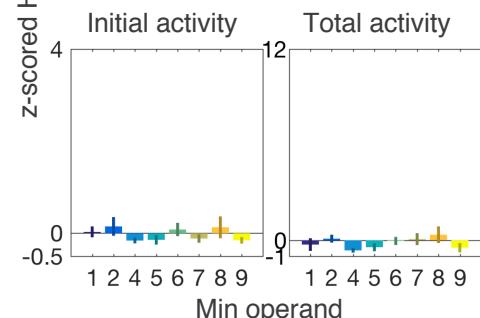
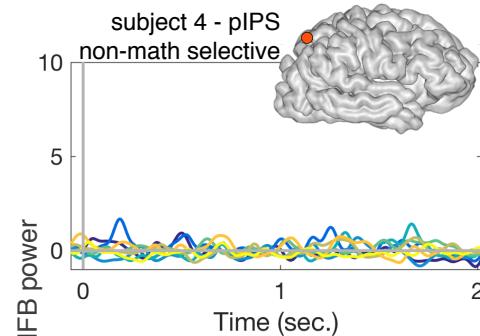
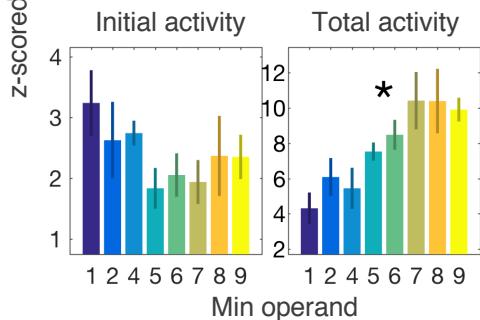
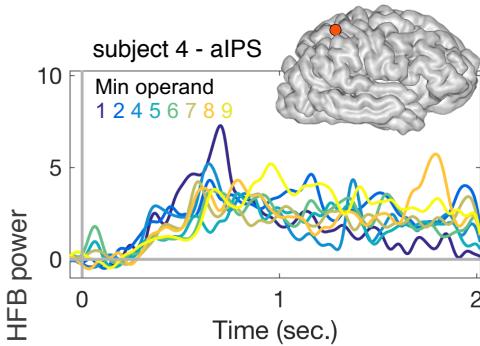


Figure 2.7 Comparison of the time course of the regression effects

The shaded area indicates a significant difference ($p < 0.05$)

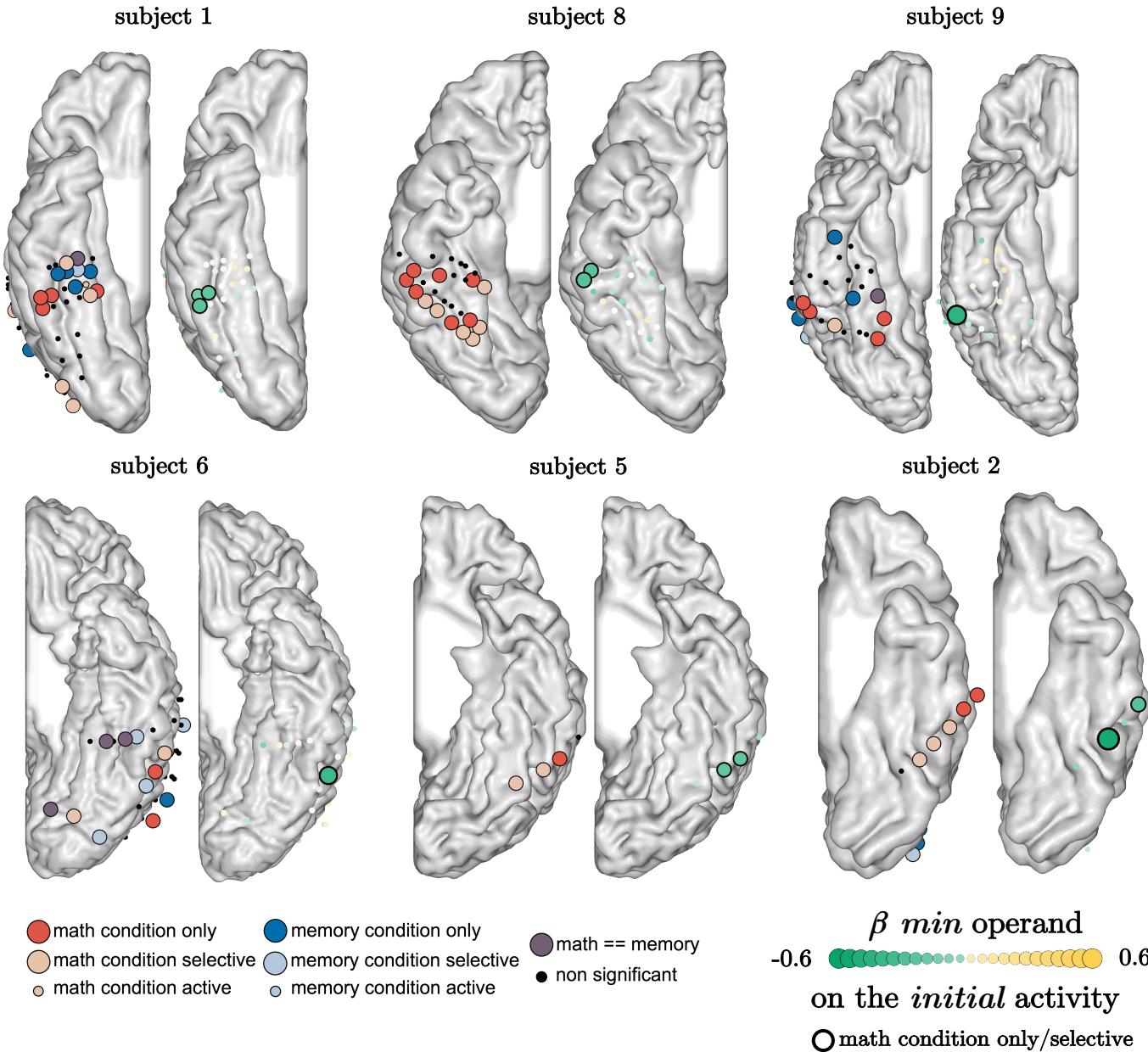
Chapter 3. Brain mechanisms of arithmetic: a crucial role for ventral temporal cortex

Modulation of HFB activity by problem-size (*min operand*)

