## Project

## August 12, 2025

# 1 Association Between Final Grade in Math and Family/Social Life Aspects of Students in Secondary Education in Portugal -Research Paper

## 1.1 Introduction

The dataset "Student Performance" created by Paulo Cortez and Alice Silva was collected during the 2005-2006 school year from the public schools Gabriel Pereira and Mousinho da Silveira in Portugal, consisting of 395 observations. In total, there are 32 explanatory variables and the response variable: the final grade of a participant in Mathematics. It has both continuous and categorical attributes and addresses classification tasks.

Our group will focus on students' performance, particularly in mathematics, in secondary education where information such as personal, family, and school aspects were collected using school reports and questionnaires.

**Research Question**: Which aspects of family and social life are significantly associated with the final grade in Mathematics?

To answer this question, we will examine ten possible covariates that may affect a student's final grade in mathematics. This data can be accessed from ttps://archive.ics.uci.edu/dataset/320/student+performance

Reference: Cortez, P., & Silva, A. M. G. (2008). Using data mining to predict secondary school student performance. In A. Brito, & J. Teixeira (Eds.), Proceedings of 5th Annual Future Business Technology Conference, Porto, 5-12.

| Variable                 | Unit  | Values   |
|--------------------------|-------|--|
| sex: student's sex       | NA    | 'F' = female; 'M' = male                                     |
| age: student's age       | years | integers from 15 to 22                                       |
| Pstatus: parent's        | NA    | T' = living together; A' = apart                             |
| cohabitation status      |       |  |
| Medu: mother's education | NA    | 0 = none; 1 = primary education (4th grade); 2 =             |
|                          |       | (5th to 9th grade); $3 = \text{secondary education}$ ; $4 =$ |
|                          |       | higher education   |
| Fedu: father's education | NA    | 0 = none; 1 = primary education (4th grade); 2 =             |
|                          |       | (5th to 9th grade); $3 = \text{secondary education}$ ; $4 =$ |
|                          |       | higher education   |

| Variable                               | Unit | Values  |
|--|------|---|
| activities: extracurricular activities | NA   | 0 = no; 1 = yes                                     |
| freetime: free time after school       | NA   | from $1 = \text{very low to } 5 = \text{very high}$ |
| absences: number of school absences    | NA   | 0 to 93   |
| G1: first period grade                 | NA   | 0-20  |
| G2: first period grade                 | NA   | 0-20  |

Table 0.1: List of Variable Names

## 1.2 Methods

Our objective is to find the covariates that best explain a student's final grade. The measures we will take to do this are as follows: 1. Read in and tidy the dataset: After loading in the dataset, it must be tidied. 2. Visualize the dataset: Create some simple scatterplots and boxplots to understand potential relationships between variables. 3. Residual Plots and Normality Plots: Validate Assumptions. 4. Discussion of results.

## 1.3 Analysis

## 1.3.1 Dataset and Analysis Preparation

```
[1]: install.packages("leaps") # Run this if an installation of leaps is required install.packages("patchwork") # Run this if an installation of Patchwork is required
```

Installing package into '/home/jupyter/R/x86\_64-pc-linux-gnu-library/4.4' (as 'lib' is unspecified)

Installing package into '/home/jupyter/R/x86\_64-pc-linux-gnu-library/4.4' (as 'lib' is unspecified)

