

Recursive Partitioning

Practical Machine Learning (with R)

UC Berkeley

Fall 2015



Topics

- ➔ Review and Expectations
- ➔ Project Work and Questions
- ➔ New Topics



REVIEW AND EXPECTATIONS



REVIEW AND EXPECTATION

- ➔ Use resampling techniques to calculate error rates (–or– any statistics)
 - Evaluating model performance is not the same thing as training. They are separate processes
 - Differences between repeated splitting, k-fold cross-validation and bootstrap
- ➔ Create, edit Rmarkdown documents using Rstudio and knitr



REVIEW AND EXPECTATION

- ➔ Use model formula to specify interaction effects and more complex relationships between predictors and response variables
- ➔ Nearest neighbor methods (briefly)
- ➔ Understand Bias Variance Trade-off



REVIEW AND EXPECTATION

- ➔ Definitions for all the binomial performance measurements: accuracy, error rate, TP, FP, TN, FN, Type I Error, Sensitivity, Specificity, Recall, True Error





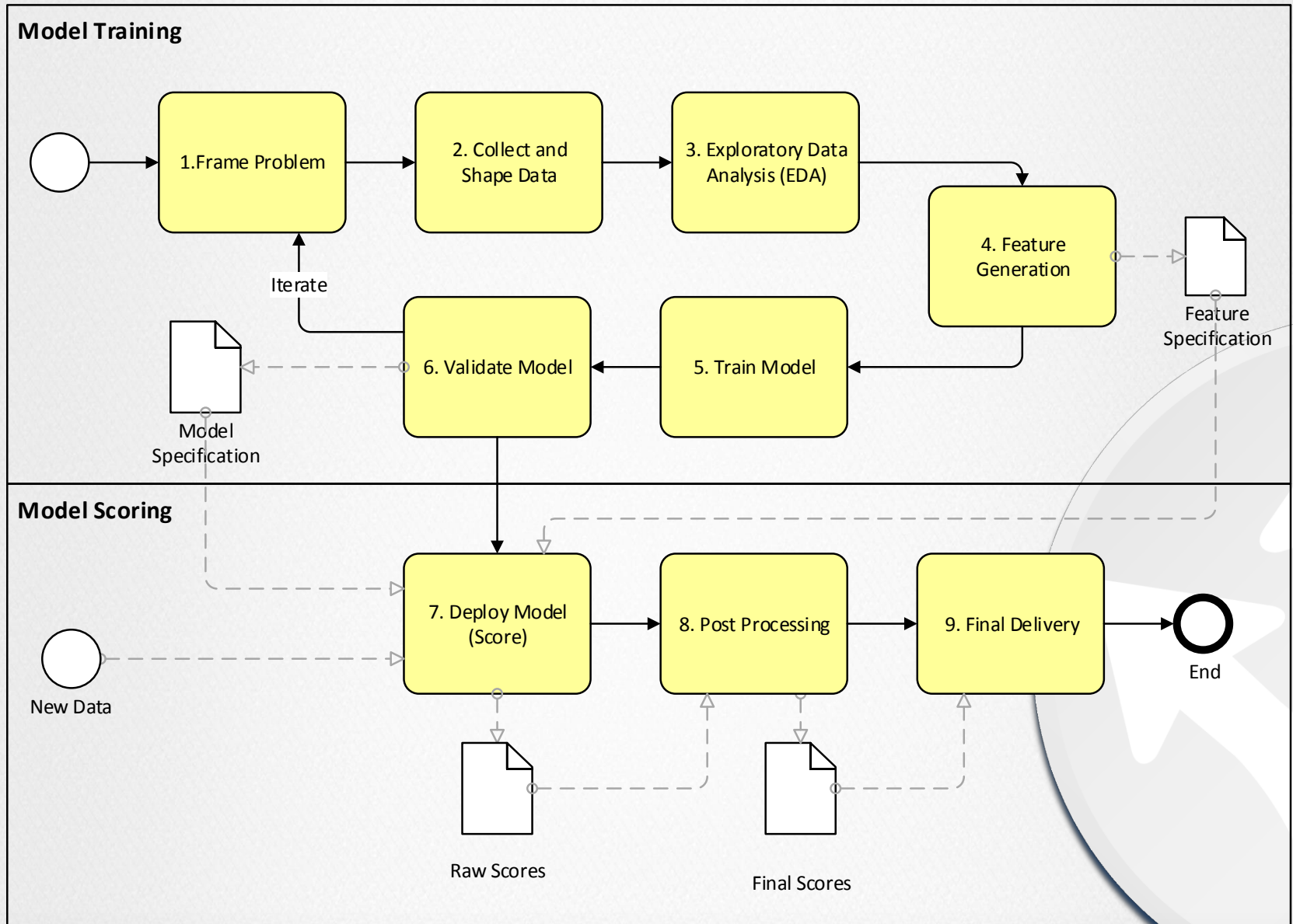
QUESTIONS



QUIZ



Comprehensive ML Process



ASSIGNMENT FROM LAST LECTURE: RESAMPLING



NEW TOPICS



MULTI-CLASS PERFORMANCE



TERMS

- ⇒ Kappa Statistic,
 - ⇒ S-Statistics, F-Statistic
-



DECISION TREES / RECURSIVE PARTITIONING



LINEAR METHODS: LIMITATIONS

Advantages

➔ ...

➔ ...

Disadvantages

➔ ...

➔ ...

➔ ...



LINEAR METHODS: LIMITATIONS

Advantages

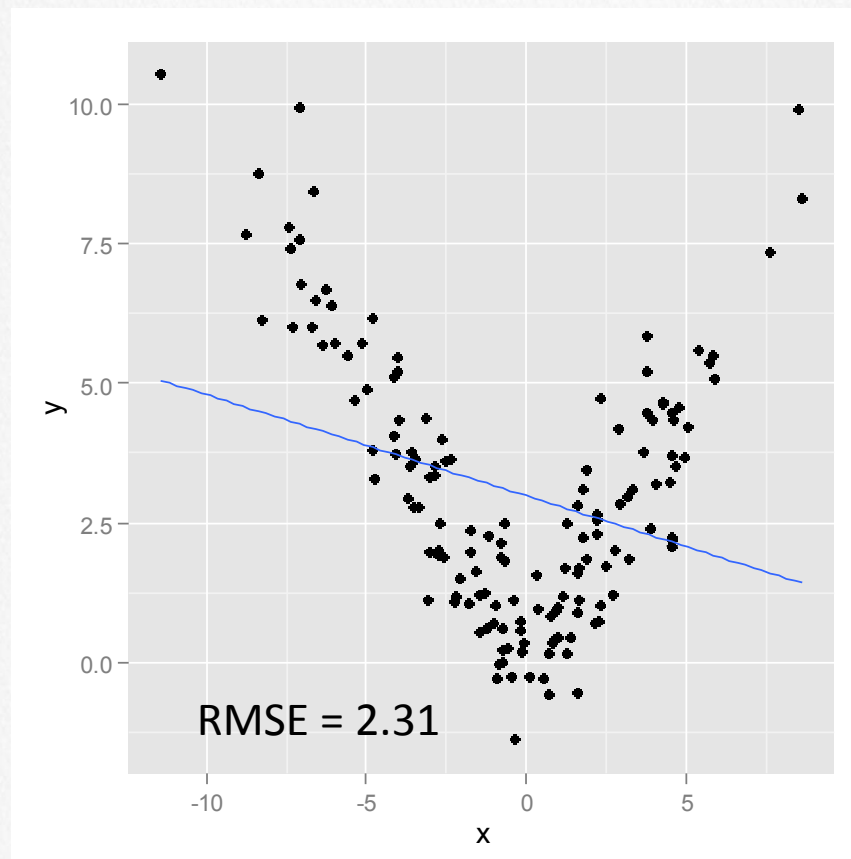
- ⇒ Interpretable
- ⇒ Easy to train

Disadvantages

- ⇒ Logistic regression: multiclass problems
- ⇒ Highly sensitive to inputs
- ⇒ Linear functions →
do not model real data well