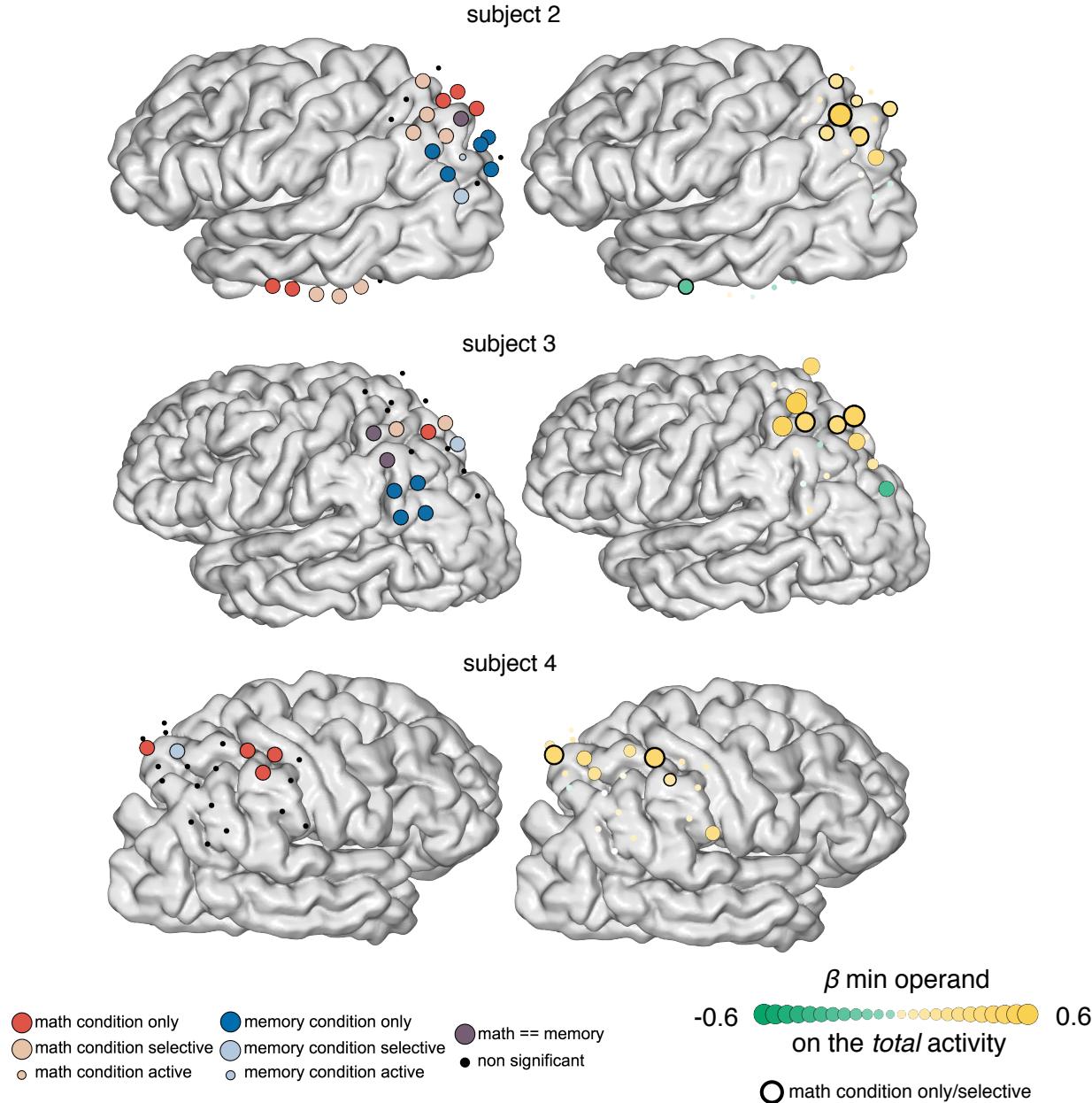


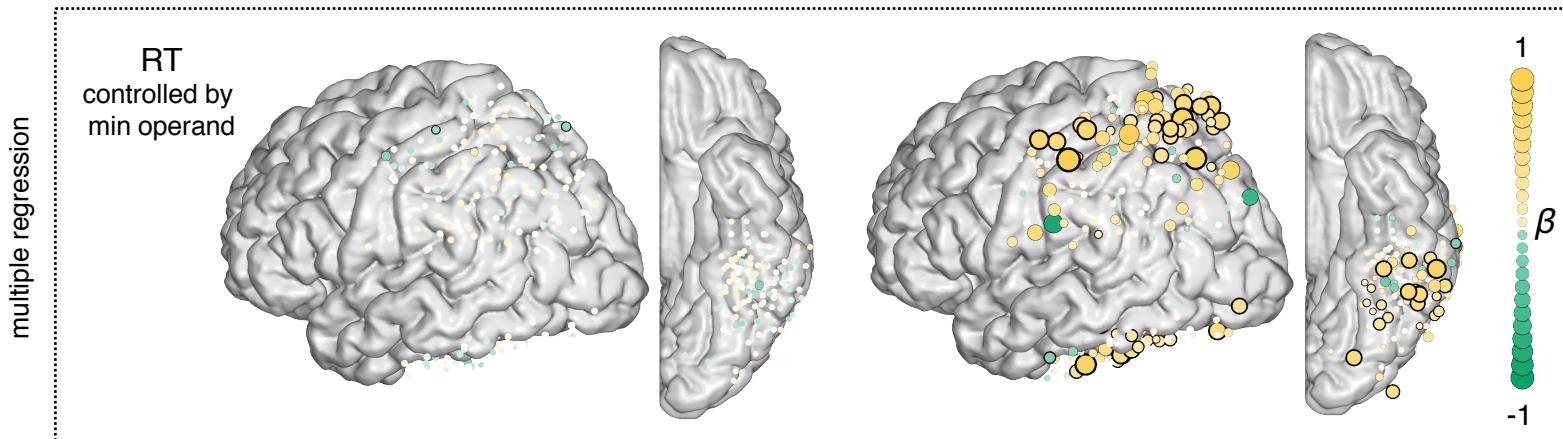
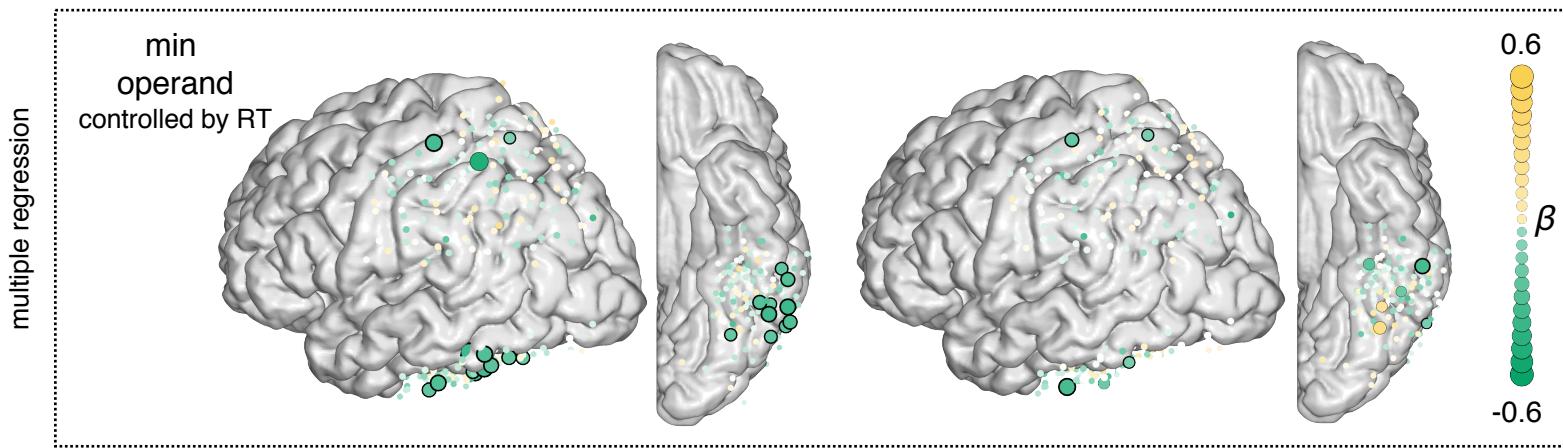
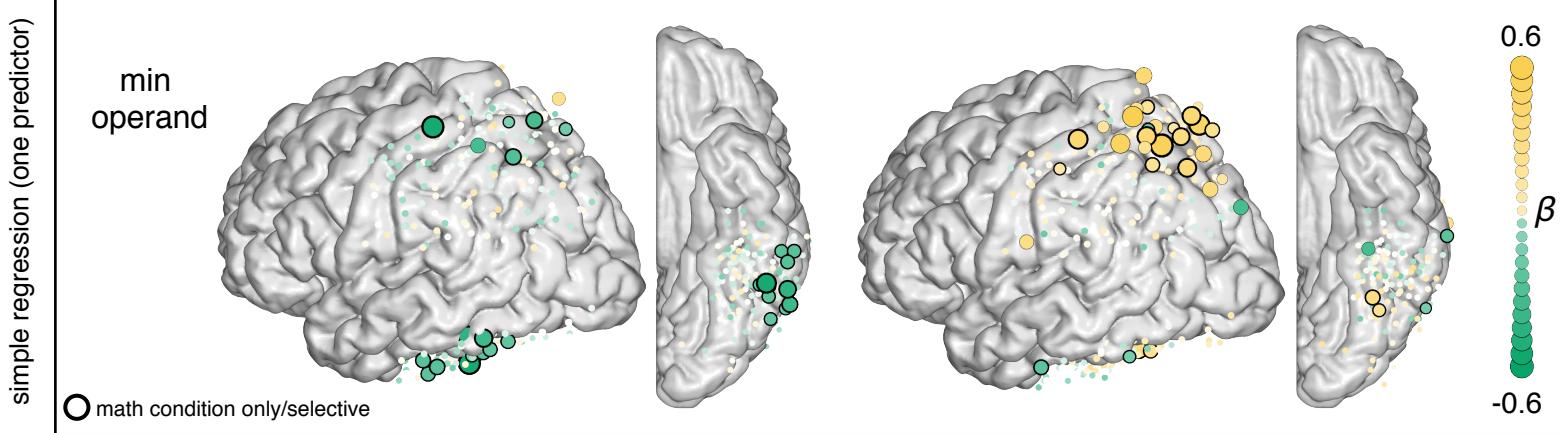
p-values
FDR-corrected
for all channels
within subject