Warning message in install.packages("patchwork"):
"installation of package 'patchwork' had non-zero exit status"

```
[4]: library(leaps)
    library(tidyverse)
    library(dplyr)
    library(car)
    library(MASS)
    library(ggplot2)
    library(patchwork)
    options(repr.plot.width=12, repr.plot.height=5)
    set.seed(1234)
```

```
[5]: studentData <- read.table("student-mat.csv", sep=";", header=TRUE) head(studentData)
```

```
school
                                      sex
                                                age
                                                         address
                                                                    famsize
                                                                               Pstatus
                                                                                          Medu
                                                                                                   Fedu
                                                                                                             Mjob
                            <chr>
                                                         <chr>
                                                                    <chr>
                                                                               <chr>
                                                                                          <int>
                                      <chr>
                                                <int>
                                                                                                   <int>
                                                                                                             < chr >
                            GP
                                      \mathbf{F}
                                                18
                                                         U
                                                                    GT3
                                                                               Α
                                                                                          4
                                                                                                   4
                                                                                                             at home
                            GP
                                      F
                                                         U
                                                                               Τ
                                                17
                                                                    GT3
                                                                                          1
                                                                                                   1
                                                                                                             at_home
A data.frame: 6 \times 33
                            GP
                                      \mathbf{F}
                                                         U
                                                                               T
                                                                                          1
                                                                                                   1
                                                15
                                                                    LE3
                                                                                                             at home
                                                         U
                                                                                                   2
                            GP
                                      \mathbf{F}
                                                15
                                                                    GT3
                                                                               Τ
                                                                                          4
                                                                                                             health
                        5
                            GP
                                      \mathbf{F}
                                                16
                                                         U
                                                                    GT3
                                                                               Τ
                                                                                          3
                                                                                                   3
                                                                                                             other
                        6
                            GP
                                      Μ
                                                16
                                                         U
                                                                    LE3
                                                                               Τ
                                                                                          4
                                                                                                   3
                                                                                                             services
```

```
[6]: # Extract the explanatory terms and the response studentData <- studentData[, c('sex', 'age', 'Pstatus', 'Medu', 'Fedu', □ ⇔'activities', 'freetime', 'absences', 'G1', 'G2', 'G3')]
```

```
[7]: # Check for missing data to handle sum(is.na(studentData))
```

0

We also want to distinguish each variable as numeric or a factor in this study. Sex, Pstatus, and activities are factors due to their binary nature. Medu and Fedu are decided to be factors since they use numbers to represent categorical education levels. Freetime is a rating system, but is numeric due to its ordinal nature. Age, absences, G1, G2, and G3 are numeric in nature.

```
[8]: studentData <- studentData %>%
    mutate(sex = as.factor(sex),
        age = as.numeric(age),
        Pstatus = as.factor(Pstatus),
        Medu = as.factor(Medu),
        Fedu = as.factor(Fedu),
        activities = as.factor(activities),
        freetime = as.numeric(freetime),
        absences = as.numeric(absences),
        G1 = as.numeric(G1),
        G2 = as.numeric(G2),
        G3 = as.numeric(G3))
    head(studentData)
```

|                             |   | sex         | age      | Pstatus  | Medu     | $\operatorname{Fedu}$ | activities | freetime | absences | G1       |
|-----------------------------|---|-------------|----------|----------|----------|-----------------------|------------|----------|----------|----------|
|                             |   | <fct></fct> | <dbl $>$ | <fct $>$ | <fct $>$ | <fct $>$              | <fct $>$   | <dbl $>$ | <dbl $>$ | <dbl $>$ |
| A data.frame: $6 \times 11$ | 1 | F           | 18       | A        | 4        | 4                     | no         | 3        | 6        | 5        |
|                             | 2 | F           | 17       | ${ m T}$ | 1        | 1                     | no         | 3        | 4        | 5        |
|                             | 3 | F           | 15       | ${ m T}$ | 1        | 1                     | no         | 3        | 10       | 7        |
|                             | 4 | F           | 15       | ${ m T}$ | 4        | 2                     | yes        | 2        | 2        | 15       |
|                             | 5 | F           | 16       | ${ m T}$ | 3        | 3                     | no         | 3        | 4        | 6        |
|                             | 6 | M           | 16       | ${ m T}$ | 4        | 3                     | ves        | 4        | 10       | 15       |