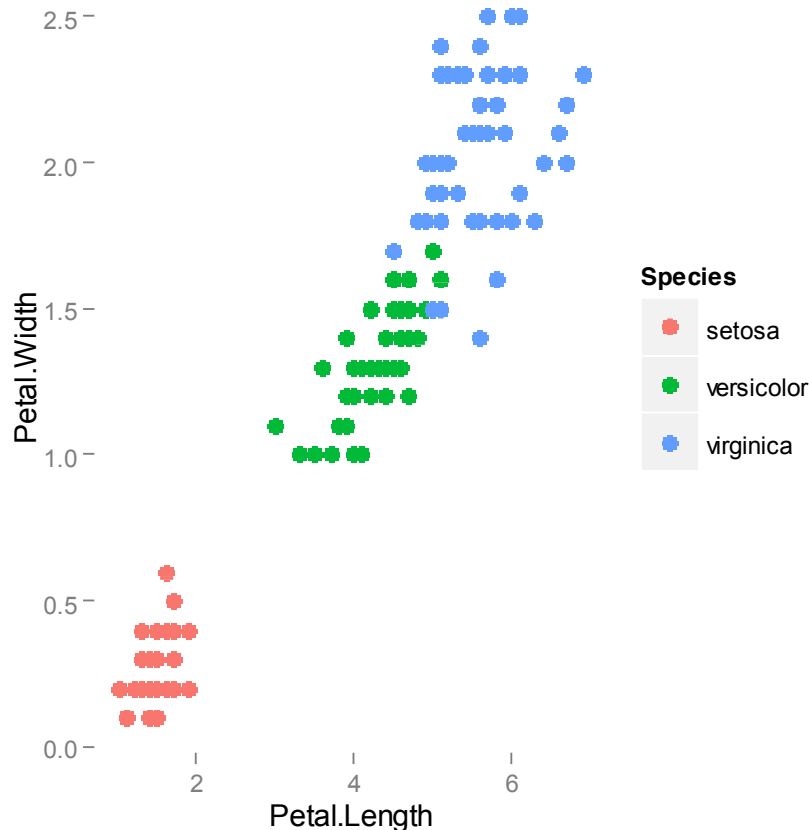
Linear Models: abs



A Simple Example

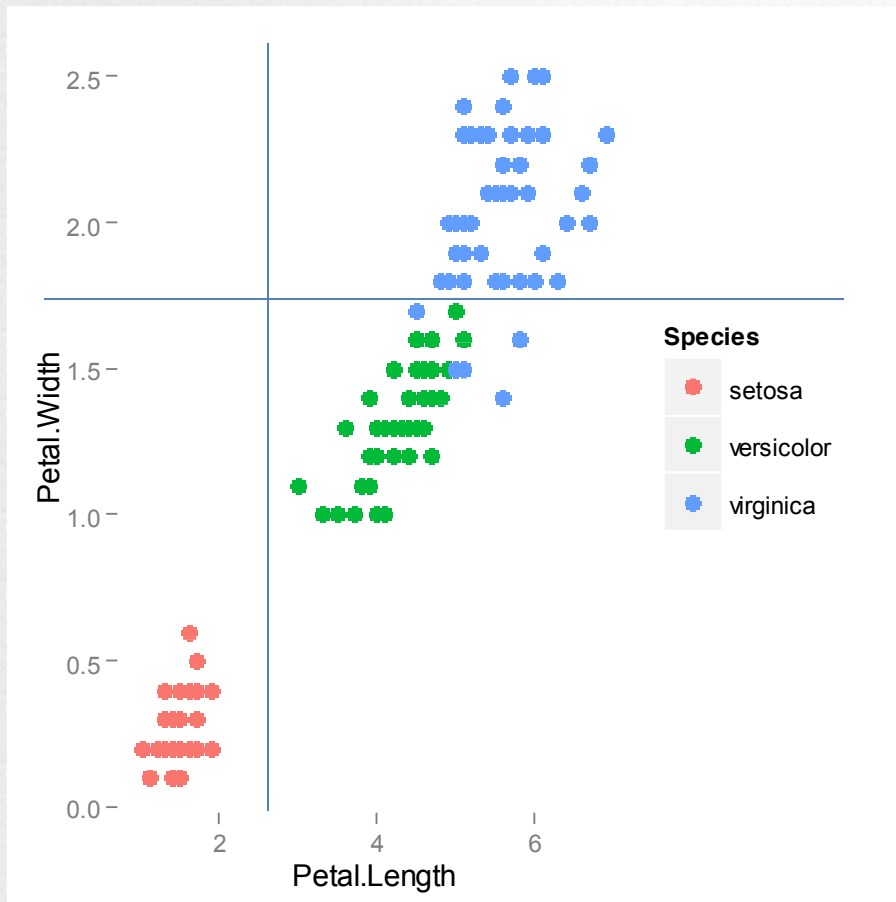
Partitioning Requirements

- ➔ **Restricted Class of Functions**
 - First order propositional logic (for partitions)
 - Aggregation (for outcomes)
- ➔ **Error Methods**
 - Normal error calculations
- ➔ **Search Methods**