Anatomical and functional precision of the pITG modulation

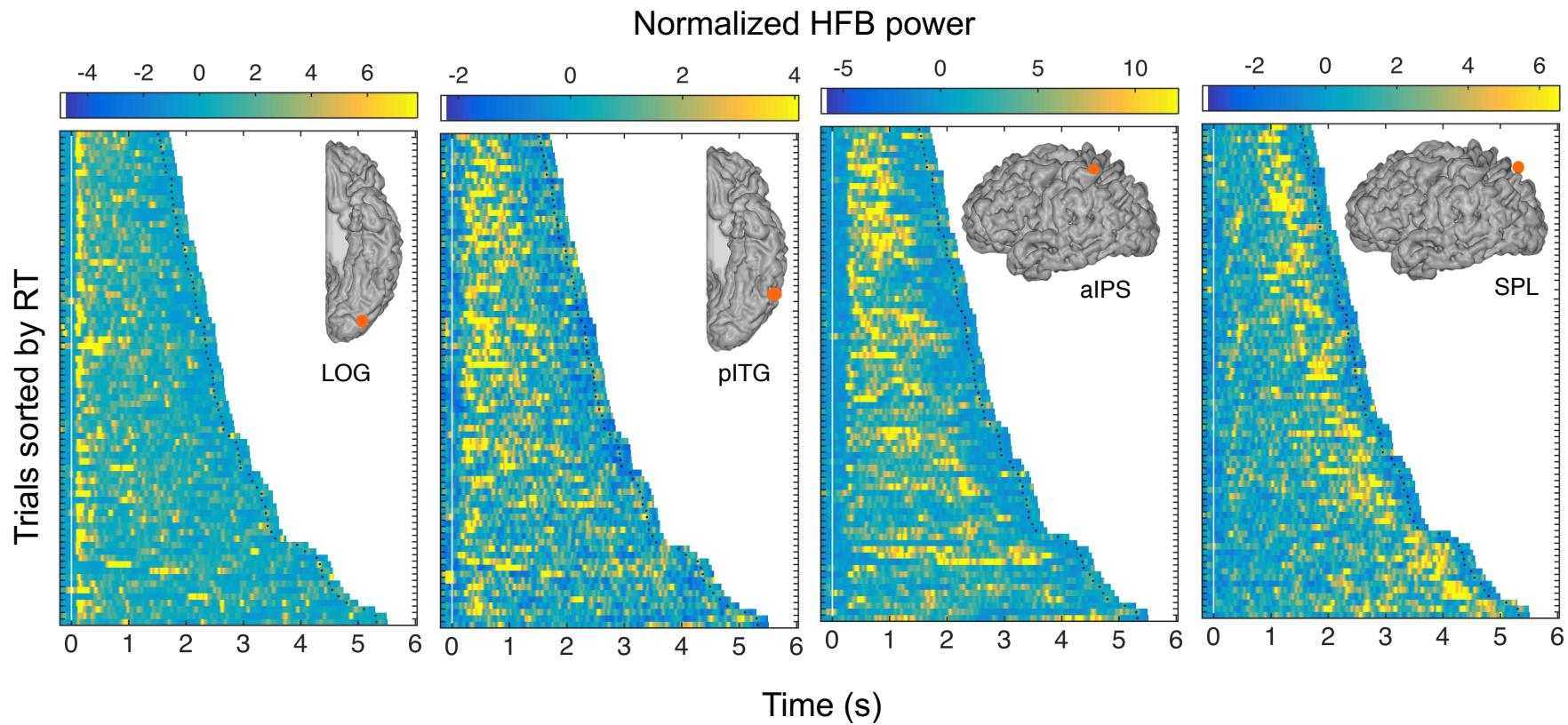


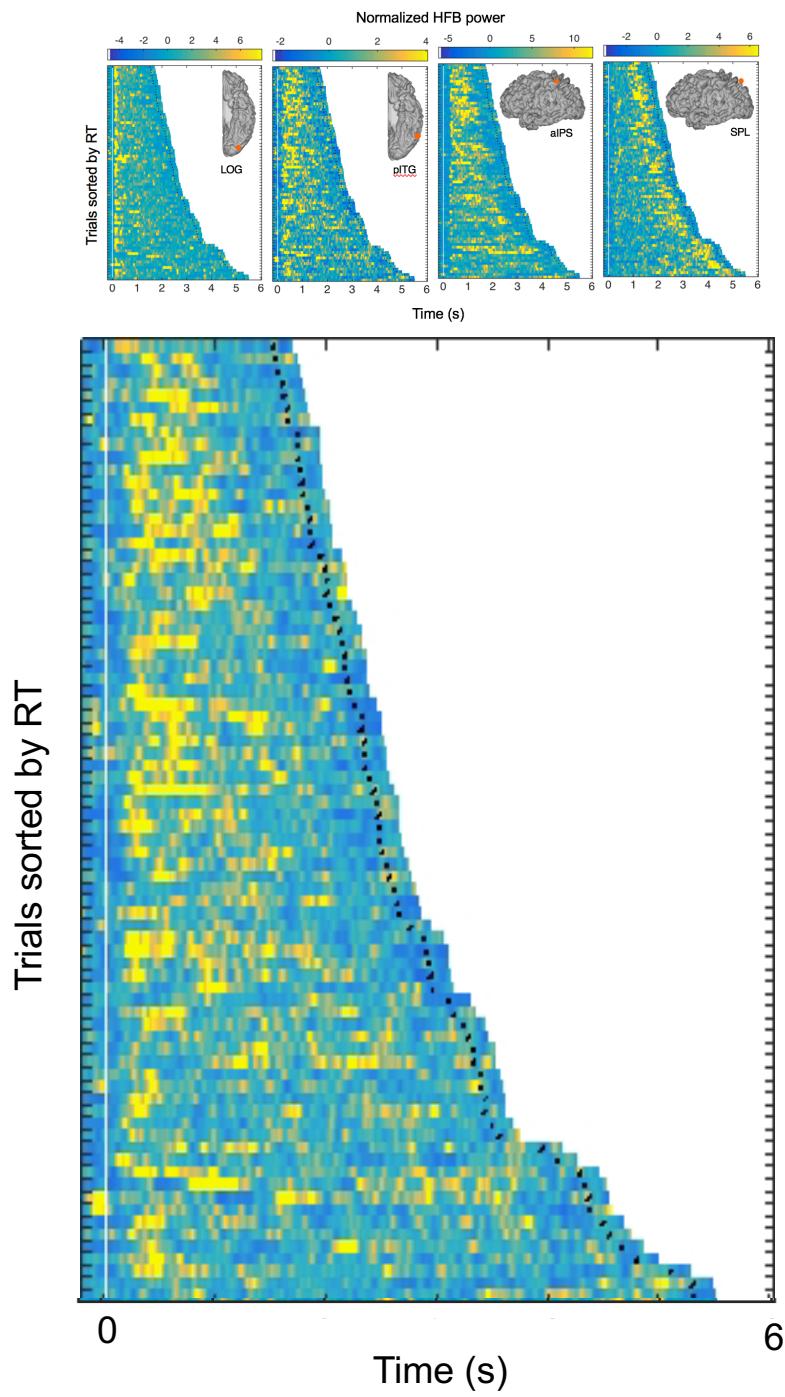
Anatomical and functional precision of the IPS and SPL modulation



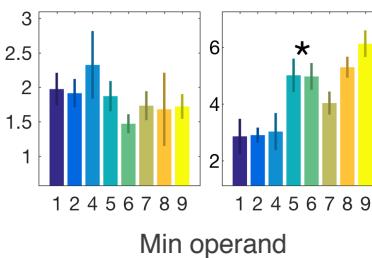
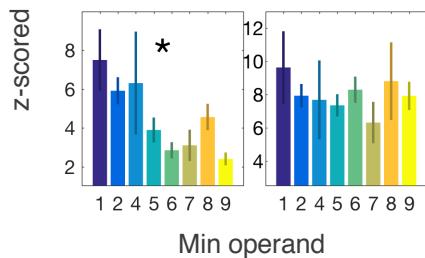
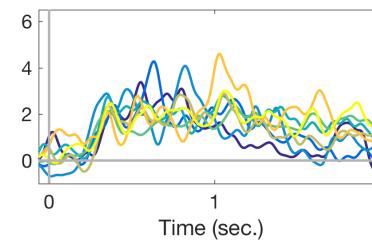
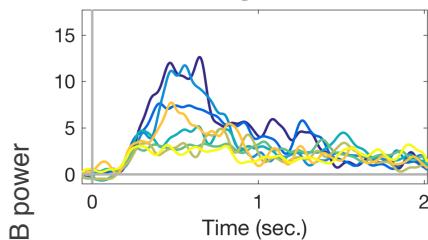
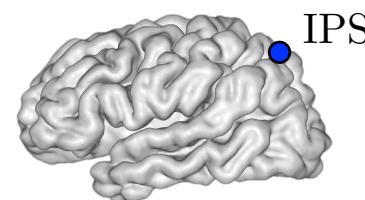
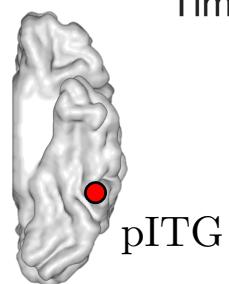
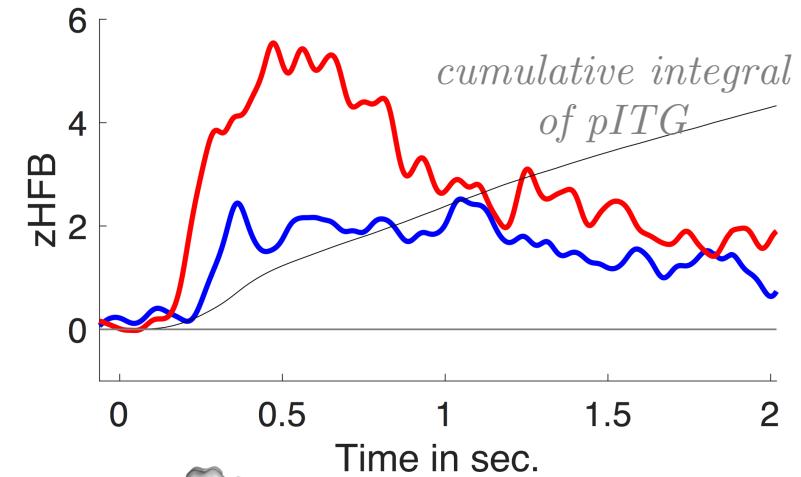


Spatial-temporal dynamics of arithmetic processing in 1 subject





Relationship between decrease initial in pITG and increased total in IPS

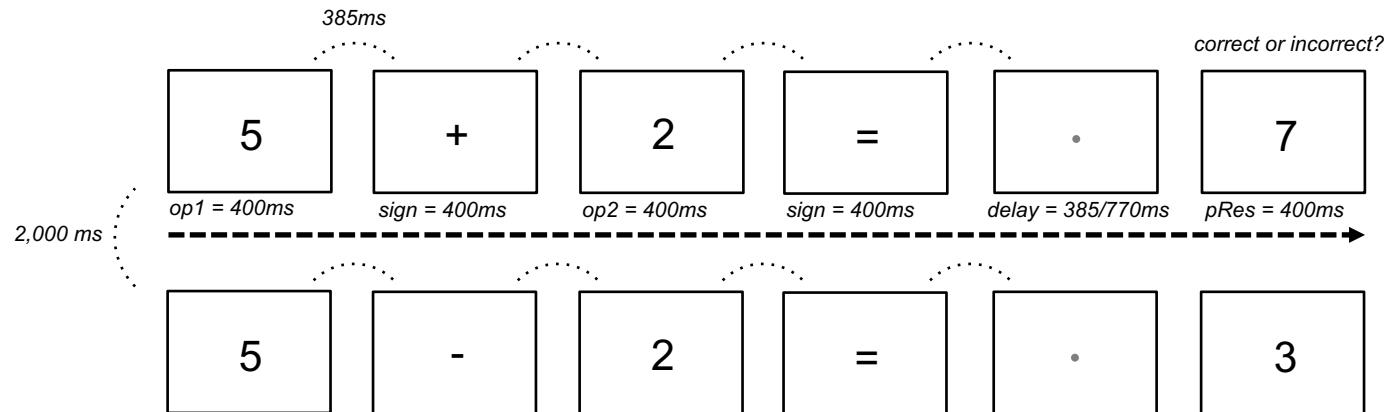


Chapter 4. Decoding the processing stages of mental arithmetic with MEG

- New insights on the neurocognitive mechanisms of mental calculations discovered in the previous studies.
- Still lacking a comprehensive picture of the organization of brain processes.
- Time-resolved multivariate pattern analysis applied to MEG.
- Can we decode the identity of the operands? Representational codes?
- Can we track in time the emergence of the internally computed result?
- Are the brain processes completely serial or do they partially overlap in a form of a cascade of computations that can be simultaneously decoded?

Calculation verification task - Experimental Design

20 adults, students, right-handed



Factors

OP1 = 3, 4, 5, 6

OP2 = 0, 1, 2, 3

Result correct = correct 0:9

pRes incorrect = distance from correct 1, 2, 3, 4

(no results that could be correct if the other operation)

Operation = addition, subtraction

Delay from last '=' sign = 385 or 770 ms

Event duration = 400 ms

ISI: 385 ms

ITI = 2,000 ms

Trials

160 additions

160 subtractions

10 blocks of 32 trials each

Experiment duration = ~40 min

Stimuli list

$3 + 0 = 3$

$3 + 1 = 4$

$3 + 2 = 5$

$3 + 3 = 6$

$4 + 0 = 4$

$4 + 1 = 5$

$4 + 2 = 6$

$4 + 3 = 7$

$5 + 0 = 5$

$5 + 1 = 6$

$5 + 2 = 7$

$5 + 3 = 8$

$6 + 0 = 6$

$6 + 1 = 7$

$6 + 2 = 8$

$6 + 3 = 9$

$3 - 0 = 3$

$3 - 1 = 2$

$3 - 2 = 1$

$3 - 3 = 0$

$4 - 0 = 4$

$4 - 1 = 3$

$4 - 2 = 2$

$4 - 3 = 1$

$5 - 0 = 5$

$5 - 1 = 4$

$5 - 2 = 3$

$5 - 3 = 2$

$6 - 0 = 6$

$6 - 1 = 5$

$6 - 2 = 4$

$6 - 3 = 3$

Frequency of operand 1

Value	Count	Percent
3	80	25.00%
4	80	25.00%
5	80	25.00%
6	80	25.00%

Frequency of operand 2

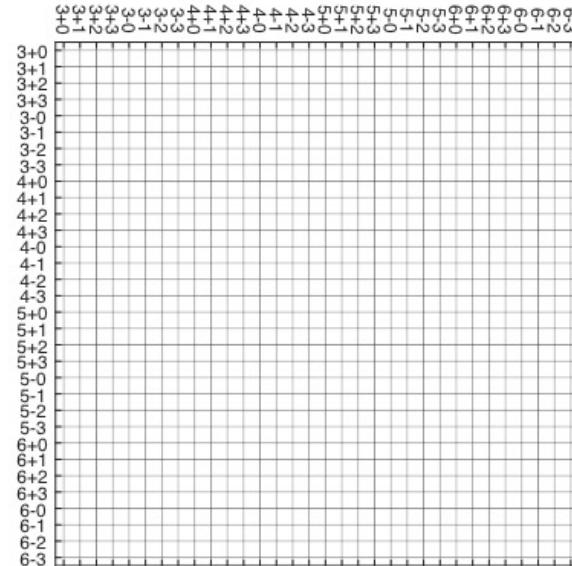
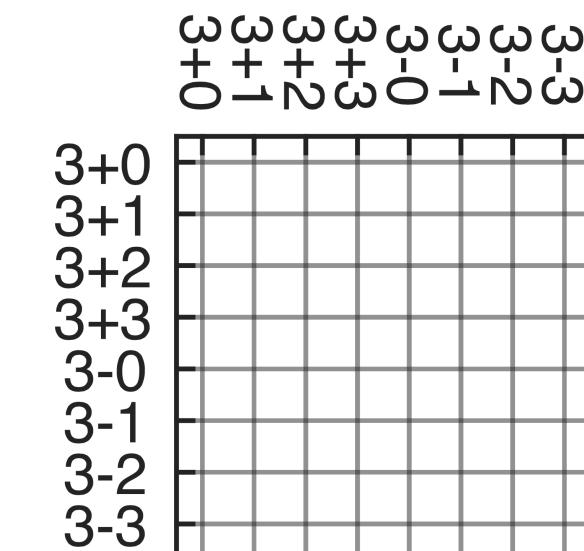
Value	Count	Percent
0	80	25.00%
1	80	25.00%
2	80	25.00%
3	80	25.00%