### 1.3.2 Preliminary Visualizations and Summaries

Some basic summaries and statistics can be generated with simple R commands.

```
[9]: summary(studentData)

## Number of observations
n <- nrow(studentData)
cat("There are ", n, " observations.")</pre>
```

```
Pstatus Medu
                                         Fedu
                                                                freetime
sex
             age
                                                 activities
F:208
               :15.0
                        A: 41
                                0: 3
                                         0: 2
                                                 no :194
                                                             Min.
                                                                     :1.000
        Min.
M:187
        1st Qu.:16.0
                        T:354
                                1: 59
                                         1: 82
                                                 yes:201
                                                             1st Qu.:3.000
        Median:17.0
                                 2:103
                                                             Median :3.000
                                         2:115
        Mean
               :16.7
                                 3: 99
                                         3:100
                                                             Mean
                                                                     :3.235
        3rd Qu.:18.0
                                 4:131
                                                             3rd Qu.:4.000
                                         4: 96
        Max.
               :22.0
                                                             Max.
                                                                     :5.000
   absences
                        G1
                                         G2
                                                          G3
       : 0.000
                        : 3.00
                                                           : 0.00
Min.
                 Min.
                                  Min.
                                          : 0.00
                                                   Min.
1st Qu.: 0.000
                 1st Qu.: 8.00
                                  1st Qu.: 9.00
                                                   1st Qu.: 8.00
Median : 4.000
                 Median :11.00
                                  Median :11.00
                                                   Median :11.00
       : 5.709
                                          :10.71
                                                           :10.42
Mean
                 Mean
                         :10.91
                                  Mean
                                                   Mean
3rd Qu.: 8.000
                  3rd Qu.:13.00
                                  3rd Qu.:13.00
                                                    3rd Qu.:14.00
Max.
       :75.000
                  Max.
                         :19.00
                                  Max.
                                          :19.00
                                                    Max.
                                                           :20.00
```

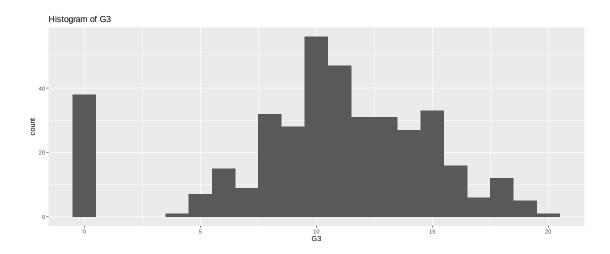
There are 395 observations.

### [10]: str(studentData)

```
'data.frame':
                395 obs. of 11 variables:
             : Factor w/ 2 levels "F", "M": 1 1 1 1 1 2 2 1 2 2 ...
$ sex
             : num 18 17 15 15 16 16 16 17 15 15 ...
$ age
             : Factor w/ 2 levels "A", "T": 1 2 2 2 2 2 1 1 2 ...
$ Pstatus
$ Medu
             : Factor w/ 5 levels "0","1","2","3",...: 5 2 2 5 4 5 3 5 4 4 ...
             : Factor w/ 5 levels "0","1","2","3",..: 5 2 2 3 4 4 3 5 3 5 ...
$ Fedu
$ activities: Factor w/ 2 levels "no","yes": 1 1 1 2 1 2 1 1 1 2 ...
            : num 3 3 3 2 3 4 4 1 2 5 ...
$ freetime
$ absences : num 6 4 10 2 4 10 0 6 0 0 ...
$ G1
             : num 5 5 7 15 6 15 12 6 16 14 ...
$ G2
             : num 6 5 8 14 10 15 12 5 18 15 ...
                   6 6 10 15 10 15 11 6 19 15 ...
$ G3
```

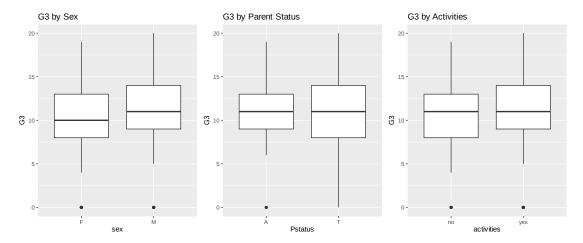
However, these numbers may seem a little cryptic, so we follow with some visualizations that can better describe the data that we are working with.

```
[11]: # Distribution of G3
ggplot(studentData, aes(x = G3)) +
    geom_histogram(binwidth=1) +
    ggtitle("Histogram of G3")
```



This histogram shows an approximately normal distribution about the mean (10.42), despite a number of outliers sitting at the left end of the distribution (with a G3 score of zero).