 - Recursion



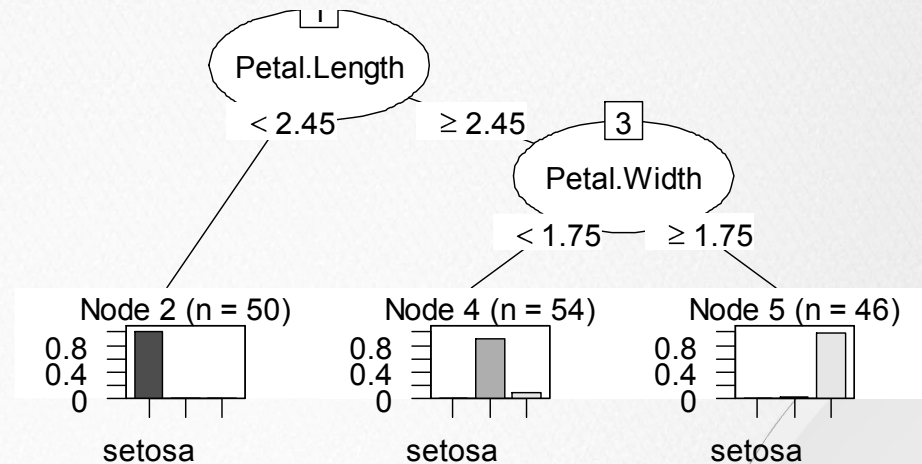
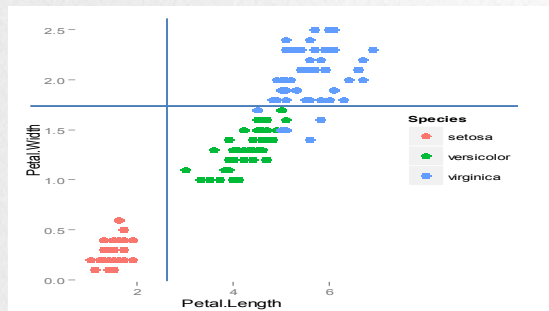
A Simple Example

Partitioning Requirements



SOME NOTES

Splitting by planes is the same as a tree



Partitions define a rule*

- Rules can be associated with outcomes → aggregation method

Trees always partition “all of of space”