Frequency of results add and sub together

Value	Count	Percent
0	10	3.12%
1	20	6.25%
2	30	9.38%
3	50	15.62%
4	50	15.62%
5	50	15.62%
6	50	15.62%
7	30	9.38%
8	20	6.25%
9	10	3.12%

Representational Similarity Analysis (RSA)

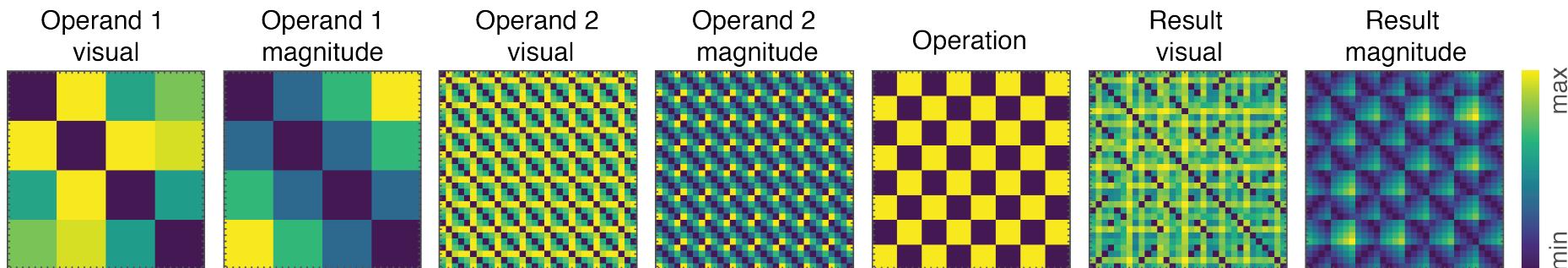
1. Calculate a dissimilarity matrix based on the pairwise correlation between experimental conditions across the 306 MEG sensors, per each time sample.
2. Correlate the observed matrix with theoretical dissimilarity matrices derived from the stimuli features. Repeated for each time sample separately.



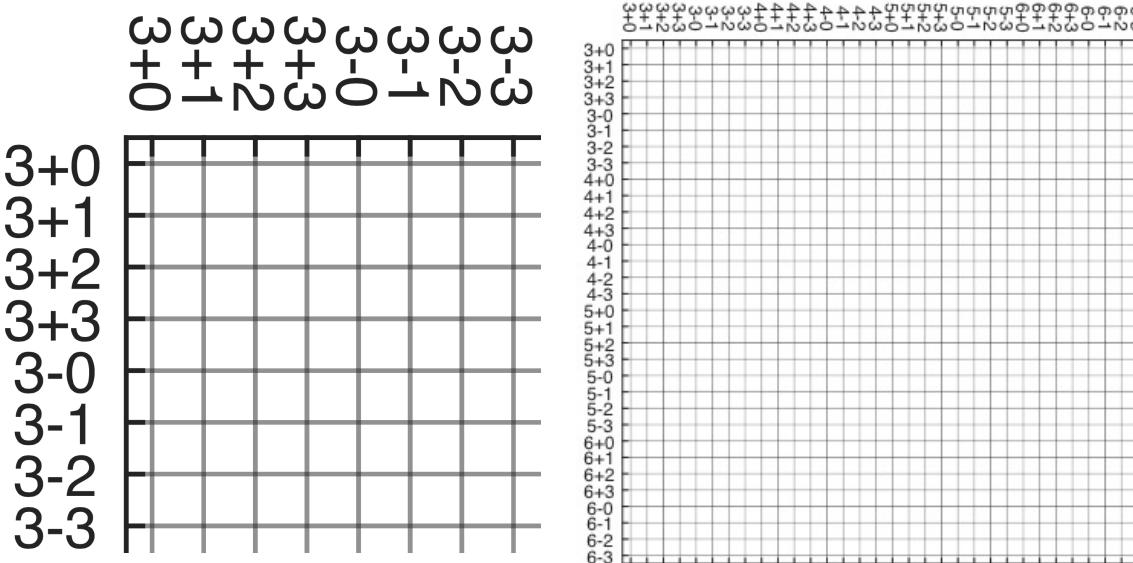
COSMO MVPA

RDM models

1 - Spearman's rho

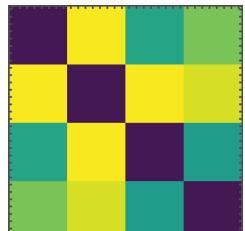


Representational Similarity Analysis (RSA)