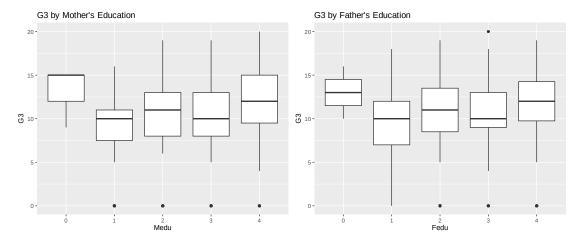
```
[12]: # Boxplots for binary explanatory variables
p1 <- ggplot(studentData, aes(x = sex, y = G3)) +
    geom_boxplot() +
    labs(title = "G3 by Sex")
p2 <- ggplot(studentData, aes(x = Pstatus, y = G3)) +
    geom_boxplot() +
    labs(title = "G3 by Parent Status")
p3 <- ggplot(studentData, aes(x = activities, y = G3)) +
    geom_boxplot() +
    labs(title = "G3 by Activities")
(p1 | p2 | p3)</pre>
```



We can see that the median G3 score is identical among the two different Pstatuses; however,

there is a much larger spread among the scores of those with the "T" Pstatus (which means that the parents are living together). For activities, we also see that the median score is the same for those that with or without extracurricular activities, although it seems that the two boxplots have different tails in their distributions. Finally, for the sex variable, it seems that the distribution is fairly similar, with male students having slightly higher G3 scores overall. There can be confounding variables that affect conclusions made solely based on these visualizations, however.

```
[13]: # Multi-level boxplots for Medu and Fedu factor variables
p4 <- ggplot(studentData, aes(x = Medu, y = G3)) +
    geom_boxplot() +
    labs(title = "G3 by Mother's Education")
p5 <- ggplot(studentData, aes(x = Fedu, y = G3)) +
    geom_boxplot() +
    labs(title = "G3 by Father's Education")
    (p4 | p5)</pre>
```

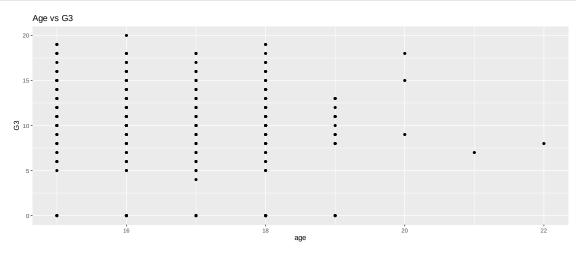


The boxplots comparing G3 scores with the educational levels of both mothers (Medu) and fathers (Fedu) show a general upward trend in G3 as Medu/Fedu scores increase, with the exception of having a Medu or Fedu score of 0 (these individuals seems to have a fairly high G3 score, with lower spread as well). However, the boxplot doesn't show how many responses are in each Medu/Fedu level, which can be slightly misleading.

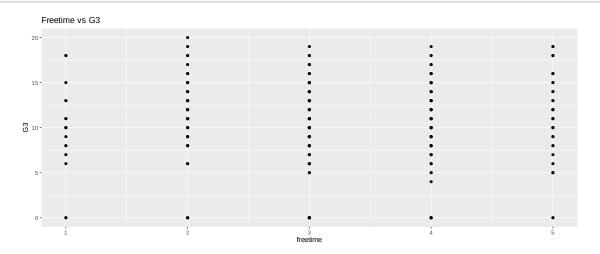
```
[14]: # Scatterplots for numeric data
# Age vs G3
p6 <- ggplot(studentData, aes(x = age, y = G3)) +
    geom_point() +
    ggtitle("Age vs G3")

# Freetime vs G3b
p7 <- ggplot(studentData, aes(x = freetime, y = G3)) +
    geom_point() +
    ggtitle("Freetime vs G3")</pre>
```

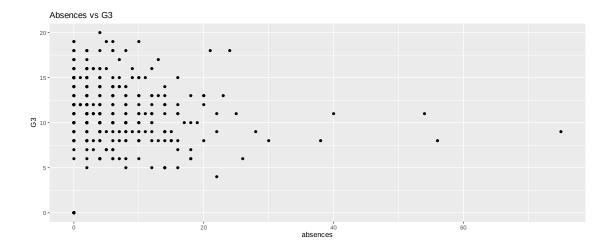
```
# absences vs G3
p8 <- ggplot(studentData, aes(x = absences, y = G3)) +
  geom_point() +
  ggtitle("Absences vs G3")
p6</pre>
```



## [15]: p7



[16]: p8



These scatterplots do not show a clear linear relationship between a singular numeric explanatory variables and G3. We will further explore how a combination of these variables, as well as categorical covariates, may help us draw more thorough conclusions.