Partition Goal:

**PARTITION INPUT SO THAT THE
RESULTING SMALLER GROUPS ARE
MORE HOMOGENEOUS**



Splitting on Categorical Variable

- ➔ Select “metric”
- ➔ For each categorical variable
 - Find
 $\operatorname{argmin}_{s \in S} (\sum_{S_i} \text{err}_i), i = 1..2$
- ➔ Calculate:
 - $\sum_{S_i} \text{err}_i$
- ➔ Metric (e.g.)
 - misclassification rate etc.
 - *Gini index*



SPLITTING ON CONTINUOUS VARIABLE

- ⇒ Determine Metric
- ⇒ Order data
 - If metric is a “cumulative” function calculate as cumulative function:

e.g. $FPR = \text{cumsum}(FP) / \text{cumsum}(TN + FP)$

- Otherwise calculate at all possible split points or subset of split points

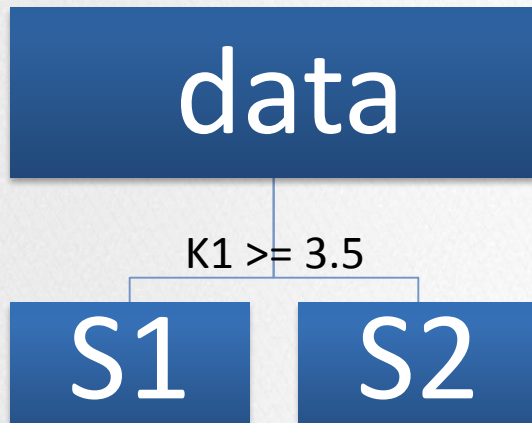
$$\text{argmin}_{x=n} \left(\sum_{i=1..2} \text{err}_i \right)$$



data

Choose the split that
minimizes the error
 $\operatorname{argmin}_S(\text{Error})$

Ordinal							
Categorical			Continuous				
K1	K2	K3	V1	V2	V3	V4	V5
E_{K1}	E_{K2}	E_{K3}	E_{V1}	E_{V2}	E_{V3}	E_{V4}	E_{V5}



Choose the split that
minimizes the error
 $\operatorname{argmin}_S(\text{Error})$

REPEAT WITH S1 AND S2

* Very often predictor will be used again.

Ordinal							
Categorical			Continuous				
K1	K2	K3	V1	V2	V3	V4	V5
E_{K1}	E_{K2}	E_{K3}	E_{V1}	E_{V2}	E_{V3}	E_{V4}	E_{V5}

Tree Method Advantages I

- ➔ Highly interpretable
- ➔ Easy to implement (even in SQL)
- ➔ Handle many predictors (sparse, skewed, continuous, categorical) --> little need to pre-process them
- ➔ Non-parametric: do not require specification of predictor-response relationship



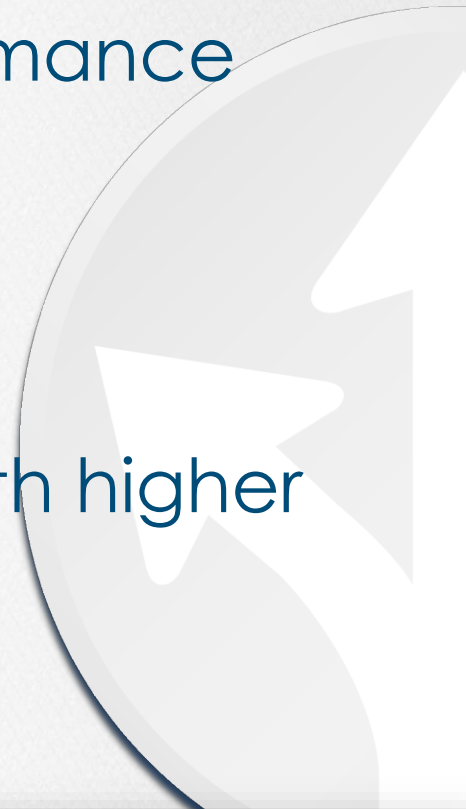
Tree Method Advantages I

- Inherent method for handling missing data
- Trees insensitive to monotonic (order-preserving) transformation of inputs
 - 2^x
 - No use in scaling and centering
- Intrinsic feature selection
- Computational simple and quick