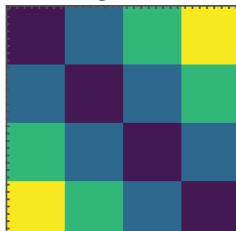


RDM models
1 - Spearman's rho

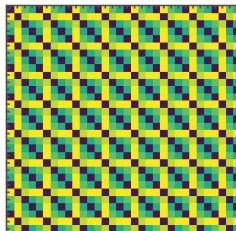
Operand 1
visual



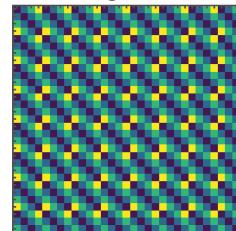
Operand 1
magnitude



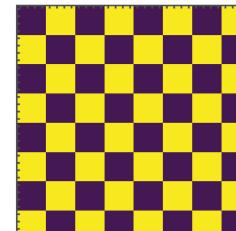
Operand 2
visual



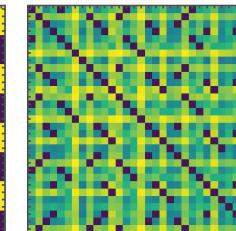
Operand 2
magnitude



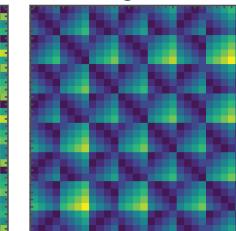
Operation



Result
visual

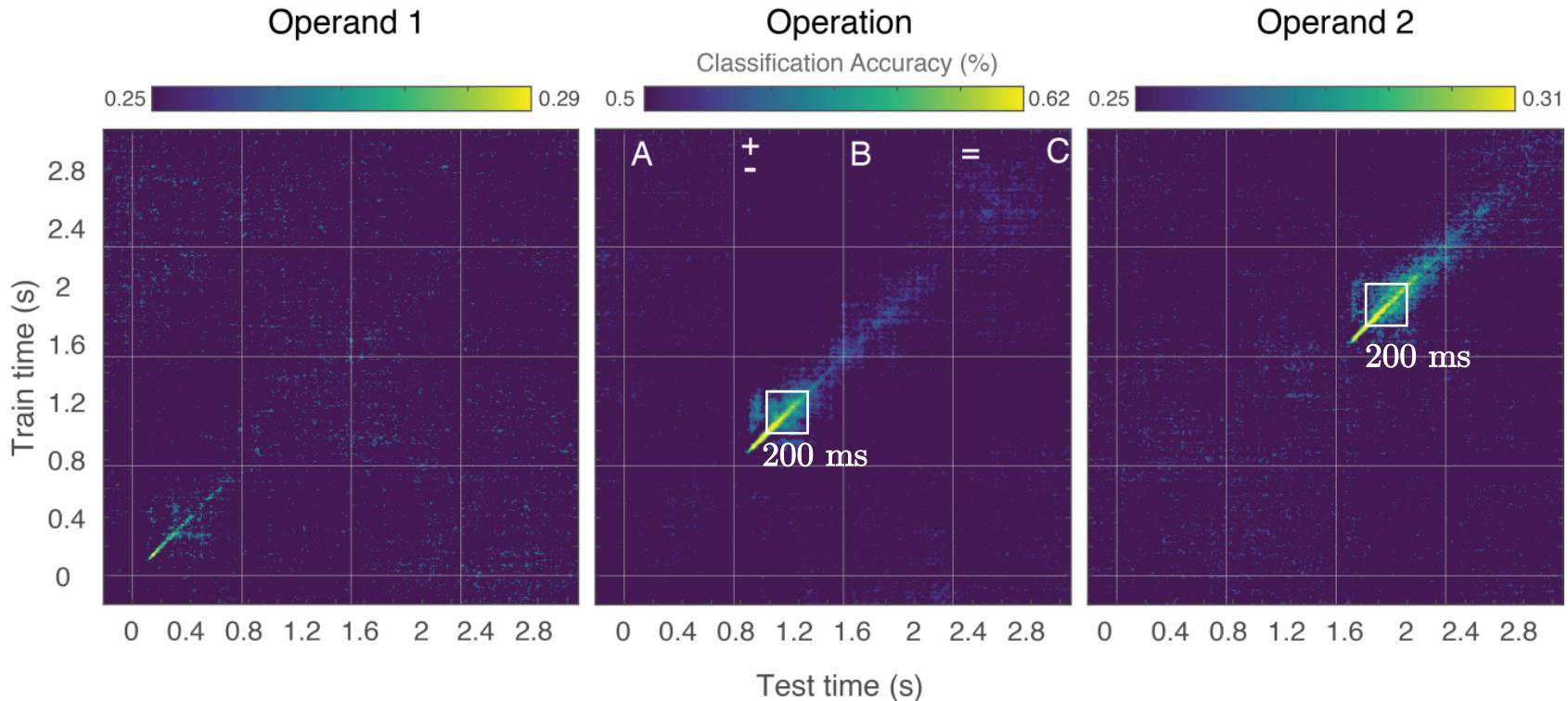


Result
magnitude



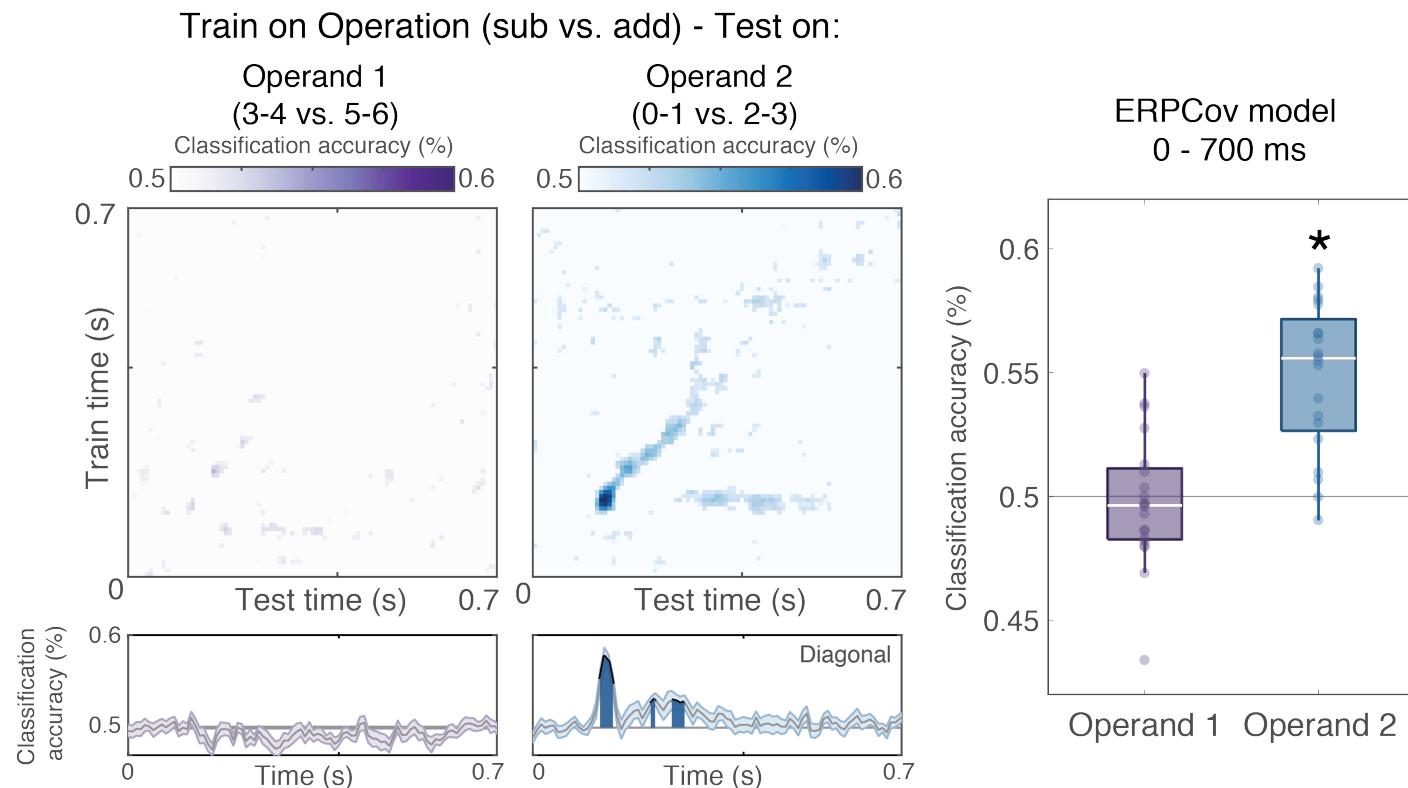
Generalization across time

brief - highly dynamic coding scheme



- Temporal dynamics of the representational codes?
 - Operand 1: visual \succ magnitude?
 - Operand 2: visual \succ magnitude.

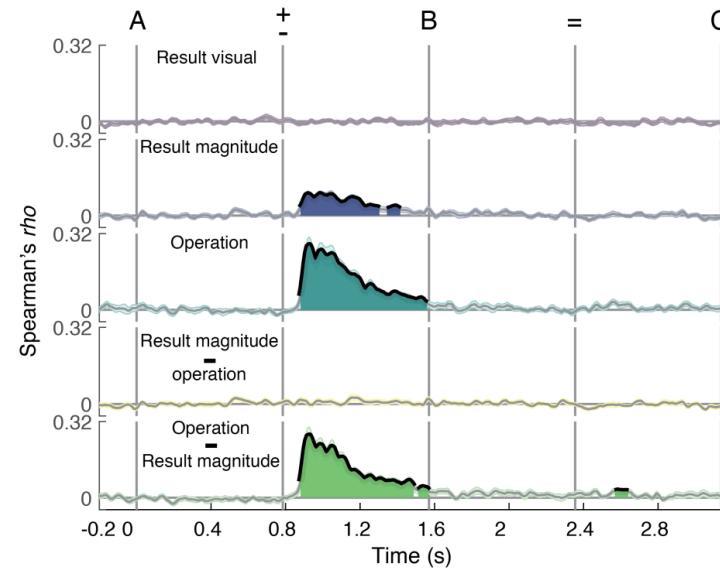
Common code: operation and magnitude of operand 2



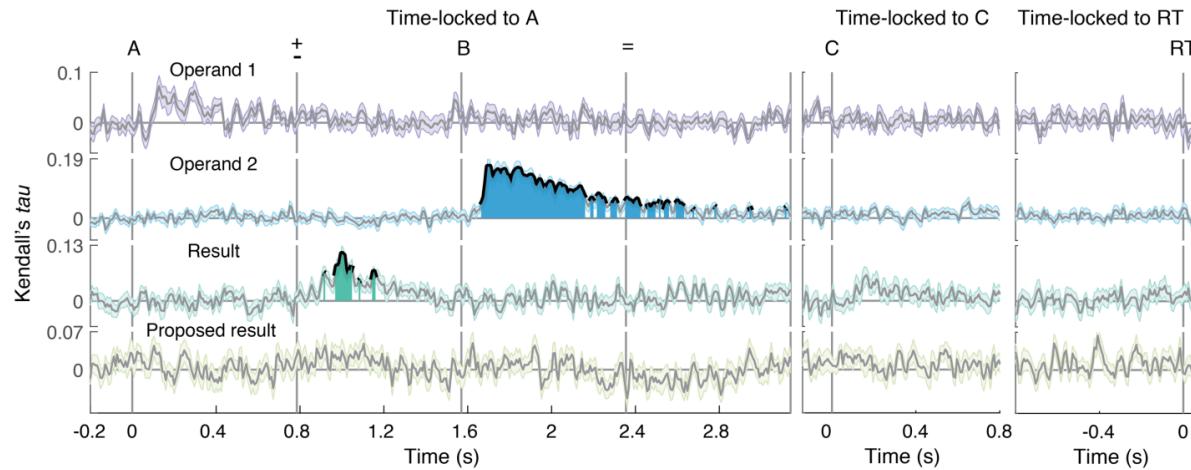
- Subtractions: smaller operand 2 (0-1); Additions: larger operand 2 (2-3)

Searching for a neural signature of the internal result

RSA



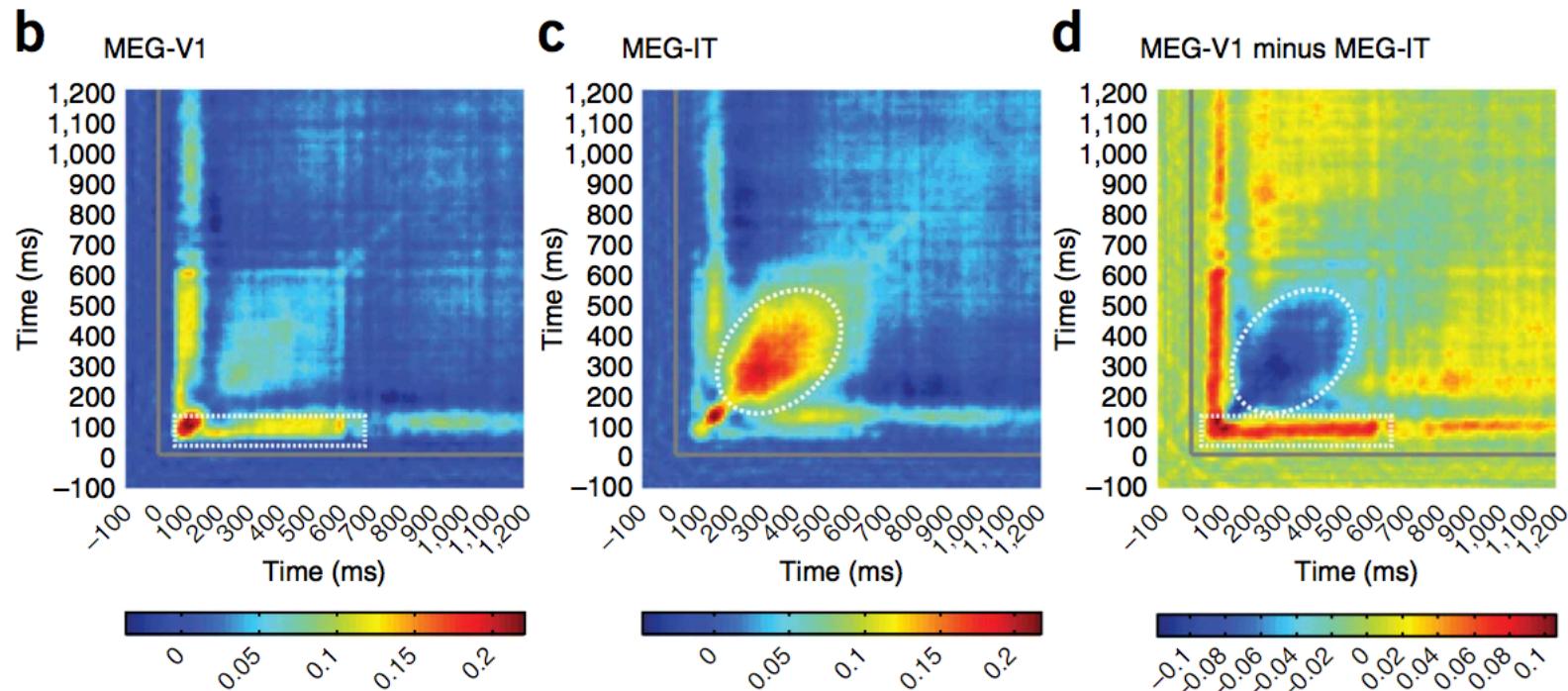
Decoding (regression)