## 1.4 Analysis

The initial part of the analysis is to check for correlation among the numeric covariates.

```
[17]: numeric_vars <- c("age", "freetime", "absences", "G1", "G2")
    df_numeric <- studentData[, numeric_vars]

## Correlation check, round to 4 decimals
    cor_matrix <- cor(df_numeric, use = "pairwise.complete.obs")
    round(cor_matrix, 4)</pre>
```

```
age
                                                   freetime
                                                             absences
                                                                        G1
                                                                                  G2
                                   age
                                         1.0000
                                                  0.0164
                                                             0.1752
                                                                        -0.0641
                                                                                  -0.1435
                                         0.0164
                                                  1.0000
                                                             -0.0581
                              freetime
                                                                        0.0126
                                                                                  -0.0138
A matrix: 5 \times 5 of type dbl
                              absences
                                         0.1752
                                                  -0.0581
                                                             1.0000
                                                                        -0.0310
                                                                                  -0.0318
                                    G1
                                         -0.0641
                                                                        1.0000
                                                                                  0.8521
                                                  0.0126
                                                             -0.0310
                                    G2
                                        -0.1435
                                                  -0.0138
                                                             -0.0318
                                                                        0.8521
                                                                                  1.0000
```

It is clear from the correlation matrix that G1 and G2 are highly correlated, which tracks with the literature where the authors state a similar conclusion. For the initial model, we will remove these to estimate the total effect of the selected family and social variables on final grade, G3.

```
[18]: ## Initial Model without G1 and G2
model_initial <- lm(G3 ~ . -G1 -G2, data = studentData)
summary(model_initial)</pre>
```

```
Call:
lm(formula = G3 ~ . - G1 - G2, data = studentData)
```