TREE DISADVANTAGES

- ➔ Model instability (sensitive to data)
 - Derives from each subsequent split is dependent on prior splits
- ➔ Less than optimal predictive performance
 - Rectangular regions
- ➔ Limited number of outcome values
- ➔ Selection bias toward predictors with higher number of distinct values
- ➔ Tuning parameter



RPART EXAMPLE



CARET



Caret

- ➔ “Misc functions for training and plotting classification and regression models.”
- ➔ Really:
 - Wraps 100's of modeling functions
 - Automates tediousness of model building
 - Manages a process
- ➔ Competitors:
 - [mlr](#) (machine learning with R): task focused
 - [Rattle](#) : Graham Williams et al. / Togaware.com
 - [R Commander](#) : Statistical workbench



Caret Goals

Does a couple things:

- evaluate, using resampling, the effect of model tuning parameters on performance
- choose the “optimal” model across these parameters
- estimate model performance from a training set
- Variable Importance
- Aids feature selection



Process

```
1 Define sets of model parameter values to evaluate
2 for each parameter set do
3   for each resampling iteration do
4     Hold-out specific samples
5     [Optional] Pre-process the data
6     Fit the model on the remainder
7     Predict the hold-out samples
8   end
9   Calculate the average performance across hold-out predictions
10 end
11 Determine the optimal parameter set
12 Fit the final model to all the training data using the optimal parameter set
```

LOTS OF CONFIGURATIONS

- ⇒ Easy if you know what you are doing
- ⇒ which method?

Caret Model List*

- ⇒ Controlled mostly through
 - `train`
 - `trainControl`



APPENDIX



data

Ordinal							
Categorical			Continuous				
K1	K2	K3	V1	V2	V3	V4	V5



EXAMPLE OF ML ALGORITHM(S)

- ⇒ Spam Filter
- ⇒ handwriting recognition (svm)
- ⇒ Traffic engineering (lights)
- ⇒ Weather prediction
- ⇒ Sentiment analysis (social media)
- ⇒ Netflix Recommender
- ⇒ Fraud detection (Visa)
- ⇒ Imaging processing
- ⇒ (network) Intrusion detection
- ⇒ Self-driving cars



COMPARISON OF MODELS (CHART)



TRANSFORMATIONS

- Centering and Scaling: `scale`*
- Resolve skewness: `log`, `sqrt`, `inv`
- Resolve outliers: `spatial sign`, `PCA`

Some algorithms require scaling

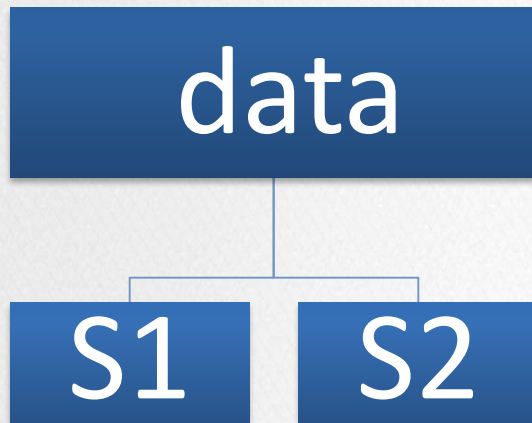
Some are insensitive

Time consuming

Somewhat of an art

- Genetic algorithms (GA)





N1	N2	N3	V1	V2	V3	V4	V5

X_1