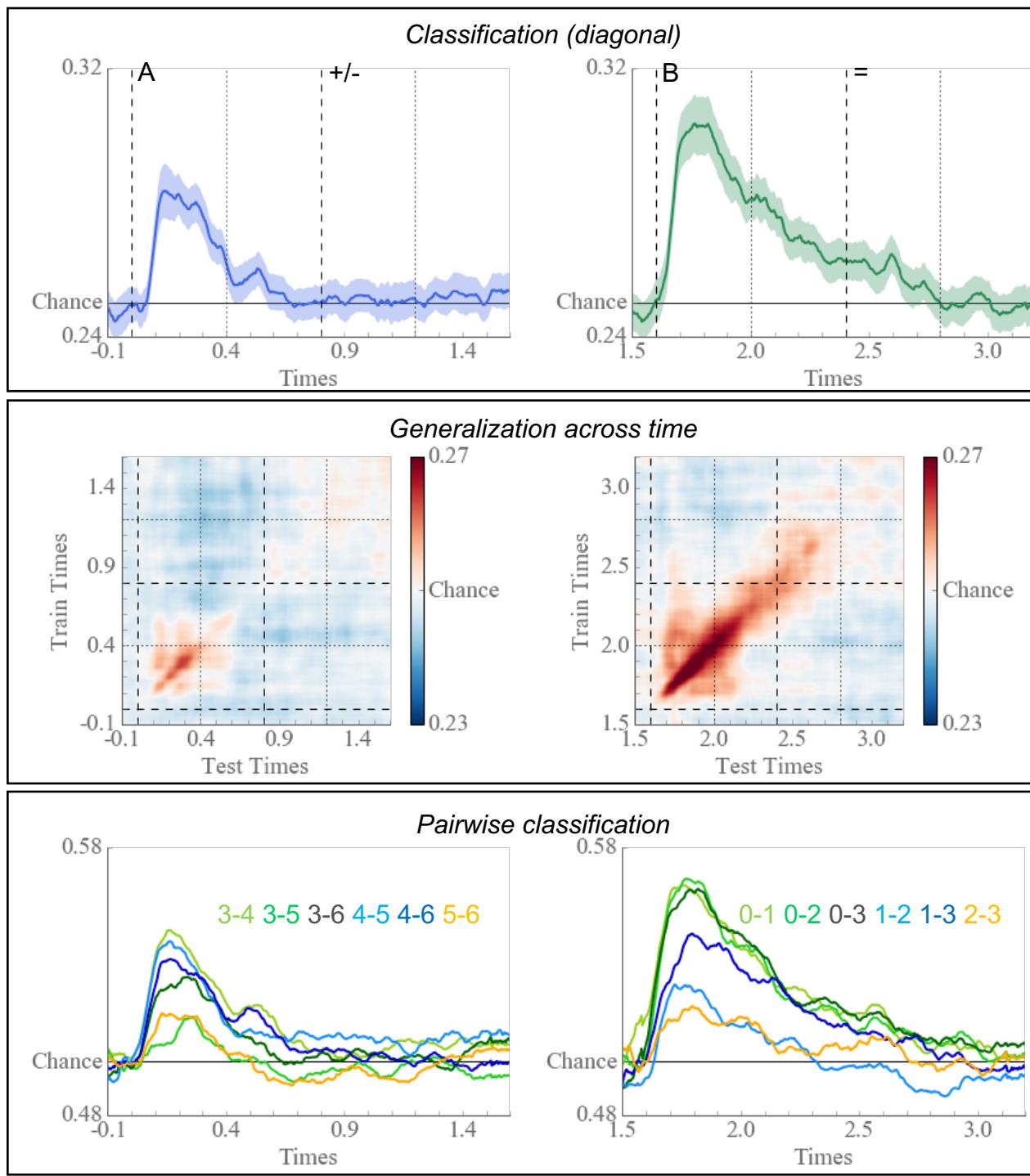
- Transient decoding after sign – Result correlates with operation

Time-resolved decoding of object with MEG

(Cichy et al., 2014)

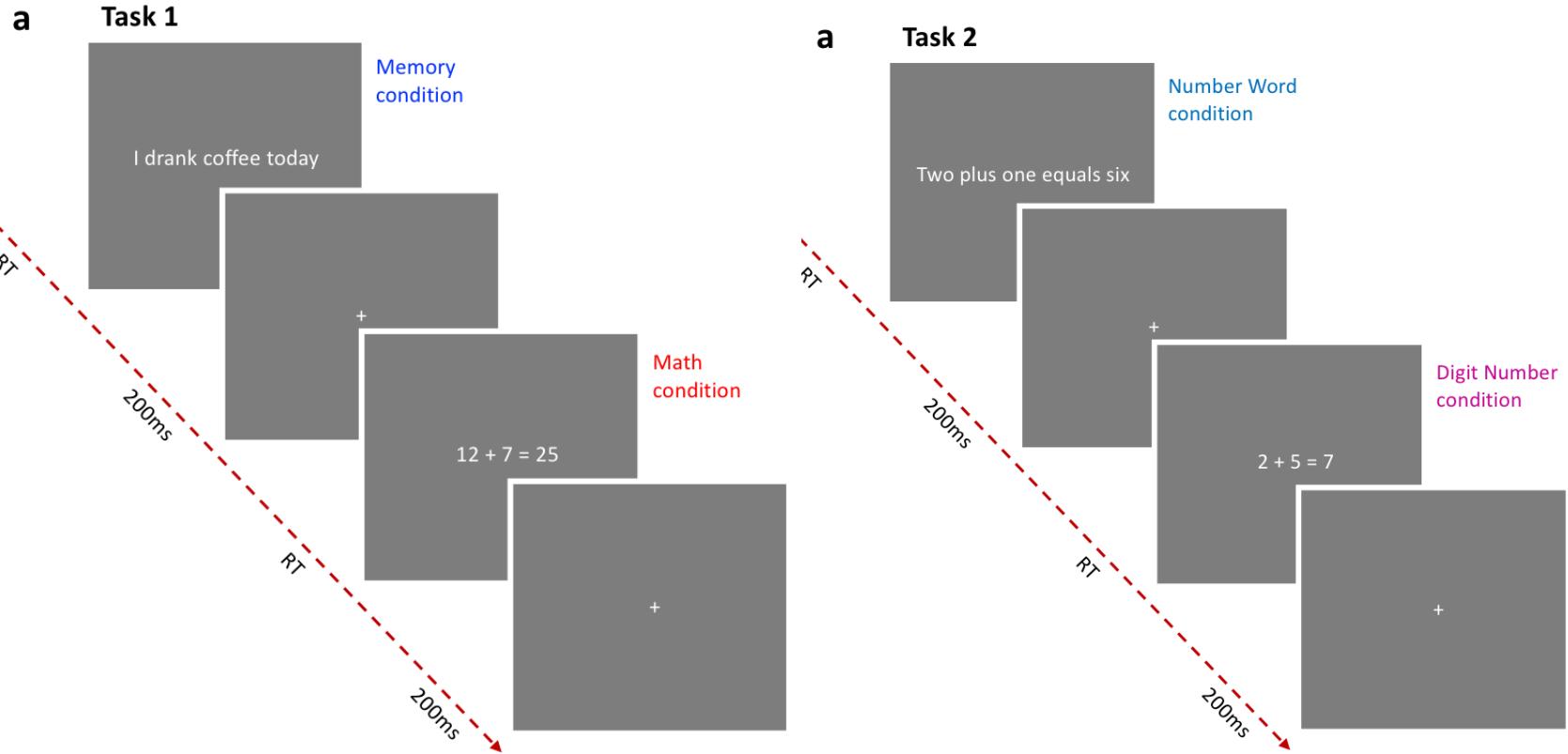


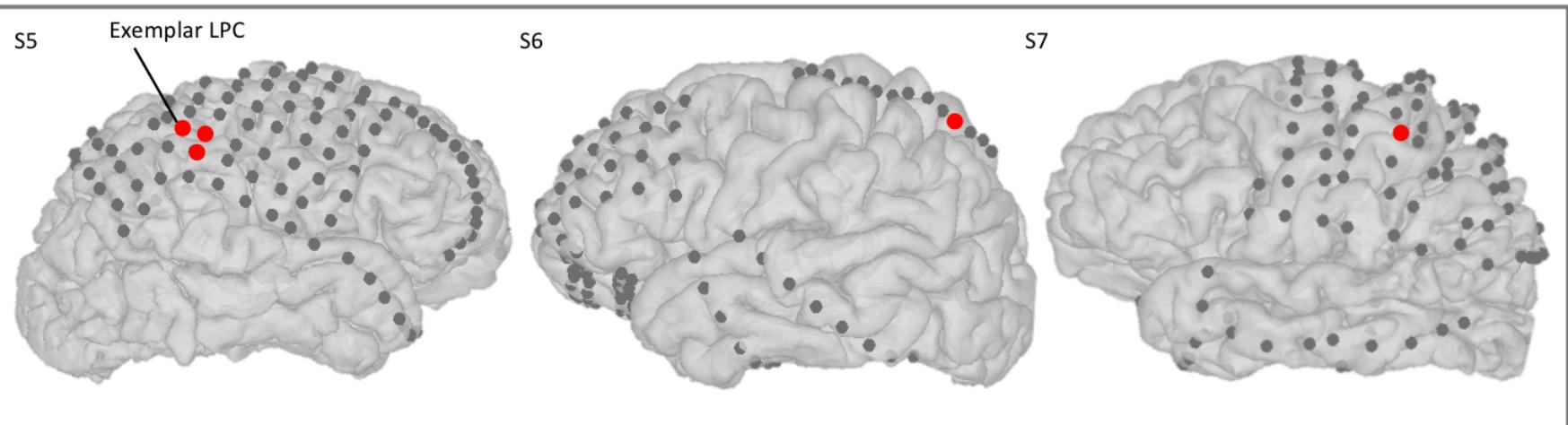
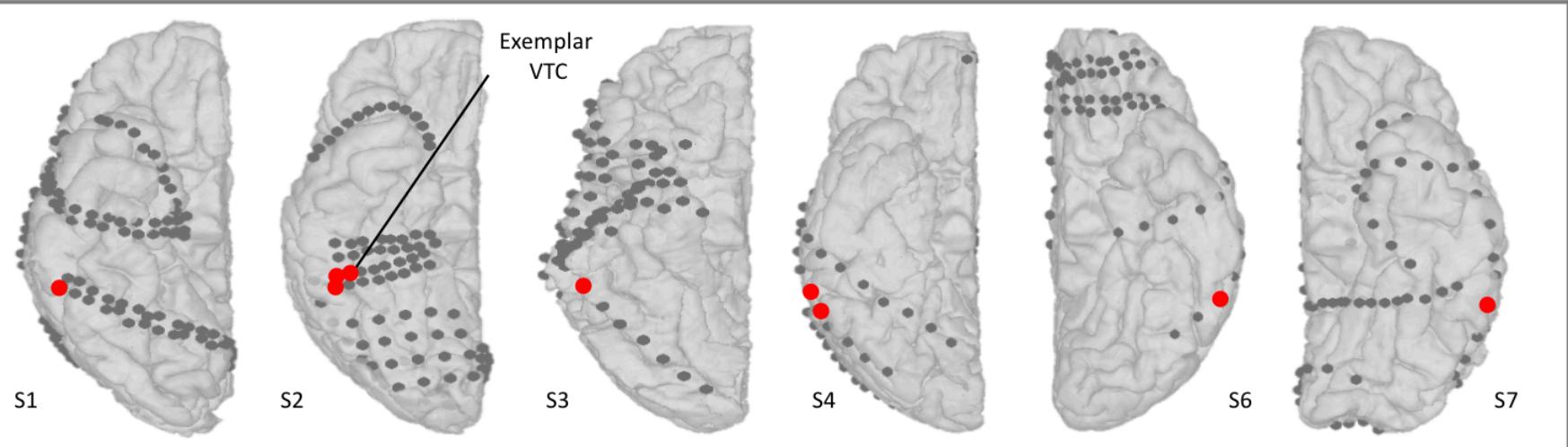
- Decoding in V1 is peaked and classifiers converge to the first 100 ms.
- Decoding in IT is much more persistent.