### Residuals:

```
Min 1Q Median 3Q Max -12.7259 -2.0180 0.4977 2.9607 10.0940
```

#### Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
(Intercept)
               23.51051
                           5.15272
                                      4.563 6.82e-06 ***
sexM
                0.83440
                           0.46835
                                      1.782
                                               0.0756 .
age
               -0.47869
                           0.18504
                                     -2.587
                                               0.0101 *
PstatusT
               -0.46287
                           0.76034
                                     -0.609
                                               0.5430
Medu1
               -4.52803
                           2.65965
                                     -1.702
                                               0.0895
Medu2
               -3.70281
                           2.62965
                                     -1.408
                                               0.1599
Medu3
               -3.29692
                           2.65134
                                     -1.243
                                               0.2145
Medu4
               -2.00099
                           2.66975
                                     -0.750
                                               0.4540
               -2.04376
Fedu1
                           3.23259
                                     -0.632
                                               0.5276
Fedu2
               -1.84011
                           3.22027
                                     -0.571
                                               0.5681
Fedu3
                           3.22158
                                     -0.587
                                               0.5576
               -1.89106
Fedu4
               -1.81772
                           3.22532
                                    -0.564
                                               0.5734
activitiesyes -0.19460
                           0.46462
                                     -0.419
                                               0.6756
freetime
               -0.04186
                           0.23357
                                     -0.179
                                               0.8578
absences
                0.02867
                           0.02936
                                      0.976
                                               0.3295
```

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.457 on 380 degrees of freedom

Multiple R-squared: 0.0873, Adjusted R-squared: 0.05368

F-statistic: 2.596 on 14 and 380 DF, p-value: 0.001347

This model is a poor fit for the data, as the adjusted R-squared value (0.05368) indicates that a very low portion of the variance in G3 is explained by family and social covariates even when controlling for age and sex. Additionally, the magnitudes of the standard errors are high relative to the estimates, given that only 5.5% of the variation in G3 is explained.

At 5% significance, age is the only significant covariate here. - For age, it suggests that older students are associated with lower G3 scores holding all other variables constant.

We observe that for every covariate, the magnitude of their association to final grade in Mathematics (G3) appears relatively small (all less than 1 in either direction). It may indicate that family and social variables of a student have little to no practical significance on their final grade in Math, but it may also indicate a presence of collinearity in other covariates which are not numerical.

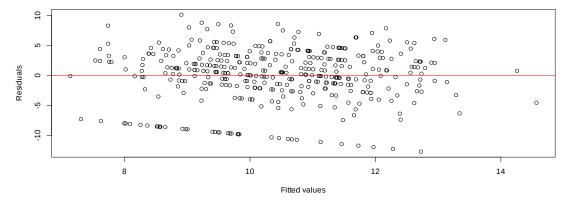
A Variance Inflation Factor (VIF) check was conducted to check for any issues there.

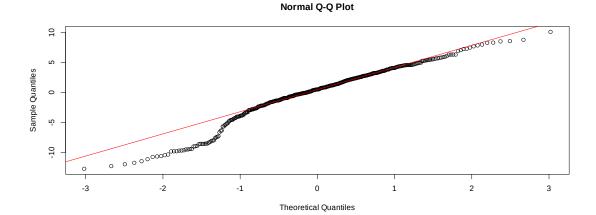
```
[19]: ## VIF check
  vif_values <- round(vif(model_initial), 4)
  vif_values_table <- data.frame(vif_values)
  vif_values_table</pre>
```

|   | GVIF                                      | Df   | GVIF12.Df  |
|---|---|--|--|
|   | <dbl $>$                                  | <dbl $>$   | <dbl $>$   |
| $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | 1   | 1.0428   |  |
|   | 1.0516                                    |  |  |
| Pstatus   | 1.0695                                    | 1  | 1.0342   |
| Medu  | 2.0453                                    | 4  | 1.0936   |
| Fedu  | 1.9808                                    | 4  | 1.0892   |
| activities  | 1.0729                                    | 1  | 1.0358   |
| free time   | 1.0797                                    | 1  | 1.0391   |
| absences  | 1.0950                                    | 1  | 1.0464   |
|   | age Pstatus Medu Fedu activities freetime | sex 1.0874 age 1.1059 Pstatus 1.0695 Medu 2.0453 Fedu 1.9808 activities 1.0729 freetime 1.0797 | sex       1.0874       1         age       1.1059       1         Pstatus       1.0695       1         Medu       2.0453       4         Fedu       1.9808       4         activities       1.0729       1         freetime       1.0797       1 |

The VIF values do not surpass the threshold of 5, so there are no causes for concern of multicollinearity. However, it is clear that the initial model does not explain the variation of G3 very well. we should check the residuals and q-q plots to check if the assumptions for the linear model hold.

### **Residual Plot**





We note that independence is satisfied assuming that each observation represents a student and no repeated measurements were taken by the authors.

Looking at the residual plot: - We see that the residuals span a large range extending from about -10 to 10; large considering that the G3 scale ranges from 0 to 20. - There are no signs of curvature in the residuals so linearity is relatively satisfied here, but the spread is not even across the range of fitted values, perhaps some signs of non-constant variance there. - Although the residuals appear to form very straight line patterns, this is due to the response variable being discrete with integer grades so there are no causes of concern there.

Looking at the qq-plot: - Most of the residuals between -1 to 1 of the theoretical quantile reasonably fit the reference line. - The tails deviate below the reference line, so the plot is negative skewed. It indicates that the model overestimated students' final grades in Math, more evidence supporting that factors other than family and social variables are more strongly associated to their performance. - Considering the size of the sample (n = 395), the Central Limit Theorem implies that the sampling distribution of the estimated coefficients are approximately Normal, so normality is satisfied here.

Overall, we indicate that there is some non-constant variance in the residuals but the model satisfies linearity, normality, and independence.

Although we understand that the initial model now supports the conclusion that family and social variables have little to no association with Math final grade, we want to explore what other variables in the dataset ARE more associated. This time, we will fit another linear model including G1 and G2, as the authors signal that G3 is strongly correlated with G1 and G2.