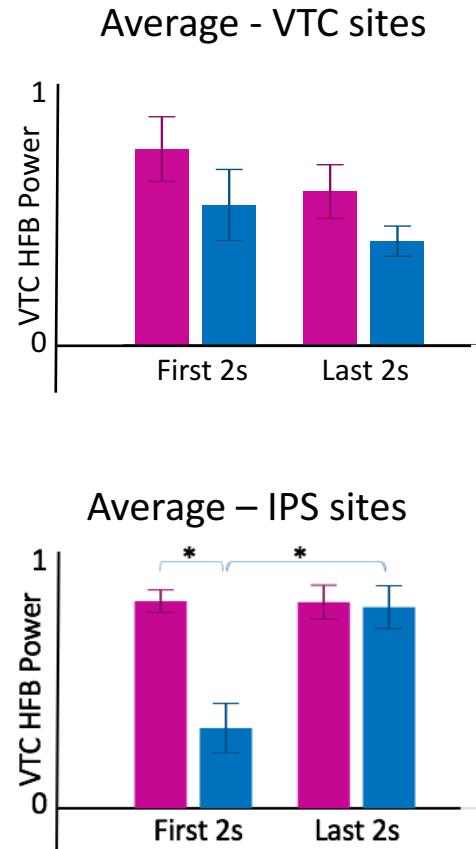
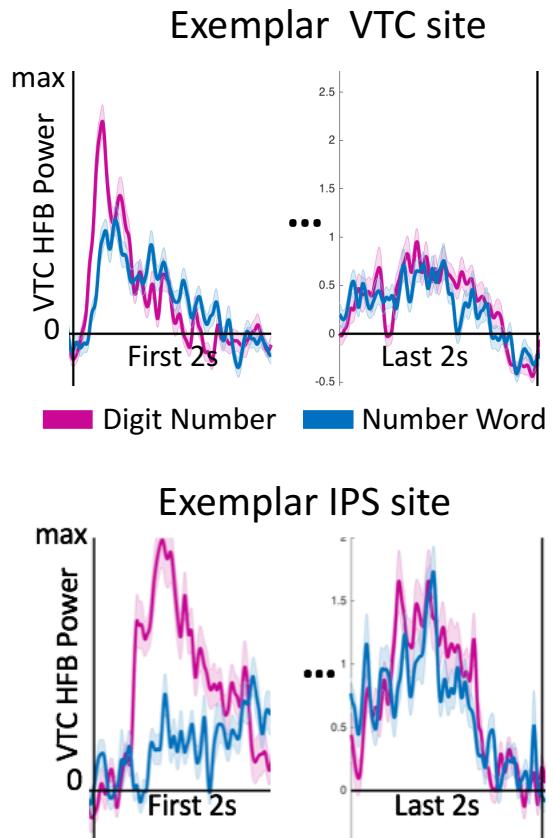
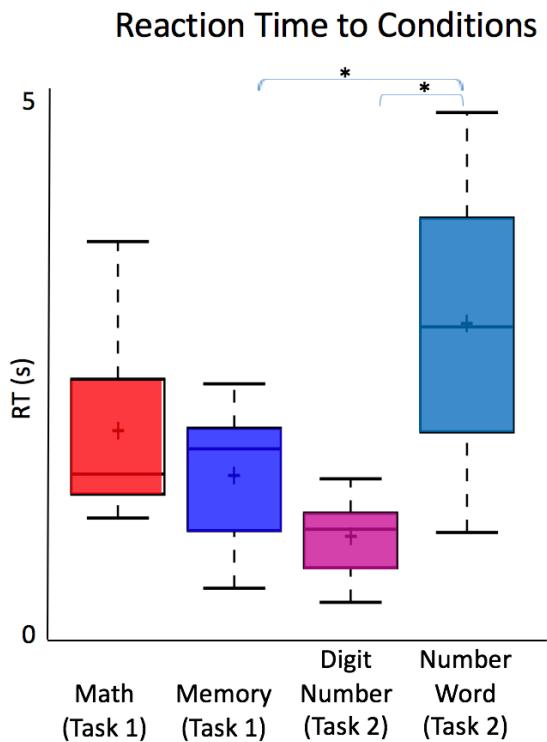
other

Responses to calculations with Arabic numerals and number words in LPC and VTC

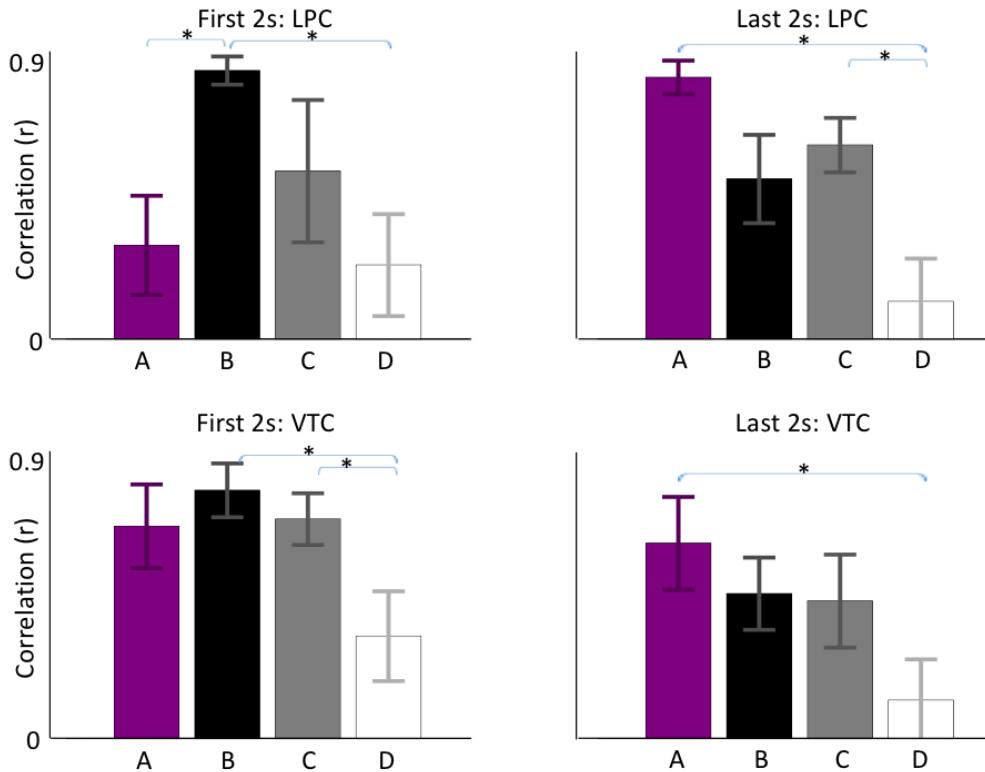




Responses to calculations with Arabic numerals and number words in LPC and VTC

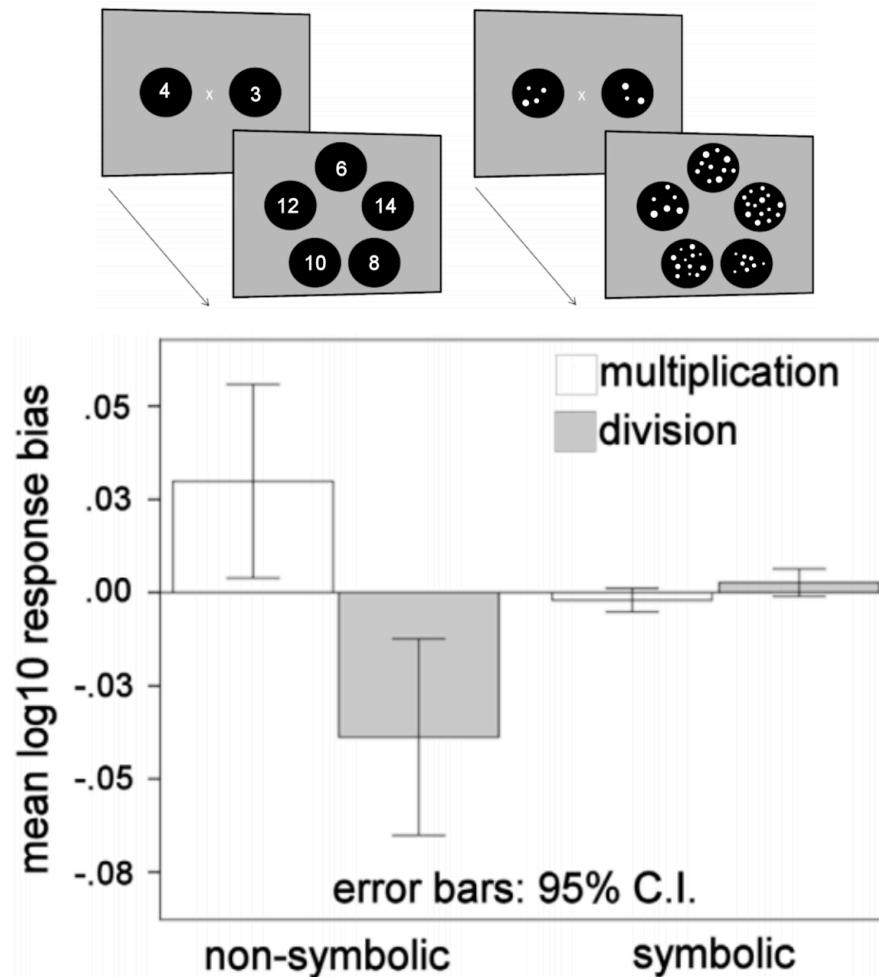


Responses to calculations with Arabic numerals and number words in LPC and VTC

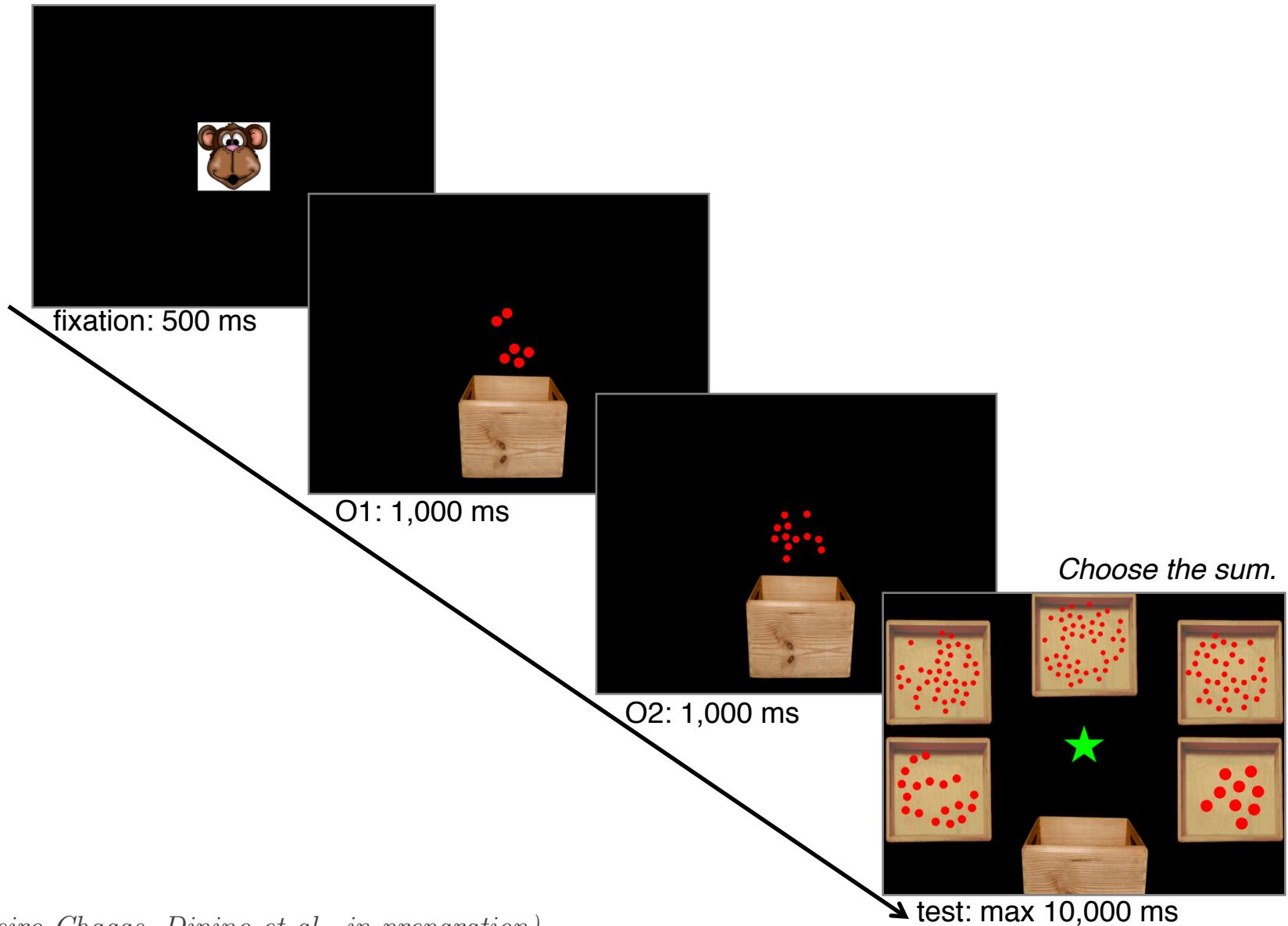


- A: digit number – number word (within task)
- B: digit number – digit number (across task)
- C: digit number – number word (across task)
- D: digit number – non-number (across task)

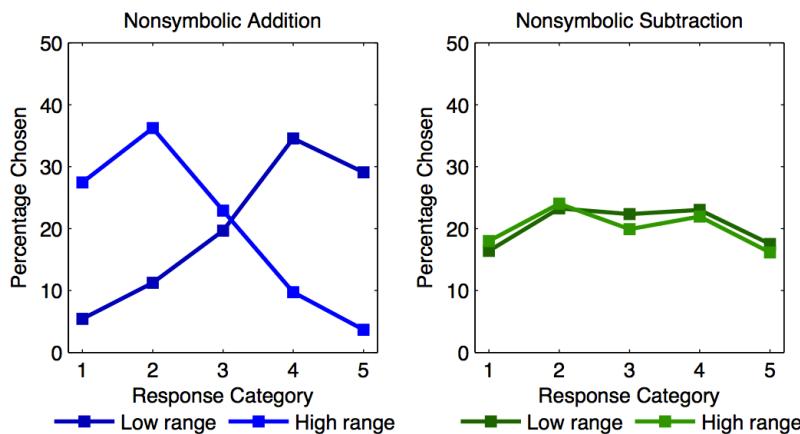
OM multiplication and division: only in non-symbolic notation



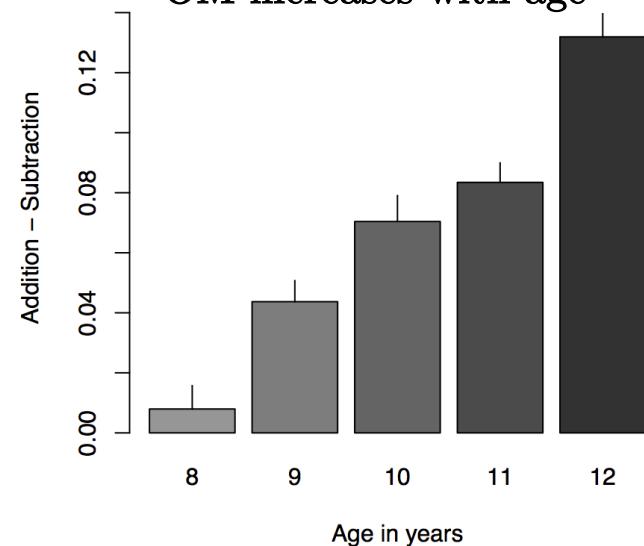
Development of the OM effect – Experimental Design



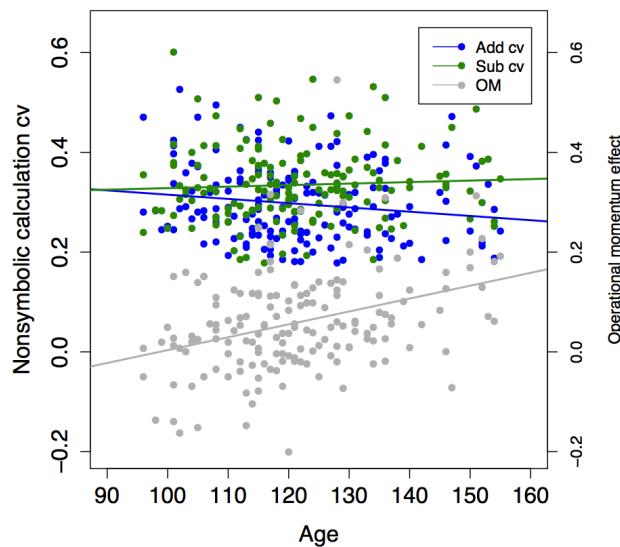
Development of the OM effect



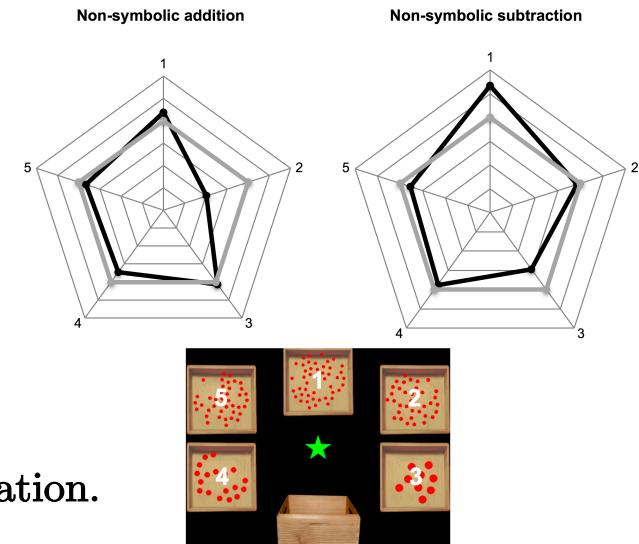
OM increases with age



Not a by-product of decrease in accuracy



Dissociates from SOAR in children



- Does not correlate with non-symbolic comparison and estimation.

(Pinheiro-Chagas, Dinino et al., in preparation)

Chapter 5. General Discussion

- Trajectory tracking can dissect the calculation process, revealing the absolute timing of some of the **covert stages**
- Serial processing of the **operands**: larger operand **first** independent of its location. The deviation from the larger operand to the correct result unfolds **serially and proportionally** to the size of the **min operand**
- Transient **OM effect** during the **integration of min**: visuospatial attention system actively engaged during the calculation
- Supports a model whereby **additions** and **subtractions** are computed by a **stepwise displacement on the mental number line**
Compatible with automated procedures and fact retrieval based on a tabular search
- What is the **precise mechanism** of this **serial processing**? Children slower, adults faster. How does learning or procedure automatization happen?
Modelling work with Thomas Hannagan

Chapter 5. General Discussion

- IPS and SPL activity increase with arithmetic **problem-size**: engaged in the calculation mechanism *per se* and might index the accumulation of evidence to achieve a decision
- Surprising role of pITG in mental arithmetic beyond digit recognition: higher activity for smaller/easier problems
Early identification of problem difficulty (semantic evidence?)
- Re-evaluation of neurocognitive models of arithmetic and developmental dyscalculia: pITG as an **important hub for calculation**
- Expands the classical view of the VTC: contains regions specifically involved in **sophisticated symbolic forms of reasoning**, such as mental arithmetic
- Does pITG process magnitude? How do pITG and IPS interact? Does IPS integrates the activity of pITG? Is this process controlled by PFC? What is the role of subcortical structures? *Postdoc directions with Josef Parvizi*

Chapter 5. General Discussion

- Time resolved MPVA applied to MEG: first comprehensive picture of the unfolding processing stages underlying calculation at a single-trial level
- Decoding of **operand 1**: **visual dimension**; **operand 2**: visual and **magnitude** dimensions; Possibly sharing a common code with operation type? Ultimately grounded in a basic mechanism of the orienting of spatial attention?
- Fast and highly overlapping dynamics at the decision stage
- Where, how and when is the internal result computed?
 - Internally generated code: '*silent states*', rare gamma bursts, sparse code?
Hard to capture with MEG
- New experiments with iEEG - *Stanford-Unicog* collaboration
- Beyond numbers: the **syntactic structure** of **arithmetic** expressions (*with Dror*)

Questions

Can the + sign as fixation explain the transient processing of the absolute value of the smaller operand in subtractions?