```
[21]: ## Full Model including G1 and G2
model_full <- lm(G3 ~., data = studentData)
summary(model_full)</pre>
```

```
Call:
```

lm(formula = G3 ~ ., data = studentData)

Residuals:

```
Min 1Q Median 3Q Max -8.8228 -0.4612 0.3141 1.0098 4.1768
```

### Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
                                     1.045 0.296556
(Intercept)
               2.35328
                           2.25132
sexM
               0.19326
                           0.19956
                                     0.968 0.333456
                                    -2.926 0.003643 **
age
              -0.23291
                           0.07961
PstatusT
              -0.13866
                           0.32332
                                    -0.429 0.668275
Medu1
              -0.85371
                           1.13385
                                    -0.753 0.451959
Medu2
              -0.98847
                                    -0.883 0.377741
                           1.11932
Medu3
              -0.70963
                           1.12828
                                    -0.629 0.529762
Medu4
              -0.68996
                           1.13486
                                    -0.608 0.543572
Fedu1
               0.44589
                           1.37465
                                     0.324 0.745839
Fedu2
              -0.31696
                           1.36893
                                    -0.232 0.817019
Fedu3
                           1.36971
                                     0.160 0.872823
               0.21940
Fedu4
              -0.15062
                           1.37199
                                    -0.110 0.912640
activitiesyes -0.37173
                           0.19746
                                    -1.883 0.060526 .
               0.11986
                           0.09937
                                     1.206 0.228458
freetime
               0.04262
                           0.01248
                                     3.415 0.000706 ***
absences
G1
               0.18482
                           0.05608
                                     3.296 0.001074 **
G2
               0.96118
                           0.04975
                                    19.322 < 2e-16 ***
                0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
Signif. codes:
```

Residual standard error: 1.893 on 378 degrees of freedom Multiple R-squared: 0.8362, Adjusted R-squared: 0.8292

F-statistic: 120.6 on 16 and 378 DF, p-value: < 2.2e-16

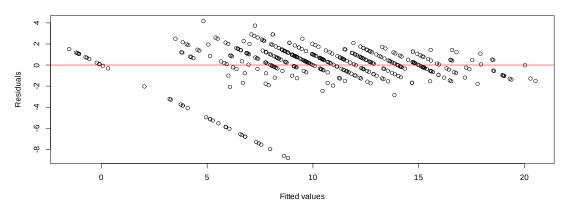
The full model exhibits a massive improvement in the adjusted R-squared (0.05368 to 0.8292), indicating prior grades (G1 and G2) are extremely predictive of the final grade G3. The magnitudes of the standard errors are also reduced, which improves the accuracy.

In this model, the significant covariates are age, absences, G1, and G2 at 5% significance. - For age, it suggests that older students are associated with lower G3 scores holding all other variables constant. - For absences, it suggests that more absences are associated with higher G3 scores holding all other variables constant. - For G1 and G2, higher interim grades are associated with higher G3 scores holding all other variables constant.

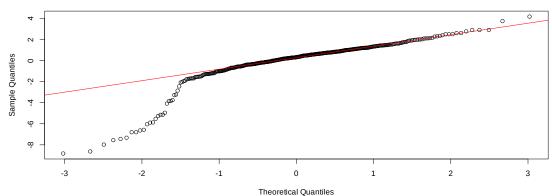
It does not make sense, however, that more absences are associated with higher G3 scores. In our initial model, absences is not a significant covariate. Here, it may be because G1 and G2 are masking the true effect of absences as interim grades are largely associated with G3 scores.

```
[22]: # Residual plot and QQ plot of model_full
res <- residuals(model_full)
fitted_vals <- fitted(model_full)</pre>
```

#### **Residual Plot**



## Normal Q-Q Plot



- For Residual Plot: the residuals show a certain pattern across fitted values, not entirely random, suggesting possible heteroscedasticity or model misspecification.
- For Normal QQ Plot: the residuals deviate from the straight line in the tails, especially in the lower left, indicating potential heavy tails or skewness. Given the sample size (n = 395), however, we can assume that the Central Limit Theorem holds such that the distribution of the estimated coefficients is approximately Normal.

## 1.5 Conclusion

Based on our initial research question, we fitted several linear models, hoping to determine what aspects of a student's social and family life are significantly associated with students' final grades. From the initial model without including G1 and G2, only age was a significant variable. However, the adjusted R-squared is very low (0.05368). Then, adding G1 and G2, our adjusted R-squared increases drastically (0.8292), indicating that the two added variables are very significant.

This shows that students' final grades don't depend linearly on family and social life, but mostly on their interim grades.